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### Identifying the perfect absorption of metamaterial absorbers

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We present a detailed analysis of the conditions that result in unity absorption in metamaterial absorbers to guide the design and optimization of this important class of functional electromagnetic composites. Multilayer absorbers consisting of a metamaterial layer, dielectric spacer, and ground plane are specifically considered. Using interference theory, the dielectric spacer thickness and resonant frequency for unity absorption can be numerically determined from the functional dependence of the relative phase shift of the total reflection. Further, using transmission line theory in combination with interference theory we obtain analytical expressions for the unity absorption resonance frequency and corresponding spacer layer thickness in terms of the bare resonant frequency of the metamaterial layer and metallic and dielectric losses within the absorber structure. These simple expressions reveal a redshift of the unity absorption frequency with increasing loss that, in turn, necessitates an increase in the thickness of the dielectric spacer. The results of our analysis are experimentally confirmed performing reflectionbased terahertz time-domain spectroscopy on fabricated absorber structures covering a range of dielectric spacer thicknesses with careful control of the loss accomplished through water absorption in a semi-porous polyimide dielectric spacer. Our findings can be widely applied to guide the design and optimization of the metamaterial absorbers and sensors.

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#### I. INTRODUCTION

Absorbers have been investigated across the electromagnetic spectrum from microwave to optical region [1-4]. The traditional absorber at microwave frequencies is the circuit-analog absorber usually configured with quarter wavelength thickness with a carefully selected resistivity for the high impedance surface, and the application are limited within the microwave range [5-7]. To overcome these limitations, metamaterial absorbers were proposed and widely studied as three-layer configurations consisting of a dielectric spacer separating two additional layers that are often comprised of metals [1,2,8]. Usually one (or both) of the separated layers is a metasurface designed with a resonance frequency dictated by the subwavelength geometry and local dielectric environment [9-12]. In an absorber configuration at resonance, incident electromagnetic radiation is effectively trapped between the two separated layers and is absorbed in the dielectric and metallic regions, ultimately being dissipated entirely as heat. Although this intuitive explanation is straightforward, theoretical analysis of the nature of unity absorption is important to gain quantitative insights into the underlying physics. Various theories and models have been utilized to advance the understanding of perfect absorption [2, 13-17]. For example, in Ref. [18] mode-coupled theory provides a detailed description of unity absorption in terms of absorptive and radiative losses. However, it is important to develop alternative numerical and analytical strategies that transparently connect with the electromagnetic and dielectric properties of the constituent materials to better understand how experimentally accessible parameters ultimately determine the absorption.

We analyze the conditions resulting in perfect absorption in metamaterials by employing inference theory and transmission line theory. Our results show that the dielectric spacer thickness and frequency for unity absorption can be numerically obtained from the relative phase shift of the total reflection. Additional analysis using transmission line theory reveals that the critical spacer thickness for unity absorption is correlated with the system loss. The results are experimentally verified employing semi-porous polyimide as the dielectric spacer. Our analysis offers new insights towards a more complete understanding of metamaterial perfect absorbers, and can be generally applied to guide the design and optimization of arbitrary absorber geometries.

#### **II. INTERFERENCE THEORY AND PERFECT ABSORPTION**

#### A. Absorber design and interference theory

Without loss of generality, a THz metamaterial absorber composed of an array of split ring resonators (SRRs), a dielectric spacer, and a ground plane was employed as a testbed for the ensuing analysis. The SRR geometry is shown as the inset in Fig. 1(a). The periodicity of the array was 45  $\mu$ m and the permittivity of the spacer material was taken as 2.81×(1+0.03i) for cured polyimide (PI-5878G). The reflection and transmission characteristics of the MMs on top of the spacer in the absence of a ground plane were simulated using the CST Microwave Studio frequency domain solver with periodic boundary conditions. Gold was modeled as lossy metal with conductivity of  $4.56 \times 10^7$  S/m. The complex reflection ( $r_{12}$ ) and transmission ( $t_{12}$ ) coefficients (for the air/SRR array interface) and  $r_{21}$  and  $t_{21}$  (for the spacer/SRR array interface) determined from the simulations are plotted in Fig. 1. According to interference theory the overall reflection of the metamaterial absorber with spacer thickness of *d* can be considered as the interference between the multiple reflections and is expressed as [19,20]:

$$r = r_{12} - \frac{t_{12}t_{21}}{r_{21} + e^{-i2\beta}}$$
(1)

where *r* is the total reflection,  $\beta = n \ k \ d$  is the one-way phase delay in the spacer, and *n*, *k* are the refractive index of the spacer material and the wave number in vacuum, respectively. In the remainder of this manuscript, we term  $r_{12}$  as the first reflection,  $-t_{12}t_{21}/(r_{21}+e^{-i2\beta})$  as the secondary reflection with the absorption expressed as  $A=1-|r|^2$  (due to zero transmission because of the ground plane). As is well known, to subsequently obtain a perfect absorber with the metamaterial structure and spacer material described above, the correct spacer layer thickness for the spacing between the SRR array and a metallic ground plane must be utilized. For a spacer thickness of 5 µm, the gold line in Fig. 1(a) results in unity absorption. The design process for perfect absorption will be explained in detail in the following paragraphs.



FIG. 1. The retrieved reflection and transmission parameters from simulation. (a) Amplitude spectra and (b) phase spectra. The inset shows the geometry of the SRR unit cell with period of 45  $\mu$ m for the array. The perfect absorption spectrum is plotted in (a) for a spacer thickness of 5  $\mu$ m.

#### **B.** Phase shift and perfect absorption

In Eq. 1, the overall reflection is directly related to the spacer thickness which governs the amplitude and phase of the secondary reflection. When the secondary reflection and the first reflection are anti-phased and of the same amplitude for a critical spacer thickness, there will be complete destructive interference, leading to perfect absorption. In this paper, we are only considering the "metamaterial regime," corresponding to the thinnest spacer layer that results in perfect absorption. The phase and amplitude of the first reflection and the secondary reflection for different spacer thicknesses are plotted in Fig. 2(a) and Fig. 2(b), along with labeled absorption peak frequencies. From the phase spectra (Fig. 2(a)), it is evident that the phase difference between the first and secondary reflection is approaches  $\pi$  at the absorption peak frequencies (highlighted with circles). At the critical spacer thickness of  $d = 5 \,\mu$ m the phase shift is almost exactly  $\pi$  as required for perfect absorption. Moreover, as the spacer thickness larger than the amplitude of the first reflection (Fig. 2(b)) increases and gradually becomes larger than the amplitude of the first reflection. As expected, where the amplitudes are equal (Fig. 2(b)) and the phase shift is  $\pi$ , perfect absorption results.



FIG. 2. The (a) phase and (b) amplitude spectra of the first (dashed line) and secondary reflection (solid lines) with different spacer thicknesses. The absorption peak frequency points are labeled with circles. (c) Phase spectra of the total reflection for different spacer thicknesses with the inset showing the corresponding absorption (d) Color plot of the calculated total phase shift as a function of frequency and spacer thickness. The white dashed lines show the spacer thickness (5  $\mu$ m) and the corresponding frequency (1.28 THz) for the perfect absorption.

Of particular importance is the dramatic evolution of the overall phase shift spectrum for spacer thicknesses close to the critical thickness. As shown in Fig. 2(c), at and beyond the critical spacer thickness the phase can cover a full  $2\pi$ . This makes it is possible to pinpoint the perfect absorption point based on the phase shift diagram of the total reflection. Fig. 2(d) depicts the phase shift diagram of the overall reflection versus frequency and spacer thickness. When the spacer thickness is thinner than the critical spacer thickness value, the phase coverage of the total reflection is smaller than  $\pi$ . However, when it is thicker than the critical value, the phase of the overall reflection is able to extend beyond zero and cover the entire  $2\pi$  range due to the increasing effect of the secondary reflection. The critical spacer thickness is the point at which

perfect absorption can be achieved, and can be visually identified on the phase diagram as 5  $\mu$ m and as 1.28 THz in this example. Importantly, although the results of the analysis carried out above apply to the specific metamaterial structure model utilized, the phase shift diagram can, in principle, be employed to pinpoint the spacer thickness and the corresponding frequency for perfect absorption for any other metamaterial structures using their unique reflection and transmission coefficients. In the following, we first verify these results experimentally, and then obtain analytical expressions for the perfect absorption spacer thickness and frequency in terms of the properties of the SRRs and the dielectric function of the spacer layer.

