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Critical behavior and magnetocaloric effect in $\text{Mn}_3\text{Si}_2\text{Te}_6$

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The critical properties and magnetocaloric effect of semiconducting ferrimagnet $\text{Mn}_3\text{Si}_2\text{Te}_6$ single crystals have been investigated by bulk magnetization and heat capacity around T_c . Critical exponents $\beta = 0.41 \pm 0.01$ with a critical temperature $T_c = 74.18 \pm 0.08$ K and $\gamma = 1.21 \pm 0.02$ with $T_c = 74.35 \pm 0.05$ K are deduced by the Kouvel-Fisher plot, whereas $\delta = 4.29 \pm 0.05$ (3.40 ± 0.02) is obtained by a critical isotherm analysis at $T = 74$ (75) K. The magnetic exchange distance is found to decay as $J(r) \approx r^{-4.79}$, which lies between the mean-field and 3D Heisenberg models. Moreover, the magnetic entropy change $-\Delta S_M$ features a maximum at T_c , i.e., $-\Delta S_M^{max} \sim 2.53$ (1.67) J kg $^{-1}$ K $^{-1}$ with in-plane(out-of-plane) field change of 5 T, confirming large magnetic anisotropy. The heat capacity measurement further gives $-\Delta S_M^{max} \sim 2.94$ J kg $^{-1}$ K $^{-1}$ and the corresponding adiabatic temperature change $\Delta T_{ad} \sim 1.14$ K with out-of-plane field change of 9 T.

I. INTRODUCTION

Layered intrinsically ferromagnetic (FM) semiconductors hold great promise for both fundamental physics and applications in spintronic devices.¹⁻⁴ CrI_3 has recently attracted much attention since the long-range magnetism persists in monolayer with T_c of 45 K.⁵ Intriguingly, the magnetism in CrI_3 is layer-dependent, from FM in monolayer, to antiferromagnetic (AFM) in bilayer, and back to FM in trilayer.⁶ It can further be controlled by electrostatic doping, providing great opportunities for designing magneto-optoelectronic devices.^{7,8}

Ternary $\text{Cr}_2\text{X}_2\text{Te}_6$ ($\text{X} = \text{Si}, \text{Ge}$) exhibit FM order below T_c of 32 K for $\text{Cr}_2\text{Si}_2\text{Te}_6$ and 61 K for $\text{Cr}_2\text{Ge}_2\text{Te}_6$, respectively,⁹⁻¹¹ and also promising candidates for long-range magnetism in nanosheets.¹²⁻¹⁴ Many efforts have been devoted to shed light on the nature of FM in this system.¹⁵⁻¹⁷ Multiple domain structure types, self-fitting disks and fine ladder structure within the Y-connected walls, were observed by magnetic force microscopy,¹⁸ confirming two-dimensional (2D) long-range magnetism with non-negligible interlayer coupling.¹⁹ $\text{Mn}_3\text{Si}_2\text{Te}_6$ is a little-studied three-dimensional (3D) analog of $\text{Cr}_2\text{Si}_2\text{Te}_6$.²⁰⁻²² The $\text{Mn}_2\text{Si}_2\text{Te}_6$ layer is composed of MnTe_6 octahedra that are edge sharing within the ab plane (Mn1 site) and along with Si-Si dimers [Fig. 1(a)], similar to $\text{Cr}_2\text{Si}_2\text{Te}_6$. However, the layers are connected by filling one-third of Mn atoms at the Mn2 site within interlayer, yielding a composition of $\text{Mn}_3\text{Si}_2\text{Te}_6$.²³ Recent neutron diffraction experiment gives that $\text{Mn}_3\text{Si}_2\text{Te}_6$ is a ferrimagnet below $T_c \approx 78$ K and the moments lie within the ab plane.²⁴

In the present work we investigated the critical behavior of $\text{Mn}_3\text{Si}_2\text{Te}_6$ single crystal by using modified Arrott plot, Kouvel-Fisher plot and critical isotherm analysis, as well as its magnetocaloric effect. Critical exponents $\beta = 0.41$ (1) with $T_c = 74.18$ (8) K, $\gamma = 1.21$ (2) with $T_c = 74.35$ (5) K, and $\delta = 4.29$ (5) at $T = 74$ K. The magnetic exchange distance is found to decay as $J(r) \approx r^{-4.79}$,

which lies between mean-field and 3D Heisenberg models. The rescaled $-\Delta S_M(T, H)$ curves can well collapse onto a universal curve, confirming its nature of second-order.

