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Persistent low-energy phonon broadening near the charge order *q*-vector in bilayer cuprate $Bi_2Sr_2CaCu_2O_{8+\delta}$

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We report a persistent low-energy phonon broadening around $q_B \sim 0.28$ r.l.u. along the Cu-O bond direction in the high- T_c cuprate Bi₂Sr₂CaCu₂O_{8+ $\delta}$ (Bi-2212). We show that such broadening exists both inside and outside the conventional charge density wave (CDW) phase, via temperature dependent measurements in both underdoped and heavily overdoped samples. Combining inelastic hard x-ray scattering, diffuse scattering, angle-resolved photoemission spectroscopy, and resonant soft x-ray scattering at the Cu L_3 -edge, we exclude the presence of a CDW in the heavily overdoped Bi-2212 similar to that observed in the underdoped systems. Finally, we discuss the origin of such anisotropic low-energy phonon broadening, and its potential precursory role to the CDW phase in the underdoped region.}

I. INTRODUCTION

The phase diagram of the high- T_c cuprate superconductors has many intertwined broken-symmetry states. At the heart of them lies the superconductivity (SC), whose origin has eluded our understanding amid many adjacent phases (Fig. 1(a))¹. Observations of one-dimensional spin stripe order in La_{1.48}Nd_{0.4}Sr_{0.12}CuO₄ (Nd-LSCO) from inelastic neutron scattering (INS) first provided experimental evidence for a charge-spin interlocked density wave order inside the superconducting phase ². Later, a concomitant pattern of charge stripes with half the period was discovered using resonant x-ray scattering ³. Recent discoveries of charge order in all families of underdoped cuprates have raised a central question ⁴⁻⁹ - what is the cause of the charge order?

The effect of electronic correlations has been put forward as one leading explanation. The charge order momentum q_{co} appears to coincide in some families with a qvector that bridges regions of the partially gapped Fermi surface in the pseudogap state, facilitating an ostensible nesting condition ^{4,8,9}. However, this simple nesting picture cannot reconcile with a series of mismatched phononic and electronic properties in Bi-2212 ^{8,10,11}. Furthermore, numerical solutions to the 2D Hubbard model show that hole-doping the half-filled Mott system introduces an instability towards interlocked charge and spin stripes with remarkable similarities to those seen in La-based cuprates, such as a q_{co} that increases with hole doping^{12,13}. However, the decrease of q_{co} upon doping observed in some cuprate families¹⁴ has not been demonstrated in these and similar calculations, which so far only takes into consideration electronic correlations.

On the other hand, anomalies in the phonon spectra have been widely observed around q_{co} , suggesting an intimate role of the lattice in the charge ordering phenomenon. In underdoped YBa₂Cu₃O_{6+y} (YBCO), the low-energy phonon dispersions show anomalous softening and broadening behavior at q_{co} , both of which respond strongly to the superconducting T_c^{15} . It's also proposed that this softening and broadening may also arise from a combined effect of multiple phonon branches ¹⁶. Single layer compound La_{2-x}Ba_xCuO₄ (LBCO) also shows lowenergy phonon broadening near q_{co} at $x = 0.125^{17}$. In addition to low-energy phonons, a recent resonant inelastic x-ray scattering (RIXS) study of underdoped Bi-2212 shows that a ~60 meV oxygen breathing phonon also significantly softens and broadens near q_{co} up to 240 K ¹¹.

The relation of lattice vibrations to superconductivity is also highly relevant. Low-energy electron dispersion anomalies have been observed in Bi₂Sr₂CuO_{6+ δ} (Bi-2201), Bi-2212 and La_{2-x}Sr_xCuO₄ (LSCO) via angleresolved photoemission spectroscopy (ARPES) ¹⁸⁻²¹, where a full hierarchy of bosonic modes imprinting on the electronic structure ²²⁻²⁴. Among them, two lowenergy phonon modes are proposed to have the ability to enhance the *d*-wave Cooper pairing, thus boosting the superconducting T_c ^{25,26}. The notion is further bolstered by recent reports of enhanced T_c induced by strong



