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Epsilon-Near-Zero Response and Tunable Perfect Absorption in Weyl Semimetals

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We theoretically study the electromagnetic response of type-I and type-II centrosymmetric Weyl metals. We derive an anisotropic permittivity tensor with off-diagonal elements to describe such gyrotropic media. Our findings reveal that for appropriate Weyl cones tilts, the real part of the transverse component of the permittivity can exhibit an epsilon-near-zero response. The tilt parameter can also control the amount of loss in the medium, ranging from lossless to dissipative when transitioning from type-I to type-II. Similarly, by tuning either the frequency of the electromagnetic field or the chemical potential in the system, an epsilon-near-zero response can appear as the permittivity of the Weyl semimetal transitions between positive and negative values. Employing the obtained permittivity tensor, we consider a setup where the Weyl semimetal is deposited on a perfect conductive substrate and study the reflection and absorption characteristics of this layered configuration. We show that by choosing the proper geometrical and material parameters, devices can be created that perfectly absorb electromagnetic energy over a wide angular range of incident electromagnetic waves.

I. INTRODUCTION

Since the advent of metamaterials, efforts to design materials that can be used to control electromagnetic (EM) fields has flourished. One prominent route involves developing anisotropic structures whose EM response is described by a permittivity tensor \( \mathbf{\varepsilon} \) that has components with extreme values, including epsilon-near-zero (ENZ) media, where the real part of a component of \( \mathbf{\varepsilon} \) vanishes along a given coordinate axis. Within the ENZ regime, the phase of the entering EM wave can be uniform, and the wavefront conforms to the shape of the exit side of the ENZ medium.3 A number of ENZ-based architectures have been fabricated, including sub-wavelength dielectric coatings that control the resonant coupling of light with ENZ regions.3 Experimental work with microwave waveguides4,5 demonstrated how a narrow ENZ channel can lead to enhanced electromagnetic coupling. A nanoparticle mixture containing dielectric and metal constituents with an effective ENZ response exhibited an increase in the superconducting critical temperature.6 The propagation of a transverse magnetic optical beam through a subwavelength slit demonstrated a transmission enhancement1 when the InAsSb semiconductor substrate was tuned to its ENZ frequency.

Many pathways have been studied that lead to the creation of ENZ materials, including intricate combinations of metal-dielectric multilayers and arrays of rods, or transparent conducting oxides. Other approaches involve the use of more exotic materials like graphene8 with its intrinsic two dimensionality and linear dispersion around the Dirac point. Recently, Weyl semimetals9–16 have been added to the ever expanding class of materials that have useful EM properties. The band structure of a Weyl semimetal (WS) is characterized by a conical energy spectrum with an even number of Weyl nodes that are topologically protected. The chiralities of Weyl nodes correspond to topological charges that result in monopoles and anti-monopoles in the Berry curvature11,12. Indeed, the Weyl semimetal phase manifests itself in unusual surface states with Fermi arcs and chiral anomalies10–13,16. Weyl semimetals are topologically nontrivial materials that are predicted for the magnetic compounds \( \text{Y}_2\text{IrO}_7 \), \( \text{Eu}_2\text{IrO}_7 \), and \( \text{HgCr}_2\text{Se}_4 \),17,18 and in some nonmagnetic samples, including \( \text{TaAs}, \text{TaP}, \text{NbAs}, \) and \( \text{NbP}19–23 \). The WS \( \text{TaAs} \) was shown to have a wide spectral range as a room temperature photodetector24.

The synthesis of different alloys into Weyl semimetal crystals can result in a novel type of Weyl semimetal that is characterized by tilted Weyl nodes and an open Fermi surface. This class of Weyl semimetals is identified as type-II if the tilt of the Weyl cone exceeds the Fermi velocity.25–32 Since condensed matter systems do not require Lorentz invariance, Weyl semimetals are not restricted to closed point-like Fermi surfaces, and support type-II Weyl fermions24,25,30. This new type of Weyl fermion appears at the boundary between electron and hole pockets25,30. The experimental signatures of this new phase were recently reported in Refs. 27 and 28. The effects of Weyl cone tilt on the optical conductivity and polarization was recently studied.33 The effect of a tilt on the absorption of circular polarized light was studied for both type-I and type-II cases and it was shown that reversing the tilting direction of Weyl nodes the right-hand and left-hand responses of Weyl semimetal becomes reversed.34 Also, it was found that chirality or the tilt-sign in Weyl semimetals with tilted cones in the absence of time-reversal and inversion symmetries can change the sign of the Weyl contribution to the absorptive Hall conductivity35.

Tunable metamaterial absorbers with active materials have been explored with a variety of different materials.36–39 The broad tunability of the chemical potential in a WS makes it a promising material for photonics and plasmonics applications40–50. The chiral anomaly in a WS can alter surface plasmons and the EM response40,45–50. It has been shown theoretically49 that measurements of the optical conductivity and the temperature dependence of the free carrier response in pyrochlore \( \text{Eu}_2\text{Ir}_2\text{O}_7 \) is consistent with the WS phase. Also, the interband optical conductivity reduces to zero in a continuous fashion at low frequencies as predicted for a WS. The analysis of experimental data resulted in a Fermi velocity on
blocks, as first proposed theoretically. The Hamiltonian describing the low energy physics around the two Weyl nodes, defined by \( s = \pm \), is given by:

\[
H_s(p) = v_F[\beta_s(p_z - sQ) + s\sigma(p - sQe_z)].
\]  

