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Phys. Rev. B **97**, 104506 — Published 14 March 2018

DOI: [10.1103/PhysRevB.97.104506](https://doi.org/10.1103/PhysRevB.97.104506)

¹³⁹La and ⁶³Cu NMR investigation of charge order in La₂CuO_{4+y} ($T_c = 42$ K)

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We report ¹³⁹La and ⁶³Cu NMR investigation of the successive charge order, spin order, and superconducting transitions in super-oxygenated La₂CuO_{4+y} single crystal with stage-4 excess oxygen order at $T_{stage} \simeq 290$ K. We show that the stage-4 order induces tilting of CuO₆ octahedra below T_{stage} , which in turn causes ¹³⁹La NMR line broadening. The structural distortion continues to develop far below T_{stage} , and completes at $T_{charge} \simeq 60$ K, where charge order sets in. This sequence is reminiscent of the charge order transition in Nd co-doped La_{1.88}Sr_{0.12}CuO₄ that sets in once the low temperature tetragonal (LTT) phase is established. We also show that the paramagnetic ⁶³Cu NMR signals are progressively wiped out below T_{charge} due to enhanced low frequency spin fluctuations in charge ordered domains, but the residual ⁶³Cu NMR signals continue to exhibit the characteristics expected for optimally doped superconducting CuO₂ planes. This indicates that charge order in La₂CuO_{4+y} does not take place uniformly in space. In addition, unlike the typical second order magnetic phase transitions, low frequency Cu spin fluctuations as probed by ¹³⁹La nuclear spin-lattice relaxation rate do not exhibit critical divergence at $T_{spin}(\simeq T_c) = 42$ K. These findings, including the spatially inhomogeneous nature of the charge ordered state, are qualitatively similar to the case of La_{1.885}Sr_{0.115}CuO₄ [T. Imai et al., Phys. Rev. B **96** (2017) 224508, and A. Arsenault et al., Phys. Rev. B (submitted)], but both charge and spin order take place more sharply in the present case.

I. INTRODUCTION

Recent success in detecting the charge order Bragg peaks in many different classes of high T_c cuprates based on modern x-ray scattering techniques [1] has led to renewed interest in the charge order in La₂CuO₄-based cuprates. In the case of Nd³⁺ co-doped La_{1.48}Nd_{0.4}Sr_{0.12}CuO₄, in which Tranquada et al. initially discovered the charge order phenomenon [2], charge order sets in at $T_{charge} \sim 65$ K only after the structural phase transition from the low temperature orthorhombic (LTO) to the low temperature tetragonal (LTT) phase takes place at $T_{LTT} \sim 70$ K.

The LTT structure induced by Nd³⁺ severely suppresses T_c from ~ 38 K to ~ 6 K. Accordingly, many researchers speculated early on that charge order is a byproduct of the LTT structure with low T_c and hence absent in the superconducting CuO₂ planes, despite our early NMR reports that even superconducting La_{1.885}Sr_{0.115}CuO₄ ($T_c = 30$ K) with the LTO structure exhibits nearly identical NMR anomalies observed at the charge order transition of La_{1.48}Nd_{0.4}Sr_{0.12}CuO₄ [3–6]. Recent confirmation of the existence of charge order Bragg peaks in La_{1.885}Sr_{0.115}CuO₄ [7–9] finally settled the two decades old controversy.

On the other hand, these latest x-ray scattering work on La_{1.885}Sr_{0.115}CuO₄ also revealed that charge order sets in gradually starting from as high as $T_{charge} \simeq 80$ K [7–9], indicating that our initial NMR report of $T_{charge} \simeq 50$ K [3] overlooked the gradual onset. Therefore, we

recently revisited ⁶³Cu [10] and ¹³⁹La NMR [11] evidence for charge order in La_{1.885}Sr_{0.115}CuO₄. We demonstrated that the normal ⁶³Cu NMR signals is gradually wiped out below $T_{charge} \simeq 80$ K, and the lost spectral weight is transferred to a wing-like anomalous ⁶³Cu NMR signal with extremely fast NMR relaxation rates. The transverse T_2 relaxation time of the wing-like signal is so short that one can detect it only with the NMR pulse separation time shorter than $\tau \sim 4$ μ s. Our NMR results confirmed that charge order does *not* proceed uniformly in space in La₂CuO₄-based cuprates [3], and a diminishing fraction of CuO₂ planes remains unaffected by charge order even at $T_c = 30$ K.

These recent developments raised a new question. Why is $T_{charge} \simeq 80$ K in orthorhombic La_{1.885}Sr_{0.115}CuO₄ even higher than $T_{charge} = 65$ K of La_{1.48}Nd_{0.4}Sr_{0.12}CuO₄? Do the LTT structure and/or disorder induced by Nd³⁺ substitution play a role? Clearly, we need more investigations to understand the structural effects on charge order.

