

This is the accepted manuscript made available via CHORUS. The article has been published as:

## Pressure-induced structural modulations in coesite

Ye Wu, Hanyu Liu, Haijun Huang, Yingwei Fei, Xiaolei Feng, and Simon A. T. Redfern

Phys. Rev. B **98**, 104106 — Published 20 September 2018

DOI: [10.1103/PhysRevB.98.104106](https://doi.org/10.1103/PhysRevB.98.104106)

# Pressure-induced structural modulations in coesite

Ye Wu<sup>1\*</sup>, Hanyu Liu<sup>2,3,4\*</sup>, Haijun Huang<sup>1</sup>, Yingwei Fei<sup>4</sup>, Xiaolei Feng<sup>5,6</sup>,  
Simon A. T. Redfern<sup>5,6\*</sup>

<sup>1</sup> *School of Science, Wuhan University of Technology, Wuhan, Hubei 430070, China*

<sup>2</sup> *Innovation Center for Computational Physics Method and Software, College of Physics, Jilin  
University, Changchun 130012, China*

<sup>3</sup> *State Key Laboratory of Superhard Materials, College of Physics, Jilin University, Changchun  
130012, China*

<sup>4</sup> *Geophysical Laboratory, Carnegie Institution for Science, Washington, DC 20015, USA*

<sup>5</sup> *Center for High Pressure Science and Technology Advanced Research (HPSTAR), Shanghai  
201203, China*

<sup>6</sup> *Department of Earth Sciences, University of Cambridge, Downing Street, Cambridge, CB2 3EQ,  
UK*

\*Corresponding author: [yew@whut.edu.cn](mailto:yew@whut.edu.cn), [haliu@ciw.edu](mailto:haliu@ciw.edu), [satr@cam.ac.uk](mailto:satr@cam.ac.uk)

Silica phases, SiO<sub>2</sub>, have attracted significant attention as important phases in the fields of condensed matter physics, materials science, and (in view of their abundance in Earth's crust) geoscience. Here, we experimentally and theoretically demonstrate that coesite undergoes structural modulations under high pressure. Coesite transforms to a distorted modulated structure, coesite-II, at 22-25 GPa with modulation wave vector  $q = 0.5b^*$ . Coesite-II displays further commensurate modulation along the

21 y-axis at 36-40 GPa and the long-range ordered crystalline structure collapses beyond  
22 ~40 GPa and starts amorphizing. First-principles calculations illuminate the nature of  
23 the modulated phase transitions of coesite and elucidate the modulated structures of  
24 coesite caused by modulations along y-axis direction. The structural modulations are  
25 demonstrated to result from phonon instability, preceding pressured-induced  
26 amorphization. The recovered sample after decompression develops a rim of  
27 crystalline coesite structure, but its interior remains low crystalline or partially  
28 amorphous. Our results not only clarify that the pressure-induced reversible phase  
29 transitions and amorphization in coesite originate from structural modulations along  
30 y-axis direction, but also shed light on the densification mechanism of silica under  
31 high pressure.

## 32 **I. Introduction**

33 Silica,  $\text{SiO}_2$ , as the principal component of Earth's crust, is of great significance  
34 in geoscience and materials science [1]. Despite its simple chemical composition,  
35 silica shows rich polymorphism at elevated pressures and temperatures with many  
36 stable or metastable phases [2-5]. An understanding of the mechanisms of phase  
37 transition between its polymorphs is essential to understand the pressure/temperature  
38 behavior of silica, and the resultant variations in its properties [6-8]. Coesite, a  
39 polymorph of  $\text{SiO}_2$ , is the densest known polymorph of silica that still retains the  
40 tetrahedral coordinated (by oxygen) arrangement of silicon atoms familiar in quartz  
41 [9]. Coesite is found in nature in rocks subjected to high pressure, such as the shocked  
42 sandstones of meteor impact craters and certain high-pressure metamorphic rocks. It

43 is widely accepted as a high-pressure indicator in rocks [10]. Coesite can also be  
44 synthesized from quartz in the laboratory at 3-9 GPa and high temperature and it  
45 undergoes a further phase transition to stishovite at even higher pressure [11-13].  
46 Given its importance in high-pressure mineral physics, it is particularly important to  
47 understand the structure features and thermodynamic stability of coesite at high  
48 pressure.

49 Coesite is a framework silicate with corner-sharing  $\text{SiO}_4$  tetrahedra arranged in a  
50 monoclinic unit cell (space group  $C2/c$ ,  $Z = 16$ ) [14], that is pseudo-hexagonal with  
51 almost equal  $a$ - and  $c$ -axes, and a  $\beta$  angle close to  $120^\circ$ . Static compression studies  
52 conclude that coesite is structurally stable up to 9.6 GPa but highly anisotropic, with  
53 the stiffest direction parallel to the chains of tetrahedra along  $c$ -axis [15-17]. The  
54 dominant mechanism of compression is the reduction of four of the five independent  
55 Si-O-Si angles within the structure and the fifth Si1-O1-Si1 angle is constrained to  
56  $180^\circ$  due to symmetry requirements [18]. In addition, spectroscopic experiments and  
57 powder X-ray diffraction (XRD) studies at room temperature suggest that coesite  
58 transforms to a metastable phase at 22-25 GPa before becoming amorphous above 30  
59 GPa [19-21]. Recently, Černok *et al.* [22,23] reported two phase transitions of coesite  
60 on compression by Raman and single-crystal XRD. Instead of becoming amorphous,  
61 they reported that coesite remains crystalline up to at least  $\sim 51$  GPa at room  
62 temperature. Coesite transforms to a reduced structure (coesite-II: space group  $P2_1/n$ ,  
63  $Z = 32$ ) with a doubled  $b$ -cell parameter at  $\sim 23$  GPa and then to a triclinic structure  
64 (coesite-III) at  $\sim 35$  GPa. Additionally, these two phase transitions are reversible on

65 decompression and coesite is retrieved after decompressing to ambient pressure. More  
66 recently, using single-crystal XRD and theoretical simulations, Hu *et al.* [24]  
67 concluded that four triclinic metastable phases bridge the phase transformation from  
68 coesite to a post-stishovite structure (space group  $P2/c$ ), and this represents the phase  
69 transition pathway from four-coordinated to six-coordinated silica. Powder XRD  
70 results up to ~31 GPa by Chen *et al.* [25] confirm a phase transition from coesite to  
71 coesite-II occurring at ~20 GPa, although the powder X-ray diffraction patterns of  
72 coesite-II could not be indexed.

