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Spin-isotropic continuum of spin excitations in antiferromagnetically ordered $\text{Fe}_{1.07}\text{Te}$

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Unconventional superconductivity typically emerges in the presence of quasi-degenerate ground states, and the associated intense fluctuations are likely responsible for generating the superconducting state. Here we use polarized neutron scattering to study the spin space anisotropy of spin excitations in $\text{Fe}_{1.07}\text{Te}$ exhibiting bicollinear antiferromagnetic (AF) order, the parent compound of $\text{FeTe}_{1-x}\text{Se}_x$ superconductors. We confirm that the low energy spin excitations are transverse spin waves, consistent with a local-moment origin of the bicollinear AF order. While the ordered moments lie in the ab -plane in $\text{Fe}_{1.07}\text{Te}$, it takes less energy for them to fluctuate out-of-plane, similar to BaFe_2As_2 and NaFeAs . At energies above $E \gtrsim 20$ meV, we find magnetic scattering to be dominated by an isotropic continuum that persists up to at least 50 meV. Although the isotropic spin excitations cannot be ascribed to spin waves from a long-range ordered local moment antiferromagnet, the continuum can result from the bicollinear magnetic order ground state of $\text{Fe}_{1.07}\text{Te}$ being quasi-degenerate with plaquette magnetic order.

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Unconventional superconductivity in cuprate and heavy fermion superconductors emerge in the vicinity of multiple exotic orders that are quasi-degenerate in energy^{1–4}, providing a plethora of fluctuations that may enhance or even generate superconductivity. Iron-based superconductors are found close to several different magnetic instabilities^{5–14}, suggesting an important role for magnetism in their superconductivity^{15,16}. In addition, these materials may exhibit quasi-degenerate ground states, realized through magnetic frustration and electron correlations^{17,18}. These interactions are epitomized in the iron chalcogenide $\text{FeTe}_{1-x}\text{Se}_x$ series, with magnetism evolving from bicollinear (BC) magnetic order in Fe_{1+y}Te ^{7,19} towards competing stripe and Néel fluctuations without static magnetic order in FeSe ²⁰. Understanding the nature of magnetic fluctuations and manifestations of magnetic frustration is therefore a key step towards elucidating the physics of these materials.

Compared to the parent compounds of iron pnictides that order at the in-plane wave vector $\mathbf{Q} = (0.5, 0.5)$ of the paramagnetic tetragonal unit cell corresponding to the nesting wave vector of electron and hole Fermi surfaces (stripe AF order)^{21,22}, the parent compound of iron chalcogenide superconductors Fe_{1+y}Te orders at or near $\mathbf{Q} = (0.5, 0)$ ^{7,19}, despite sharing a similar electronic structure with the iron pnictides^{23,24}. Furthermore, Fe_{1+y}Te exhibits significantly larger ordered moments^{7,19} and stronger electronic correlations²⁵ than iron pnictides. These results point to localized magnetism in Fe_{1+y}Te , although the presence itinerant carriers can cause damping of the magnetic excitations.

At low interstitial iron concentrations ($y < 0.12$), Fe_{1+y}Te exhibits long-range BC order with the ordering vector $\mathbf{Q} = (0.5, 0)$ and ordered moments along the b -axis

[Figs. 1(a) and 1(b)]. For $y \sim 0.12$, a collinear short-range-ordered phase that orders at $\mathbf{Q} = (\delta, 0)$ ($\delta \sim 0.45$) with moments along b -axis is found. For $y > 0.12$, helical magnetic order at $\mathbf{Q} = (\delta, 0)$ ($\delta \sim 0.38$) with moments rotating in the bc -plane is stabilized^{26,27}.

The complexity of magnetism in Fe_{1+y}Te likely arises from frustration, suggested experimentally by spin fluctuations that persist to ~ 200 meV^{28–30} compared to a much smaller Curie-Weiss temperature³¹. Competition between different ground states is also manifested above T_N in Fe_{1+y}Te exhibiting BC order, with fluctuations at an incommensurate wave vector $\mathbf{Q} = (\delta, 0)$ shifting to the commensurate wave vector $\mathbf{Q} = (0.5, 0)$ below T_N ^{27,32}. Theoretically, BC order is degenerate with plaquette (PQ) order that also orders at $\mathbf{Q} = (0.5, 0)$ ³³, this degeneracy is removed through spin-lattice coupling³⁴ or ring-exchange³³ in Fe_{1+y}Te , with BC order prevailing as the ground state although PQ order remains quasi-degenerate in energy. Spin fluctuations associated with the two orders are also difficult to disentangle, with measurements using unpolarized neutrons scattering interpreted as damped spin waves from BC order²⁸ or short-range PQ fluctuations³⁰. Separating spin fluctuations associated with competing states is therefore an integral part to elucidating the nature of magnetism in Fe_{1+y}Te .