The latest addition in the growing list of charge ordered cuprates is the super-oxygenated La₂CuO_{4+y} ($y \sim 0.11$) with $T_{charge} \simeq 60$ K as determined by x-ray diffraction [9, 12]. La₂CuO_{4+y} undergoes simultaneous superconducting and spin density wave (SDW) order at $T_c \simeq T_{spin} = 42$ K [13, 14] within the charge ordered state, similarly to La_{1.885}Sr_{0.115}CuO₄ with $T_c \simeq T_{spin} = 30$ K [15] and $T_{charge} \simeq 80$ K [7–9]. Unlike the La₂CuO₄-based materials substituted by Sr²⁺ or Ba²⁺, it is the excess O²⁻ ions located at the interstitial sites that do

nate holes into CuO_2 planes [13, 16–22]. These O^{2-} ions are highly mobile near room temperature, and form a stage-4 superstructure below $T_{\text{stage}} \simeq 290$ K [18, 19]. In the stage-4 ordered phase, interstitial O^{2-} ions occupy LaO layers separated by four CuO_2 planes, and create anti-phase domain boundaries for the tilting direction of CuO_6 octahedra [19]. Upon further cooling, O^{2-} ions lose mobility around $T_{\text{mobility}} \simeq 200$ K [23] and develop a superstructure within the plane [19]. Unlike the quenched disorder induced by Sr^{2+} or Ba^{2+} substitution, super-oxygenated $\text{La}_2\text{CuO}_{4+y}$ therefore possesses unique, *annealed disorder* [19].

In this paper, we report ^{139}La and ^{63}Cu NMR study of a $\text{La}_2\text{CuO}_{4+y}$ ($y \sim 0.11$) single crystal, taking full advantage of the unique characteristics of NMR as a local probe. We identify NMR anomalies associated with the stage-4 oxygen order at $T_{\text{stage}} \simeq 290$ K and $T_{\text{mobility}} \simeq 200$ K. We show that, at the slow observation time scale of NMR, some ^{139}La sites remain unaffected by the stage-4 order down to $T_{\text{charge}} \simeq 60$ K. This may be an indication that the stage-4 order plays an analogous role as the LTT structural transition in $\text{La}_{1.48}\text{Nd}_{0.4}\text{Sr}_{0.12}\text{CuO}_4$ [2] and $\text{La}_{1.88}\text{Ba}_{0.12}\text{CuO}_4$ [24], in which charge order does not set in until the LTT structure is established below T_{LTT} . We also show that charge order does not proceed homogeneously in space. Nearly 1/3 of the volume fraction of the CuO_2 planes is still unaffected by charge order at T_c , and exhibits NMR properties expected for canonical superconducting CuO_2 planes.

II. EXPERIMENTAL

We super-oxygenated a single crystal of La_2CuO_4 using the electrochemical doping technique [13, 17]. We determined the superconducting critical temperature $T_c = 42$ K of our crystal with the Superconducting Quantum Interference Device (SQUID). Both elastic neutron scattering [13] and μSR [14] measurements found the onset of the spin density wave order at $T_{\text{spin}} (= T_c) = 42$ K for a different piece of crystal cut from the same boule. Unlike the case of lower excess O^{2-} composition [25], we did not find evidence for a phase separation into antiferromagnetic and superconducting domains in the ^{139}La NMR lineshape nor the bulk susceptibility data.

We used a piece of single crystal with the approximate dimensions of $5 \times 5 \times 1$ mm for our NMR measurements. We conducted all the NMR measurements at M.I.T. between 1997 and 1999 using the NMR spectrometer built with a Tecmag Aries console. The Aries was a state-of-the-art NMR system at the time, but the spectrometer dead time $t_{\text{dead}} = 8$ to $10 \mu\text{s}$ caused by the ring down was very long in today's standard. Accordingly, we conducted all the NMR measurements with $\tau = 12 \mu\text{s}$ or longer, and hence we were unable to detect the wing-like ^{63}Cu NMR signals that we recently discovered in the charge ordered state of $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ [10]; the wing-like NMR signal has extremely fast T_1 and T_2 relaxation rates, and its