II. METHODS

A. Experimental details

Single crystals of $\text{Mn}_3\text{Si}_2\text{Te}_6$ were fabricated by melting stoichiometric mixture of Mn (3N, Alfa Aesar) chip, Si (5N, Alfa Aesar) lump and Te (5N, Alfa Aesar) shot. Starting materials were vacuum-sealed in a quartz tube, heated to 1100 °C over 20 h and then cooled to 850 °C at a rate of 1 °C/h. X-ray diffraction (XRD) data were taken with Cu K_α ($\lambda = 0.15418$ nm) radiation of a Rigaku Miniflex powder diffractometer. The magnetization and heat capacity were collected in Quantum Design MPMS-XL5 and PPMS-9 systems. The magnetic entropy change $-\Delta S_M$ from the magnetization data was estimated using a Maxwell relation.

B. Scaling analysis

According to the scaling hypothesis, the second-order phase transition around the Curie point T_c is characterized by a set of interrelated critical exponents $\alpha, \beta, \gamma, \delta, \eta, \nu$ and a magnetic equation of state.²⁵ The exponent α can be obtained from specific heat and β and γ from spontaneous magnetization M_s and inverse initial susceptibility χ_0^{-1} , below and above T_c , respectively, while δ is the critical isotherm exponent. The mathematical definitions of the exponents from magnetization measurement are given below:

$$M_s(T) = M_0(-\varepsilon)^\beta, \varepsilon < 0, T < T_c, \quad (1)$$

$$\chi_0^{-1}(T) = (h_0/m_0)\varepsilon^\gamma, \varepsilon > 0, T > T_c, \quad (2)$$

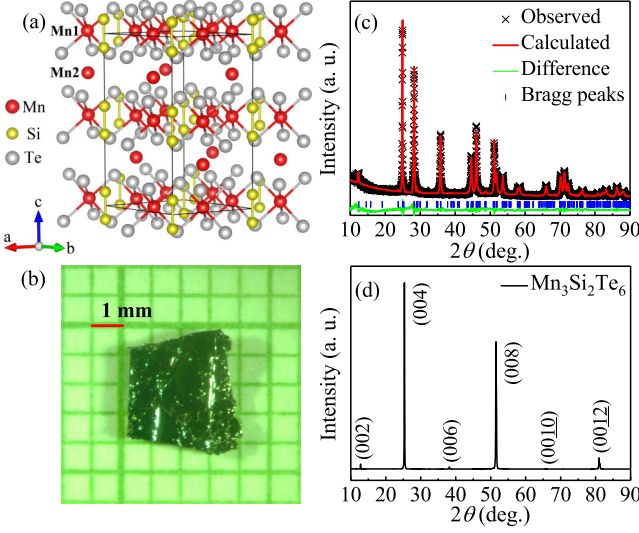


FIG. 1. (Color online) (a) Crystal structure and (b) representative single crystal of $\text{Mn}_3\text{Si}_2\text{Te}_6$. (c) Powder x-ray diffraction (XRD) and (d) single-crystal XRD patterns of $\text{Mn}_3\text{Si}_2\text{Te}_6$ at room temperature. The vertical tick marks represent Bragg reflections of the $P\bar{3}1c$ space group.

$$M = DH^{1/\delta}, T = T_c, \quad (3)$$

where $\varepsilon = (T - T_c)/T_c$ is the reduced temperature, and M_0 , h_0/m_0 and D are the critical amplitudes.[?]

The magnetic equation of state in the critical region is expressed as

$$M(H, \varepsilon) = \varepsilon^\beta f_\pm(H/\varepsilon^{\beta+\gamma}), \quad (4)$$

where f_+ for $T > T_c$ and f_- for $T < T_c$, respectively, are the regular functions. Eq.(4) can be further written in terms of scaled magnetization $m \equiv \varepsilon^{-\beta} M(H, \varepsilon)$ and scaled field $h \equiv \varepsilon^{-(\beta+\gamma)} H$ as

$$m = f_\pm(h). \quad (5)$$

This suggests that for true scaling relations and the right choice of β , γ , and δ values, scaled m and h will fall on universal curves above T_c and below T_c , respectively.