In this work, we study the spin space anisotropy of spin fluctuations in $\text{Fe}_{1.07}\text{Te}$ exhibiting BC order below $T_N \approx 68$ K using polarized neutron scattering. We observe two transverse spin wave modes associated with the BC order that display different spin-anisotropy gaps. Although the ordered moments lie in the Fe-Te plane, spin waves corresponding to spins rotating out of the plane occur at a lower energy, similar to BaFe_2As_2 ^{35,36} and NaFeAs ³⁷. Surprisingly, we observe a continuum of

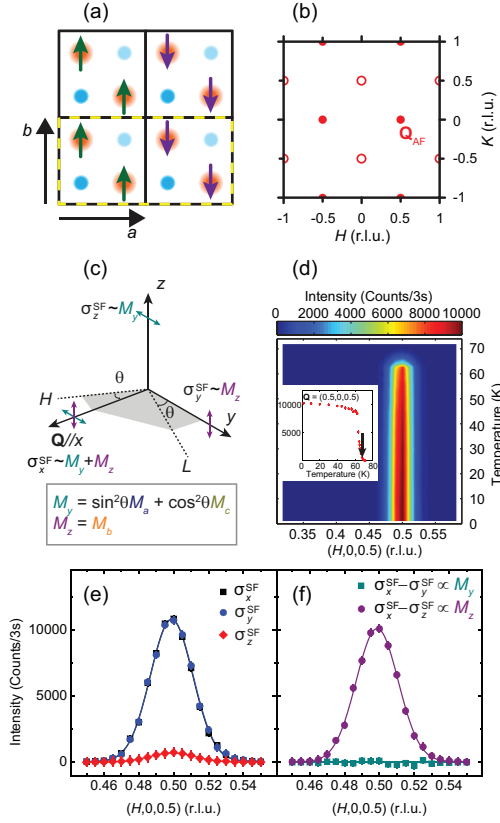


Figure 1: (Color online) (a) The in-plane BC AF structure of $\text{Fe}_{1.07}\text{Te}$ with the ordered moments along the b -axis. The solid black lines enclose chemical unit cells. Anti-parallel ordered moments are shown with different colors. (b) The reciprocal space of magnetically ordered $\text{Fe}_{1.07}\text{Te}$, with AF zone centers represented by red circles. For BC order domains ordering at $\mathbf{Q} = (0.5, 0)$ (closed circle) or $\mathbf{Q} = (0, 0.5)$ (open symbol) can form. (c) Schematic of experimental geometry, the $[H, 0, L]$ scattering plane is represented by the shaded gray area, and the angle between \mathbf{Q} and $(1, 0, 0)$ is θ . In this scattering plane, only the domain ordering at $\mathbf{Q} = (0.5, 0)$ is probed. (d) Color-coded temperature dependence of elastic scans along $[H, 0, 0.5]$ for σ_x^{SF} demonstrating a first-order magnetic transition with $T_N \approx 68$ K. The inset shows the temperature dependence of intensity measured at $\mathbf{Q}_{AF} = (0.5, 0, 0.5)$, the arrow marks $T_N \approx 68$ K. No discernible intensity is seen at incommensurate wave vectors below T_N , although above T_N there is diffuse magnetic scattering centered at an incommensurate position⁴¹. (e) Elastic scans of $\sigma_\alpha^{\text{SF}}$ ($\alpha = x, y, z$) along $[H, 0, 0.5]$ at $T = 2$ K. (f) The differences $\sigma_x^{\text{SF}} - \sigma_y^{\text{SF}}$ and $\sigma_x^{\text{SF}} - \sigma_z^{\text{SF}}$ obtained from results in (e).

isotropic scattering that extends to at least 50 meV. Our findings can be understood to result from the BC order ground state of Fe_{1+y}Te being quasi-degenerate with PQ order, producing an excitation spectra consisting of transverse spin waves and an isotropic spin-liquid-like response.

