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360° domain walls in magnetic thin films with uniaxial and random anisotropy

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X-ray photoemission electron microscopy (XPEEM) and magneto-optic Kerr effect (MOKE) microscopy have been performed on a metal-insulator multilayer of [Co$_{80}$Fe$_{20}$ (t = 1.8 nm)/Al$_2$O$_3$ (3 nm)]$_n$ to image 360° domain walls (DWs) along easy and hard axes, respectively. Their creation and annihilation can be directly visualized under application of a magnetic field. XPEEM experiments and micromagnetic simulations show that 360° DWs occur by the merger of 180° DWs of opposite chirality along the easy axis. They are stable even under application of large magnetic fields. Formation of 360° DWs observed along the hard axis is attributed to symmetry breaking of the coherent spin rotation. Their formation in metal-insulator multilayers is explained to be due to the presence of an orientational dispersion of anisotropy axes in the film grains being comparable to an overall uniaxial anisotropy term. Our results are confirmed numerically using micromagnetic simulations.

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Magnetic multilayers comprising ferromagnetic and non-magnetic layers have been intensely studied to understand various fundamental physics problems and because of their potential use in magnetoresistive device applications. It is desirable that such devices exhibit a reliable and uniform magnetization reversal. Hence, for improving and engineering the performance of these devices, it is necessary to understand the magnetic properties like the reversal process. Here, the role of domains is of paramount importance. Their formation is well understood in terms of the minimization of the free energy. The total energy density $E_{\text{total}}$ of a ferromagnetic material is the sum of exchange ($E_{\text{exch}}$), anisotropy ($E_{\text{anis}}$), Zeeman ($E_{\text{Zeem}}$) and demagnetization ($E_{\text{demag}}$) energy densities. $E_{\text{total}}$ can be expressed as

$$E_{\text{total}} = E_{\text{exch}} + E_{\text{anis}} + E_{\text{Zeem}} + E_{\text{demag}}$$

$$= A(\nabla \phi)^2 + K_u \sin^2 \phi - \mu_0 H M - \frac{1}{2} \mu_0 H_{\text{demag}} M$$  \hspace{1cm} (1)

where $A$ is the exchange constant, $K_u$ the uniaxial anisotropy constant, $\phi$ the angle between the easy axis (EA) arising due to $K_u$ and the magnetization $M$, while $H$ is the applied external magnetic field and $H_{\text{demag}}$ the demagnetization field. $K_u$ can be due to various origins such as magnetocrystalline, shape, surface and strain anisotropies.

The uniaxial anisotropy can also be induced by the growth conditions, e.g. deposition under oblique angle of incidence, preparation under an external magnetic field or post annealing in the presence of a magnetic field. It should be noted that magnetic films usually consist of grains with an average size, a certain size distribution, textures and further morphological characteristics. This may lead to an orientational dispersion in the local anisotropies of the grains. The spatial fluctuations given by such orientational dispersion in local anisotropies may not be very strong, however, they may have a sizeable global effect. Precise measurements of such a spatial distribution of local anisotropy axes are difficult to obtain experimentally. Hence, the presence of such a distribution of local anisotropy axes is only indirectly observable. Alben et al. proposed the so-called random anisotropy (RA) model for amorphous ferromagnetic systems. The average anisotropy constant $\langle K_{ri} \rangle$ in a magnetic thin film with a polydisperse grain size distribution can be expressed with the help of the RA model as

$$\langle K_{ri} \rangle = \sum_i |K_{ri}| \left( \frac{D_i}{L_0} \right)^6$$  \hspace{1cm} (2)

where $K_{ri}$ represents the local magnetic anisotropy of the grains, $D_i$ is the diameter of the grains, and $L_0$ is the ferromagnetic exchange length. The theory relies on the assumption that $L_0$ is larger than the average $D_i$. The RA model assumes that the magnitude of local anisotropy of grains remains constant for each site $(i)$, but varies spatially in its direction, i.e. in reality the local anisotropy may have a directional dispersion.
Thus, the total energy density ($E_{\text{total}}$) given in eq. (1) for $\langle N \rangle$ randomly oriented exchange coupled grains will be modified to