Here \( e_z \) is the unit vector along the \( z \) direction, and we take the Fermi velocity \( v_F \) to be positive. The separation between two Weyl points in the \( z \) direction in momentum space is defined by \( 2|Q| \), where the sign of \( Q \) depends on the sign of the magnetization. The quantities \( \beta_\pm \) are tilting parameters that control the transition between the type-I and type-II phases. For centrosymmetric materials with broken time reversal symmetry, we apply the condition \( \beta_+ = -\beta_- \). The corresponding electron Green functions are given by

\[
G_s(\varepsilon_n, p) = \frac{1}{2} \sum_{t = \pm} \frac{1 + st\sigma p^{(s)}/|p^{(s)}|}{i\varepsilon_n + \mu - v_F[\beta_sp_z^{(s)} + t|p^{(s)}|]},
\]

where the index \( t \) identifies each of the two subbands, \( p^{(s)} = p - sQe_z \), and \( \mu \) is the chemical potential, in which we set \( \mu \geq 0 \) without loss of generality. The fermionic Matsubara frequency is \( \varepsilon_n = \pi T(2n + 1) \), in which \( T \) represents temperature and \( n \) is an integer. The dielectric function \( \varepsilon_{ab}(\omega) \) (where \( a, b = x, y, z \)) is defined through the optical conductivity \( \sigma_{ab} \):
in which \( \alpha = e^2/(4\pi\epsilon_0hR_F) \) and \( \Gamma \sim v_F|Q| \), such that \( \Gamma \gg (\omega, \mu) \) is the high-energy cut-off where applicability of the linear model no longer holds. Here \( \Theta(X) \) represents the usual step function. The remaining components involve integrals, which for \( \Gamma \gg (\omega, \mu) \), are written in the limit of zero temperature:

\[
\epsilon_{zz}(\omega) = 1 - \frac{\pi\alpha}{\omega^2} \sum_{t=\pm 1} \sum_{s=\pm 1} \int \frac{d^3p}{(2\pi)^3} \left\{ -\frac{p_z^2 t \omega_z^2}{4} \frac{\Theta(\mu - \xi_{s,t})}{p^2 + \omega_z^2/4} + \left( \beta_s + t \frac{p_z}{p} \right)^2 \delta(\mu - \xi_{s,t}) \right\} \bigg|_{i\omega_k \rightarrow \omega + i\delta}.
\]

(5c)

It is convenient to separate Fermi surface and vacuum contributions to \( \gamma(\omega) = \sum_{s=\pm} \left[ \gamma^{(s)}_{FS}(\omega) + \gamma^{(s)}_0(\omega) \right] \), where

\[
\gamma^{(s)}_{FS}(\omega) = \frac{8\alpha}{\omega^2} \int_0^{p_+} \int_{-\pi}^{\pi} \int_{-\pi}^{\pi} \frac{dp_z dp_x dp_y}{2\pi^2} \left( \Theta(\mu - \xi_{s,+}) - \Theta(\mu - \xi_{s,-}) - 1 \right) \bigg|_{i\omega_k \rightarrow \omega + i\delta}.
\]

(6)

\[
\gamma^{(s)}_0(\omega) = \frac{8\alpha}{\omega^2} \int_0^{p_+} \int_{-\pi}^{\pi} \int_{-\pi}^{\pi} \frac{dp_z dp_x dp_y}{2\pi^2} \left( \Theta(\mu - \xi_{s,+}) - \Theta(\mu - \xi_{s,-}) - 1 \right) \bigg|_{i\omega_k \rightarrow \omega + i\delta}.
\]

(5d)

in which we have defined \( \xi_{s,t} \equiv tp + p_x \beta_s, p = \sqrt{p_x^2 + p_y^2} \), and a momentum cutoff along the \( z \) axis, \( \Gamma \). Generally, the cut-off \( \Gamma \) is a function of the tilt parameter. Nevertheless, in our calculations, we choose a large enough cut-off and neglect the contribution of \( \beta \) to \( \Gamma \). The cut-off \( \Gamma_0 > v_F|Q| \) is introduced for the correct definition of the vacuum contribution.

### B. Zero tilt phase: \( \beta = 0 \)

It is evident that \( \epsilon_{xx,yy}(\omega) \) are independent of the tilting parameters \( \beta_s \). To reduce \( \Gamma \) to the situation where the Weyl nodes experience no tilt, it suffices to set \( |\beta_+| = |\beta_-| = 0 \). In this case, \( \epsilon_{zz}(\omega) = \epsilon_{xx,yy}(\omega) \), and the off-diagonal frequency dependent component \( \gamma(\omega) \) reduces to

\[
\gamma(\omega) = \frac{2\alpha}{\pi} \frac{v_F Q}{\omega}, \quad (6)
\]

The gyrotropic parameter \( \gamma(\omega) \) can play an important role in changing the polarization state of electromagnetic waves interacting with the WS via Faraday and Kerr rotations.\(^{32}\) The imaginary term in Eq. (5b) describes the interband contribution to the optical conductivity, which exists only when the frequency \( \omega \) of the EM wave satisfies \( \omega > 2\mu \). The interval of frequencies in which \( \epsilon_{xx,yy} \) is real and positive correspond to

\[
2\mu > \omega > 2\mu \sqrt{\frac{\alpha}{3\pi(1 + \frac{\alpha}{3\pi} \ln(\frac{\Gamma_0}{\Gamma}))}}. \quad (7)
\]

Thus, for frequencies around the chemical potential, \( 2\mu > \omega \approx \mu \), the diagonal components \( \epsilon_{xx,yy} \) do not contribute to dissipation in the medium. On the other hand, when \( \omega > 2\mu \), \( \epsilon_{xx,yy} \) acquires an imaginary part, leading to dissipation.

### C. Finite tilt phase: \( \beta \neq 0 \)

We now examine some limiting cases for the integrals in Eqs. (5c) and (5d) when the tilting parameter is nonzero. At the charge neutrality point, \( \mu = 0 \), the off-diagonal gyrotropic component \( \gamma(\omega) \) reduces to

\[
\gamma(\omega) = \frac{\alpha}{\pi} \frac{v_F Q}{\omega} \left[ \min(1, |\beta_+|^{-1}) + \min(1, |\beta_-|^{-1}) \right]. \quad (8)
\]

It is seen that \( \gamma(\omega) \) is independent of the tilt parameter if \( |\beta_+| < 1 \), while inversely proportional to it when \( |\beta_+| > 1 \). The \( \epsilon_{zz} \) component of the dielectric tensor in the limit of zero chemical potential, \( \mu = 0 \), can be calculated exactly as well. For \( |\beta_s| < 1 \), we find

\[
\epsilon_{zz} = 1 + \frac{\alpha}{3\pi} \left[ \ln \left( \frac{4\Gamma^2}{\omega^2} \right) + i\pi \Theta(\omega) \right], \quad (9)
\]

and when the tilt parameter satisfies \( |\beta_s| > 1 \), we arrive at

\[
\epsilon_{zz} = 1 + \frac{\alpha}{3\pi} \left[ \ln \left( \frac{4\Gamma^2}{\omega^2} \right) + i\pi \Theta(\omega) \right] \sum_{s=\pm} \frac{1}{4|\beta_s|} \left( \frac{3 - 1}{\beta_s^2} \right) - \frac{\alpha\Gamma^2}{\pi\omega^2} \sum_{s=\pm} |\beta_s| \left( \frac{3 - 1}{\beta_s^2} \right)^2. \quad (10)
\]