FIG. 1: (a) Generic phase diagram for the Bi-2212 system, where the grey shade indicates the hitherto-known charge density wave region. The colored circles indicate the four measurement conditions. The inset shows the tetragonal CuO₂ unit cell convention used in this study, where H is parallel to the Cu-O bond direction. Abbreviations are: AFM - long range antiferromagnetic order, PG - pseudogap, CDW - charge density wave, SC - superconductivity. (b)(c) Low-energy longitudinal phonon dispersion along the ($H \ 0 \ 0$) direction for conditions B and C in panel (a), where doping is 7% (UD32). (d)(e) Low-energy longitudinal phonon dispersion for conditions D and E in panel (a), where doping is 23% (OD53). The green dashed lines are guides to the eye, and q_B indicates the phonon broadening momentum.

electron-phonon coupling (EPC) at the FeSe-SrTiO₃ interface^{27–29}.

Despite the importance of knowing details of the phonon spectrum of Bi-based cuprate superconductors, there are only limited reports. Phonon measurements by inelastic neutron scattering have mainly focused on systems where large bulk crystals are available, including YBCO ^{30,31} and Hg-1201 ^{32,33}, both of which lack systematic comparisons to ARPES and scanning tunneling microscopy (STM). Recent advances in high-resolution inelastic x-ray scattering (IXS) enables investigations of materials with limited sample volume such as crystals of the single layer compound Bi-2201 and its bi-layer counterpart Bi-2212 ^{34,35}. A recent INS study reports putative low-energy phonon anomalies around q_{co} in optimally doped Bi-2212³⁶, but leaves open the discussion about their origin. Given this observation, we raise the following questions: is there a connection between this anomaly and the CDW observed in underdoped Bi-2212? More fundamentally, is the phonon anomaly playing a causal role in the formation of CDW and the enhancement of superconductivity in the high- T_c cuprates?

To gain insights into these open questions, we hereby report a comparative series of photon-scattering experiments performed on samples of underdoped (hole doping p = 0.07) and heavily overdoped (p = 0.23) Bi-2212. We utilize high-resolution IXS to measure the low-energy phonon excitation spectrum, and find a persistent broadening near the q_{co} for both dopings. To inspect whether there is CDW in the overdoped regime, we conducted a thorough set of diffraction experiments surveying the reciprocal space of the overdoped sample. These include diffuse scattering (DS), IXS, and (energy integrated) resonant elastic x-ray scattering (REXS). We observe no diffraction signal of CDW analogous to that of overdoped Bi-2201 ³⁷ or any other underdoped cuprates. Importantly, there is a region of reciprocal space where the longitudinal acoustic (LA) phonon branch crosses an extremely low-energy optical branch, potentially creating a broad hybridization zone that encompasses the charge ordering q_{co} . We speculate that the low-energy phonon broadening may act as a lattice precursor, which, when coinciding with strong electronic correlation effects in the underdoped cuprates (e.g. the pseudogap), can result in CDW.

This paper is organized as follows. First, we discuss the details of the various experimental techniques and sample information. Then, we present the IXS data from both samples and temperatures. We discuss our analysis of the phonon excitation spectrum, the fitting model used, and the results. Then, we argue for a null observation of a CDW order in the overdoped Bi-2212 based on REXS, IXS and DS measurements. A discussion and outlook is lastly presented, highlighting the implications of our

findings as well as an outlook of how our hypothesis could be further tested.

II. METHODS

Single crystals of Bi-2212 were grown at AIST, Japan with the optical floating zone method. Underdoping was achieved via partial replacement of Ca with Dy to form $Bi_2Sr_2(Ca,Dy)Cu_2O_{8+\delta}$. Heavy overdoping was achieved by annealing the sample in a 400 bar, high pressure oxygen environment to form super-oxygenated $Bi_2Sr_2CaCu_2O_{8+\delta}$. The superconducting transition temperatures were then confirmed using a Quantum Design SQUID magnetometer. Throughout this paper, we refer to the underdoped sample $(T_c=32 \text{ K})$ as UD32, and to the overdoped sample ($T_c=53$ K) as OD53. The lattice constants at 300 K, determined using the multiple scattering techniques described below, are $a \approx b=3.829$ Å, c=30.45 Å for UD32, and $a \approx b$ 3.825 Å, c=30.81 Å for OD53 in a tetragonal cell convention (Fig. 1(a)). The reciprocal lattice units throughout this paper are based on this convention $(q_x = \frac{2\pi}{a} * H, q_y = \frac{2\pi}{b} * K, q_z = \frac{2\pi}{c} * L)$. To characterize the phonon spectra, we employed IXS