III. RESULTS AND DISCUSSIONS

The powder XRD pattern of $\text{Mn}_3\text{Si}_2\text{Te}_6$ confirms high purity of the single crystals, in which the observed peaks can be well fitted with the $P\bar{3}1c$ space group [Fig. 1(c)]. The determined lattice parameters $a = 7.046(2)$ Å and $c = 14.278(2)$ Å are very close to the reported values.[?] ? In the single-crystal XRD [Fig. 1(d)], only (00 l) peaks are detected, indicating that the crystal surface is parallel to the ab plane and perpendicular to the c axis.

Figure 2 presents the temperature dependence of magnetization measured in $H = 1$ and 50 kOe applied in the ab plane and parallel to the c axis, respectively. The

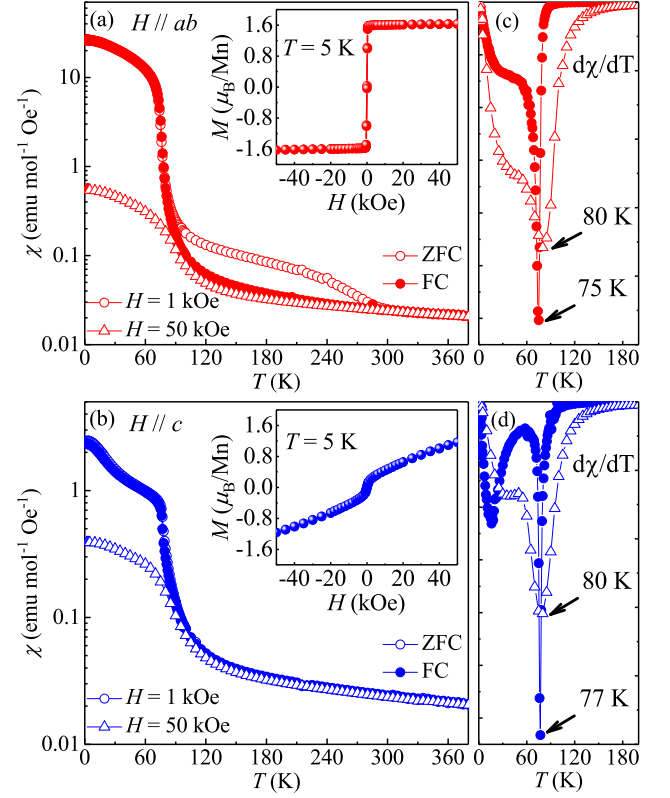


FIG. 2. (Color online) Temperature dependence of dc magnetic susceptibility χ and corresponding $d\chi/dT$ for $\text{Mn}_3\text{Si}_2\text{Te}_6$ measured in the magnetic field $H = 1$ and 50 kOe applied (a,c) in the ab plane and (b,d) along the c axis, respectively. Insets: field dependence of magnetization measured at $T = 5$ K.

magnetization is nearly isotropic in 50 kOe, however, significant magnetic anisotropy is observed in 1 kOe at low temperatures. The ordered moments lie primarily within the ab plane. An additional upturn well above T_c till to 300 K is clearly seen in zero-field-cooling (ZFC) curve for $\mathbf{H} // \mathbf{ab}$, which may be associated with short-range order or the presence of correlated excitations in the paramagnetic region.[?] Isothermal magnetization at $T = 5$ K [insets in Fig. 2] shows saturation moment of $M_s \approx 1.6 \mu_B/\text{Mn}$ for $\mathbf{H} // \mathbf{ab}$ and a small FM component for $\mathbf{H} // \mathbf{c}$. No remanent moment for either orientation confirms the crystal of high quality. The T_c can be roughly determined by the minimum of $d\chi/dT$ [Figs. 2(c,d)], i.e., $T_c = 75$ K for in-plane field and $T_c = 77$ K for out-of-plane field of 1 kOe, which shifts to $T_c = 80$ K in an increase field of 50 kOe.[?]