#### C. Experimental validation

Metamaterial absorbers with unit cell structure and geometries illustrated in the inset of Fig. 1(a) (i.e. with the parameters used in the simulations above) were fabricated with different spacer thicknesses by employing polyimide (PI-5878G) as the spacer material. The thickness of the spacer was measured as 3.8  $\mu$ m, 5.3  $\mu$ m, and 6.0  $\mu$ m using surface profilometry. Subsequently, the samples were characterized with THz time domain spectroscopy (THz-TDS). The measured absorption and phase spectra are depicted in Fig. 3 (solid lines) with simulated spectra as comparison (dashed lines). The insets in Fig. 3(a) and Fig. 3(b) show the image of a fabricated sample and the unit cell structure. The evolution of the phase spectra is clearly revealed, with the critical spacer thickness of 5.3  $\mu$ m having near-unity absorption with an abrupt phase shift of  $2\pi$  in the vicinity of the perfect absorption frequency. With the basic description of the perfect absorption phenomena and experimental verification of the phase shift at the critical spacer thickness, we now present a derivation of equations to gain additional insight into metamaterial perfect absorbers.



FIG. 3. Experiment (solid lines) and simulation (dashed lines). (a) Absorption spectra and (b) total reflection phase spectra for metamaterial absorbers with different spacer thicknesses of  $3.8 \mu m$ ,  $5.3 \mu m$ , and  $6.0 \mu m$ . The insets in (a) and (b) show the image of a fabricated sample and the unit cell structure.

#### **III. MATERIAL DEPENDENCE AND PERFECT ABSORPTION**

#### A. Transmission line model

In order to analytically locate the frequency and the spacer thickness to achieve perfect absorption, transmission line theory is used to model the SRRs and calculate the reflection and transmission coefficients ( $r_{12}$ ,  $t_{12}$ ,  $r_{21}$  and  $t_{21}$ ) analytically. SRRs can be modeled as having LC and dipole resonant modes connected in parallel [21]. Further, the impedance of each mode can be expressed as series RLC resonators given as [22]

$$Z_{\text{LC,dipole}} = R_{\text{LC,dipole}} + \frac{2\varepsilon_{\text{i}}}{\omega C_{\text{LC,dipole}} \left(\varepsilon_{\text{r}} + 1\right)^{2}} + j\omega L_{\text{LC,dipole}} + \frac{2}{j\omega C_{\text{LC,dipole}} \left(\varepsilon_{\text{r}} + 1\right)}$$
(2)

where  $\varepsilon_r$  and  $\varepsilon_i$  are the real part and imaginary part of the spacer permittivity.  $Z_{LC}$  and  $Z_{dipole}$  are the impedance of the LC and dipole modes, respectively, and  $R_{LC,diople}$ ,  $L_{LC,diople}$ , and  $C_{LC,diople}$  are the fitted resistance, inductance, and capacitance value for the free standing SRRs (applies to only the metallic structure *without* spacer material), respectively. On the right-hand side of the equation, the first term represents the metallic loss contributed by the joule heating in the SRRs. The second term represents the dielectric loss of the spacer layer and the third and the forth terms are the reactance from the equivalent inductance and capacitance of the SRRs. The Supplementary Material [23] provides details of the fitting to obtain the effective circuit parameters. To simplify the analysis, the coupling between the two modes was neglected and, therefore, the impedance of the MMs can be calculated as:

$$Z_{\rm m} = \frac{Z_{\rm LC} \cdot Z_{\rm dipole}}{Z_{\rm LC} + Z_{\rm dipole}} \tag{3}$$