and Raman scattering spectroscopy. The IXS measurements on UD32 were done at the ID28 beamline of the European Synchrotron Radiation Facility (ESRF) with 17.79 keV (instrument energy resolution $\Delta E \sim 3.0$ meV) and 23.73 keV ($\Delta E \sim 1.5$ meV) incident photons. The IXS measurements on OD53 were done at both ESRF and the 30-ID HERIX beamline at the Advanced Photon Source, Argonne National Laboratory, where the photon energy used was 23.724 keV with an energy resolution of $\Delta E \sim 1.5$ meV. In both cases the samples were glued to a sample holder inside a closed-cycle cryostat on a 4-circle goniometer. The IXS experiments were all performed in constant wave-vector mode using transmission geometry. Every inelastic spectrum scan was performed to include the elastic line as a calibration reference for energy drift corrections ^{38,39}. Room-temperature mixed-polarization Raman scattering experiments were carried out on both samples at the Stanford Nano Shared Facility at Stanford University using a Horiba Labram Raman spectrometer with 1.96 eV incident photons. The experiment geometry, in Porto notation, was $\bar{z}(xu)z$ and $\bar{z}(yu)z$, where u means no polarization analysis for the outgoing light. Diffuse scattering measurements were done at the ID29 beamline at the ESRF with 12.65 keV photons, where the temperature control was achieved with a nitrogen cryostream down to 120 K. The resonant soft x-ray scattering experiments were performed at the UE46-PGM1 beamline of the Helmholtz Zentrum Berlin, Germany and at beamline 13-3 of the Stanford Synchrotron Radiation Lightsource (SSRL). In both cases, the photons were resonant to the Cu L_3 -edge (931.5 eV), and the scattering geometries were identical to previous studies of charge ordering in cuprates ⁴⁰. Angle-resolved photoemission (ARPES) measurements were done at SSRL beamline 54 using 18.4 eV incident photon energy with the linear photon polarization aligned with the Cu-O bond direction. The doping of each sample was determined using the parabolic T_c -doping relation ⁴¹.

III. RESULTS

A. Phonon spectra

Figure 1(a) displays a generic phase diagram of the superconducting cuprates with four points labeled using letters B-E, corresponding to the doping/temperature conditions for which the phonon dispersion spectra were studied. Two samples, UD32 and OD53, were mainly probed at two different temperatures: 28 K and 240 K. Only the low-temperature measurement of UD32 falls within the CDW region (point C). The OD53 measurements (points D and E) were chosen so to be far from the pseudogap phase. Figure 1 (b-e) correspondingly display intensity color maps of the low-energy phonon spectra stitched together from individual IXS energy-loss cuts at different momenta along the longitudinal $(H \ 0 \ 0)$ direction for each of these conditions. The window of energy $\Delta E \in [-1, 2]$ meV contains the elastic contribution of the spectrum and has been masked out for clarity. A strong elastic Bragg peak lies at $(2\ 0\ 0)$ which floods the inelastic spectrum, precluding the measurements near the zone center.

Let us now discuss the phonon branches away from the zone center discernible in all spectra. First, a streak of intensity within the energy range $E \in [3,7]$ meV can be seen in all four panels. This low-energy phonon mode has been observed by INS in Bi-2212 and by IXS in YBCO 15,16,36 and LBCO¹⁷, making it plausible that this is a universal cuprate feature. Second, a branch with energy $E \in [10, 15]$ meV can be resolved in all four spectra for $H \in [2.2, 2.5]$ r.l.u. Finally, a weak signal can be identified at high energies $E \gtrsim 10 \text{ meV}$ for $H \in [2.1, 2.25]$ r.l.u., matching an A_{1g} phonon found in calculations ³³. At 240 K (Figure 1(b,d)), the intensity of those phonon branches are more prominent due to the Bose factor. We point out a broadening of the linewidth of the low-energy mode near $q_B \in [2.2, 2.35]$ r.l.u., particularly obvious for the high temperature spectra in OD53, which requires a closer look.