73 In spite of these extensive experimental and theoretical studies, discrepancies  
74 regarding the structural features of coesite at high pressure remain. Pressure-induced  
75 amorphization of coesite remains a rather controversial issue. Spectroscopic  
76 measurements demonstrated that amorphization of coesite under pressure can be  
77 promoted by the presence of large non-hydrostatic stresses [20]. Hemley *et al.* [19]  
78 pointed out that amorphization may be driven principally by the elastic instability of  
79 coesite upon compression. Dean *et al.* [26] also suggested that coupling between shear  
80 instability and phonon softening plays an important role in pressure-induced  
81 amorphization. Similarly, the transition from crystalline to amorphous phase in quartz  
82 occurs at pressure range of 25-30 GPa due to elastic instability [27,28]. Moreover,  
83 early studies reported that amorphization of coesite is irreversible upon  
84 decompression [19,20], but more recently a reversible crystalline-amorphous  
85 transition has been reported [22]. Further disagreement is found regarding  
86 descriptions of the transformation pathways of coesite under pressure. A high-pressure

87 structure (coesite-II), distorted with respect to coesite, appears at 20-25 GPa and  
88 further transforms to triclinic coesite-III at ~35 GPa [23], but four alternative triclinic  
89 structures have been reported as intermediate phases of coesite during the transition to  
90 post-stishovite [24]. It is worth mentioning that samples in both studies remain  
91 crystalline up to ~50 GPa rather than transforming to amorphous as reported by  
92 Hemley *et al.* [19].

93 It is clear that the high-pressure behavior of coesite needs to be resolved. Here,  
94 we describe an investigation of transformation pathways of coesite on compression  
95 and decompression by single-crystal XRD and Raman spectroscopy coupled with the  
96 diamond anvil cell (DAC). We find reversible pressure-induced phase transitions and  
97 amorphization in coesite, associated with commensurate structural modulations along  
98  $y$ -axis of the coesite structure. Theoretical simulations reveal that these are due to  
99 phonon instability along the  $\Gamma$ -Y direction of the Brillouin zone. Our study helps  
100 resolve the high-pressure behavior and phase transition mechanisms of coesite.

## 101 **II. Sample and Experimental Methods**

### 102 **A. Sample synthesis and characterizations**

103 Single-crystal coesite was synthesized in a 1500 ton multi-anvil apparatus at the  
104 Geophysical Laboratory (GL), Carnegie Institution for Science (RUN #: PR1397).  
105 The multi-anvil experiment was conducted with a 14/8 (octahedron edge  
106 length/truncated edge length) octahedron made from Cr<sub>2</sub>O<sub>3</sub>-doped MgO fitted with a  
107 ZrO<sub>2</sub> sleeve and a Re heater. Temperature was monitored with a C-type  
108 W5%Re-W26%Re thermocouple. The starting material (SiO<sub>2</sub>· $n$ H<sub>2</sub>O,  $n = 0.85$ ) was

109 sealed in a platinum capsule with outer diameter 2.5 mm and length 3.0 mm. The  
110 assembly was cold-pressurized to 10 GPa and heated up to 1600 °C for 1 hour, then  
111 slow cooled down to 1200 °C at a rate of 2 °C/min. After holding for 2 hours at 10  
112 GPa and 1200 °C, the experiment was quenched to room temperature by turning off  
113 the power directly. Finally, pressure was automatically released to ambient pressure.  
114 Water-saturated conditions and slow cooling promote the growth of relatively large  
115 single crystals [29].

116 The recovered samples consist of mostly anhedral single crystals, 100-400 μm in  
117 diameter. Raman spectroscopy on the recovered sample confirmed that it is coesite.  
118 Optically-clear single crystals were selected for unpolarized infrared (IR)  
119 measurements in order to calculate water content. Two single crystals were  
120 double-sided polished to thicknesses of 130 and 195 μm, respectively. The IR  
121 measurements were conducted on a JASCO FT/IR-6300 Fourier Transform Infrared  
122 Spectrometer at GL. The spectra were obtained from 512 scans over a spatial scan  
123 range of  $150 \times 150 \mu\text{m}^2$ . The unpolarized IR spectrum of the synthesized coesite  
124 shows five O-H vibration bands in the region of 2800-4000  $\text{cm}^{-1}$  (Fig. S1). According  
125 to the Lambert-Beer law, the intensity of the OH bands in a sample is proportional to  
126 its OH concentration:  $A_i = \varepsilon_i \cdot t \cdot c$ , where  $A_i$  is the total integrated absorbance;  $\varepsilon_i$  is  
127 integrated molar absorption coefficient ( $\varepsilon_i = 190000 \text{ l mol}_{\text{H}_2\text{O}}^{-1} \text{ cm}^{-2}$ ) [30];  $t$  is  
128 thickness (cm);  $c$  is water concentration ( $\text{mol}_{\text{H}_2\text{O}}/\text{l}$ ). The calculated water content in  
129 the synthesized coesite is 185(±30) ppm. This is consistent with earlier studies on the  
130 pressure dependence of hydroxyl solubility in coesite, according to which coesite

131 incorporates hydrogen at  $P$ - $T$  conditions above 5 GPa and 1000 °C [30,31].

## 132 **B. Single-crystal X-ray diffraction**

133 High-pressure single-crystal X-ray diffraction experiments were performed at the  
134 GeoSoilEnviroConsortium for Advanced Radiation Sources (GSECARS) and the  
135 High-Pressure Collaborative Access Team (HPCAT) sectors of the Advanced Photon  
136 Source (APS), Argonne National Laboratory (ANL). Monochromatic X-ray beams  
137 were used, with wavelength  $\lambda = 0.33440$  Å for GSECARS and  $\lambda = 0.40663$  Å for  
138 HPCAT. Experiments were carried out using a symmetric-type DAC equipped with  
139 300  $\mu\text{m}$  culet size diamonds and a pre-indented rhenium gasket with the thickness  
140 30~40  $\mu\text{m}$ . A piece of single-crystal coesite with a diameter of ~20  $\mu\text{m}$  and a thickness  
141 of ~12  $\mu\text{m}$  was loaded into a sample chamber of 120  $\mu\text{m}$  diameter. Neon gas was used  
142 as pressure transmitting medium and fine gold powder was placed next to the crystal  
143 for pressure calibration [32]. Step-scan diffraction patterns were collected at each  
144 X-ray incident angle from -10 ° to 10 ° and a wide-scan image was taken continuously  
145 for the same range. Single-crystal diffraction patterns were evaluated to determine  
146 orientation matrix and index  $d$ -spacings with Miller indices ( $hkl$ ) using the GSE\_ADA  
147 and RSV programs [33].