$$E_{\text{total}} = A \sum_{i=1}^{N} (\nabla \phi_i)^2 + K_u \sin^2 \phi + \sum_{i=1}^{N} K_{ri} \sin^2 (\phi - \phi_i)$$

$$- \mu_0 \mathbf{H} \sum_{i=1}^{N} \mathbf{M}_i - \frac{1}{2} \mu_0 \mathbf{H}_{\text{demag}} \cdot \sum_{i=1}^{N} \mathbf{M}_i \quad (3)$$

where $\phi_i$ denotes the direction of the local EA with respect to the global one and $M_i$ the magnetization vector of the $i^{th}$ grain.

Thus, the domain microstructure in a ferromagnetic thin film is governed by the energy given in Eq. (3). Such energy minimization leads to various shapes and sizes of domains. Further, this will have a decisive effect on the nature of the walls separating the domains. In ferromagnetic thin films or in general in magnetic nanostructures various types of DWs separate regions with different orientations of M e.g. $90^\circ$, $180^\circ$, $360^\circ$. Among these the $360^\circ$ DWs are particularly interesting, because they separate regions (domains) with the same magnetization state.

The occurrence of $360^\circ$ DWs are rare as compared to e.g. $180^\circ$ DWs. Nevertheless, $360^\circ$ DWs have been observed in exchange coupled and exchanged biased systems, when Bloch lines present in a $180^\circ$ Néel walls get pinned at structural inhomogeneities or defects. However, there have been reports, where $360^\circ$ DWs are observed in the absence of any defects. In such cases the formation of $360^\circ$ DWs was possible due to the presence of the directional dispersion of EA in permalloy films. Such a dispersion in local anisotropy directions can be treated as a perturbation leading to opposite spin curling and, hence, formation of $360^\circ$ DWs. Heln et al. predicted that the curling in magnetic tunnel junction will depend on the variation of the local anisotropy, thermal fluctuations and by the torque created by the dipolar field of the hard magnetic layer. In some cases, $360^\circ$ DWs can be formed due to the magnetization rotation of nearby grains in opposite directions due to the presence of the distribution of EA in the film.

Apart from thin films, several experimental and theoretical studies from various groups have been performed to understand the origin of the observed $360^\circ$ DWs in nanostructures like nanodots, rings and nanowires. These walls were also observed in composite nanostructures of Co and permalloy by magnetic force microscopy, scanning electron microscopy with polarization analysis and Kerr microscopy. It has been shown that once such $360^\circ$ walls are formed usually it is very difficult to annihilate them even at relatively large magnetic fields. Such a field stability would deteriorate the sensitivity of magnetoresistive sensors and, hence, must be avoided during reversal.

Even though $360^\circ$ DWs have been considered to be undesirable in data storage technology, it is still being explored in view of possible applications. Diegel et al. proposed to use the stability of $360^\circ$ DWs as a future sensor application with certain spin valve geometries. By applying magnetic fields perpendicular to the exchange bias direction concentric $360^\circ$ DWs were formed in the free layer. The authors in Ref. claimed that their observation of nested $360^\circ$ DWs can be used to count the number of magnetization reversals taken place in a device.

It is understood that $360^\circ$ DWs are formed by the merger of two $180^\circ$ Néel walls interacting magnetostatically. The present understanding of the origin and formation of $360^\circ$ DWs is either based on the presence of defects or inhomogeneities in the grain magnetizations, which breaks the local symmetry of magnetization rotation. In this paper, we report the effect of random anisotropy (i.e. orientational dispersion in local easy axes) in the creation of $360^\circ$ DWs. We discuss our results on a magnetic/ non-magnetic multilayer along the easy and hard axes by X-ray photoemission electron microscopy (XPEEM) and magneto-optic Kerr effect (MOKE) based microscopy. Micromagnetic simulations using the object oriented micromagnetic framework (OOMMF) software indicate that the competing effect of uniaxial and random anisotropies contributions leads to the occurrence of $360^\circ$ DWs.
during deposition was relatively small, a certain random anisotropy due to the directional dispersion caused by the granularity of the film with an overall in-plane uniaxial anisotropy is expected. Fig. 1(b) shows the pictorial representation of this uniaxial (large red arrow) and random anisotropy (small black arrows) present in the sample. This is also evident by the square and s-shaped hysteresis loops shown in Fig. 2(a) and (b) measured by longitudinal MOKE magnetometry along the EA and hard axis (HA), respectively. Note that the CoFe film deposited on glass substrate is polycrystalline in nature and exhibits a clear in-plane anisotropy. During the growth of the films a magnetic field was applied and this direction is found to be the EA.