Polarized neutron scattering measurements were carried out using the IN22 triple-axis spectrometer equipped with CRYOPAD at Institut Laue-Langevin, Grenoble,

France. Heusler monochromator and analyzer with fixed k_f of 2.66 \AA^{-1} or 3.84 \AA^{-1} were used to carry out longitudinal polarization analysis. We aligned 7 grams of Fe_{1+y}Te single crystals with $y = 0.07(2)$ ($a \approx b \approx 3.80 \text{ \AA}$, $c \approx 6.24 \text{ \AA}$) in the $[H, 0, L]$ scattering plane, the amount of excess iron is estimated by comparing $T_N \approx 68$ K [inset in Fig. 1(d)] of our sample with the well-established Fe_{1+y}Te phase diagram²⁶. Using the tetragonal chemical unit cell of Fe_{1+y}Te , BC AF order is observed at $\mathbf{Q}_{AF} = (0.5, 0, L)$ with $L = 0.5, 1.5, 2.5 \dots$ [Fig. 1(b)]. Magnetic neutron scattering directly measures the magnetic scattering function $S^{\alpha\beta}(\mathbf{Q}, E)$, which is proportional to the imaginary part of the dynamic susceptibility $\text{Im}\chi^{\alpha\beta}(\mathbf{Q}, E)$ through the Bose factor, $S^{\alpha\beta}(\mathbf{Q}, E) \propto [1 - \exp(-\frac{E}{k_B T})]^{-1} \text{Im}\chi^{\alpha\beta}(\mathbf{Q}, E)$ ³⁸. We denote the diagonal components of the magnetic scattering function $S^{\alpha\alpha}$ as M_α ³⁹. Three neutron spin-flip (SF) cross sections σ_x^{SF} , σ_y^{SF} , and σ_z^{SF} were measured and normalized by monitor count units (m.c.u.), with the usual convention $x \parallel \mathbf{Q}$, $y \perp \mathbf{Q}$ in the scattering plane, and z perpendicular to the scattering plane [Fig. 1(c)]. Neutron SF cross sections measure components of M_α that are perpendicular to both \mathbf{Q} and the polarization direction, therefore M_y contributes to σ_x^{SF} and σ_z^{SF} whereas M_z contributes to σ_x^{SF} and σ_y^{SF} [Fig. 1(c)]. Since ordered moments in Fe_{1+y}Te with BC order are oriented along b -axis which is parallel to z , elastic magnetic scattering should be seen in σ_x^{SF} and σ_y^{SF} , as confirmed in our experiment [Fig. 1(e)]. A small peak is also observed in σ_z^{SF} due to non-perfect polarization of neutrons resulting in a flipping ratio of $R \approx 14.5$. M_y and M_z can be obtained through $M_y = c(\sigma_x^{\text{SF}} - \sigma_y^{\text{SF}})$ and $M_z = c(\sigma_x^{\text{SF}} - \sigma_z^{\text{SF}})$, with $c = (R - 1)/(R + 1)$. Doing so eliminates effects due to background, non-magnetic scattering and non-ideal polarization of the neutron beam⁴⁰. For elastic magnetic scattering, a peak is seen in M_z while M_y is completely flat [Fig. 1(f)], as expected for BC order with moments along the b -axis.

In $\text{Fe}_{1.07}\text{Te}$, M_z is uniquely associated with the direction of the ordered moments (longitudinal direction), while M_y is a combination of the two transverse directions [Fig. 1(c)]. This contrasts with similar setups in BaFe_2As_2 ³⁶ and NaFeAs ³⁷ where M_z corresponds to a transverse direction and M_y is a mixture of the longitudinal direction and another transverse direction. Therefore for Fe_{1+y}Te , fluctuations along the longitudinal direction can be directly probed in M_z .