## 148 **C. Raman spectroscopy**

149 High-pressure Raman spectra were collected using a JASCO NRS-3100 Laser  
150 Raman Spectrophotometer at GL. The spectrometer is equipped with holographic  
151 gratings, a single monochromator, and a  $1024 \times 128$  Andor DV401-F1 CCD



152 Peltier-cooled detector operating at -70 °C. The 531.8 nm line of a coherent solid-state  
153 laser was used for sample excitation, with a power of 6.3 mW at the sample. The  
154 spectrometer was calibrated using the silicon peak at 520 cm<sup>-1</sup>. Raman spectra of  
155 sample were recorded using a 1200 grooves/mm grating with three accumulations,  
156 each of an exposure time of 120 seconds. The same type of DAC and Re gasket were  
157 used as for the X-ray experiments, with neon pressure-transmitting medium, while  
158 pressure was determined by fluorescence shift of a ruby sphere placed next to coesite  
159 crystal [34].

#### 160 **D. Theoretical simulations**

161 Structural relaxations were performed using density functional theory (DFT)  
162 within the Perdew-Burke-Ernzerhof (PBE) parametrization of the generalized gradient  
163 approximation (GGA) [35], as implemented in the Vienna *Ab initio* Simulation  
164 Package (VASP) [36]. The all-electron Projector Augmented-Wave (PAW) [potentials](#)  
165 [37] were used in which the 3s<sup>2</sup>3p<sup>2</sup> and 2s<sup>2</sup>2p<sup>4</sup> are treated as valence electrons for Si  
166 and O atoms, respectively. The Brillouin zone was sampled with Monkhorst-Pack  
167 *k*-meshes [38] with the resolution of  $2\pi \times 0.04 \text{ \AA}^{-1}$  for all phases.

168 Phonons in crystals provide definitive indicators of structural stability. We  
169 employed the supercell approach as implemented in the PHONOPY code [39] to  
170 calculate the phonon dispersion of coesite and its high-pressure phase. According to  
171 the crystal symmetry, the finite displacements of the atoms could be generated. Then  
172 the Hellmann-Feynman forces could be obtained from the single point self-consistent  
173 total energy calculation. Once the force constant is determined, the phonon frequency

174 can be calculated at selected  $q$  points along the symmetry lines in the Brillouin zone.

175 First-principles MD simulations using the canonical  $NVT$  ( $N$ -number of particles,  
176  $V$ -volume, and  $T$ -temperature) and  $NPT$  ( $N$ -number of particles,  $P$ -pressure, and  
177  $T$ -temperature) ensembles were performed for the coesite structure to examine its  
178 thermal stability. The simulation consists of 10000 steps with an integration time of 1  
179 fs. The self-consistency on the total energy was  $1 \times 10^{-5}$  eV.

### 180 **III. Results and Discussion**

181 The combination of XRD with DAC enables us to track the structural behavior  
182 of coesite as a function of pressure up to 50 GPa. At pressures below  $\sim 22$  GPa, all  
183 diffraction peaks except for saturated diamond peaks and diffraction rings from Ne  
184 and Re can be indexed as monoclinic coesite ( $C2/c$ ,  $Z = 16$ ) (Fig. 1a). We observed an  
185 abrupt change in the diffraction pattern between  $\sim 22$  and  $\sim 25$  GPa, which is  
186 characterized by an increase in the number of diffraction peaks with increasing  
187 pressure and an overall decrease in their intensities. This is in agreement with  
188 previous Raman spectroscopy and single-crystal XRD observations of a  
189 pressure-induced structural transformation in coesite to a lower-symmetry coesite-II  
190 [20,22,23]. The diffraction pattern at 25.2 GPa can be indexed according to the  
191 coesite-II structure ( $P2_1/c$ ,  $Z = 32$ ,  $a = 6.632(3)$  Å,  $b = 23.321(2)$  Å,  $c = 6.858(5)$  Å,  $\beta$   
192  $= 120.1(1)^\circ$ , and  $V = 917.5(18)$  Å<sup>3</sup>) (Fig. 1b), which is equivalent to the  $P2_1/n$   
193 structure reported by Černok *et al.* [23], but with a different cell setting. The enlarged  
194 regions of the diffraction patterns at 20.3 and 25.2 GPa show that the  $b^*$  reciprocal  
195 lattice parameter for coesite-II is half of that for coesite (Figs. 1c and 1d), which



209 These new weak peaks also occur along  $y^*$ -axis of the coesite-II reciprocal lattice.  
210 Specifically, new diffraction intensity appears between (2 2 2) and (2 3 2) of the  
211 diffraction patterns of the coesite-II structure at 36.8 GPa as marked by grids in Fig.  
212 3b. These indicate that the coesite-II structure undergoes commensurate modulation  
213 along  $y$ -axis at pressures above  $\sim 36$  GPa. We denote the new modulated structure as  
214 coesite-X, since it is different from the coesite-III structure reported by Černok *et al.*  
215 [23]. Due to the low crystallinity of sample at pressures above  $\sim 36$  GPa, the coesite-X  
216 structure cannot be indexed and solved. The coesite-X phase does not persist above 40  
217 GPa and neither did we observe any strong diffraction peaks from the original coesite  
218 at these pressures (Fig. 3). There is only a broad and weak diffraction intensity  
219 occurring originally close to the (0 4 0) peak of coesite and then persisting at higher  
220 pressures where this becomes the (0 8 0) peak of coesite-II, as indicated by the orange  
221 box in Fig. 3. At 50.3 GPa, this peak with  $d = 2.653$  Å (momentum transfer  $Q = 2.368$   
222 Å<sup>-1</sup>) coincides with the first sharp diffraction peak (Si-O bond correlation,  $Q =$   
223  $2.39\sim 2.40$  Å<sup>-1</sup>) of SiO<sub>2</sub> glass at  $\sim 50$  GPa [41,42]. These changes indicate that the  
224 coesite sample is very weakly crystalline and commences amorphization above  $\sim 40$   
225 GPa.

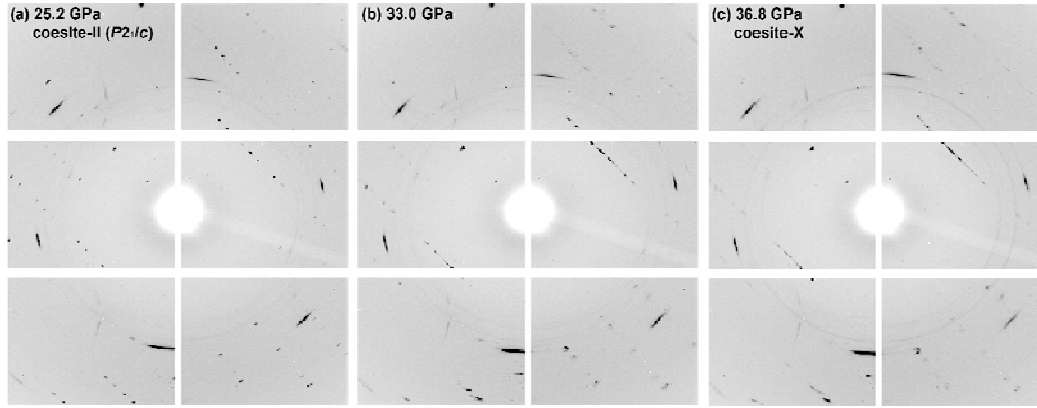


FIG. 2. X-ray diffraction patterns of coesite at 25.2, 33.0, and 36.8 GPa.