Magnetic domain imaging along the EA was performed by X-ray photoemission electron microscopy (X-PEEM) using the X-ray magnetic circular dichroism (XMCD) at the L₃ absorption edge of Co (778 eV)²⁹. These experiments were performed at the beamline 11.0.1.1 at Advanced Light Source (ALS) in Berkeley, CA, U.S.A under magnetic field pulses and at UE 49 SPEEM beamline at BESSY, Berlin, Germany under variable magnetic field with a specially designed set-up²⁹. In this article we show the results obtained from BESSY. The magnetization reversal was studied using longitudinal MOKE (LMOKE) microscopy at a spatial resolution better than 1 μm manufactured by Evico Magnetics Ltd., Germany. It should be noted that in both XPEEM and Kerr microscopy the imaging is limited to the top layers because these are surface sensitive techniques. Further, in order to understand the observed experimental results micromagnetic simulations were employed by using the OOMMF code.

We have performed XPEEM under external magnetic fields on the MIM sample of [Co₈₀Fe₂₀ (t = 1.8 nm)/Al₂O₃ (3 nm)]₉. The external magnetic field was applied along the EA of the sample. First, the sample was saturated with a negative magnetic field. Then the field was switched towards the positive saturation direction and imaging was performed at fields close to coercivity. Fig. 3(a) - (b) shows the domain images observed by XPEEM along EA at μ₀H = 1.9 mT (a) and 1.95 mT (b), respectively. The image in Fig. 3(c) was recorded a few seconds after the image in (b) was recorded. The image in Fig. 3(c) was recorded few seconds after taking the image in (b). It is seen in Fig. 3(a) that two 180° domains are present while in the center a thread-like 360° DW appears. With further increase of the magnetic field we observed that the domains have shrunk further towards a positive magnetization state. By keeping the magnetic field constant the 180° domains merge and form a 360° DW, which is evidenced as the black colored thread in Fig. 3(c).

Fig. 4 shows XPEEM domain images of [Co₈₀Fe₂₀ (t = 1.8 nm)/Al₂O₃ (3 nm)]₉ at room temperature at magnetic fields of μ₀H = 5.48 mT (a), 9.12 mT (b), and 23.7 mT (c), respectively. The 360° DWs are observed as white colored threads. It should be noted that the positive magnetization is defined as black color. The typical field stability of the 360° DWs is clearly evidenced by the field dependent images shown in Fig. 4. For better visualization see supplementary video VS1 showing the annihilation of these walls under the increasing magnetic field imaged by XPEEM. It should be noticed that even at ~ 23.7 mT, 360° DWs exist whereas the hysteresis loop (Fig. 2) for a measurement parallel to the EA indicates that saturation is reached. Although the 360° DWs shown in Fig. 4 hints that these DWs extend over several tens of micrometers, there exist smaller loop-like 360° DWs as seen in Fig. 4(b). The pinning potential due to the defects present in the film may also have effect on the 360 DWs. On the other hand the dipolar repulsion between neighbouring DWs may lead to such non-linear structure of 360 DWs.