Here the last term describes the contribution from the Fermi pocket, which is bounded by \( \Gamma/\nu \) along the \( z \) axis in momentum space. Thus demonstrating that the real part of \( \epsilon_{zz} \) is always positive, and independent of the tilt parameters if \( |\beta_+| < 1 \). Only when the conical tilt parameters exceed unity (\( |\beta_s| > 1 \)) can the real part of \( \epsilon_{zz} \) become negative or zero, thus allowing for the possibility of an ENZ response. Note that the amplitude of the imaginary component declines monotonically with increasing the tilt parameter \( \beta \).

We now turn our attention to the tilted case when the chemical potential is finite. In general, the integral in Eq. (5c) for \( \epsilon_{zz} \) is highly complicated, and solutions must be obtained numerically. Nonetheless, when \( |\beta_s| < 1 \), it is possible to approximate \( \epsilon_{zz} \) as follows:
Finally, in the limit $\omega \rightarrow 0$, the off-diagonal component has the form

$$
\gamma = \frac{\alpha}{\pi \omega} \left[ \nu_F Q - \sum_{s=\pm} \frac{s \mu}{2 \beta_s} \left( \frac{1}{1 + \beta_s} \ln \left| \frac{1 + \beta_s}{1 - \beta_s} \right| - 2 \right) \right], |\beta_s| \ll 1
$$

(13a)

$$
\gamma = \frac{\alpha}{\pi \omega} \sum_{s=\pm} \left[ \frac{\nu_F Q}{|\beta_s|} - \frac{s \mu}{2 \beta_s} \ln \left| \frac{\beta_s^2}{\mu} \right| \right], |\beta_s| \gg 1.
$$

(13b)

Thus, for fixed $\beta$, these expressions show that for small values of the tilt parameter, $\gamma$ is linear function of $\mu$, declining as the chemical potential increases. For $\beta \gg 1$, $\gamma$ strongly diminishes with $\mu$, eventually changing sign. If on the other hand, we have a set chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu$. In both regimes, at a vanishing chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu$. In both regimes, at a vanishing chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu$. In both regimes, at a vanishing chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu$. In both regimes, at a vanishing chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu$. In both regimes, at a vanishing chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu$. In both regimes, at a vanishing chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu$. In both regimes, at a vanishing chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu$. In both regimes, at a vanishing chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu$. In both regimes, at a vanishing chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu$. In both regimes, at a vanishing chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu$. In both regimes, at a vanishing chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu. In both regimes, at a vanishing chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu. In both regimes, at a vanishing chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu. In both regimes, at a vanishing chemical potential, increasing the tilt also reduces the gyrotropic effect by weakening $\gamma$, and more rapidly for larger $\mu. In both regimes, at a vanishing chemical potential, increasing the tilt also reduc...
tial $\mu \to 0$, we recover our previously discussed results at the charge neutrality point.

D. Susceptibility and epsilon-near-zero responses

When characterizing the nontrivial behavior of $\chi$ in the WS, there are several relevant parameters to consider, including the chemical potential, frequency of the EM wave, tilt of the Weyl cones, and the node separation parameter $Q$, which is taken to be positive. Although it may be possible to generate a mixture of type-I and type-II Weyl points, we consider here the simpler configuration where $\beta_+ = -\beta_- = \beta$. In presenting the results, we write $\omega$ in units of energy, and the complex component $\epsilon_{zz}$, is written in terms of its real and imaginary parts: $\epsilon_{zz} = \epsilon_{zz}' + i\epsilon_{zz}''$. When presenting results, we plot the normalized susceptibility $\chi_{zz}$, defined as $\chi_{zz} \equiv (\epsilon_{zz}' - 1)3\pi/\alpha$. Therefore the ENZ regime corresponds to $\chi_{zz} = -3\pi/\alpha$. We also normalize the dissipative component by $\alpha$. One of the primary aims is to locate in parameter space, the particular $\omega$, $\mu$, and $\beta$ that result in the real part of $\epsilon_{zz} \approx 0$. Therefore, when varying the chemical potential in the WS, we consider a dimensionless $\mu$ ranging from the charge neutrality point, $\mu = 0$, up to $\mu/|v_F|Q| = 0.5$. Similarly, in order to have as complete a picture as possible, a wide spectrum of dimensionless frequencies is considered corresponding to $0.05 \leq \omega/|v_F|Q| \leq 1$. When the frequency is not varying, we set it to its dimensionless value of $\omega/|v_F|Q| = 0.3$. Of particular importance is the tilt of the Weyl cones, which determines the corresponding $\mu$ and $\omega$ that lead to a vanishing of the real part of $\epsilon_{zz}$. A broad range of cone inclinations covering both type-I and type-II scenarios is therefore examined.

When computing the integrals, it is necessary to specify an energy cutoff $\Gamma$. Here we set $\Gamma/|v_F|Q| \sim 8$, recalling that the linearized model breaks down when $\Gamma > |v_F|Q|$, and which is consistent with the requirement $\Gamma \gg (\omega, \mu)$ discussed in conjunction with Eq. (5b). Since the linear model is most suitable away from the Lifshitz transition between type-I and type-II Weyl semimetals, a qualitatively correct description of the system can still be obtained with the linearized model near the transition by simply taking either larger cut-offs, or by incorporating higher order momenta into the linear model.