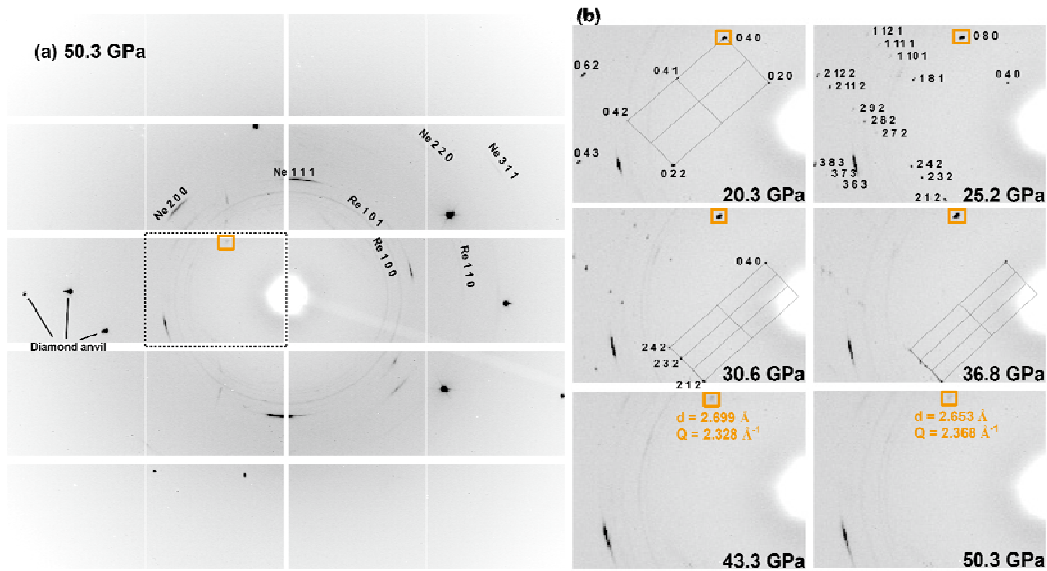


FIG. 3. X-ray diffraction patterns of coesite at high pressures. (a) X-ray diffraction pattern at 50.3 GPa. (b) Zoomed-in pictures corresponding to the dashed box in (a) and track phase transformations of coesite from 20.3 to 50.3 GPa. The diffraction peak marked in orange box starts from (0 4 0) of coesite and then (0 8 0) of coesite-II.

High-pressure Raman spectra measurements on single-crystal coesite confirm our XRD observations. Coesite shows eight Raman active peaks ( $\nu_1 \sim \nu_8$ ) in the region of 150-800  $\text{cm}^{-1}$  with the strongest peak ( $\nu_8$ ) at  $\sim 519 \text{ cm}^{-1}$  assigned to the Si-O-Si

236 stretching mode (Fig. 4). The intensities and positions of these peaks are in good  
237 agreement with previous studies [20,22]. All the vibration bands show continuous  
238 positive pressure shift during compression and can be followed up to ~22 GPa. The  
239 spectrum changes abruptly between ~22 and ~25 GPa. The strongest band ( $\nu_8$ ) splits  
240 into a doublet, accompanied by similar splitting of three weaker bands ( $\nu_3$ ,  $\nu_4$ , and  $\nu_7$ ).  
241 We also note that Raman mode  $\nu_1$  disappears gradually at pressures above ~22 GPa  
242 and two further modes ( $\nu_5$  and  $\nu_6$ ) show contrasting pressure-dependence below and  
243 above ~22 GPa. These results are in agreement with those of Hemley [20] and Černok  
244 *et al.* [22] and their conclusions. The observed splitting of Raman modes suggests that  
245 a phase transformation occurs at 22-25 GPa and that this is accompanied by a  
246 distortion of the coesite structure. The new phase has been confirmed as coesite-II  
247 structure by means of single-crystal XRD in this study and that of Černok *et al.* [23].  
248 The Raman spectra weaken and broaden at pressures above ~36 GPa. At 37.5 GPa, a  
249 triplet near  $600\text{ cm}^{-1}$  was observed, indicating that the coesite-II structure further  
250 transforms to another distorted structure, coesite-X, as suggested by our single-crystal  
251 XRD. All Raman peaks disappeared at the highest pressure 42.8 GPa. This suggests  
252 that the sample is very weakly crystalline and amorphization starts above ~40 GPa,  
253 supported by our single-crystal XRD data above.

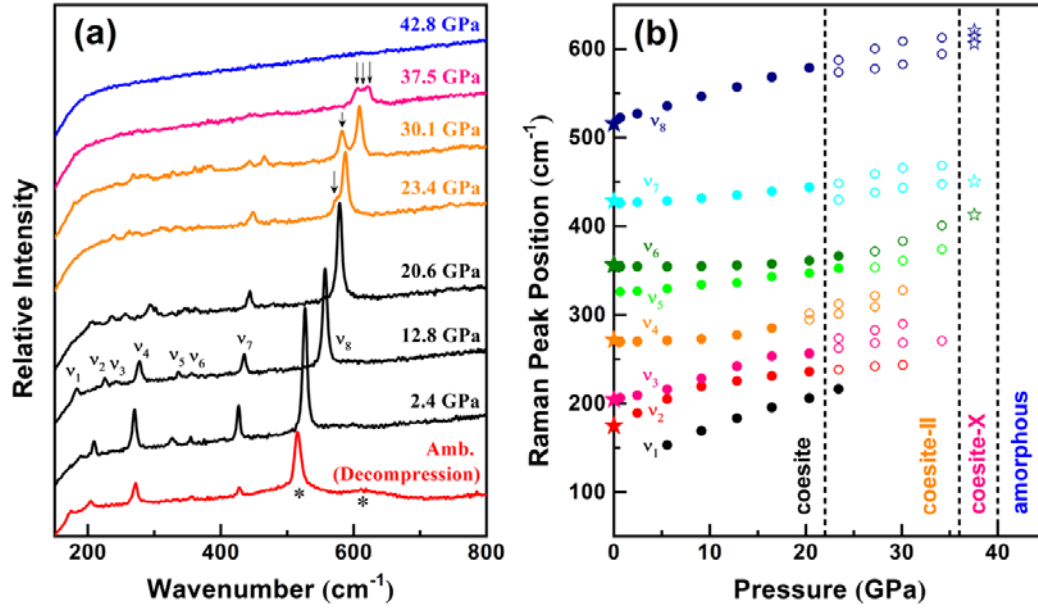
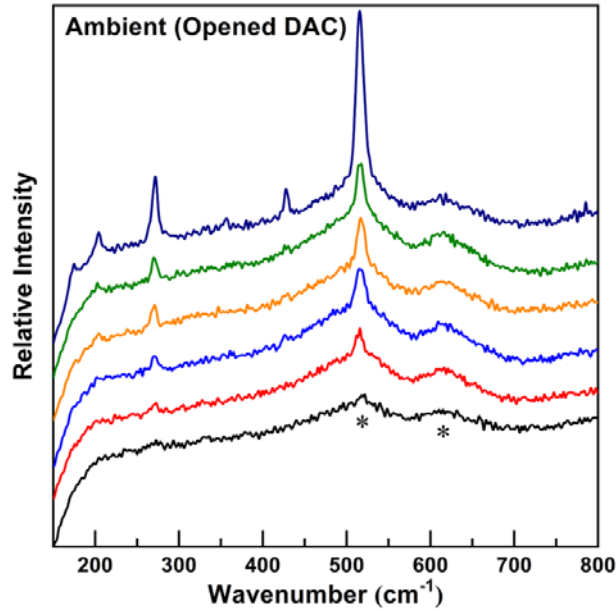