Fig. 5(a) - (e) shows the domain images observed by LMOKE microscopy along the HA for [Co₈₀Fe₂₀ (t = 1.8 nm)/Al₂O₃ (3 nm)]₉ for μ₀H = -16 (a), 1 (b), 3.07 (c), 9.12 (d), and 23.7 mT (e), respectively. Note that the CoFe film deposited on glass substrate is polycrystalline in nature and exhibits a clear in-plane anisotropy due to the directional dispersion caused by the granularity of the film with an overall in-plane uniaxial anisotropy is expected. Fig. 1(b) shows the pictorial representation of this uniaxial (large red arrow) and random anisotropy (small black arrows) present in the sample. This is also evident by the square and s-shaped hysteresis loops shown in Fig. 2(a) and (b) measured by longitudinal MOKE magnetometry along the EA and hard axis (HA), respectively. Note that in both XPEEM and Kerr microscopy the imaging is limited to the top layers because these are surface sensitive techniques. Further, in order to understand the observed experimental results micromagnetic simulations were employed by using the OOMMF code. We have performed XPEEM under external magnetic fields on the MIM sample of [Co₈₀Fe₂₀ (t = 1.8 nm)/Al₂O₃ (3 nm)]₉. The external magnetic field was applied along the EA of the sample. First, the sample was saturated with a negative magnetic field. Then the field was switched towards the positive saturation direction and imaging was performed at fields close to coercivity. Fig. 3(a) - (b) shows the domain images observed by XPEEM along EA at μ₀H = 1.9 mT (a) and 1.95 mT (b), respectively. The image in Fig. 3(c) was recorded a few seconds after taking the image in (b). It is seen in Fig. 3(a) that two 180° domains are present while in the center a thread-like 360° DW appears. With further increase of the magnetic field we observed that the domains have shrunk further towards a positive magnetization state. By keeping the magnetic field constant the 180° domains merge and form a 360° DW, which is evidenced as the black colored thread in Fig. 3(c).

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For better visualization, the corresponding field points have been marked as points (1) - (5) in the hysteresis loop measured along HA shown in Fig. 2(b). At negative saturation ($\mu_0H=-16$ mT), the sample is in its single domain state as observed from the uniform grey color of the domain image (Fig. 5(a)). When the field is reversed ($\mu_0H=1$ mT), nucleation of fine domains occur, which are observed in Fig. 5(b). On further increasing the magnetic field e.g. at $\mu_0H=3.07$ mT, thick black loop like features (360° DWs) are observed as shown in the domain image 5(c). The zoomed-in image of these features for the highlighted area of image 5(c). The thick black loop like features are 360° DWs.

The 360° DWs formed along HA in MIMs can be explained by the difference in the sense of the rotation of the magnetization of the grains 17, which occurs due to the orientational dispersion of anisotropy of grains. In MIMs, the granular thin film is formed by coalescence of CoFe nanoparticles 6,25. It was shown in previous reports that for $t <1.6$ nm CoFe layers are discontinuous, while for $t \geq 1.6$ nm percolation threshold is reached giving rise to continuous thin films 33. Therefore, the MIM sample studied here with $t =1.8$ nm will be dominated by the underlying granular morphology of the film. Hence, in this case the exchange coupling responsible for coherent rotation will not be sufficient to overcome the energy barrier due to the random anisotropy 9.

In order to understand the experimental observation, micromagnetic simulations were performed using the OOMMF software 30 for $[\text{Co}_{80}\text{Fe}_{20}]_n$ ($t =1.8$ nm)/$\text{Al}_2\text{O}_3$ (3 nm)$_n$, where $n$ corresponds to the number of bilayers. In order to save computational time we have performed a detailed micromagnetic simulations for two magnetic layers i.e. $n =2$. Nevertheless we have also performed several simulations for $n =9$ and found that the results are consistent. Therefore, our interpretation from the series of simulations made for the case of two magnetic layers can be extended to the sample studied experimentally in this work.

The lateral size of the sample was 304 x 304 nm$^2$. The cell size was defined to be 3.2 x 3.2 x 1.8 nm$^3$. The value of exchange energy used in OOMMF simulations was 10.3 X 10$^{-12}$ J/m. The saturation magnetization was assumed to be 1.44 x 10$^5$ A/m which corresponds to bulk Cobalt. The model is based on minimization of the free energy, Eq. (3), by respecting the Landau-Lifshitz-Gilbert equation of motion of the magnetization 34.