To begin, in Fig. 1, we examine the frequency response of the normalized susceptibility $\chi_{zz}$ and $\epsilon_{zz}''$ over a broad range of $\beta$. The other diagonal components can be compared by examining the $\beta = 0$ cases, whereby $\epsilon_{xx,yy} = \epsilon_{zz}$. When $\mu = 0$, we calculate $\epsilon_{zz}$ using Eq. (9) for $\beta < 1$ and Eq. (10) for $\beta > 1$. For finite $\mu$ and $\beta < 1$, we utilize the expressions in Eq. (11a) and Eq. (11b). If however the WS is type-II with $\beta > 1$, we must resort to the general integral in Eq. (5c) and solve for $\epsilon_{zz}$ numerically. The results are separated into three columns, where each column represents a different chemical potential, as labeled. Figures 1(a)-1(b) show $\chi_{zz}$ and $\epsilon_{zz}$ when $\mu/|v_F|Q| = 0$, 1(c)-1(d) $\mu/|v_F|Q| = 0.2$, and 1(e)-1(f) when $\mu/|v_F|Q| = 0.4$. Beginning with the charge neutrality point, $\mu/|v_F|Q| = 0$, we see in Figs. 1(a)-1(b) that for $\beta \leq 1$, $\chi_{zz}$ remains positive over the given frequency range, similar to a conventional dielectric. As $\beta$ increases, and the system transitions towards a type-II WS ($\beta > 1$), the susceptibility gets shifted down overall, leading to regions where $\epsilon_{zz}'' < 0$. Indeed, within the type-II regime and $\beta \gg 1$, the ENZ frequency can be found from Eq. (10), to be approximately written as,

$$\omega^2_{\text{ENZ}} \approx \frac{2\alpha}{\pi} |\beta|\Gamma^2.$$  

(14)

The dissipative component does not depend on frequency, and for $\beta \gg 1$, declines towards zero.

Next, in Figs. 1(c)-1(d), the normalized chemical potential is increased to $\mu/|v_F|Q| = 0.2$, so that now the frequency range of interest is shifted accordingly. The top panel shows that for the case $\beta = 0$, a peak in $\chi_{zz}$ arises. This peak emerges due to the inter-band transition, which leads to the singularity arising from the logarithmic term at $\omega = 2\mu$ in Eq. (5b). For most $\beta$, we again find at the lowest frequencies, $\epsilon_{zz}'' < 0$, similar to the behavior of some metals at optical frequencies. Upon increasing $\omega$, $\epsilon_{zz}''$ increases until arriving at the ENZ frequency where $\epsilon_{zz}' = 0$. The bottom panel (d) exhibits the dissipation characteristics of this WS. There are now several distinct features that $\epsilon_{zz}''$ has compared to the $\mu = 0$ case. In particular, for $\beta = 0$, the imaginary component abruptly changes from lossless to lossy at the frequency $\omega = 2\mu$. Increasing $\beta$ causes the dissipation at the transition point to broaden, until $\beta = 1$, after which the imaginary component becomes independent of the tilt parameter. Note that for $\beta < 1$, $\epsilon_{zz}'$ vanishes for $\omega \lesssim 2\mu/(1 + \beta)$, and increases as a function of $\omega$ in the interval $2\mu/(1 + \beta) < \omega < 2\mu/(1 - \beta)$ [See Eq. (11b)]. Lastly, in panels (c) and (d), a larger chemical potential corresponding to the dimensionless value of $\mu/|v_F|Q| = 0.4$ is considered. It is observed that when increasing $\mu$, there is a widening of the frequency window in which the ENZ response occurs. There is also a broadening off the imaginary component resulting in finite dissipation over more frequencies.

One of the salient features of Weyl semimetals is the ability to systematically change their chemical potential. It is possible to shift $\mu$ about the charge neutrality point through doping, varying the temperature, or altering the lattice constant of the material through pressure variations. $^{23,41,42}$ For instance, upon increasing the temperature, the number of thermally excited charged carriers increases near the Weyl points that increases the chemical potential$^{41}$. The injection of various dopants into the Weyl semimetal also can increase the number of free charged carriers, depending on the dopant type$^{42,43,45}$. To examine how changes in $\mu$ can alter the EM response of a WS, we examine in Fig. 2(a) $\chi_{zz}$, and 2(b) the dimensionless $\epsilon_{zz}'$ as functions of $\mu$. Figure 2(a) shows that for $\beta \leq 1$ and $\mu = 0$, all curves originate at $\chi_{zz} = \ln(4\Gamma^2/\omega^2) \approx 7.85$ [see Eq. (9)]. For Weyl cones that are tilted with $\beta \leq 1$, increasing $\mu$ causes a splitting of the curves which then monotonically decline. Further increases in $\beta$ causes $\chi_{zz}$ to shift downward, becoming negative for all $\mu$. Figure 2(b) exhibits how the normalized dissipation $\epsilon_{zz}''/\alpha$ can be drastically manipulated through changes in $\mu$. The type-I case at $\mu = \omega/2$ has an abrupt transition at $\beta = 0$. By increasing the tilt angle of the Weyl cones, the dissipative response broadens and $\epsilon_{zz}''$ is finite over a larger
interval of chemical potentials. This can be of significance in anisotropic ENZ systems with dielectric losses and system parameters are tuned to control beam directivity or EM wave absorption.59,60