FIG. 4. Raman spectra of coesite (a) and mode frequencies (b) during compression and decompression. The asterisks on the quenched ambient spectrum in (a) indicate two diffuse Raman bands at  $\sim 520 \text{ cm}^{-1}$  and  $\sim 620 \text{ cm}^{-1}$ . The solid stars in (b) represent Raman peak positions of quenched ambient spectrum. The dashed lines in (b) indicate the phase boundaries of polymorphs for coesite.

Upon decompression to ambient pressure, an interesting phenomenon is observed in the recovered sample. The recovered sample develops a rim of a back-transformed coesite phase, but its interior remains very low crystalline or amorphous. All spectra of the pressure-quenched coesite from 42.8 GPa exhibit two diffuse Raman bands at  $\sim 520 \text{ cm}^{-1}$  and  $\sim 620 \text{ cm}^{-1}$  marked with asterisks in Figs. 4a and 5, which are also observed for quartz and silica glass quenched from high pressure [20,43]. Decompression from 42.8 GPa is accompanied by recrystallization of the coesite structure and partial preservation of the low crystalline or amorphous phase. Shear stresses concentrated at the boundary between the sample and the



269 pressure medium could well play an important role in the transformation during the  
 270 decompression. Similar features of recrystallization and reversible amorphization  
 271 during decompression have also been observed on berlinite and zeolites under  
 272 quasi-hydrostatic conditions [44-46].



273  
 274 FIG. 5. Raman spectra collected at different positions within the recovered sample after  
 275 decompression from 42.8 GPa to ambient conditions. The asterisks indicate two diffuse Raman  
 276 bands at  $\sim 520 \text{ cm}^{-1}$  and  $\sim 620 \text{ cm}^{-1}$ .

277 To further elucidate the phase transition mechanism of coesite at high pressure,  
 278 we performed first-principles simulations based on DFT. According to previous  
 279 studies, phonon softening plays an important role in the phase transition and  
 280 amorphization of quartz under pressure [47]. Similar pressure-induced behaviors  
 281 occur in coesite according to our experimental results. Here, a  $2 \times 1 \times 2$  coesite supercell  
 282 with 192 atoms was employed. Coesite is dynamically stable at 0 GPa, since there is



no imaginary phonon mode across the entire Brillouin zone (Fig. 6a), validating our computational scheme. However, imaginary vibrational modes are found along  $\Gamma$ -Y direction of the Brillouin zone at 25 GPa (Fig. 6b), indicating that by this point the coesite structure is dynamically unstable.

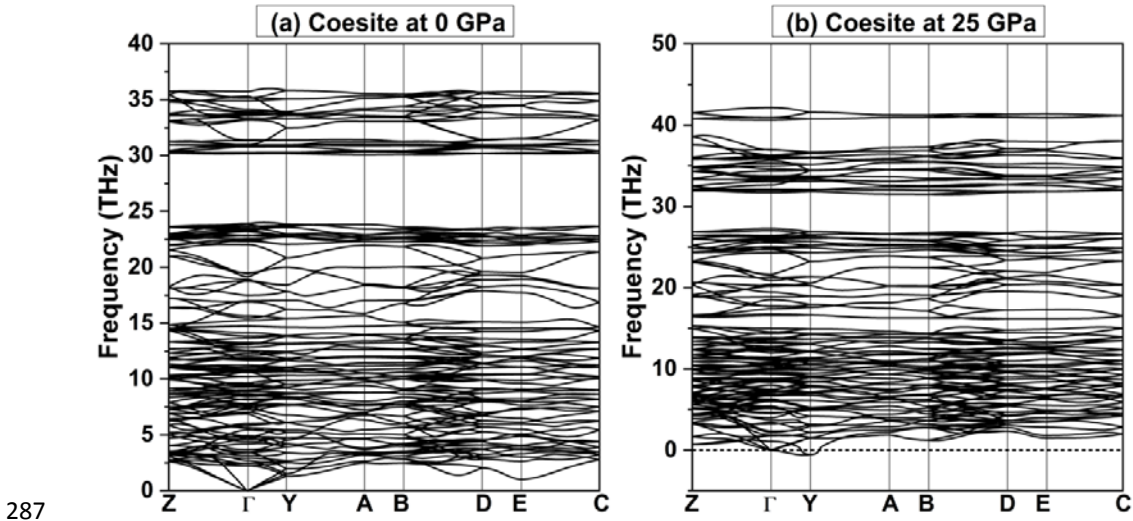
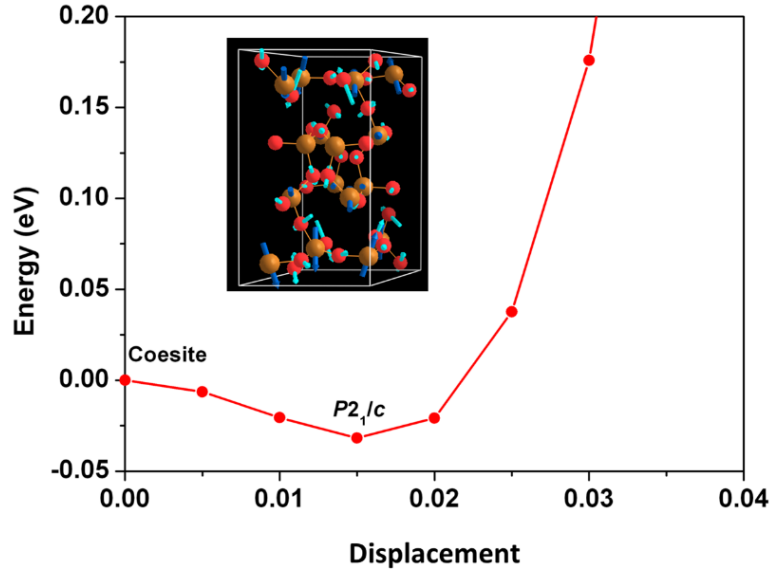


FIG. 6. Phonon dispersion curves of coesite ( $C2/c$ ) at 0 GPa (a) and 25 GPa (b).