As mentioned above, the sample studied in this work exhibits uniaxial anisotropy ($K_u$) and a non-negligible random anisotropy ($K_r$). Therefore, in addition to the uniaxial anisotropy ($K_u$) we introduced a random anisotropy term ($K_r$) in the OOMMF simulation. i.e. each individual simulation cell, which represents exactly one grain, exhibits two anisotropy terms. The uniaxial term is constant in magnitude and direction for all cells. However, the random anisotropy term has a constant magnitude for each cell but a direction which is drawn randomly from a unit sphere using mathematical algorithms implemented in the OOMMF code. The latter accounts for the directional dispersion in local anisotropy of the grains in the real sample. Fig. 6 shows the simulated hysteresis and the domain images for comparison of different values of $K_u$ and $K_r$ along EA. Three cases are shown in Fig. 6 where $K_u$ is equal to $K_r$ (case I), $K_u$ and $K_r$ are comparable (case II) and $K_u$ is stronger than $K_r$ (case III). The domain images for the field points marked in the hysteresis from A to F for case (I), (II) and (III) are shown and marked as A1, A2 to E1, E2, respectively. The suffixes 1 and 2 for each domain image refer to the bottom and top cobalt layers, respectively. The red and blue pixels in the images denote magnetization $M_r <0$ and $M_r >0$, respectively. The simulations were performed by negatively saturating the sample and then reversing the field towards positive direction.

It was found that 360° DWs were formed when either $K_u = K_r = 0.1 x 10^6$ J/m$^3$ (Fig. 6(I)), or $K_u =0.15 \times 10^6$ J/m$^3$ and $K_r = 0.1 x 10^6$ J/m$^3$ (Fig. 6(II)), i.e. when uniaxial and random anisotropies are comparable ($K_u \sim K_r$). It can be observed from Fig. 6, that 360° DWs were formed in the Co$_2$ (i.e. top cobalt) layer for case (I) and (II) depicted by domain images C$_2$ and D$_2$, respectively. The blue color on either side of these DWs denotes the same magnetization direction at both sides of the walls. This simulation result is in accordance with
the XPEEM and Kerr microscopy observations. The spins inside these walls rotate by 360° as shown in supplementary Fig. S1, which is a zoomed-in view of the wall obtained from OOMMF simulations. The formation of 360° DWs results from combination of two 180° Néel walls. These 360° DWs require larger fields (as compared to the switching field) for annihilation as can be observed at the field point E in the insets of Fig. 6 (for cases I and II). Again this evidences the anomalous stability of double DWs due to repulsive magnetostatic fields as discovered previously. Very probably the extraordinary stability of these 360° DW (fragments) is due to magnetostatic fields giving rise to dipolar repulsion of the 360° DW core from the antiparallel magnetized environment. Simultaneously deroughening of the 360° DWs is observed (Fig. 3, 4 and S3) similarly as observed in the creep regime of a thin Co layer with perpendicular anisotropy. It evidences strong correlations between two one-dimensional walls moving in a random potential, but bound through forces derived from the dipolar interaction energy. The dipolar repulsion increases the effective line tension for small wall separations, resulting in a stable, long lived state, in which both walls are flat over long distances. For better visualization of formation and annihilation of 360° DWs during magnetization reversal for case (I) and (II) see supplementary video VS4 and VS5, respectively. Further, on increasing the field to very high value (at point F), the sample gets saturated as is evident from the blue pixels in images F2 for both cases I and II.

For case (III) where $K_u \gg K_r$, i.e. $K_u = 0.2 \times 10^6 J/m^3$ and $K_r = 0.1 \times 10^6 J/m^3$ (Fig. 6(III)), no 360° DWs were formed. However, due to the dipolar coupling between the Co layers, mirrored domains were formed as observed in domain images B1, B2 to D1, D2 for case (III) Fig. 6. For better visualization of this magnetization reversal see supplementary video VS6. Hence, the formation of 360° DWs along EA (for case I and II) can be attributed to the competing effect of uniaxial and random anisotropies.

Micromagnetic simulations were performed along the HA as well for the case (II). Along the HA, the reversal is not due to domain wall motion, but via coherent rotation. In this case, the random anisotropy being comparable to the uniaxial one, the exchange interaction cannot outweigh it and, hence, the magnetic moments (or magnetization of domains formed at remanence) rotate oppositely to form the 360° DWs [see supplementary Fig. S2].