Next, in Fig. 3 we investigate how tilting of the Weyl cones influences the normalized susceptibility, 3(a), and dissipation 3(b). Each curve represents different equally spaced $\mu$, normalized as shown in the legend. Starting with $\mu = 0$ and $\beta < 1$, we observe that the permittivity is independent of the tilt, in agreement with Eq. (9). As $\beta$ increases however, $\chi_{zz}$ rapidly drops. The same type of behavior is seen in the other curves with small $\mu$, where regions of relatively constant $\chi_{zz}$ diminish as $\mu$ increases. Thus, when the chemical potential is in the vicinity of the charge neutrality point, only a type-II WS, with $\beta > 1$, can exhibit ENZ behavior. As $\mu$ increases, each corresponding curve gets shifted down towards the ENZ line, so that smaller $\beta$ can lead to a transition to a metallic-like state. Eventually, for the largest chemical potential shown, $\chi_{zz}$ cannot exhibit an ENZ response for any value of tilt. The observed peak at $\omega/\mu = 2$ (corresponding to $\mu/(v_F|Q|) = 0.15$) becomes diminished for other values of $\mu$. For relatively weak chemical potentials, $\mu/(v_F|Q|) \leq 0.2$, an ENZ response is seen to be induced only when the WS is type-II. For $\beta \leq 1$, the ENZ regime arises only for larger $\mu$. For example, the ENZ state is reached at $\beta \approx 0.4$, and $\mu/(v_F|Q|) = 0.45$. Thus, if the Weyl semimetal is to demonstrate an ENZ response, it should be type-I with sufficiently large $\mu$, or it can be type-II with smaller $\mu$. In either case, the dissipative component will be strongly affected, as panel (b) illustrates how cone tilt inclinations strongly influence $\epsilon''_{zz}$. The normalized $\epsilon''_{zz}$ component is shown to not exceed $1/3$. When $\mu/(v_F|Q|) = 0.15$ (or equivalently $\omega/\mu = 2$), the dimensionless $\epsilon''_{zz}$ is constant and has the value $1/6$. Above this value of the chemical potential, the dissipative response tends to decline as $\beta$ increases, while below it, the dissipation increases as $\beta$ increases. At the charge neutrality point $\epsilon''_{zz}$, is unaffected by changes in the tilt for type-I, but for type-II ($\beta \gtrsim 1$), there is a weak decline, according to Eq. (10). Comparing with (a), it is evident that for $\mu/(v_F|Q|) \gtrsim 0.3$, an ENZ response with zero effective loss can be achieved for a type-I WS. This situation could be relevant to waveguide structures, where localized electromagnetic waves propagate over long distances near the surface of the WS.

To estimate the feasibility of achieving an ENZ response in a type-II WS, we consider $Q = 1 \text{ nm}^{-1}$, $\mu = 0.08 \text{ eV}$, $\beta = 1.02$, and $\omega = 0.2 \text{ eV}$, to give $\epsilon''_{zz} \sim 0$, and $\epsilon''_{zz} \sim$
The incident electric and magnetic fields thus have the following forms: 
\[ E = (E_{0x} \hat{x} + E_{0z} \hat{z}) e^{i(k_0 x + k_0 z - \omega t)}, \]
and 
\[ H = H_{0y} \hat{y} e^{i(k_0 x + k_0 z - \omega t)}. \]
Here \( k_0 \) is invariant across each layer, with \( k_{0x} = k_0 \sin \theta, k_{0z} = k_0 \cos \theta \), and \( k_0 = \omega/c \). For both regions \( 0 \) and \( 1 \), we implement Maxwell’s equations for time harmonic fields,

\[ \nabla \times E_i = i\omega \mu_0 H_i, \quad (15a) \]
\[ \nabla \times H_i = -i\omega D_i, \quad (15b) \]

where \( i = 0 \) or \( 1 \). Within the WS, the propagation vector \( k_1 \) replaces the spatial derivatives, transforming Maxwell’s equations into the forms, 
\[ k_1 \times E_1 = \omega \mu_0 H_1 \]
and 
\[ k_1 \times H_1 = -\omega \varepsilon_0 E_1. \]

These two equations together result in the following expression for the \( E_1 \) field in \( k \)-space:

\[ k_1 \times (k_1 \times E_1) = -k_0^2 \varepsilon E_1. \quad (16) \]

Using \( k_1 = k_0 \hat{x} + k_{1z} \hat{z} \), and the identity \( k_1 \times (k_1 \times E_1) = k_1(k_1E_1) - k_1^2 E_1 \), permits expansion of Eq. (16),

\[ \begin{pmatrix}
  \gamma k_1 & i\gamma k_{1z} & k_{1z}k_{ox} \\
  ik_{1z} & k_1 & 0 \\
  k_{ox}k_{1z} & 0 & k_0^2 \varepsilon_{zz} - k_{ox}^2
\end{pmatrix}
\begin{pmatrix}
  E_{1x} \\
  E_{1y} \\
  E_{1z}
\end{pmatrix}
= 0,
\]

where \( k_1 = \sqrt{k_{1x}^2 + k_{1z}^2} \), and \( k_{1x} = k_{0x} \), due to translational invariance. The coupling of all three components of the \( E \) fields in Eq. (17) illustrates that although the electric field of the incident beam is polarized in the \( x-z \) plane, it can now acquire an additional \( y \) component when entering the gyrotropic medium. Similarly, despite having an initial polarization state along the \( x \) direction, the incident \( H \) field can also in general become polarized in all three directions once entering the WS. Thus, the EM wave exiting the WS structure can have a different overall polarization state that depends on the WS material and geometrical parameters.

### B. Results and discussions

Since the incident beam propagates in the \( x-z \) plane with wavevector \( k = \hat{x}k_{0x} + \hat{z}k_{0z} \) (see Fig. 4), each component of \( \varepsilon \) must be accounted for in the EM response of the WS. Taking the determinant of the matrix in Eq. (17) and setting it equal to zero, gives the dispersion equation for the WS that can be solved for \( k_{1z} \):

\[ (\varepsilon_{xx}k_{ox}^2 - k_{1z}^2)(\varepsilon_{xx}\varepsilon_{zz}k_0^2 - \varepsilon_{xx}k_{0x}^2 - \varepsilon_{zz}k_{1z}^2) + k_0^2(k_{0x}^2 - \varepsilon_{zz}k_{0z}^2) = 0. \quad (18) \]

Solving for the roots in Eq. (18) results in two types of solutions to \( k_{1z} \), denoted by \( k_+ \) and \( k_- \). We have,

\[ k_{1z}^2 = \frac{k_0^2}{2\varepsilon_{zz}} \left[ 2\varepsilon_{zz}(\varepsilon_|| + \varepsilon_{zz}) \sin^2 \theta \right. \]
\[ \left. \pm \sqrt{4\varepsilon_{zz}^2 \gamma^2 - 4\varepsilon_{zz}^2 \sin^2 \theta + (\varepsilon_|| - \varepsilon_{zz})^2 \sin^4 \theta} \right]. \quad (19) \]
where $\epsilon_{||}$ represents the components of $\mathbf{\epsilon}$ parallel to the interfaces: $\epsilon_{xx} = \epsilon_{yy} = \epsilon_{||}$. The dispersion equation (18) can now be compactly written in terms of the two types of waves:

$$k_0^2 \epsilon_{zz} (k_{1z}^2 - k_+^2)(k_{1z}^2 - k_-^2) = 0. \quad (20)$$

For the configuration shown in Fig. 4, where the $x$-$y$ plane is translationally invariant, the magnetic field components in the vacuum region, $\mathbf{H}_0$, are written in terms of incident and reflected waves:

$$H_{x0} = r_3 e^{-ik_0x} e^{ik_0zx}, \quad (21a)$$
$$H_{y0} = (e^{ik_0x} + r_1 e^{-ik_0x}) e^{ik_0zy}, \quad (21b)$$
$$H_{z0} = r_2 e^{-ik_0x} e^{ik_0zx}, \quad (21c)$$

where the $x$ and $z$ components represent the change of the incident polarization state upon reflecting from the Weyl semimetal. The coefficients $r_2$ and $r_3$ take into account the generation of additional polarization components upon interacting with the gyrotropic WS layer. Note that from the Maxwell’s equation $\nabla \cdot \mathbf{H}_0 = 0$, there exists a simple relation between the coefficients $r_2$ and $r_3$:

$$r_3 = \frac{k_{0z}}{k_{0x}} r_2. \quad (22)$$

From the magnetic field components above, we can use Eq. (15b) to easily deduce the electric field components for region 0.

For region 1, when using Maxwell’s equations, we need to take into account the anisotropic nature of the WS. The general solution to the $\mathbf{E}$ field in the WS region is thus a linear combination of the four wavevector components $k_{1z} = \{k_+,-k_+,k_-,-k_-\}$:

$$E_{y1} = (a_1 e^{ik_+x} + a_2 e^{-ik_+x} + a_3 e^{ik_-x} + a_4 e^{-ik_-x}) e^{ik_{0x}x}. \quad (23)$$

To determine the coefficients $\{a_1, a_2, a_3, a_4\}$, it is necessary to invoke matching interface conditions and boundary conditions. But first we must construct the remaining $\mathbf{E}$ and $\mathbf{H}$ fields. This is achieved via the two Maxwell’s equations, Eqs. (15a) and (15b). First, using (15b) gives the following relations:

$$\frac{\partial H_{y1}}{\partial z} = i\omega \epsilon_{||} E_{z1} + i\gamma E_{y1}, \quad (24a)$$
$$\frac{\partial H_{x1}}{\partial z} = -ik_{0z} H_{z1} = i\omega \epsilon_{||} E_{x1} - \epsilon_{||} E_{y1}, \quad (24b)$$
$$k_{0x} H_{y1} = -i\omega \epsilon_{zz} E_{z1}. \quad (24c)$$

While, from Eq. (15a) we have,

$$\frac{\partial E_{y1}}{\partial z} = -i\omega \mu_0 H_{z1}, \quad (25a)$$
$$\frac{\partial E_{x1}}{\partial z} = -ik_{0z} E_{z1} = i\omega \mu_0 H_{y1}, \quad (25b)$$
$$k_{0x} E_{y1} = \omega \mu_0 H_{z1}, \quad (25c)$$

where we have used the fact that $x$ component is invariant, i.e., $\partial_x \rightarrow ik_{0x}$. Inserting Eq. (23), into the equations above, it is now possible to write all components of the EM field in terms of the coefficients $\{a_1, a_2, a_3, a_4\}$. For example, $H_{z1}$ and $H_{z1}$ are easily found from Eqs. (25a) and (25c) respectively. From that, one can solve Eq. (24b) for $E_{z1}$, and so on.

Upon matching the tangential electric and magnetic fields at the vacuum/WS interface, and using the boundary conditions of vanishing tangential electric fields at the ground plane, it is straightforward to determine the unknown coefficients. The first reflection coefficient $r_1$ is defined as $r_1 = 1 - r_0$, where

$$r_0 = \frac{2k_-^2 [k_+ q_+^2 \cos(k_-d) \sin(k_-d) - [k_- q_+^2 \cos(k_-d) + ik_{0z}(k_-^2 - k_+^2) \sin(k_-d)] \sin(k_-d)]}{k_- \cos(k_-d) [f_2 \sin(k_-d) + ik_{0z} k_{1z} (k_+^2 - k_+^2) \cos(k_-d)] + \sin(k_-d) [f_1 k_+ \cos(k_-d) - ik_{0z} k_+^2 (k_+^2 - k_-^2) \sin(k_-d)]}, \quad (26)$$

$$k_z = k_0 \sqrt{\epsilon_{zz} - \sin^2 \theta}, \quad q_\pm = \sqrt{\epsilon_{||} k_0^2 - k_{0z}^2 - k_{\pm}^2},$$
$$f_1 = k_0^2 q_+^2 - \epsilon_{zz} k_{0z}^2 q_+^2,$n$$f_2 = -k_0^2 q_+^2 + \epsilon_{zz} k_{0z}^2 q_-^2.$n

The $r_2$ coefficient is expressed compactly in terms of $r_1$ and $r_0$:

$$r_2 = \frac{k_{0z} [k_0^2 (r_1 + 1) \sin(k_-d) - i \epsilon_{zz} k_{0z} k_- r_0 \cos(k_-d)]}{\epsilon_{zz} k_0^2 [ik_{0z} \sin(k_-d) - k_- \cos(k_-d)]} . \quad (27)$$

In the absence of gyrotropy, $\gamma = 0$, $r_2 = r_3 = 0$, and the corresponding reflection coefficient $r_1$ reduces to

$$r_1 = 1 - \frac{2k_-}{k_- + ik_{0z} \epsilon_{||} \cot(k_-d)}, \quad (28)$$

in which $k_- = \sqrt{\epsilon_{||} (k_{0z}^2 - k_+^2) / \epsilon_{zz}}$. Thus, when $\gamma = 0$, the reflection coefficient reverts to that of a diagonally anisotropic medium, as it should. When the gyrotropic parameter van-
The system is in the ENZ regime, whereby \( \varepsilon'_{zz} = 0 \). The normalized frequency is set to \( \omega/(v_F|Q|) = 0.3 \), and \( d/\lambda = 1/100 \).