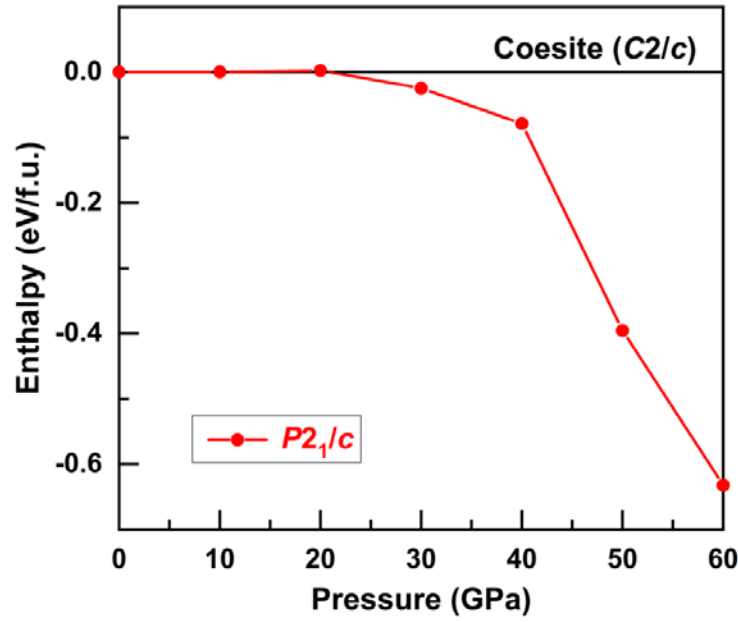
It is noteworthy that the instability mode occurs at the Y zone-boundary point (0 0.5 0), suggesting that the wavelength of the unstable vibrational mode corresponds to doubling along the  $y$ -axis in real space. Therefore, we doubled the  $y$ -axis of our computational coesite cell and gradually moved the atoms along the unstable vibrational eigenvectors (Fig. 7). The coesite structure tends to become unstable with increasing the atomic displacement and the energy is lowest at a displacement amplitude of 0.015. Full geometry optimization at this displacement point at 25 GPa results in the coesite-II structure ( $P2_1/c$ ,  $Z = 32$ ) with a doubled  $b$ -axis with respect to coesite.



298

299 FIG. 7. The energy of coesite with the increased atomic displacement. Atomic displacement is  
 300 defined as the proportion of atomic amplitude. Blue and cyan arrows represent the directions of  
 301 displacement for Si and O atoms, respectively, along the unstable vibrational Eigenvectors.

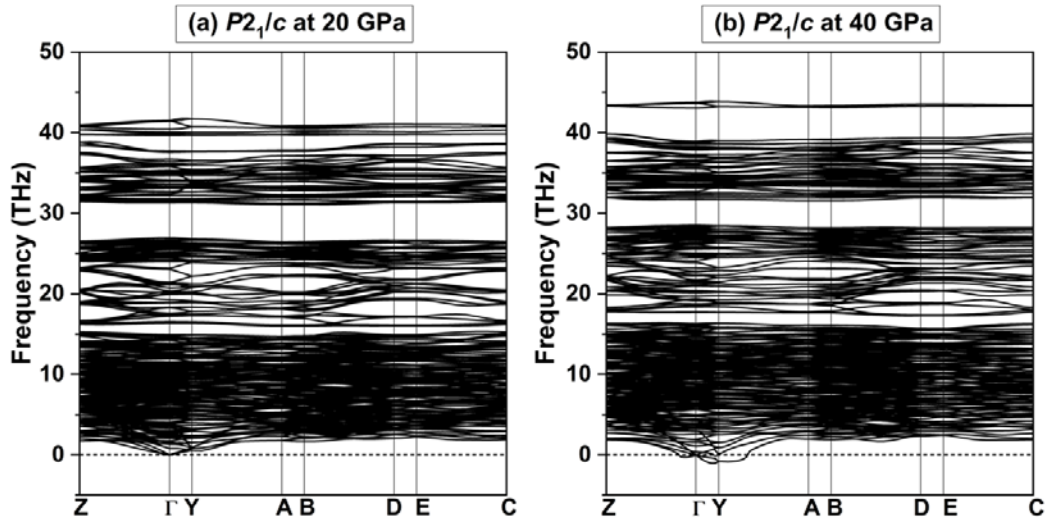
302 The coesite-II ( $P2_1/c$ ) phase has almost identical enthalpy to that of coesite  
 303 below 20 GPa (Fig. 8). Above 20 GPa, the coesite-II phase becomes  
 304 thermodynamically stable over coesite as suggested by its relatively lower enthalpy.  
 305 Moreover, the difference of enthalpy between coesite and  $P2_1/c$  structures increases  
 306 with increasing pressure. These results support the idea that the phase transition from  
 307 coesite to coesite-II observed experimentally is driven by acoustic softening at Y-point  
 308 (0 0.5 0) of the coesite Brillouin zone and suggest that this phase transition is a typical  
 309 ferroelastic-related symmetry-breaking transition, potentially second-order in  
 310 character.



311

312 FIG. 8. The relative enthalpies of coesite ( $C2/c$ ) and coesite-II ( $P2_1/c$ ) structures at high pressures.

313 Phonon calculations show that the coesite-II structure is dynamically stable at 20  
 314 GPa without phonon softening (Fig. 9a). It is interesting to note that vibrational  
 315 modes along  $\Gamma$ -Y direction are imaginary at 40 GPa (Fig. 9b), indicating that at this  
 316 pressure the coesite-II structure is dynamically unstable. Our calculated phonon  
 317 softening along  $\Gamma$ -Y direction suggests that the coesite-II structure may undergo  
 318 further structural modulation along its  $y$ -axis.



319

FIG. 9. Phonon dispersion curves of coesite-II ( $P2_1/c$ ) at 20 GPa (a) and 40 GPa (b).