In Figure 2, we present raw individual energy-loss spectra at varying reciprocal space directions shown schematically in Fig. 2(d) by solid red bars. Purely longitudinal cuts were taken along the *H*-direction near $(2+h\ 0\ 0)$, while a cut with mixed longitudinal and transverse components was taken along the *H*-direction near $(2+h\ 0\ 14)$. Purely transverse cuts were taken along the *K*-direction near $(2\ K\ 0)$ direction but only for OD53. Panels (a) and (b) show the raw inelastic data of the longitudinal cuts for UD32 and OD53, with 3 meV and 1.5 meV energy resolution respectively. The energy-loss spectra are shifted vertically for clarity. High (red) and low (blue)



FIG. 2: Normalized IXS energy-loss scans. Longitudinal cuts along $(H \ 0 \ 0)$ at 240 K (red) and 28 K (blue) for (a) UD32 ($\Delta E \sim 3.0 \text{ meV}$) and (b) OD53 ($\Delta E \sim 1.5 \text{ meV}$). (c) Transverse cuts along (2 K 0) at 300 K in OD53. (d) Schematics of the scan directions in reciprocal space. (e) Line cuts for OD53 with a mixture of transverse and longitudinal channels along (H 0 14). All spectra displayed here are normalized to the elastic peak intensity and offset for clarity.

temperature data are compared for each sample.

For OD53, panel (c) shows the transverse cut measured at T=300 K, and panel (e) shows the high L cut taken at three different temperatures at the labeled Hpositions. The circles mark the positions of possible phonon modes. And the broadening of the low-energy longitudinal branch (Fig. 2(a) and (b)) readily contrasts the lack of that in the transverse branch (Fig. 2(c)). A similar broadening has been observed in the low-energy acoustic mode of YBCO for temperatures below the onset of the CDW, and maximizes around the superconducting T_c ^{15,16}. However, the broadening effect we hereby report can be observed in both underdoped and overdoped samples, for both high and low temperatures (Fig. 1(a)). Particularly interesting is the fact that the effect is clearly manifested in OD53 - a phase region far away from any common electronic order instability or anomalous Fermi surface phenomena, for example, the pseudogap. We note a recent INS report also observed such broadening for optimal doping at room and low temperatures in Bi-2212 ³⁶.

To obtain quantitative information about the broadening of the low-energy phonon, the energy-loss spectra were fitted to the resolution-convolved damped harmonic oscillator functions with the Bose factor correction⁴². Fig. 3(a) shows two typical fits with a single Gaussian and two Bose-factor corrected damped harmonic oscillator functions, all convolved with the respective energy resolution. Figure 3 (b) and (c) present the dispersions for the low-energy modes. The IXS spectral fitting results in the longitudinal geometry for UD32 and OD53 samples are shown in panels (b) and (c), respectively. Panel (c), in addition, displays the fitted energy positions of the low-energy modes from the mixed geometry $(H \ 0 \ 14)$ as red circles. Since the zone-center IXS measurements are flooded by the Bragg intensity at $(2 \ 0 \ 0)$, Raman spectroscopy was used to determine the mode energies at $q \sim 0$. The room-temperature Raman spectra for both samples are shown in panel (d). The dispersive nature of three modes can thus be identified. The low-energy A_{1q} optical mode starts for both samples at E=7.5 meV at the zone center (Fig. 3(d)), and quickly trends upwards with increasing in-plane momentum (Fig. 3(b,c), open circles). The $\sim 6 \text{ meV}$ zone boundary phonon may initially appear as a natural candidate for the acoustic branch, as implied in an early Hg-1201 study ³³. Meanwhile, calculations in LSCO, NCCO and Bi-2212 all show acoustic branches extending up to \sim 13-16 meV at the zone boundary $^{43-45}$. A simple diatomic spring-ball model yields a linear to sinusoidal small-q dispersion relations for acous-