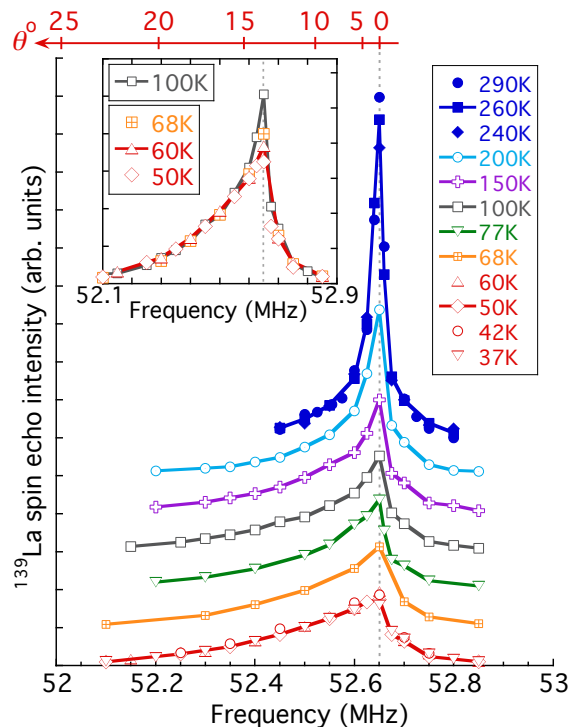


FIG. 1. Representative ^{139}La NMR lineshapes in $B_{\text{ext}} = 8.7521$ T applied along the c-axis. For clarity, the vertical origin is shifted at different temperatures. The gray vertical dashed line marks the peak frequency $^{139}f_o = 52.65$ MHz. Asymmetrical line broadening becomes significant below ~ 220 K. (Inset) The very sharp, needle shaped peak at $^{139}f_o = 52.65$ MHz, which arises from ^{139}La sites neighboring to untilted CuO_6 octahedra, remains observable down to ~ 60 K.

detection requires much shorter spectrometer dead time ($t_{\text{dead}} = 2$ to $4 \mu\text{s}$).

III. RESULTS AND DISCUSSIONS

1. Stage-4 order as probed by ^{139}La NMR

In Fig. 1, we summarize ^{139}La NMR lineshape observed for the nuclear spin $I_z = +1/2$ to $-1/2$ central transition in an external magnetic field $B_{\text{ext}} = 8.7521$ T applied along the crystal c-axis. At 295 K, the peak frequency is $^{139}f_o = 52.650$ MHz and the linewidth is as narrow as $\Delta f = 0.028$ MHz. Using the nuclear gyromagnetic ratio $^{139}\gamma_n/2\pi = 6.0146$ MHz/T, we estimate the apparent NMR frequency shift to be as small as $0.018 \pm 0.02\%$, as expected for non-magnetic ions with closed shells and with a negligibly small second order nuclear quadrupole shift $\Delta\nu_Q^{(2)}$ by the electric field gradient (EFG). The latter implies that CuO_6 octahedra are not statically tilted away from the main principal axis of the EFG tensor

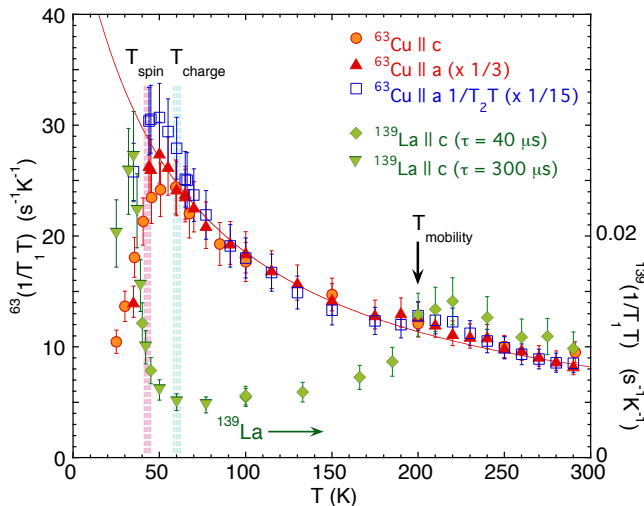


FIG. 2. Temperature dependence of $^{63}(1/T_1T)_c$, the ^{63}Cu nuclear spin-lattice relaxation rate $1/T_1$ divided by temperature T , measured in $B_{ext} = 9$ T applied along the c -axis. We also show $^{63}(1/T_1T)_a$ and $^{63}(1/T_2T)_a$ measured with $B_{ext} \parallel a$ -axis, by normalizing their magnitude by multiplying a factor $1/3$ and $1/15$, respectively. The red solid curve represents the best Curie-Weiss fit with $\theta_{CW} = 60$ K between $T_c = T_{spin} = 42$ K and $T_{mobility} \simeq 200$ K, which slightly underestimates the experimental results above $T_{mobility}$. Also shown using the right axis is $^{139}(1/T_1T)$ measured at the ^{139}La sites in $B_{ext} = 8.75$ T applied along the c -axis.

along the c -axis above T_{stage} . These ^{139}La NMR results are also generic in the high temperature tetragonal (HTT) structure of $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ [11, 26, 27].

The ^{139}La NMR lineshape gradually broadens below the stage-4 order at $T_{stage} \simeq 290$ K [19]. In such a stage-4 structure, the elongated axis of the CuO_6 octahedra are statically tilted away from the crystal c -axis with a significant distribution in the tilting angle. This tilting results in negative values of the second order nuclear quadrupole shift $\Delta\nu_Q^{(2)}$, and hence the line broadening. The NMR lineshape remains fairly narrow down to $T_{mobility} \simeq 200$ K, presumably due to the motional narrowing effect caused by the slow motion of O^{2-} ions. As the excess O^{2-} ions lose their mobility [23] and develop a superstructure within the plane [19, 28] near and below $T_{mobility} \simeq 200$ K, a broad, sawtooth shaped NMR line emerges underneath the narrow peak at $^{139}f_o$ with a distribution up to $\Delta\nu_Q^{(2)} \sim -0.5$ MHz.