The absorptance \( A \) varies as a function of the incident angle \( \theta \) and dissipation \( \varepsilon''_{zz} \). Here \( A \) is defined as \( A = 1 - |r_1|^2 - |r_2|^2 - |r_3|^2 \). For a given WS width \( d \), frequency \( \omega \) of the incident wave, and orientation \( \theta \), the absorption [Eq. (29)] can be calculated by incorporating the results of Sec. II, which gives the various \( \mu \) and \( \beta \) that lead to an ENZ response, and allows the remaining components of the tensor \( \mathbf{\varepsilon} \) to be determined via Eqs. (5b)-(5d).

The results from Sec. II offer clear guides for identifying ENZ regions of the parameter space. For example, it was observed in Fig. 1, that for the range of frequencies considered, it is necessary for the chemical potential to be nonzero for the dissipative component \( \varepsilon''_{zz} \) to have significant variations. We show below that \( \varepsilon''_{zz} \) plays a crucial role in determining how much of the incident beam is perfectly absorbed\(^{29}\), and that strong absorption can arise over a broader range of \( \theta \) not only when \( \varepsilon''_{zz} \) corresponds to moderate loss, but also when it is very small. Thus, we focus on the more interesting cases when \( \mu \) is away from the charge neutrality point (\( \mu = 0 \)). Indeed, Figs. 1(c)-1(f) showed that by having a finite \( \mu \), \( \varepsilon''_{zz} \) can be continuously tuned from zero to a situation having appreciable dissipation. If the dissipation vanishes entirely, the type of perfect absorption studied here does not arise since all incoming waves are reflected back from the ground plane. Increasing the loss makes it possible at appropriate frequencies and orientations of the incident beam, for the waves in the WS to destructively interact and ultimately dissipate through Joule heating. For most of the frequencies of interest here, which satisfy \( \omega/(v_F|Q|) < 2\mu/(v_F|Q|) \), the component of the permittivity parallel to the interfaces \( \varepsilon_{||} \) [Eq. (5b)], is purely real, as it has no interband contribution to the optical conductivity.

To illustrate how \( \varepsilon''_{zz} \) directly impacts the absorption characteristics of the WS structure shown in Fig. 4, we present in Fig. 5, a color map that depicts the absorptance \( A \) as a function of the incident angle \( \theta \). A broad range of normalized chemical potentials are considered (see legend). For \( \mu/(v_F|Q|) = 0.29, 0.28, 0.27, 0.25, \) and 0.2, the Weyl semimetal should be type-I, with \( \beta \approx 0.94, 0.96, 0.97, 0.98, \) and 0.99, respectively. To achieve perfect absorption for larger incident angles that more closely approach grazing (\( \theta \to 90^\circ \)), the \( \mu/(v_F|Q|) = 0.15 \) case requires a type-II WS, with \( \beta \approx 1.01 \). In all cases the normalized frequency is set to \( \omega/(v_F|Q|) = 0.3 \), and \( d/\lambda = 1/100 \).

In determining the absorptance \( A \) of the WS system, it is beneficial to study the energy flow in the vacuum region. To this end, we consider the time-averaged Poynting vector in the direction perpendicular to the interfaces (the \( z \) direction), \( S_{zz} = |E_{x0}H_{z0}^* - E_{y0}H_{x0}^*|/2 \). Inserting the electric and magnetic fields calculated for region 10 above, we find,

\[
A = 1 - |r_1|^2 - |r_2|^2 - |r_3|^2. \tag{29}
\]

Here \( A \) is defined as \( S_{zz}/S_0 \), where \( S_0 \equiv k_0/2\epsilon_0\omega \) is the time-averaged Poynting vector for a plane wave traveling in the \( z \) direction.

Having established the methods for determining the absorption and reflection coefficients, we now consider a range of material and geometrical parameters that lead to perfect absorption in the ENZ regime where \( \varepsilon''_{zz} \approx 0 \). The dissipative component \( \varepsilon''_{zz} \) on the other hand can vary, as it plays a crucial role in how electromagnetic energy is absorbed by the system.
FIG. 8. (Color online). Color maps illustrating the perfect absorption regions for various normalized widths \(d/\lambda\) and incident angles \(\theta\). In (a) \(\beta \sim 1.01\), and \(\mu/(v_F|Q|) = 0.15\). In panel (b) \(\beta \sim 0.96\), and \(\mu/(v_F|Q|) = 0.28\). In both panels the normalized frequency is set to \(\omega/(v_F|Q|) = 0.3\).

ponent. As was extensively discussed in Sec. II, \(\varepsilon_{zz}''\) generally depends on several system parameters. Here however, in order to isolate the effects of dissipation and its relation to angles of high absorption, \(\varepsilon_{zz}''\) varies independently. In this example, we have \(\mu/(v_F|Q|) = 0.2\), and \(\gamma = 3\). As Fig. 5 shows, depending on \(\varepsilon_{zz}''\), perfect absorption can be achieved for virtually any incident angle. Thus, for example, to determine the WS parameter needed to achieve perfect absorption around normal incidence (\(\theta \sim 0^\circ\)), it is only necessary to identify configurations where \(\varepsilon_{zz}'' \approx 0\) for small \(\varepsilon_{zz}'\). The fact that for angles near normal incidence, the loss must be extremely weak for perfect absorption is consistent with the response of isotropic ENZ slabs\(^1\). On the other hand, to have the entire incident wave’s energy absorbed at broader angles (\(\theta \sim 90^\circ\)), the ENZ structure must exhibit greater dissipation, with \(\varepsilon_{zz}'' \gtrsim 0.3\). The occurrence of perfect absorption in thin, anisotropic ENZ layers is one of the hallmarks of coherent perfect absorption\(^2\), which couples light to a fast wave propagating along the WS interface. A main feature of coherent perfect absorption is the intricate dependence on the real and imaginary parts of \(\varepsilon_{zz}\) which can lead to the formation of localized waves inside very narrow regions. The perfect conductive substrate serves as the reflecting surface that results in the destructive interference of incoming waves, so that under the proper conditions, the incident beam becomes completely absorbed.