From the Landau theory of phase transition, the Gibbs free energy G for FM-paramagnetic(PM) transition can be expressed as

$$G(T, M) = G_0 + aM^2 + bM^4 - MH, \quad (6)$$

where the equilibrium magnetization M is the order parameter, and the coefficients a and b are the temperature-dependent parameters. At equilibrium $\partial G/\partial M = 0$ (i.e.,

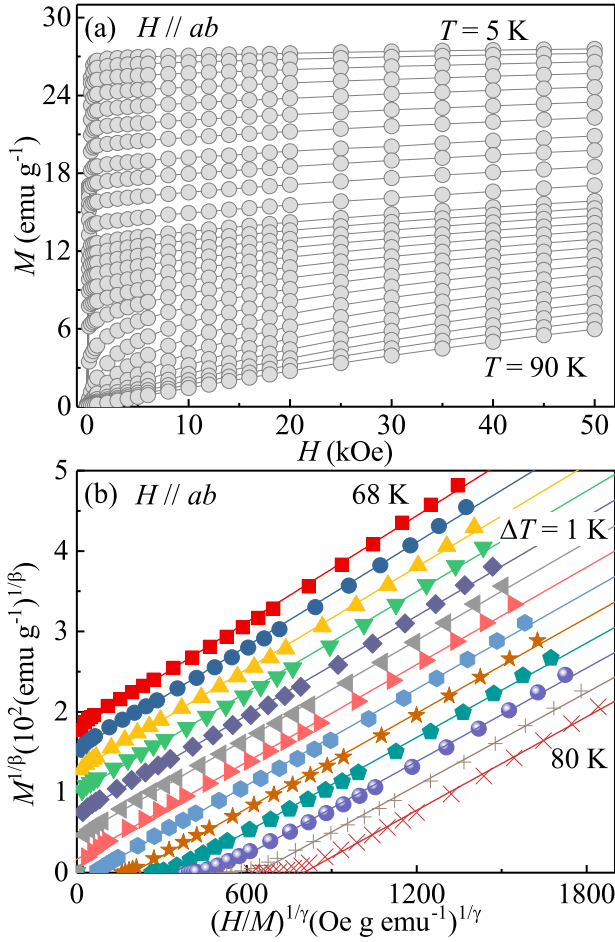


FIG. 3. (Color online) (a) Typical initial isothermal magnetization curves measured in $\mathbf{H} // \mathbf{ab}$ from 5 to 90 K for $\text{Mn}_3\text{Si}_2\text{Te}_6$. (b) the modified Arrott Plot around T_c for the optimum fitting with $\beta = 0.41$ and $\gamma = 1.21$.

energy minimization) and the magnetic equation of state can be expressed as

$$H/M = 2a + 4bM^2. \quad (7)$$

Thus, the Arrott plot of M^2 vs H/M should appear as parallel straight lines for different temperatures above and below T_c in the high field region.⁷ The intercepts of M^2 on the H/M axis is negative or positive depending on phenomena below or above T_c and the line at T_c passes through the origin. In order to properly determine the T_c as well as the critical exponents β , γ , and δ , the modified Arrott plot with a self-consistent method was used.^{7, 8} Figure 3 presents the initial isotherms ranging from 5 to 90 K and the modified Arrott plot of $M^{1/\beta}$ vs $(H/M)^{1/\gamma}$ around T_c for $\text{Mn}_3\text{Si}_2\text{Te}_6$. This gives $\chi_0^{-1}(T)$ and $M_s(T)$ as the intercepts on the H/M axis and positive M^2 axis, respectively.

Figure 4(a) exhibits the final $M_s(T)$ and $\chi_0^{-1}(T)$ as a function of temperature. According to Eqs. (1) and (2), the critical exponents $\beta = 0.41(1)$ with $T_c = 74.21(1)$ K,