Ignoring the small asymmetry in the EFG tensor (because the first order quadrupole satellite peaks do not split when we apply B_{ext} within the ab -plane), we may write $\Delta\nu_Q^{(2)} \simeq 15\nu_Q^2(1 - \cos^2\theta)(1 - 9\cos^2\theta)/(16 \cdot ^{139}\gamma_n \cdot B_{ext})$, where the nuclear quadrupole frequency $\nu_Q = 5.55$ MHz as determined from the splitting between the first order quadrupolar satellite peaks at 45 K, and θ represents the angle between the external field B_{ext} applied along the crystal c -axis and the main principal axis of

the EFG tensor at the ^{139}La sites. Thus the saw-tooth shaped NMR lineshape observed below $T_{mobility} \simeq 200$ K may be considered as a histogram of the static tilting angle θ , as shown by the upper horizontal axis of Fig. 1. We find that the most probable θ remains 0° but θ reaches $\theta \sim 25^\circ$ for the low frequency end of the spectrum.

Another important point to notice is that the needle-like, sharp central peak located at $^{139}f_o$ at 295 K remains visible on top of the broad, saw-tooth shaped lineshape down to ~ 60 K. This means that, when averaged over the NMR measurement time scale, CuO_6 octahedra in some domains remain untilted far below T_{stage} and $T_{mobility}$ down to ~ 60 K. The half-width of the lineshape observed at the onset of charge order at 60 K, $\Delta f \sim 0.2$ MHz, is nearly identical with that of $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ (~ 0.25 MHz) observed at its charge order temperature ~ 80 K [11]. This means that the tilting angle distribution is comparable between $\text{La}_2\text{CuO}_{4+y}$ and $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$. The ^{139}La NMR lineshape in the latter, however, is nearly symmetrical with a Gaussian shape below ~ 200 K, and its peak is shifted from $^{139}f_o$. The central value of the tilting angle is therefore non-zero in the case of $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$.

In Fig. 2, we summarize the temperature dependence of the nuclear spin-lattice relaxation rate $1/T_1$ divided by temperature T measured at $^{139}f_o$. The T_1 relaxation process showed a noticeable distribution due to the quadrupole relaxation effects induced by the motion of O^{2-} ions as well as by the distribution of Cu spin fluctuation frequency scales. Accordingly, we estimated $1/T_1$ based on the force fit of the recovery data to the appropriate fitting function with multiple normal modes [29]. $1/T_1$ thus deduced generally captures the volume averaged behavior of spin dynamics of La_2CuO_4 -based cuprates very well. $^{139}(1/T_1T)$ exhibits a broad hump centered somewhat above $T_{mobility} \simeq 200$ K. We attribute the enhancement of $1/T_1$ to the slow fluctuations of the EFG caused by the motion of O^{2-} and dynamic distortion of the lattice. The EFG contribution to $1/T_1$ takes the maximum value when the fluctuation frequency of the EFG slows down and becomes comparable to the NMR frequency. $^{139}(1/T_1T)$ continues to decrease below $T_{mobility}$ as the fluctuation gradually diminishes. Analogous enhancement of NMR relaxation rates are commonly observed in ionic conductors. For example, the slow motion of Na^+ ions in the battery material $\text{Na}_{1-x}\text{CoO}_2$ enhances $1/T_1$ at Na^+ sites dramatically near room temperature [30].

2. Low frequency Cu spin dynamics

In general, $1/T_1T$ probes the wave vector \mathbf{q} integral of the dynamical electron spin susceptibility at the NMR frequency $\chi''(\mathbf{q}, f_o)$. $^{139}(1/T_1T)$ begins to grow rather sharply below T_{charge} . Since a magnetic long range order is known to set in at $T_{spin} = 42$ K at the time scale of elastic neutron scattering [13] and μSR measurements

[14], our $^{139}(1/T_1T)$ results indicate that charge order triggers enhancement of low frequency Cu spin fluctuations, as noted before [3, 5]. This enhancement is commonly observed for the charge ordered La_2CuO_4 -based superconductors [3, 5, 10, 11, 27, 31, 32]. Inelastic neutron scattering measurements with low energy transfer also provide additional evidence for enhanced spin excitations below T_{charge} in $\text{La}_2\text{CuO}_{4+y}$ [13], as well as in $\text{La}_{1.48}\text{Nd}_{0.4}\text{Sr}_{0.12}\text{CuO}_4$ [33], $\text{La}_{1.88}\text{Ba}_{0.12}\text{CuO}_4$ [24], and $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ [34]. Neutron scattering, however, probes only the bulk averaged behavior of spin excitations by integrating the signals from the entire volume of the samples. We will come back to this point below.