Previously, in Fig. 2, we found that by tuning the chemical potential, not only can an ENZ response be achieved, but also that the loss in the WS can be highly sensitive to changes in \(\mu\). To study the effects that variations in \(\mu\) have on the EM response of the WS, in Fig. 6, we present the absorptance of the WS structure as a function of the normalized \(\mu\). Three different orientations of the incident wave are considered, as shown in the legend. We consider a representative value for a type-II case, \(\beta = 1.01\), which according to Fig. 2, puts the system in the ENZ regime at \(\mu/(v_F|Q|) \approx 0.17\). For this value of the chemical potential, the loss corresponds to \(\varepsilon_{zz}'' \approx 0.3\). The remaining components of the permittivity tensor are calculated from Eqs. (5b) and (5d), resulting in \(\varepsilon_{\parallel} \approx 2.8\), and \(\gamma \approx 2.9\). Note that while conventional absorbers are often restricted by their relatively large thicknesses, remarkably the WS layer exhibited here has an extremely subwavelength thickness, corresponding to \(d/\lambda = 1/100\). Thus, for an incident wavelength of \(\lambda \sim 10\mu m\), this implies \(d \sim 100\) nm. We note that the results are relatively insensitive to \(\varepsilon_{zz}\). Moreover, for the narrow WS widths considered here, the off-diagonal gyrotronic component \(\gamma\) has a limited effect on the results, so that Eq. (28) is often suitable for describing the reflection characteristics over a broad range of parameters. Overall, we find that the phenomenon presented here are dictated mainly by \(\varepsilon_{zz}\). This is consistent with the results of Fig. 6, where weak absorption occurs for smaller \(\theta\), but when \(\theta = 80^\circ\), there is complete absorption. As Fig. 5 showed, increases in the dissipative component \(\varepsilon_{zz}''\) require that the incident waves approach the interface at larger \(\theta\) in order to be absorbed perfectly.

We now proceed to show that for certain \(\mu\) and tilting \(\beta\), both type-I and type-II WS systems can completely absorb the incident EM radiation over a relatively wide range of incident wave orientations \(\theta\). In Fig. 7, the absorptance is shown as a function of \(\theta\) for a few normalized \(\mu\) (see legend). For chemical potentials outside of this range, the imaginary component \(\varepsilon_{zz}''\) is either too small or too large to achieve perfect absorption (see Fig. 2). The subwavelength slab width is again fixed at \(d/\lambda = 1/100\), and the incident wave has a frequency corresponding to \(\omega/(v_F|Q|) = 0.3\). Beginning with the largest chemical potential, \(\mu/(v_F|Q|) = 0.29\), we find that perfect absorption occurs at close to normal incidence. This is because as Fig. 2(b) showed, when \(\mu/(v_F|Q|) = 0.29\), a very small amount of loss is present. Therefore, from Fig. 5, \(\theta\) must be small in order for the incident beam to couple to the EM modes responsible for perfect absorption. Besides having loss, it is also necessary for \(\varepsilon_{zz}'' \approx 0\), which as in Fig. 2(a) shows, only small \(\beta < 1\) in this case results in an ENZ response. By decreasing the chemical potential, the WS becomes more dissipative. Thus we find that each of the perfect absorption peaks in Fig. 7 gets shifted towards grazing incidence (\(\theta \rightarrow 90^\circ\)). This however requires greater tilting of the Weyl cones to achieve \(\varepsilon_{zz}'' = 0\), which in some instances, corresponds to a type-II situation where \(\beta\) exceeds unity (see
Finally, to show the importance of using subwavelength WS structures in the ENZ regime to achieve perfect absorption, we investigate how changes in the width $d$ of the WS (see Fig. 4) affects the absorption properties of the system. In Fig. 8, the color maps depict the absorbance as a function of the normalized width $d/\lambda$ and incident angle $\theta$. Both types of WS are considered: (a) type-II with $\beta = 1.01$, and (b) type-I with $\beta = 0.96$. In panel (a) $\mu/(v_F|Q|) = 0.15$, which corresponds to $\epsilon_{zz} \approx 0.12 + 0.37i$, and a gyrotropic parameter of $\gamma \approx 3$. In (b) the chemical potential is increased to $\mu/(v_F|Q|) = 0.28$, so that the WS still has $\epsilon_{zz}$ in the ENZ regime, but with very little loss, corresponding to a small imaginary component $\epsilon_{zz}' \approx 0.005$. The gyrotropic parameter is relatively unchanged from the previous case, with now $\gamma \approx 3.1$. For both panels, the normalized frequency is set at $\omega/(v_F|Q|) = 0.3$. It is evident that the type-II WS in (a) admits perfect absorption over larger angles, and that the normalized width should satisfy $d/\lambda \lesssim 1/10$ for appreciable absorption. As the incident beam is directed more towards grazing angles ($\theta \to 90^\circ$), it is apparent that $d$ must be continuously reduced in order for the system to remain a perfect absorber. For widths that are larger than the range shown here, coupling between the incident beam and the WS system becomes substantially diminished as additional reflections are introduced that destroy the previous coherent effects. For the type-I case (b), the widths again need to be subwavelength, satisfying $d/\lambda \lesssim 1/10$, and as mentioned above, perfect absorption arises at small inclinations of the incident beam due to the weakly dissipative nature of $\epsilon_{zz}$ for these system parameters. We also see a trend similar to the type-II case in (a), where increases in $\theta$ require thinner WS widths to achieve $A \approx 1$.

In this paper, we studied the dielectric response of anisotropic type-I and type-II tilted Weyl semimetals. We presented both analytic and numerical results that characterized each component of the permittivity tensor. We showed that depending on the Weyl cone tilt, chemical potential and electromagnetic wave frequency, the component of the permittivity tensor normal to the interfaces can achieve an epsilon-near-zero (ENZ) response. At the charge neutrality point, we showed that only type-II Weyl semimetals can exhibit an ENZ response. We also discussed how losses near the ENZ frequency can be controlled and effectively eliminated by properly adjusting the Weyl cone tilt and chemical potential. Making use of the calculated permittivity tensor for the Weyl semimetal, we also investigated the electromagnetic response of a Weyl semimetal structure consisting of a planar Weyl semimetal adjacent to a perfect conductor in vacuum. Our findings showed that thin Weyl semimetals with an ENZ response can be employed as coherent perfect absorbers for nearly any incident angle, by choosing the proper geometrical and material parameters.

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2. A. Alù, M. G. Silveirinha, A. Salandrino, and N. Engheta, Phys. Rev. B 75, 155410 (2007).