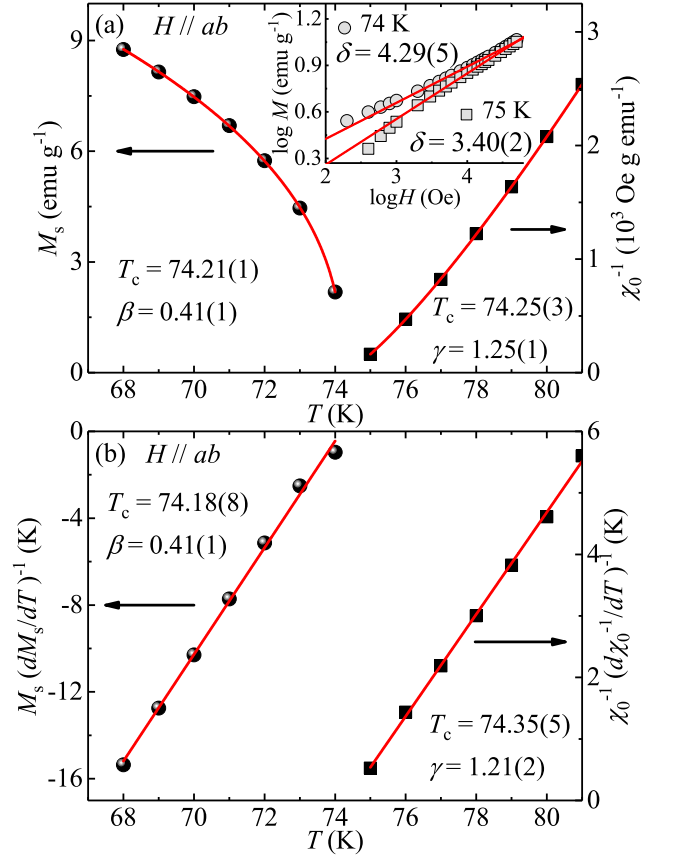


FIG. 4. (Color online) (a) Temperature dependence of the spontaneous magnetization M_s (left) and the inverse initial susceptibility χ_0^{-1} (right) with solid fitting curves. Inset shows $\log M$ vs $\log H$ collected at 74 and 75 K with linear fitting curves. (b) Kouvel-Fisher plots of $M_s(dM_s/dT)^{-1}$ (left) and $\chi_0^{-1}(d\chi_0^{-1}/dT)^{-1}$ (right) with solid fitting curves.

and $\gamma = 1.25(1)$ with $T_c = 74.25(3)$ K, are obtained. In addition, there is also the Kouvel-Fisher (KF) relation,⁹

$$M_s(T)[dM_s(T)/dT]^{-1} = (T - T_c)/\beta, \quad (8)$$

$$\chi_0^{-1}(T)[d\chi_0^{-1}(T)/dT]^{-1} = (T - T_c)/\gamma. \quad (9)$$

Linear fittings to the plots of $M_s(T)[dM_s(T)/dT]^{-1}$ and $\chi_0^{-1}(T)[d\chi_0^{-1}(T)/dT]^{-1}$ vs T in Fig. 4(b) yield $\beta = 0.41(1)$ with $T_c = 74.18(8)$ K, and $\gamma = 1.21(2)$ with $T_c = 74.35(5)$ K. The third exponent δ can be calculated from the Widom scaling relation $\delta = 1 + \gamma/\beta$. From β and γ obtained with the modified Arrott plot and the Kouvel-Fisher plot, $\delta = 4.05(5)$ and $3.95(2)$ are obtained, respectively, which are close to the direct fits of δ taking into account that $M = DH^{1/\delta}$ near T_c [$\delta = 4.29(5)$ at 74 K and $3.40(2)$ at 75 K, inset in Fig. 4(a)].

Scaling analysis can be used to estimate the reliability of the obtained critical exponents and T_c . From Eq. (5), scaled m vs scaled h , all the data collapse on two separate branches below and above T_c , as depicted in Fig. 5. The

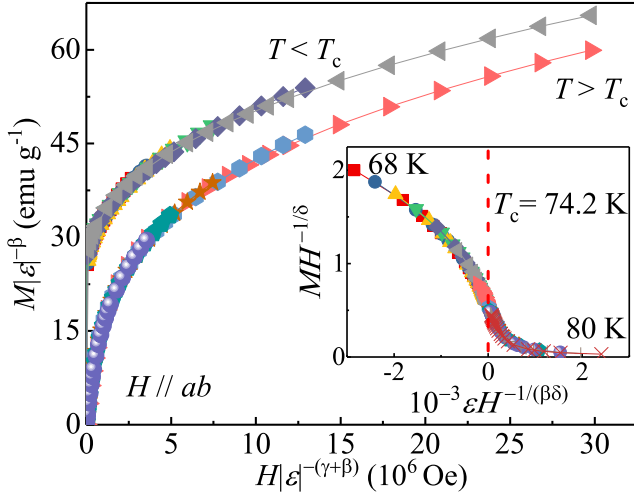


FIG. 5. (Color online) Scaled magnetization m vs scaled field h below and above T_c for $\text{Mn}_3\text{Si}_2\text{Te}_6$. Inset: the rescaling of the $M(H)$ curves by $MH^{-1/\delta}$ vs $\varepsilon H^{-1/(\beta\delta)}$.

scaling equation of state takes another form,

$$\frac{H}{M^\delta} = k\left(\frac{\varepsilon}{H^{1/\beta}}\right), \quad (10)$$

where $k(x)$ is the scaling function. From Eq. (10), all the data should also fall into a single curve. This is indeed seen [inset in Fig. 5]; the $MH^{-1/\delta}$ vs $\varepsilon H^{-1/(\beta\delta)}$ experimental data for $\text{Mn}_3\text{Si}_2\text{Te}_6$ collapse into a single curve and the T_c locates at the zero point of the horizontal axis. The well-rescaled curves further confirm the reliability of the obtained critical exponents.