In Fig. 2, we also present $^{63}(1/T_1T)$ measured at the peak of the ^{63}Cu NMR lineshape observed for the nuclear spin $I_z = +1/2$ to $-1/2$ central transition in Fig. 3(a) and (b). Since the magnetic hyperfine interaction of the ^{63}Cu nuclear spin with Cu electron spins [35, 36] is nearly two orders of magnitude larger than that of ^{139}La nuclear spins [37], the overall magnitude of $^{63}(1/T_1T)$ at ~ 60 K is greater by four orders of magnitude. Accordingly, the contribution of the fluctuating EFG to the spin-lattice relaxation process is relatively small. We observed only a small hump of $^{63}(1/T_1T)$ near T_{mobility} .

Turning our attention to the low temperature region deep inside the stage-4 ordered state, we note that $^{63}(1/T_1T)$ increases smoothly down to T_c obeying a Curie-Weiss law, which is indicative of the growth of antiferromagnetic spin correlations commonly observed in superconducting cuprates [10, 38–41]. $^{63}(1/T_1T)$ begins to dive down at T_c without exhibiting a Hebel-Slichter coherence peak. This behavior is also prototypical of the d-wave superconductors [38, 42].

Thus, the $^{63}(1/T_1T)$ results (except for a small hump near T_{mobility}) are representative of the canonical behavior expected for optimally doped high T_c superconductors both above and below T_c with no hints of anomalies associated with charge and spin orders. In contrast, $^{139}(1/T_1T)$ begins to increase below T_{charge} and shows a maximum at ~ 33 K. This indicates that Cu spin fluctuations averaged over the entire volume of the sample are slowing down to the time scale of NMR measurements at ~ 33 K. How can we reconcile the apparent contradiction between $^{63}(1/T_1T)$ and $^{139}(1/T_1T)$ results?

The key to understanding the dichotomy is that $^{63}(1/T_1T)$ and $^{139}(1/T_1T)$ do *not* probe the same parts of the CuO_2 plane. As noted earlier [3–5, 10, 11] and explained in detail in the next section, the ^{63}Cu NMR signal intensity is gradually wiped out below T_{charge} , and hence $^{63}(1/T_1T)$ in Fig. 2 reflects only the behavior of Cu electrons in a shrinking volume fraction of CuO_2 planes which has not been affected by charge order. In contrast, the ^{139}La NMR signal intensity is conserved through T_{charge} owing to the very small hyperfine interactions with Cu electron spins, and hence $^{139}(1/T_1T)$ probes the average behavior of the entire CuO_2 planes.

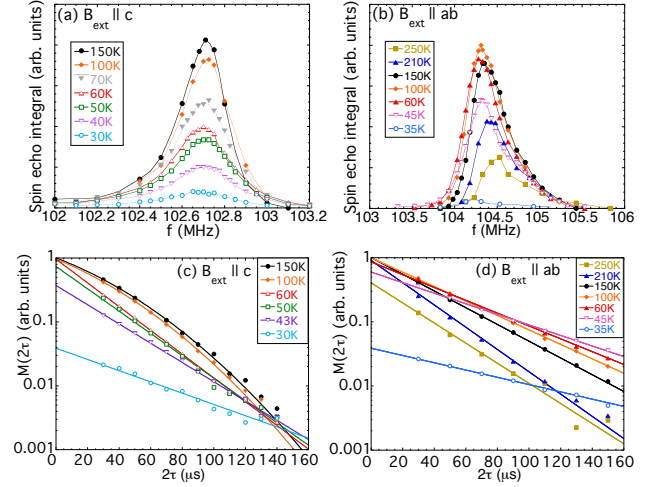


FIG. 3. Representative ^{63}Cu NMR lineshapes measured in $B_{\text{ext}} = 9$ T applied along the crystal (a) c-axis and (b) a-axis at a constant delay time $\tau = 15 \mu\text{s}$. Also shown in (c) and (d) are the spin echo decay curves in $B_{\text{ext}} \parallel c$ and $B_{\text{ext}} \parallel a$, respectively. The magnitude of the spin echo is normalized at $\tau = 15 \mu\text{s}$ using the integral of the lineshapes in (a) and (b). Solid lines are the best Gaussian-Lorentzian fit in (c) and Lorentzian fit in (d). The extrapolation of the fit to $\tau = 0$ therefore yields the integrated intensity of the lineshape in the limit of $\tau = 0$. For example, (c) shows that the intensity at $2\tau = 30 \mu\text{s}$ observed at 60 K appears much smaller than at 100 K and 150 K; but the intensity in the limit of $2\tau = 0$ is conserved above T_{charge} .