FIG. 3: Fitted dispersion. (a) Examples of damped harmonic oscillator fitting for two samples, convolved with their respective instrument resolution. Fitted peak positions for IXS data on (b) UD32 (c) OD53 Bi-2212. All IXS data shown here are taken at 240 K except for the (H 0 14) scans at 300 K. Dashed lines in (b) and (c) are fit to the acoustic mode dispersion with $\sin(qa/2)$ assuming the higher energy mode at the high q being from the longitudinal acoustic branch. The markers at $q = (2 \ 0 \ 0)$ denote energies at 3.5 meV and 7.5 meV derived from room tempearture Raman measurements on UD32 (grey) and OD53 (black) as shown in (d). Note the significant presence of the optical mode evident in the red IXS data point at (2.05 0 14), which is very close to the zone center.

tic modes, whose zero-q slope can be cross-checked with the bulk sound velocity. The dashed lines shown in panels (b) and (c) are the result of fitting the higher energy large-q mode (for $H \in [2.2, 2.5]$ r.l.u.) to a sinusoidal dispersion relation $\sin(qa/2)$, with the energy at the zone boundary around 13-14 meV. This LA branch intersects the low-energy branch at $H \sim 2.1$ r.l.u., with a corresponding longitudinal sound velocity of 4360 ± 390 m/s, consistent with both inelastic neutron scattering result in optimally doped Bi-2212 single crystals 36 , as well as the bulk ultrasound measurement of the in-plane longitudinal sound velocity of 4370 ± 10 m/s in very dense textured Bi-2212 ⁴⁶. On the other hand, a simple sinusoidal dispersion model does not appropriately describe the lowenergy mode. Instead, the low-energy mode appears to intersect the zone center at finite energy. The mixed polarization geometry allows the low-energy mode to be clearly seen at non-zero energy close to the zone center at H=2.05 r.l.u. (red circles in panel (c)). Furthermore, the Raman data of panel (d) shows an optical excitation at 3.5 meV which extrapolates well onto this branch. Thus, this flat low-energy optical mode may participate in the temperature- and doping-independent broadening effect

that we observe.

We present a quantitative analysis of this branch as a function of sample temperature in Figure 4. The fitted energy (panels (a) and (c)) and mode linewidth (panels (b) and (d)) are plotted for both samples at high and low temperatures, as labeled. The linewidths increase from ~ 2 meV near the zone center to ~ 6 meV for $H \in [2.2, 2.35]$ r.l.u., and has no appreciable temperature dependence in this momentum range. Only in UD32, an additional broadening is observed close to the zone boundary at low temperature. Similarly, the energy of the mode shows little change as a function of temperature. Previous reports on YBCO revealed a broadening of a low-energy acoustic phonon at the onset of CDW order for temperatures below T \sim 120 K ^{15,16}. No softening is observed at low temperature for UD32, where the CDW has been observed using soft x-ray resonant scattering at the Cu L_3 -edge⁸. However, the charge modulations observed by REXS in Bi-2212 are comparatively weaker and of shorter range than those in YBCO. The response of the lattice vibration near q_{co} to such a subtle CDW effect might also be weaker in Bi-2212.

The broadening also appears to be a unique property



FIG. 4: (a) High temperature dispersion for UD32 and OD53 along $(H \ 0 \ 0)$ direction. (b) High temperature phonon width. (c) Low temperature dispersion for UD32 and OD53. (d) Low temperature phonon width. Dispersion is fitted with damped harmonic oscillator model, with the Bose-factor considered. The black dashed line references the bulk in-plane longitudinal sound velocity at 4370 m/s.



FIG. 5: (a) Transverse acoustic branch dispersion (circle) and its width (square) for OD53 at 300 K. The black dashed line references the bulk in-plane fast shear sound velocity at 2460 m/s. (b) Longitudinal diagonal (Cu-Cu) dispersion and its width for OD53 at 300 K. The grey dashed line indicates the satellite branch originated from the incommensurate superstructure (SS) Bragg peak.

for the longitudinal branch along the Cu-O bond direction in Bi-2212. The transverse branch (Fig. 5(a)) and the longitudinal, diagonal dispersion (perpendicular to the superstructure direction, Fig. 5(b)) do not show any appreciable momentum-dependent broadening. This also helps rule out the trivial superstructure-induced phonon broadening, in which case a broadening would have occurred where the superstructure phonons intercept. It should also be noted that the in-plane transverse branch also yields a sound velocity of 2560 ± 150 m/s, in good agreement with the bulk in-plane fast shear sound velocity of 2460 ± 10 m/s measured with ultrasound ⁴⁶.