Next, it is important to understand the nature as well as the range of interaction in this material. In a homogeneous magnet the universality class of the magnetic phase transition depends on the exchange distance $J(r)$. In renormalization group theory analysis the interaction decays with distance r as

$$J(r) \approx r^{-(3+\sigma)}, \quad (11)$$

where σ is a positive constant.⁷ Moreover, the susceptibility exponent γ is predicted as

$$\gamma = 1 + \frac{4}{d} \left(\frac{n+2}{n+8} \right) \Delta\sigma + \frac{8(n+2)(n-4)}{d^2(n+8)^2} \times \left[1 + \frac{2G(\frac{d}{2})(7n+20)}{(n-4)(n+8)} \right] \Delta\sigma^2, \quad (12)$$

where $\Delta\sigma = (\sigma - \frac{d}{2})$ and $G(\frac{d}{2}) = 3 - \frac{1}{4}(\frac{d}{2})^2$, n is the spin dimensionality.⁷ When $\sigma > 2$, the Heisenberg model is valid for 3D isotropic magnet, where $J(r)$ decreases faster than r^{-5} . When $\sigma \leq 3/2$, the mean-field model is satisfied, expecting that $J(r)$ decreases slower than $r^{-4.5}$. In the present case, $\sigma = 1.79$, then the correlation length critical exponent $\nu = 0.676$ ($\nu = \gamma/\sigma$), and $\alpha = -0.028$

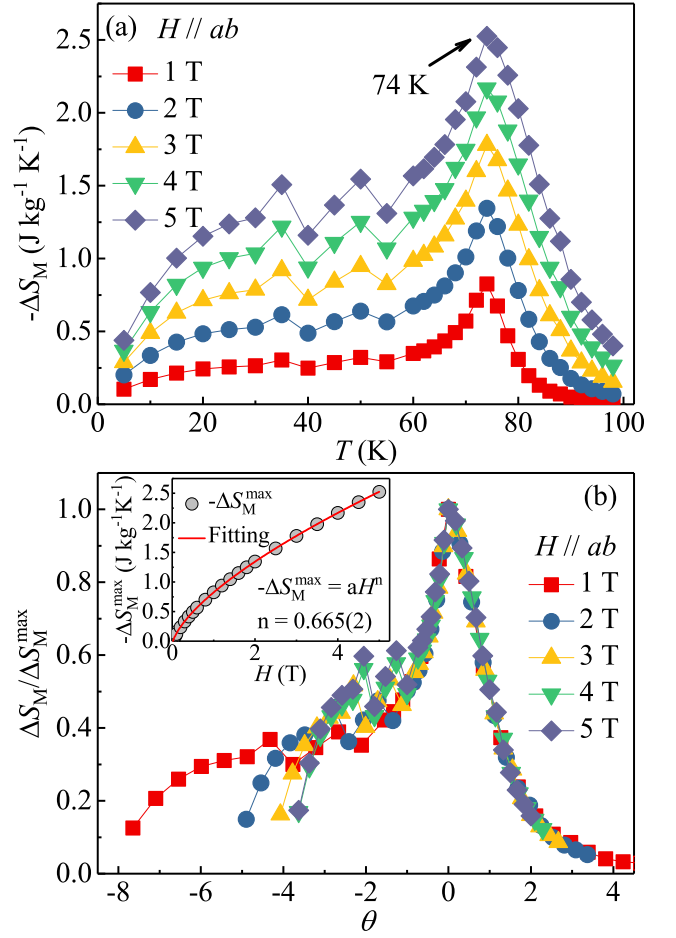


FIG. 6. (Color online) (a) The magnetic entropy change $-\Delta S_M$ obtained from magnetization at various magnetic fields change in the ab plane. (b) Normalized ΔS_M as a function of the rescaled temperature θ . Inset: magnetic field dependence of the maximum magnetic entropy change $-\Delta S_M^{\max}$ with power law fitting in red solid line.