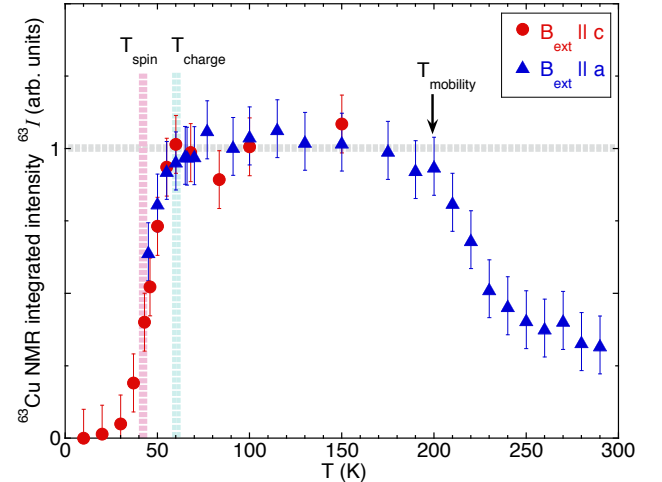


FIG. 4. Temperature dependence of the integrated intensity of ^{63}Cu NMR lineshapes, ^{63}I , corrected for the Boltzmann factor and the transverse relaxation effects based on the results in Fig. 3(c) and (d). For $B_{\text{ext}} \parallel a$, the large superconducting critical field makes the spin echo signal nearly unobservable due to the Meissner effects below T_c .

3. ^{63}Cu NMR signal intensity anomaly below T_{charge}

In Fig. 3(a), we summarize the representative ^{63}Cu NMR lineshapes observed for the $I_z = +1/2$ to $-1/2$ central transition in $B_{\text{ext}} = 9$ T applied along the c -axis. We multiplied the spin echo intensity with temperature T to account for the effect of the Boltzmann factor on the overall intensity. The c -axis ^{63}Cu NMR linewidth $^{63}\Delta f$ grows with decreasing temperature, similarly to the Curie-Weiss behavior of $^{63}\Delta f$ observed for $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ [10]. The integrated intensity is proportional to the number of nuclear spins detected, and conserved between 150 K and 100 K.

The integrated intensity of the lineshape appears to decrease progressively below 100 K down to $T_{\text{charge}} \simeq 60$ K, but it is simply because the transverse nuclear spin-spin relaxation becomes faster toward T_{charge} . As shown in Fig. 3(c), the Gaussian curvature of the spin echo decay observed at 100 K and 150 K disappears, and the spin echo decay observed above $\tau \sim 10 \mu\text{s}$ becomes Lorentzian (i.e. exponential) at T_{charge} [3, 43]. For this reason, when we measure the ^{63}Cu NMR lineshape using the same pulse separation time $\tau = 15 \mu\text{s}$, the intensity appears smaller at T_{charge} than at 100 K. We can eliminate the influence of the transverse relaxation process on the integrated intensity, by extrapolating the spin echo decay curves in Fig. 3(c) to $\tau = 0$. The integrated intensity ^{63}I in the limit of $\tau = 0$ maintains a constant value down to T_{charge} , as summarized in Fig. 4.

Below T_{charge} , however, the situation is very different. Even if we extrapolate the spin echo decay to $\tau = 0$ and eliminate the transverse relaxation effect in the intensity, ^{63}I sharply decreases in the charge ordered state. We confirmed that the integrated intensity of ^{139}La NMR lineshape is conserved even below T_{charge} , and hence the reduction of ^{63}I below T_{charge} down to T_c is not an experimental artifact.

In our recent comprehensive ^{63}Cu NMR study of $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$, we used our state-of-the-art NMR spectrometer to investigate the NMR properties for a wide range of τ between $2 \mu\text{s}$ and $30 \mu\text{s}$ [10]. We demonstrated that ^{63}Cu NMR properties show unprecedentedly strong dependence on τ below $T_{\text{charge}} \simeq 80$ K. We also confirmed that the ^{63}Cu NMR integrated intensity of the narrow central peak is gradually wiped out below T_{charge} , because the missing spectral weight is transferred to a very broad, wing-like ^{63}Cu NMR signal that appears symmetrically on both sides of the narrow central peak. The wing-like signal from the charge ordered segments of the CuO_2 planes has very fast T_1 and T_2 , and can be detected only with extremely short $\tau \sim 2 \mu\text{s}$.

Also summarized in Fig. 3(b) are the ^{63}Cu NMR lineshapes observed in $B_{\text{ext}} = 9$ T applied along the crystal a -axis. The spin echo decay is always Lorentzian in this field geometry as summarized in Fig. 4(d), because the Gaussian term induced by the indirect nuclear spin-spin coupling effect is motionally narrowed [44]. We plot the temperature dependence of the Lorentzian $1/T_2$ di-

vided by T in Fig. 2 for comparison with $1/T_1T$. Since the Redfield contribution $1/T_{2R}$ of the longitudinal relaxation process to the Lorentzian term is proportional to $1/T_1$ [44] and the contribution of the indirect spin-spin coupling term to $1/T_2T \propto \xi$ in the scaling limit, where ξ is the spin-spin correlation length [45], the observed temperature dependence of $1/T_2T$ is very similar to that of $1/T_1T$.