The impedance values of free space ( $Z_0$ ) and the spacer material ( $Z_d$ ) were set as the impedance values of the input port and output port, respectively, and can be connected by:

$$Z_{\rm d} = k_{\rm m} Z_0 \tag{4}$$

where  $k_{\rm m}$  equals to  $\sqrt{1/(\varepsilon_{\rm r} - i\varepsilon_{\rm i})}$  [24]. The ABCD parameters can be calculated by assuming the transmission line is shunt connected by the impedance of the MMs, and converted to S parameters [25]. Considering that the reference direction is negative, the reflection and transmission parameters are the conjugate of the S-parameters as:

$$\begin{bmatrix} \overline{r_{12}} & \overline{t_{21}} \\ \overline{t_{12}} & \overline{r_{21}} \end{bmatrix} = \begin{bmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{bmatrix} = \frac{1}{(k_{\rm m}+1)Z_{\rm m}+k_{\rm m}Z_0} \begin{bmatrix} (k_{\rm m}-1)Z_{\rm m}-k_{\rm m}Z_0 & 2\sqrt{k_{\rm m}}Z_{\rm m} \\ 2\sqrt{k_{\rm m}}Z_{\rm m} & (1-k_{\rm m})Z_{\rm m}-k_{\rm m}Z_0 \end{bmatrix}$$
(5)

The reflection and transmission coefficients obtained from Eq. 5 can subsequently be substituted into Eq. 1 to calculate the overall reflection, as well as the absorption. The absorption diagrams calculated by using parameters retrieved from transmission line model and full wave electromagnetic simulations for different spacer thicknesses are plotted in Fig. 4 (a) and Fig. 4 (b). The marked similarity between the theoretical and numerical results validates the transmission line modeling. The absorption peak amplitude gradually increases as the spacer becomes thicker until the critical spacer thickness, beyond which the absorption peak amplitude decreases.



FIG. 4. Absorption diagram based on the reflection and transmission parameters retrieved from (a) transmission line model and (b) simulation.

#### **B.** Conditions for perfect absorption

Finally, our approach allows for the determination of analytical expressions (see derivation presented in the Supplementary Material [23]) of the critical spacer thickness ( $d_p$ ) and the corresponding frequency ( $f_p$ ) for perfect absorption which are expressed as:

$$d_{\rm p} = \frac{k_{\rm c} \cdot (k_{\rm m} + 1) \cdot c}{4\pi f_{\rm LC}} \sqrt{\frac{a}{Z_0} - \frac{a^2}{Z_0^2}}$$
(6)

$$f_{\rm p} = f_{\rm LC} - \frac{\sqrt{aZ_0 - a^2}}{4\pi L_{\rm LC}}$$
(7)

where  $k_c$  is a correction coefficient chosen as 1.4 for our case (see further details in the Supplementary Material [23]), *c* is the speed of light, *a* is the real part of  $Z_m$  composed of the metallic loss of the metamaterial structure (first term on the right side of Eq. 2) and the dielectric loss of the spacer material (second term on the right side of Eq. 2), and  $f_{LC}$  is the LC resonant frequency for the MMs on polyimide (in the absence of a ground plane):

$$f_{\rm LC} = \frac{1}{2\pi} \sqrt{\frac{2}{L_{\rm LC} C_{\rm LC} (\varepsilon_{\rm r} + 1)}}$$
(8)

#### C. Spacer permittivity and perfect absorption

The predictions from Eqns. 6-8 can be compared to the values obtained from full-wave electromagnetic simulations (e.g. phase shift diagrams like that in Fig. 2(d)) and from the analytical calculations using Eqns. 1-5. This comparison is made in Fig. 5(a) and (b) for different combinations of spacer material permittivity. The results for the three approaches are calculated at discrete points (as described below) and the lines are to guide the eye. In Fig. 5(a), the imaginary permittivity ( $\varepsilon_i$ ) was kept constant (0.0843), while the real part ( $\varepsilon_r$ ) increases from 2 to 6. With increasing  $\varepsilon_r$ , the resonant frequency of the MMs decreases due to the increased equivalent capacitance (Eq. 2) and, thus, according to Eq. 7, the absorption peak frequency undergoes a red shift. However, the critical spacer thickness for perfect absorption remains nearly constant since the SRR resonant frequency ( $f_{LC}$ ) and the loss of the system (a) decrease at the same time, essentially canceling one another (see Eqn. 6). In Fig. 5(b), the real permittivity is held constant (2.81), while  $\varepsilon_i$  increases from 0.1 to 0.5. Due to the increase in the loss caused by the larger  $\varepsilon_i$ , the spacer thickness for perfect absorption increases (according to Eq. 6), and the frequency undergoes a redshift (according to Eq. 7). Clearly, Eqns. 6-8 agree quite well with the numerical simulations and the calculations using Eqns. 1-5, although the discrepancy increases with larger loss (Fig. 5(b)) due to the low loss assumption in the derivation of Eq. 6-8. With the retrieved spacer thickness, one can optimize the design to realize perfect absorption. Fig. S3 [23] shows the absorption spectra with the optimized spacer thicknesses for different permittivity combinations. It is worthwhile to note the importance of the loss for the occurrence of the perfect absorption. As shown in Eq. 6, when the loss is zero (a = 0), the critical spacer thickness must be zero, which essentially means no perfect absorption for any spacer layer thickness.