($\alpha = 2 - \nu d$). It is found that the magnetic exchange distance decays as $J(r) \approx r^{-4.79}$, which lies between that of 3D Heisenberg model and mean-field model.

Then we estimate its magnetic entropy change

$$\Delta S_M(T, H) = \int_0^H \left[\frac{\partial S(T, H)}{\partial H} \right]_T dH. \quad (13)$$

With the Maxwell's relation $\left[\frac{\partial S(T, H)}{\partial H} \right]_T = \left[\frac{\partial M(T, H)}{\partial T} \right]_H$, it can be further written as:⁷

$$\Delta S_M(T, H) = \int_0^H \left[\frac{\partial M(T, H)}{\partial T} \right]_H dH. \quad (14)$$

In the case of magnetization measured at small discrete magnetic field and temperature intervals [Fig. 3(a)],

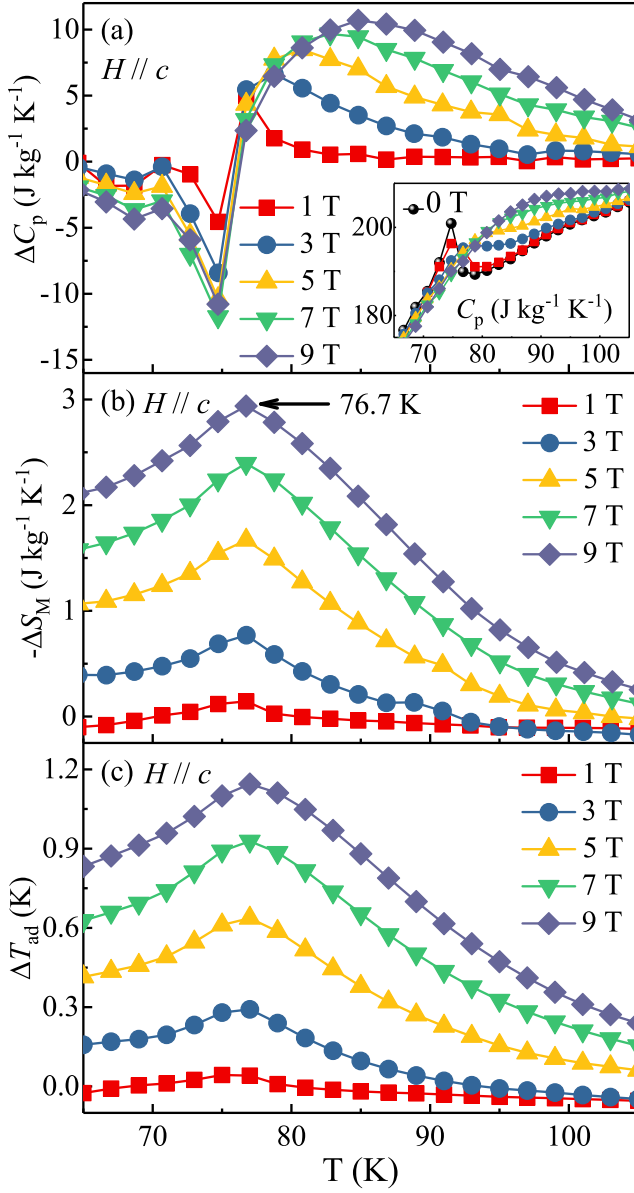


FIG. 7. (Color online) Temperature dependences of (a) the specific heat change ΔC_p , (b) the magnetic entropy change $-\Delta S_M$ and (c) the adiabatic temperature change ΔT_{ad} for $\text{Mn}_3\text{Si}_2\text{Te}_6$ at the indicated fields. Inset shows the temperature dependence of specific heat C_p .

$\Delta S_M(T, H)$ could be practically approximated as,

$$\Delta S_M(T_i, H) = \frac{\int_0^H M(T_i, H) dH - \int_0^H M(T_{i+1}, H) dH}{T_i - T_{i+1}}. \quad (15)$$

Figure 6(a) gives the calculated $-\Delta S_M$ as a function of temperature. All the $-\Delta S_M(T, H)$ curves present a pronounced peak at T_c , and the peak broads asymmetrically on both sides with increasing field. The maximum value of $-\Delta S_M$ reaches $2.53 \text{ J kg}^{-1} \text{ K}^{-1}$ with in-plane field change of 5 T. This is comparable to $\text{Mn}_{2-x}\text{Cr}_x\text{Sb}$ but smaller than in $\text{MnFeP}_{0.45}\text{As}_{0.55}$ or $\text{Gd}_5\text{Ge}_2\text{Si}_2$ magnetic

refrigerant materials.??