We extrapolated the exponential spin echo decay to $\tau = 0$ in Fig. 3(d), and estimated the temperature dependence of ^{63}I for $B_{\text{ext}} \parallel a$ in Fig. 4. ^{63}I decreases above T_{stage} , because the hopping motion of oxygen ions wipe out the ^{63}Cu NMR signals. This is typical for ionic conductors. In addition, ^{63}I decreases below T_{charge} , in agreement with the results for the $B_{\text{ext}} \parallel c$ geometry. In our recent measurements of $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ with the $B_{\text{ext}} \parallel a$ geometry (see Appendix B in [10]), we were able to observe initial quick spin echo decay from $\tau = 2$ to $10 \mu\text{s}$ arising from the nuclear spins that appear as the wing-like signal for the $B_{\text{ext}} \parallel c$ geometry. It is their contribution that is missing below T_{charge} in Fig. 4.

Since the $B_{\text{ext}} \parallel a$ configuration has one less fitting parameters in the extrapolation of the spin echo decay curves to $\tau = 0$, the ^{63}I data for $B_{\text{ext}} \parallel a$ are less scattered than $B_{\text{ext}} \parallel c$. Moreover, the $B_{\text{ext}} \parallel a$ geometry is free from the uncertainties in the extrapolation caused by the residual Gaussian curvature that manifests itself only for extremely short τ [10]. In fact, the onset of charge order $T_{\text{charge}} \simeq 60$ K in Fig. 4 agrees very well with the recent x-ray scattering reports [9, 12]. The downside of the $B_{\text{ext}} \parallel a$ geometry is that the large superconducting critical field B_{c2} makes NMR signal detection nearly impossible below T_c . Overall, our results of ^{63}I below T_{charge} are very similar to the case of $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ [10], except that charge order in the present case takes place more quickly once it sets in.

To understand the origin of the intensity anomaly in Fig. 4, it is useful to recall that ^{63}Cu NMR signals in typical high T_c cuprates has a large $1/T_1 \sim 2 \times 10^3 \text{ s}^{-1}$. Enhancement of spin correlations by a factor of ~ 5 is sufficient to make ^{63}Cu NMR spin echo signals nearly unobservable due to extremely fast relaxation rates, unless we resort to $\tau \sim 2 \mu\text{s}$ using modern NMR spectrometers. That is why, for example, our earlier ^{63}Cu NQR measurements in the paramagnetic state of La_2CuO_4 covered the temperature range only down to ~ 400 K, where $1/T_1$ reaches $\sim 10^4 \text{ s}^{-1}$ [46, 47]; the spin echo signal cannot be detected when T_1 , and hence T_2 , becomes so fast. In fact, our recent ^{63}Cu NMR study of $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ showed that $1/T_1$ measured for the aforementioned wing-like NMR signal arising from charge ordered domains is ~ 5 times enhanced compared with the normally behaving residual ^{63}Cu NMR signals below T_{charge} .

Our consideration in the previous paragraph provides the key to reconciling the dichotomy exhibited by qualitatively different $^{63}(1/T_1T)$ and $^{139}(1/T_1T)$ in Fig. 2. The former reflects only the diminishing volume fraction of CuO_2 planes that has not been affected by charge

order below T_{charge} . In other words, our NMR results imply that charge order makes the CuO_2 planes extremely inhomogeneous in $\text{La}_2\text{CuO}_{4+y}$ as well as in $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$. The charge ordered segments of CuO_2 planes have enhanced NMR relaxation rates, and they no longer contribute to the ^{63}Cu NMR lineshapes nor $^{63}(1/T_1T)$ measured for the observable signals. In contrast, ^{139}La NMR intensity is conserved except below T_c , where superconducting shielding effects limit the overall signal intensity. Therefore, $^{139}(1/T_1T)$ probes the average behavior of the entire CuO_2 planes. Likewise, the enhancement of the inelastic neutron scattering signals with low energy transfer below T_{charge} probably originates from enhanced spin correlations in charge ordered domains.

IV. SUMMARY AND CONCLUSIONS

In this paper, we described the previously unpublished NMR data to shed a new light on the interplay between the stage-4 excess O^{2-} order, charge order, spin order, and superconductivity in $\text{La}_2\text{CuO}_{4+y}$. Our NMR results show that $\text{La}_2\text{CuO}_{4+y}$ exhibit very peculiar NMR anomalies at $T_{charge} \simeq 60$ K, which we identified first at the charge order transition of the Nd co-doped $\text{La}_{1.48}\text{Nd}_{0.4}\text{Sr}_{0.12}\text{CuO}_4$ [3]. Recent x-ray scattering experiments indeed detected the charge order Bragg peaks successfully below $T_{charge} \simeq 60$ K. We note that we had pointed out the possibility of a charge order transition in $\text{La}_2\text{CuO}_{4+y}$ in [13] based on the present NMR data.