Fig. 2 summarizes constant- \mathbf{Q} scans at several equivalent wave vectors corresponding to AF zone centers. Whereas at low energies the magnetic fluctuations are dominated by transverse spin waves in M_y [Fig. 2(a)-(d)]²⁷, clear longitudinal fluctuations are seen in M_z above ~ 20 meV and the excitations become isotropic with $M_y \approx M_z$ above ~ 35 meV [Fig. 2(e)-(h)]. Isotropic scattering that appears for $E \gtrsim 20$ meV, as indicated by the broad onset of longitudinal fluctuations, depends weakly on energy and extends over a large energy range (persisting up to at least 50 meV), forming a continuum

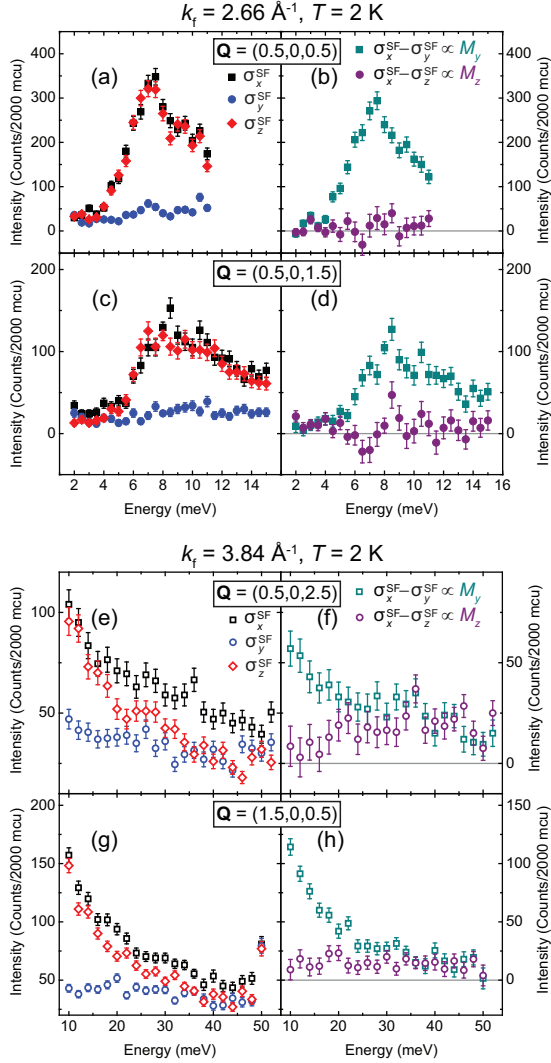


Figure 2: (Color online) Constant- \mathbf{Q} scans of σ_x^{SF} , σ_y^{SF} and σ_z^{SF} at (a) $\mathbf{Q} = (0.5, 0, 0.5)$, (c) $\mathbf{Q} = (0.5, 0, 1.5)$, (e) $\mathbf{Q} = (0.5, 0, 2.5)$ and (g) $\mathbf{Q} = (1.5, 0, 0.5)$. The corresponding differences $\sigma_x^{\text{SF}} - \sigma_y^{\text{SF}}$ and $\sigma_x^{\text{SF}} - \sigma_z^{\text{SF}}$ are respectively shown in (b), (d), (f) and (h). Closed and open symbols are measured with fixed $k_f = 2.66 \text{ \AA}^{-1}$ and $k_f = 3.84 \text{ \AA}^{-1}$, respectively.

of scattering. Measurement of non-spin-flip cross sections confirm these conclusions⁴¹. Such isotropic excitations are unexpected for an ordered local moment antiferromagnet which should exhibit transverse spin waves, and also cannot be accounted for by Fermi surfaces that are connected by $\mathbf{Q} = (0.5, 0.5)$ ^{23,24}. Instead, as discussed below, the isotropic continuum of scattering can be identified as fluctuations associated with PQ order that is quasi-degenerate with the BC ground state³³.

Since the two transverse directions are mixed in M_y depending on the angle between \mathbf{Q} and H [Fig. 1(c)], measurements at equivalent wave vectors are needed to separate them⁴⁰. Combining data from equivalent wave vectors from Fig. 2, M_a , M_b and M_c can be obtained, as shown in Fig. 3(a). For M_a and M_c corresponding to

the two transverse directions, spin wave modes exhibiting different anisotropy gaps can be clearly seen, along with a continuum of isotropic scattering at higher energies. Although the ordered moments are along the b -axis inside the ab -plane, the c -axis polarized spin waves are lower in energy similar to iron pnictide parent compounds^{36,37}. The low-energy transverse spin waves also display a dispersion of $\sim 5 \text{ meV}$ along L ⁴¹, in agreement with previous results²⁹.