Scaling analysis of $-\Delta S_M$ can be built by normalizing all the $-\Delta S_M$ curves against the respective maximum $-\Delta S_M^{max}$, namely, $\Delta S_M/\Delta S_M^{max}$ by rescaling the temperature θ as defined in the following equations,?

$$\theta_- = (T_{peak} - T)/(T_{r1} - T_{peak}), T < T_{peak}, \quad (16)$$

$$\theta_+ = (T - T_{peak})/(T_{r2} - T_{peak}), T > T_{peak}, \quad (17)$$

where T_{r1} and T_{r2} are the temperatures of the two reference points that have been selected as those corresponding to $\Delta S_M(T_{r1}, T_{r2}) = \frac{1}{2}\Delta S_M^{max}$. Following this method, all the $-\Delta S_M(T, H)$ curves in various fields collapse into a single curve in the vicinity of T_c [Fig. 6(b)]. In the framework of the mean-field theory, $-\Delta S_M^{max} = -1.07qR(g\mu_B JH/k_B T_c)^{2/3} \propto H^{2/3}$, where q is the number of magnetic ions, R is the gas constant, and g is the Lande factor.?. In fact, more universally, it should follow a power law relation, $-\Delta S_M^{max} = aH^n$, where n depends on the magnetic state of the sample. Fitting of the field dependence of $-\Delta S_M^{max}$ with \mathbf{H}/\mathbf{ab} gives $n = 0.665(2)$ [inset in Fig. 6(b)], close to the typical value of $2/3$ within mean-field model.

Finally, we also estimate the $-\Delta S_M$ from heat capacity measurement with out-of-plane fields up to 9 T. The λ peak observed at $T_c = 74.7 \text{ K}$ in zero field [inset in Fig. 7(a)], corresponding well to the PM-FM transition, is gradually suppressed in fields. Figure 7(a) shows the calculated heat capacity change $\Delta C_p = C_p(T, H) - C_p(T, 0)$ as a function of temperature in various fields. Obviously, $\Delta C_p < 0$ for $T < T_c$ and $\Delta C_p > 0$ for $T > T_c$, whilst, it changes sharply from negative to positive at T_c , corresponding to the change from FM to PM. The entropy $S(T, H)$ can be deduced by

$$S(T, H) = \int_0^T \frac{C_p(T, H)}{T} dT. \quad (18)$$

Assuming the electronic and lattice contributions are not field dependent and in an adiabatic process of changing the field, the magnetic entropy change $-\Delta S_M$ can be straightly obtained $-\Delta S_M(T, H) = S_M(T, H) - S_M(T, 0)$. The adiabatic temperature change ΔT_{ad} caused by the field change can be obtained by $\Delta T_{ad}(T, H) = T(S, H) - T(S, 0)$, where $T(S, H)$ and $T(S, 0)$ are the temperatures in the field $H \neq 0$ and $H = 0$, respectively, at constant total entropy $S(T, H)$. Figures 7(b) and 7(c) exhibit the temperature dependence of $-\Delta S_M$ and ΔT_{ad} estimated from heat capacity with out-of-plane field. The maxima of $-\Delta S_M$ and ΔT_{ad} increase with increase field and reach the values of $2.94 \text{ J kg}^{-1} \text{ K}^{-1}$ and 1.14 K , respectively, with the field change of 9 T.

IV. CONCLUSIONS

In summary, we have studied the critical behavior and magnetocaloric effect around the FM-PM transition in

Mn₃Si₂Te₆ single crystal. The ferrimagnetic transition in Mn₃Si₂Te₆ is identified to be second order in nature. The critical exponents β , γ , and δ estimated from various techniques match reasonably well and follow the scaling equation, suggesting a long-range magnetic interaction with the exchange distance decaying as $J(r) \approx r^{-4.79}$. Magnetocaloric effect is about one order of magnitude smaller when compared to other magnetorefrigerant can-

didate materials.

ACKNOWLEDGEMENTS

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