We demonstrated that the structural distortion associated with the spatial order of the mobile O^{2-} ions slow down to the NMR measurement time scale below ~ 200 K and alter the ^{139}La NMR lineshape. The static distortion of the lattice, however, does not complete down to $T_{charge} \simeq 60$ K. Once charge order sets in, the transition reflected on NMR data is sharp, similarly to the case of charge order in $\text{La}_{1.48}\text{Nd}_{0.4}\text{Sr}_{0.12}\text{CuO}_4$ and $\text{La}_{1.88}\text{Ba}_{0.12}\text{CuO}_4$ that sets in immediately after the LTT structure is established [3–5]. In contrast, charge order transition that takes place in the LTO structure of $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ is much more gradual, although the onset temperature is as high as $T_{charge} \simeq 80$ K. It suggests that the static LTT structure is not essential for charge order in La_2CuO_4 -based cuprates. We recall that conventional charge density wave order in NbSe_2 nucleates near the defects at much higher temperatures than the bulk charge density wave transition [48]. $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ must be less disordered than $\text{La}_{1.48}\text{Nd}_{0.4}\text{Sr}_{0.12}\text{CuO}_4$ and possibly $\text{La}_2\text{CuO}_{4+y}$, and defects and/or domain boundaries in the cleaner CuO_2 planes may be playing analogous roles as those in NbSe_2 . ^{139}La and ^{63}Cu NMR properties in $\text{La}_2\text{CuO}_{4+y}$ observed near and below T_{charge} are qualitatively the same as those previously observed for other charge ordered La_2CuO_4 -based cuprates [3–5, 10, 11]. We emphasize that charge order in this and other La_2CuO_4 -based

cuprates does not take place uniformly in space; the fact that ^{63}Cu NMR signals from some segments are observable yet other segments become unobservable due to enhanced spin correlations in this and other La_2CuO_4 -based cuprates implies that the charge ordered state is electronically very inhomogeneous. Even far below T_{charge} , some segments of CuO_2 planes remain unaffected by charge order and subsequent spin order at $T_{spin} = 42$ K. The NMR properties in these domains are similar to those observed for optimally doped superconducting CuO_2 planes. It is important to note that when the superconducting transition and spin order set in simultaneously at 42 K, $\sim 1/3$ of ^{63}Cu NMR signals are still observable with properties very similar to those of optimally doped superconducting phase $\text{La}_{1.85}\text{Sr}_{0.15}\text{CuO}_4$. We recently reported detailed characterization of the analogous two component behavior of the CuO_2 planes for $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$ [10, 11], in which the volume fraction under the influence of enhanced spin correlations reach $\sim 100\%$ at ~ 20 K. We refer readers to [49] for possible theoretical implications of these experimental findings, in particular the relation between the competing order and the volume fractions of the competing phases.

Unlike the typical second order magnetic phase transitions, $^{139}(1/T_1T)$ does not diverge at $T_{spin} = 42$ K, where elastic neutron scattering detect the onset of spin order. This means that the spin fluctuations do not slow down to the NMR measurement time scale at $T_{spin} = 42$ K in most of the sample volume. $^{139}(1/T_1T)$ exhibits a broad hump at ~ 33 K instead, signaling that on average, spin fluctuations slow down to the NMR frequency at a temperature much lower than the onset of spin order. We note that $^{139}(1/T_1T)$ peaks at much lower temperature, ~ 8 K, in the case of $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$. Thus both the charge and spin orders in the present case take place much more sharply than in $\text{La}_{1.885}\text{Sr}_{0.115}\text{CuO}_4$. Finally, we recall that earlier μSR measurements detected the onset of static spin order at $T_{spin} = 42$ K in *some volume* of the sample, but the volume fraction of the statically spin density wave ordered phase at the μSR time scale is less than $\sim 20\%$ even at ~ 2 K [14]. Thus our finding does not contradict with the μSR results.

V. ACKNOWLEDGEMENT

T. I. thanks K. M. Shen and A. W. Hunt for their assistance in NMR data acquisition in the early stage of this work, and B. O. Wells and S. A. Kivelson for their helpful communications during the course of preparing the manuscript. All the NMR measurements were conducted at M.I.T. between 1997 and 1999 with the financial support by NSF DMR 96-23858 and NSF DMR 98-08941. The work at McMaster was financially supported by NSERC and CIFAR. The work at Stanford and SLAC was supported by the U.S. Department of Energy (DOE), Office of Science, Basic Energy Sciences, Materials Sci-

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