The c -axis polarized spin waves dominating for $E \lesssim 10 \text{ meV}$ can also be seen in L -scan of M_y in Fig. 3(b), the fast drop of intensity with increasing L is due to the decreasing contribution of M_c as \mathbf{Q} turns towards the c -axis [Fig. 1(c)]. This should be contrasted with isotropic paramagnetic scattering above T_N with $\sigma_y^{\text{SF}} \approx \sigma_z^{\text{SF}}$ [Fig. 3(c)], which falls off with L following the magnetic form factor [Fig. 3(b)]. The L -dependence of M_y at 2 K in Fig. 3(b) is fit to a lattice sum of Lorentzians that has both the c - and a -axis polarized components, resulting in a ratio of 4(1) for the two components, consistent with Fig. 3(a). The strongly anisotropic magnetic excitations shown in Fig. 3(a) suggests spin anisotropy may affect calculation of the local susceptibility at low energies and application of the sum rule, where isotropic scattering is typically assumed^{15,42}. Previously, it has been suggested that the strong peak in energy at $\mathbf{Q}_{\text{AF}} = (0.5, 0)$ and $E \sim 7 \text{ meV}$ in Fe_{1+y}Te may be linked to the resonance seen in superconducting $\text{Fe}_{1+y}\text{Te}_{1-x}\text{Se}_x$ that occurs at a similar energy but different wave vector $\mathbf{Q} = (0.5, 0.5)$ ^{30,43}. Here we establish that the strong peak in $\text{Fe}_{1.07}\text{Te}$ is polarized along the c -axis similar to the resonance mode in FeSe ⁴⁴, but different from the resonance mode in superconducting $\text{Fe}_{1+y}\text{Te}_{1-x}\text{Se}_x$ that has both in-plane and out-of-plane components^{45,46}. Our observation that the c -axis polarized spin waves being lower in energy for Fe_{1+y}Te with BC order also accounts for rotation plane (bc -plane rather than ab -plane) of the helical magnetic structure seen in samples with $y > 0.12$ ^{26,27}.

Having established the presence of both transverse spin waves and an isotropic continuum of scattering at \mathbf{Q}_{AF} , we studied the momentum dependence of these excitations in comparison with isotropic paramagnetic scattering above T_N , as shown in Fig. 4 (temperature evolution of the scattering cross sections is shown in Supplemental Materials⁴¹). For $T = 2 \text{ K}$ [Figs. 4(a) and (c)], the momentum dependence of M_z can be described as short-range PQ correlations^{30,47}, and M_y as a sum of the same short-range PQ correlations and a Gaussian peak centered at $\mathbf{Q} = (0.5, 0)$ (dotted lines). These results provide additional evidence that below T_N , the isotropic scattering that appears in both M_y and M_z is associated with PQ order, whereas the signal only present in M_y is due to transverse spin waves of the BC ground state. Below T_N , the transverse spin waves dominate for $E = 8 \text{ meV}$ [Fig. 4(a)] whereas for $E = 22 \text{ meV}$ the two components become comparable [Fig. 4(c)]. Above T_N , the scattering becomes isotropic and centered at an incommensurate position ($\sim 0.4, 0$) [Figs. 4(b) and (d)], and can also be de-