B. CDW search

Given the observation of a lattice vibration anomaly in overdoped Bi-2212 near q_{co} , we now address in detail our search for possible CDW order in overdoped cuprates. We carried out a thorough survey of the reciprocal space which is shown in Fig. 6. First of all, Fig. 6(a) shows an in-plane Fermi surface mapped at 104 K. Full hole-like Fermi surfaces can be clearly seen. This is in agreement with previous reports of a closed Fermi surface in overdoped cuprates 47. Replicas of these surfaces can be observed along the (H - H) direction. These arise from the buckling wave of the Bi-O layer distortion. This superstructure results in satellite peaks with incommensurate vectors splitting from a Bragg peak along the (H - H)direction. Fig. 6(b) shows a diffraction map near the (0 2 1) Bragg peak, where multiple harmonics of these satellites can be observed. Importantly, we note that these superstructure peaks can be broad enough to have the tail of the first order satellite (near the zone center) intersect the $(H \ 0)$ or $(K \ 0)$ lines at reduced inplane values ~ 0.18 r.l.u. Panel (c) shows a cut of the $(H \ 0 \ L)$ plane. Sharp, intense Bragg peaks occur at (2 0 L=even) and elongated out-of-plane rods can be seen at $(2 \ 0 \ L=\text{odd})$. We focus our attention on the diffuse halos of intensity observed near $(2\pm 0.18 \ 0 \ \pm 1)$, which are reminiscent of the CDW pattern as observed by DS in underdoped YBCO ¹⁵. A similar pattern of diffuse intensity can be observed in panel (d), which is a cut in the $(H \ H \ L)$ plane near H = K = 1 that runs perpendicular to the superstructure. For comparison, panel (e) shows a cut within a plane parallel to the superstructure, i.e. (H - H L), where many of these satellite peaks can be observed, and the L = 1 first order superstructure peak intensity overwhelms that of a primary Bragg peak. The diffuse intensity observed in panel (c) at $(2\pm 0.18 \ 0)$ ± 1) can also be observed in the elastic part of the IXS scans, as plotted in panel (f). The intensity of the elastic signal increases at H=2.18 r.l.u., and persists till 240 K at least. Furthermore, the L-dependence of these diffuse features is shown in panel (g), which also compares the data measured directly by IXS at zero energy loss to the equivalent cut extracted from the DS maps. Both measurements display very broad, rod-like features. In panel (h) the H-dependence of these features can be observed for an intermediate L-value, again displaying the elastic IXS data and cuts from the DS map. There is a consistent feature at $(H \pm 0.18 \ 0 \ L)$ around every Bragg position. We measured these diffraction features up to room temperature and did not see any abrupt change

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FIG. 6: Looking for evidence of CDW in OD53. (a) ARPES Fermi surface map at 104K. The solid and dashed red lines indicate the Fermi surface from the main bands and the superstructure bands, respectively. (b) DS at $(H \ K \ 1)$ plane, where a significant intensity tail from the Bi-O superstructure (SS) can be seen even along $(H \ 0)$ direction. (c) 'butterfly' pattern in $(H \ 0 \ L)$ plane. (d) Similar pattern perpendicular to the SS in $(H \ H \ L)$ plane). (e) DS reciprocal space map along the SS direction shows that the intensity of the first order SS Bragg peak maximizes at L = 1. (f) IXS spectra of the satellite peaks along $(H \ 0)$ show their highly elastic nature. (g)(h) A comparison between IXS (zero energy-loss line) and DS (energy integration) shows agreement.

in intensity. We speculate, therefore, that the features originate as intensity leakage from the broad Bi-2212 superstructure satellite peaks - which is strongly suggested in panel (b). These features are therefore unlikely CDW peaks of the same nature as observed in the underdoped systems.