In order to understand the effect of inter-layer coupling on the formation of 360° DWs similar OOMMF simulations were also performed for two Co (1.8 nm) layers separated by a thicker (108 nm) spacer of Al$_2$O$_3$ with $K_u = 0.15 \times 10^9 J/m^3$ and $K_r = 0.1 \times 10^6 J/m^3$. Formation of 360° DWs were also observed for such case (see supplementary Fig. S3). Since the spacer of the thickness is very large, the effect of inter-layer dipolar coupling for the formation of 360° DWs must be negligible in this case.

We further performed simulations on Co (1.8 nm) single layers with the same parameters as mentioned above. 360° DWs were also observed for this case (see supplementary Fig. S4). Hence, these results indicate that the formation of 360° DWs is governed by the competing effect of uniaxial and random anisotropies. The discussion for the two Co layers given so far also holds for multilayers of [Co$_{35}$Fe$_{20}$ (t = 1.8 nm)/Al$_2$O$_3$ (3 nm)]$_9$ which approximately mimics the real sample. The corresponding OOMMF simulation was performed along the EA considering the values for case (II). The hysteresis and the domain images near coercive field for [Co (t = 1.8 nm)/Al$_2$O$_3$ (3.6 nm)]$_9$ are shown in supplementary Fig. S5(a) and (b) to (i), respectively. The formation of 360° DWs similar to case (II) described in Fig. 6 was observed in supplementary Fig. S5(d) and (e), where a few Co layers exhibit 360° DWs.

In summary, formation of 360° DWs were observed by XPEEM and LMOKE microscopy in metal-insulator multilayers of [Co$_{35}$Fe$_{20}$ (t = 1.8 nm)/Al$_2$O$_3$ (3nm)]$_9$ . Micromagnetic simulations suggest that formation of 360° DWs can be attributed to the uniaxial anisotropy and presence of orientational dispersion of local random anisotropy. Along the EA, the 360° DWs are formed by the merger of two 180° DWs. However, along the HA 360° DWs are formed as the magnetic moments do not rotate coherently with sweeping the magnetic field. When such a random distribution of anisotropy axes being modeled by a random anisotropy term ($K_r$) in the simulations is comparable to the uniaxial anisotropy, the exchange anisotropy contribution is not outweighed. This results in an opposite sense of rotation of the magnetic moments leading to the formation of 360° DWs. Therefore, we show that apart from other reasons, 360° DWs can be formed due to the competing effect of uniaxial and random anisotropy present in magnetic thin films. We have shown that inter-layer coupling effect has a negligible effect on the formation of 360° DWs. Further in this work we have considered a simple approach to mimic the dispersion in anisotropy by $K_r$ which has a fixed magnitude and its direction changes from cell to cell. However a more appropriate approach for the $K_r$ would be to consider a fixed magnitude but apply a weighting function for the direction of each grain. Further, the size of the grains in the sample may have a significant effect on the formation of such 360° DWs. Therefore, systematic simulation may be performed in future to elucidate these effects on the 360° DW physics.

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FIG. 6. Simulated hysteresis and corresponding domain images for [Co (1.8 nm)/Al₂O₃ (3.6 nm)]₂ along EA by considering different values of uniaxial ($K_u$) and random ($K_r$) anisotropies for formation of 360° DWs. The values of $K_u$ and $K_r$ are the following - Case I: $K_u = K_r = 0.1 \times 10^6$ J/m³; Case II: $K_u = 0.15 \times 10^6$ J/m³ and $K_r = 0.1 \times 10^6$ J/m³ ($K_u \sim K_r$); and Case III: $K_u = 0.2 \times 10^6$ J/m³ and $K_r = 0.1 \times 10^6$ J/m³ ($K_u \gg K_r$). The suffix 1 and 2 for each domain image refers to the bottom and top cobalt layers, respectively. The red and blue color in the images denote magnetization $M_x < 0$ and $M_x > 0$, respectively.