FIG. 5. Perfect absorption frequencies determined from simulations, analytical calculations based on Eqns. 1-5, and the explicit values from Eqns. 6-8. The lines are to guide the eye. (a) Varying  $\varepsilon_r$  while keeping  $\varepsilon_i = 0.0843$ . (b) Varying  $\varepsilon_i$  while keeping  $\varepsilon_r 2.81$ .

#### **D.** Experimental verification

The dramatic increase in the phase shift in the vicinity of the critical spacer thickness was experimentally verified in Fig. 3(b). We have used these same samples to investigate the effects of increased loss due to an increase in  $\varepsilon_i$  of the dielectric spacer layer. This was accomplished by exposing the perfect absorbers to 85% humidity for 48 hours at 40 °C for water absorption which increases the loss of the polyimide spacer [26]. THz-TDS was used to characterize the samples right after the treatment. We estimate that the dielectric response of the polyimide changes from 2.81+i0.084 to 2.9+i0.1305 – that is, the permittivity increases as does the loss with increasing humidity. The measured absorption spectra and reflection phase spectra are plotted in Fig. 6 with solid lines, and the simulation results are depicted in Fig. 6 with dashed lines. By comparing with Fig. 3(a) and 6(a), it is clear that the increase in the real part of the permittivity of the spacer material (from 2.81 to 2.90) causes the red shift of the absorption peaks. More interestingly, comparing Fig. 3(b) with 6(a) reveals that as the loss in the spacer material increases (from 0.0843 to 0.1305), the critical spacer thickness increases from 5.3  $\mu$ m to 6.0  $\mu$ m. This is evident because the phase shift spectra for the 5.3  $\mu$ m film no longer exhibits a full  $2\pi$  phase shift following water absorption by the polyimide indicating that this is below the critical spacer layer thickness required for near-unity absorption.



FIG. 6. Experiment (solid lines) and simulation (dashed lines). (a) Absorption spectra and (b) total reflection phase spectra for treated metamaterial absorbers with different spacer thicknesses.

#### **IV. DISCUSSION AND CONCLUSION**

Our theoretical and experimental results demonstrate that the perfect absorption frequency of metamaterial absorbers is closely related to the bare resonant frequency of the SRR array, and is determined by the metallic structure of the SRRs ( $L_{LC,dipole}$  and  $C_{LC,dipole}$ ) and by the permittivity of the spacer material ( $\varepsilon_r$ ). The frequency shifts are governed by the material loss stemming from both the metallic loss of the metamaterial structure ( $R_{LC,dipole}$ ) and the dielectric loss of the spacer material ( $\varepsilon_i$ ). More specifically, an increase in  $\varepsilon_r$  redshifts the absorption peak frequency, and with higher material loss, a larger spacer thickness is needed for perfect absorption. The frequency and the spacer thickness can be accurately identified on the phase diagram as shown in Fig. 2(d) or approximately calculated with Eq. 6 and Eq. 7.

In conclusion, we demonstrate that the perfect absorption frequency and spacer layer thickness can be visually pinpointed on plot of the phase shift of the total reflection. Additionally, using the transmission line theory to model the metamaterial resonators, we have obtained analytical formulas for the perfect absorption frequency and spacer layer thickness that reveal the functional dependence on material losses. We note that our findings are not directly applicable to absorbers with other configurations, such as all metal or all dielectric absorbers [27, 28]. Nonetheless, our findings offer a powerful tool for the design and optimization of metamaterial

absorbers with a metamaterial - dielectric spacer - metal configuration. Our results can be reasonably scaled across the spectrum.

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