To further test for the potential presence of weak CDW correlations with very short correlation length in the overdoped sample OD53, we have also performed a series of REXS experiments following a similar procedure as with underdoped Bi2212 and other cuprate families 40 . Figure 7 shows the results from both a photodiode point detector and a CCD 2D detector. Panel (a) displays rocking curve scans projected onto the *H*-axis, measured with a point detector scattering photons with energies close to the Cu- L_3 absorption edge (E=931.5 eV). The range in L of these arched rocking curves is $L \in [4.5, 1.6]$ r.l.u. To identify a potentially weak and short-ranged CDW signal, we compare high and low temperature data. Unlike in the underdoped Bi-based cuprates ^{8,9} where at low temperatures the signal shows an increase in intensity near $H \in [0.25, 0.3]$ r.l.u., no intensity excess can be observed in these low-temperature scans for the overdoped system. Figure 7(b) shows reciprocal space maps of the $(H \ K \ 3.5)$ plane taken with the two-dimensional CCD detector at high/low temperature and on/off resonance. No sign of a peak associated with CDW correlations can be discerned. We have thus surveyed the entirety of reciprocal space afforded by the small Ewald sphere and geometry limitations at $Cu-L_3$ edge. In summary, using several scattering techniques that reliably detect CDW order in underdoped cuprates, we conclude a null observation of CDW order in overdoped Bi-2212.

IV. DISCUSSION AND OUTLOOK

First, our result reopens the discussion on the scenario where a low-energy forward scattering phonon enhances superconductivity in Bi-2212 system. While previous studies identify the ~ 13-14 meV acoustic phonon to be responsible for the low-energy electron dispersion anomaly in Bi-2212 ^{18,26,36}, our result suggests that the energy position of the electron dispersion anomaly and the small-q requirement of the mode coupling cannot be simultaneously satisfied on the LA/TA branches, mainly due to the energy mismatch at the q of interest. Instead, other higher energy zone center optical phonons are the more likely candidates.

The possible origins of the observed phonon linewidth broadening are discussed schematically in Fig. 8 and 9. The first explanation requires an existing CDW instability - the low-energy phonon broadens through an interaction with the valence electron CDW and its associated soft mode, as described in panel (a). This is suggested by the evidence in underdoped YBCO and Bi-2212, where the softening and broadening momentum region is extremely narrow, akin to a Kohn anomaly; but the effect maximizes near the superconducting T_c rather than the onset temperature of the CDW $^{11,\overline{15},16,48}$. In this case, the onset of an incommensurate CDW associated with the valence electrons concomitantly triggers broadening and softening in the phonon spectra, displayed as gray regions in Fig. 8(a). However, as a major caveat to this hypothesis, we find in Bi-2212 that the linewidth broadening at q_{co} does not undergo a change below the onset of the static CDW order in UD32. More strongly, the broadening takes place even at the heavily overdoped region p = 0.23, far away from the hitherto known static CDW phase region. These combined results disfavor static CDW as the root cause for low-energy phonon broadening specifically in Bi-2212. We are thus compelled to consider scenarios in which the CDW phenomenon is either not the driver of such broadening, or is too short-ranged and short-lived to be detected in the heavily overdoped Bi-2212.

A second possibility is a non-CDW driven, q-dependent electron-phonon coupling for this optical mode, where the mode coupling strength peaks at q_B (Fig. 8(b)). In fact, q-dependent electron-phonon coupling is demonstrated to be an important alternative route to realize CDW in correlated systems like NbSe₂⁴⁹. Such a property can generally be satisfied for small-q scattering phonons, where similar q-dependence is expected along both Cu-O and Cu-Cu bond directions ²⁶. However, as indicated in Fig. 5(b), such broadening is absent along the (H H) direction at small q, which disfavors the electron-phonon coupling explanation.