To further examine the thermodynamic stability of coesite, we carried out MD simulations at 300 K using the canonical  $NVT$  ensemble. A  $2\times 2\times 2$  supercell of coesite with 384 atoms was employed. We found that coesite transforms to a new  $P2_1/c$  structure with 96 atoms per unit cell at 30 GPa, which supports our single-crystal XRD results and the theoretical calculations of phonon dispersion and structural relaxations in this study. At 50 GPa, the coesite structure becomes a long-range disordered structure and contains multiple coordination states of silicon, with 4-, 5-, and 6-coordinated Si atoms (Fig. S2). A  $1\times 4\times 1$  supercell of coesite-II ( $P2_1/c$ ) with 384 atoms was employed to further explore the size effects along its  $y$ -axis. At 40 GPa and 300 K, a new modulated structure (labelled coesite-XI), corresponding to modulation along the  $y$ -axis of coesite-II, is found and its  $b$  cell parameter is  $\sim 90$  Å (four times the  $b$  cell parameter of coesite-II). The structure information of coesite-XI is presented in supplementary materials. As shown in Movie S1, the coesite-XI structure appears as a wave along its  $y$ -axis. These theoretical results confirm that coesite transforms to modulated structures, with structural modulation along  $y$ -axis under high pressure, and that this triggers amorphization at higher pressure.

To further examine the pressure-induced structural modulation mechanism, single-crystal XRD experiments were also performed on coesite up to 54.0 GPa using argon as pressure transmitting media. Argon media provide less hydrostatic conditions than neon media. Selected representative XRD patterns are shown in Fig. S3. The phase transition from coesite to coesite-II occurs at pressures around 22~24 GPa.

342 With increasing pressure, the coesite-II phase undergoes further structural modulation  
343 along its  $y$  axis. There are only a few weak diffraction peaks up to 54.0 GPa,  
344 suggesting that the coesite tends towards amorphization at higher pressure. These  
345 results elucidate that pressure-induced structural modulations in coesite along its  $y$   
346 axis is independent on pressure-transmitting media used.

347 The phase transition from coesite to coesite-II at  $\sim 25$  GPa is confirmed by means  
348 of both experimental and theoretical studies in this and previous studies [20,23]. Four  
349 intermediate phases at  $\sim 26$  GPa reported by Hu *et al.* [24] can be related to the  
350 coesite-II structure, since their reported XRD patterns at  $\sim 26$  GPa display features of a  
351 modulated structure, with a main peak surrounding by several satellite peaks.  
352 Although helium was used as pressure transmitting medium in their studies, both neon  
353 and helium media provide good hydrostatic conditions in the DAC at pressures below  
354 30 GPa, with typical deviatoric stress of less than 0.25 GPa [48]. At pressures above  
355 35 GPa, we did not observe phase transitions from either coesite-II to triclinic  
356 coesite-III or intermediate phases to monoclinic post-stishovite [23,24], but rather we  
357 found modulated structures (coesite-X and coesite-XI), showing structural  
358 modulations along the  $y$ -axis of coesite-II, which precedes amorphization. The  
359 amorphous phase of coesite has a long-range disordered structure with 4-, 5-, and  
360 6-coordinated Si atoms at 50 GPa and 300 K based on our MD simulations, which  
361 may be considered as an intermediate state towards the octahedrally-coordinated  
362 post-stishovite phase proposed by Hu *et al.* [24] seen under hydrostatic conditions.

363 Pressure-induced reversible phase transitions and amorphization in coesite have

364 been observed in this study. The two phase transitions from coesite to coesite-II and  
365 then to coesite-III are also reversible, although amorphization is absent in the study of  
366 Černok *et al.* [22]. The reversibility of the crystal-to-crystal phase transitions is  
367 completely consistent the with symmetry-breaking phonon-softening ferroelastic  
368 transitions that we see, and reflects the fact that the polymorphs at high pressure have  
369 group-subgroup relationships with this coesite family of structures. Our combined  
370 experimental results and theoretical simulations indicate that coesite-II as a  
371 commensurate modulated structure of coesite undergoes further modulation along its  
372  $y$ -axis until, eventually, the long-range crystalline ordered structure collapses. The  
373 high-pressure modulated structures (coesite-II and coesite-X) are distorted relative to  
374 the coesite structure and can be considered as precursors to amorphization. The  
375 modulation transition mechanism is reversible upon decompression, as has been  
376 verified by both our Raman measurements and those of Černok *et al.* [22].

#### 377 IV. CONCLUSIONS

378 Pressure-induced structural modulations in coesite have been observed  
379 experimentally and confirmed theoretically. Coesite transforms to a distorted  
380 coesite-II structure at 22-25 GPa, with a doubled  $b$ -axis with respect to coesite. The  
381 coesite-II structure undergoes further structural modulation along its  $y$ -axis at 36-40  
382 GPa and starts amorphization above  $\sim 40$  GPa under quasi-hydrostatic conditions.  
383 These modulation-induced phase and amorphization transitions are reversible  
384 experimentally. Theoretical calculations confirm that the modulation wavelength  
385 increases along the  $y$ -axis of coesite upon compression and we have proposed a new

modulated structure (coesite-XI) that results from modulation along the  $y$ -axis of coesite-II. Phonon instability plays a key role in driving the phase modulated transformations in coesite which precede amorphization. A new mechanism of pressure-induced phase transitions and amorphization in coesite originating from structural modulations along the  $y$ -axis direction is proposed based on our experimental and theoretical results.

## ACKNOWLEDGMENTS

We thank Bjorn O. Mysen and Renbiao Tao for experimental assistance, Sergey N. Tkachev for loading gas medium, and Przemek Dera for helpful discussion. Y. W. acknowledges the financial support from the National Science Foundation of China (41602036) and the program of China Scholarship Council (No. 201606955099). H. L. acknowledges support by EFree, an Energy Frontier Research Center funded by the DOE, Office of Science, Basic Energy Sciences under Award No. DE-SC-0001057. S. A. T. R. acknowledges the support of the UK Natural Environment Research Council under grant NE/P012167/1. High-pressure XRD experiments were performed at GSECARS of the APS, ANL. GSECARS is supported by the NSF-Earth Sciences (EAR-1128799) and the DOE-Geosciences (DE-FG02-94ER14466). APS is a U.S. DOE Office of Science User Facility operated for the DOE Office of Science by ANL under contract DEAC02-06CH11357.

## References

- [1] P. J. Heaney, C. T. Prewitt, and G. V. Gibbs, *Mineralogical Society of America* **29** (1994).
- [2] H. J. Russell, C. T. Prewitt, and K. J. Kingma, (1994).

408 [3] Y. Tsuchida and T. Yagi, *Nature* **347**, 267 (1990).

409 [4] K. J. Kingma, R. J. Hemley, H. Mao, and D. R. Veblen, *Phys. Rev. Lett.* **70**, 3927 (1993).

410 [5] J. Haines, J. M. Léger, F. Gorelli, and M. Hanfland, *Phys. Rev. Lett.* **87**, 155503 (2001).

411 [6] L. Huang, M. Durandurdu, and J. Kieffer, *Nat. Mater.* **5**, 977 (2006).

412 [7] R. Martonák, D. Donadio, A. R. Oganov, and M. Parrinello, *Nat. Mater.* **5**, 623 (2006).

413 [8] Y. Liang, C. R. Miranda, and S. Scandolo, *Phys. Rev. Lett.* **99**, 215504 (2007).

414 [9] L. Coes, *Science* **118**, 131 (1953).

415 [10] E. C. Chao, E. M. Shoemaker, and B. M. Madsen, *Science* **132**, 220 (1960).

416 [11] S. Stishov and S. Popova, *Geokhimiya* **10**, e841 (1961).

417 [12] M. Akaogi, H. Yusa, K. Shiraishi, and T. Suzuki, *J. Geophys. Res. Solid Earth* **100**,

418 22337 (1995).

419 [13] S. Ono, T. Kikegawa, Y. Higo, and Y. Tange, *Phys. Earth Planet. Inter.* **264**, 1 (2017).

420 [14] G. Gibbs, *Zeitschrift für Kristallographie-Crystalline Materials* **145**, 108 (1977).

421 [15] R. Angel, J. Mosenfelder, and C. Shaw, *Phys. Earth Planet. Inter.* **124**, 71 (2001).

422 [16] L. Levien and C. T. Prewitt, *Am. Mineral.* **66**, 324 (1981).

423 [17] H. Kimizuka, S. Ogata, and J. Li, *J. Appl. Phys.* **103**, 131 (2008).

424 [18] R. Angel, C. Shaw, and G. Gibbs, *Phys. Chem. Miner.* **30**, 167 (2003).

425 [19] R. Hemley, A. Jephcoat, H. K. Mao, L. Ming, and M. Manghnani, *Nature* **334**, 52 (1988).

426 [20] R. Hemley, *High-Pressure Research in Mineral Physics: a Volume in Honor of Syun-iti*

427 *Akimoto*, 347 (1987).

428 [21] Q. Williams, R. Hemley, M. Kruger, and R. Jeanloz, *J. Geophys. Res. Solid Earth* **98**,

429 22157 (1993).

430 [22] A. Černok, T. B. Ballaran, R. Caracas, N. Miyajima, E. Bykova, V. Prakapenka, H.-P.

431 Liermann, and L. Dubrovinsky, *Am. Mineral.* **99**, 755 (2014).

432 [23] A. Černok, E. Bykova, T. B. Ballaran, H.-P. Liermann, M. Hanfland, and L. Dubrovinsky,

433 *Zeitschrift für Kristallographie-Crystalline Materials* **229**, 761 (2014).

434 [24] Q. Hu, J.-F. Shu, A. Cadieu, Y. Meng, W. Yang, H. Sheng, and H.-K. Mao, *Nat. Commun.*

435 **6** (2015).

436 [25] T. Chen, X. Wang, X. Qi, M. Ma, Z. Xu, and B. Li, *Am. Mineral.* **101**, 1190 (2016).

437 [26] D. W. Dean, R. M. Wentzcovitch, N. Keskar, J. R. Chelikowsky, and N. Binggeli, *Phys.*

438 *Rev. B* **61**, 3303 (2000).

439 [27] N. Binggeli and J. R. Chelikowsky, *Phys. Rev. Lett.* **69**, 2220 (1992).

440 [28] K. J. Kingma, C. Meade, R. J. Hemley, H.-k. Mao, and D. R. Veblen, *Science* **259**, 666

441 (1993).

442 [29] A. Shatskiy, D. Yamazaki, Y. M. Borzdov, T. Matsuzaki, K. D. Litasov, T. Cooray, A.

443 Ferot, E. Ito, and T. Katsura, *Am. Mineral.* **95**, 135 (2010).

444 [30] M. Koch-Müller, Y. Fei, E. Hauri, and Z. Liu, *Phys. Chem. Miner.* **28**, 693 (2001).

445 [31] J. Mosenfelder, *Phys. Chem. Miner.* **27**, 610 (2000).

446 [32] Y. Fei, A. Ricolleau, M. Frank, K. Mibe, G. Shen, and V. Prakapenka, *Proc. Natl. Acad.*

447 *Sci.* **104**, 9182 (2007).

448 [33] P. Dera, K. Zhuravlev, V. Prakapenka, M. L. Rivers, G. J. Finkelstein, O.

449 Grubor-Urosevic, O. Tschauner, S. M. Clark, and R. T. Downs, *High Pressure Res.* **33**, 466

450 (2013).

451 [34] H. K. Mao, J. Xu, and P. M. Bell, *J. Geophys. Res.* **91**, 4673 (1986).



- 452 [35] J. P. Perdew, K. Burke, and M. Ernzerhof, Phys. Rev. Lett. **77**, 3865 (1996).  
453 [36] G. Kresse and J. Furthmüller, Phys. Rev. B **54**, 11169 (1996).  
454 [37] G. Kresse and D. Joubert, Phys. Rev. B **59**, 1758 (1999).  
455 [38] H. J. Monkhorst and J. D. Pack, Phys. Rev. B **13**, 5188 (1976).  
456 [39] A. Togo, F. Oba, and I. Tanaka, Phys. Rev. B **78**, 134106 (2008).  
457 [40] T. Janssen, A. Janner, A. Looijenga-Vos, and P. De Wolff, in *International Tables for*  
458 *Crystallography Volume C: Mathematical, physical and chemical tables* (Springer, 2006), pp.  
459 907.  
460 [41] T. Sato and N. Funamori, Phys. Rev. B **82**, 184102 (2010).  
461 [42] T. Sato and N. Funamori, Phys. Rev. Lett. **101**, 255502 (2008).  
462 [43] R. Hemley, H. Mao, P. Bell, and B. Mysen, Phys. Rev. Lett. **57**, 747 (1986).  
463 [44] P. Gillet, J.-M. Malezieux, and J.-P. Itie, Am. Mineral. **81**, 651 (1996).  
464 [45] T. D. Bennett, P. Simoncic, S. A. Moggach, F. Gozzo, P. Macchi, D. A. Keen, J.-C. Tan,  
465 and A. K. Cheetham, Chemical communications **47**, 7983 (2011).  
466 [46] P. Gillet, J. Badro, B. Varrel, and P. F. McMillan, Phys. Rev. B **51**, 11262 (1995).  
467 [47] N. Choudhury and S. Chaplot, Phys. Rev. B **73**, 094304 (2006).  
468 [48] S. Klotz, J. C. Chervin, P. Munsch, and G. Le Marchand, Journal of Physics D: Applied  
469 Physics **42**, 075413 (2009).