A third scenario involves an anomaly in the phonon dispersions including a hybridization of two crossing phonon branches or the presence of multiple neardegenerate phonon branches, shown in Fig. 9. As indicated earlier, the LA mode disperses through the lowenergy optical mode, intercepting at an intermediate momentum, displayed as a gray area in Fig. 9. The suspected hybridization, moreover, may require the involved optical branch to exhibit anharmonic coupling therefore a quartic term in the local lattice potential. This possibility can be quantitatively evaluated with dynamical lattice calculations. It should be noted that, in principle, multiple optical branches in this energy range could be induced by symmetry reduction from dopant disorder or structural distortions. However, given the presence of this low-energy mode in other cuprates of distinct structures and its associated broadening at similar momenta $^{15-17,36}$, it is unlikely a disorder effect specific to Bi-2212.

Therefore, either this phonon broadening is completely independent of the CDW, or the agreement between q_B and q_{co} is more than mere coincidence. In the latter case, instead of having the CDW as the cause, such lowenergy phonon broadening may serve as the universal precursory instability to the CDW phase. At this lowenergy $E \sim 5$ meV, very little thermal energy is required to significantly populate this phonon at this momentum. When combined with the strong electronic correlation



FIG. 7: Lack of resonance and temperature response from the expected CDW-ordering q for OD53 system. (a) High temperature (300 K, red) and low temperature (12 K, blue) photon energy dependence near the Cu L_3 -edge via REXS. (b) 2D reciprocal space map in the ($H \ K \sim 3.5$) plane at the Cu- L_3 -edge also shows a flat background, for both off and on-resonance (top and middle), below and above T_c (middle and bottom). The red dashed circles are where potential CDW signals are anticipated if they were to resemble the underdoped Bi-2212 or overdoped Bi-2201.



FIG. 8: Two potential scenarios for the broadening (schematics): (a) low-energy phonon interacts with the CDW soft mode.(b) anisotropic electron-phonon interaction due to the possible forward scattering nature of this phonon. The maximum phonon broadening q_B roughly agrees with the reported CDW wavevector q_{co} .

effects (e.g. the pseudogap) in the underdoped region, the electronic instability may be triggered in a concerted way. In the case of near-degenerate low energy phonons, small symmetry-allowed interactions also become easier to couple to the lattice. Indeed, correlation-enhanced electron-lattice interaction has been captured both experimentally and theoretically in underdoped cuprate systems ^{47,50}. In this coordinated process, the eventual q_{co} may slightly shift from the phonon broadening momentum q_B to accommodate the electronic correlation



FIG. 9: Intrinsic phonon-phonon hybridization induced broadening. The dashed lines are the non-interacting phonon branches. Red shade indicates the low-energy optical component, and black shade indicates the longitudinal acoustic component. The grey shade indicates the potential hybridization and broadening zone.

effect. This temperature dependent q-shift effect has recently been observed in several cuprate systems ^{11,17}. On the other hand, with the low-energy phonon broadening taking part in the CDW formation, it becomes natural

to anticipate a strong pressure effect on the CDW order, as lattice modes are directly perturbed in such a process 48,51 .

In summary, we have measured high resolution lowenergy optical and acoustic phonon dispersions in the high- T_c compound Bi-2212, and achieved quantitative agreement with bulk sound velocity measurements as well as the recent INS measurements. We find the acoustic mode to be unlikely the cause of the 10-15 meV electronic dispersion anomaly in underdoped Bi-2212, while other zone-center optical modes are the more likely candidates.

Importantly, we have observed persistent low-energy longitudinal phonon broadening at $q_B \sim 0.28$ r.l.u. along the Cu-O bond direction, similar to the charge order momenta q_{co} in many underdoped cuprates. Such broadening has very little temperature dependence up to 240 K. This broadening is likely to happen on a very low-energy optical branch, and may originate from an acousticoptical phonon crossing. Combining non-resonant and resonant x-ray scattering techniques, we find no evidence for CDW in the heavily overdoped Bi-2212. These suggest that if the low-energy phonon broadening were to be related to the CDW in the underdoped cuprates at all, in lieu of being induced by the CDW, it actually may provide the precursory instability to the CDW formation, which is eventually triggered when combined with the much stronger electronic correlations in the underdoped phase region. We hope these results would motivate future theoretical phonon calculations towards a fuller understanding of the link between the lattice degree of freedom and various electronic correlations effects in cuprates.

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