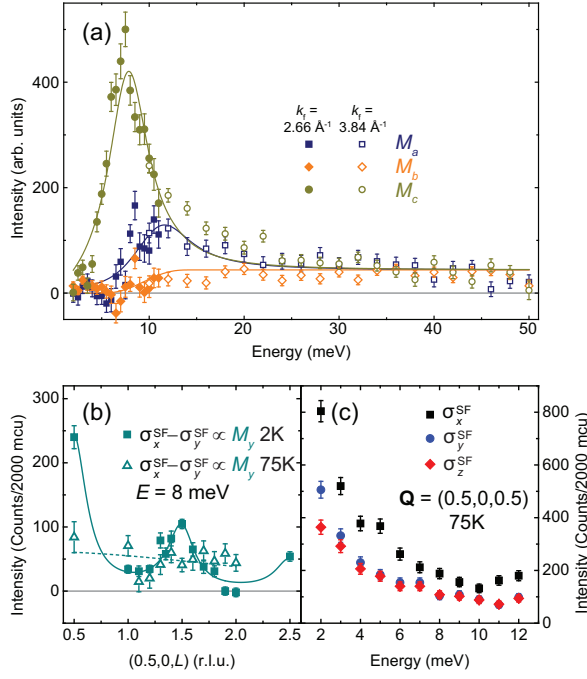


Figure 3: (Color online) (a) M_a , M_b and M_c for the AF zone centers obtained from data in Fig. 2. Results obtained using different k_f are scaled for best match at $E = 10 \text{ meV}$. The solid lines are fits to damped harmonic oscillators in M_a and M_c , and a broad isotropic response appears in all three channels. (b) Constant-energy scans of M_y along $(0.5, 0, L)$ for $E = 8 \text{ meV}$ at 2 K and 75 K. The solid line is fit to a lattice sum of Lorentzian peaks, the dashed line represents L -independent isotropic scattering that is only modulated by the Fe^{2+} magnetic form factor. (c) Constant- \mathbf{Q} scans of the three SF cross sections in the paramagnetic state ($T = 75 \text{ K}$) at $\mathbf{Q} = (0.5, 0, 0.5)$. Anisotropy is only observed for $E \lesssim 2 \text{ meV}$, extending down to $E = 0$ forming anisotropic diffuse magnetic scattering⁴¹.

scribed as a sum of short-range PQ correlations (dashed lines) and a Gaussian peak centered at $\mathbf{Q} = (0.5, 0)$ (dotted lines). Our results suggest above T_N fluctuations associated with BC and PQ orders are both present, with the overall intensity centered at $\mathbf{Q} \sim (0.4, 0)$. When BC order is selected as the ground state below T_N , transverse spin waves become dominant at low energies and the overall signal shifts to $\mathbf{Q} = (0.5, 0)$, as experimentally observed^{27,32}.

The isotropic continuum of scattering in $\text{Fe}_{1.07}\text{Te}$ is clearly inconsistent with transverse spin waves arising from BC order, it also cannot be interpreted as two-magnon scattering which only appears along the longitudinal direction^{48,49}. Instead, it is most naturally associated with short-range PQ order⁵⁰: while a long-range PQ order would generate spin waves which appear only in the transverse channels, a short-range PQ order produces collective excitations that are isotropic. The quasi-degeneracy³³ of the short-range PQ order with the long-range BC order ensures that such excitations occur at rel-

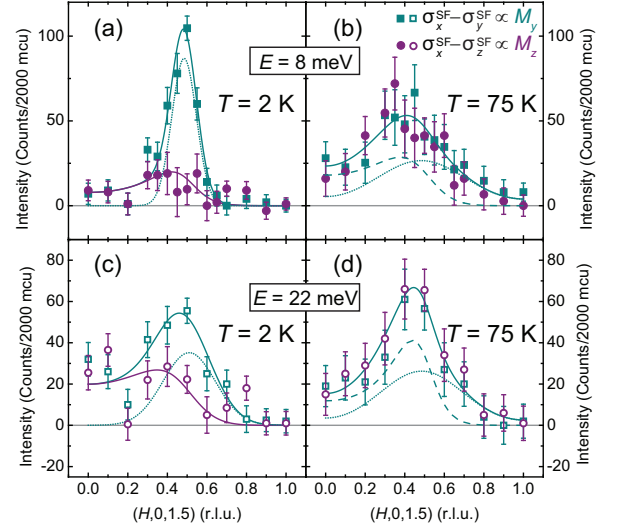


Figure 4: (Color online) Scans of $\sigma_x^{\text{SF}} - \sigma_y^{\text{SF}}$ and $\sigma_x^{\text{SF}} - \sigma_z^{\text{SF}}$ along $[H, 0, 1.5]$ for $E = 8 \text{ meV}$ at (a) 2 K and (b) 75 K. Similar scans are shown for $E = 22 \text{ meV}$ at (c) 2 K and (d) 75 K. The closed and open symbols are measured with fixed $k_f = 2.66 \text{ \AA}^{-1}$ and $k_f = 3.84 \text{ \AA}^{-1}$, respectively. Lines are fits as described in the text.

atively low energies, as we have observed here. The presence of both spin waves and a continuum of scattering is also observed in proximate spin liquid materials such as KCuF_3 ⁵¹ and $\alpha\text{-RuCl}_3$ ⁵², where weak magnetic order is the ground state. Spin excitations in these materials are from quasi-degeneracy of spin liquid states and magnetically ordered states, with spin waves from ordered state appear at lower energies⁵². In Fe_{1+y}Te below T_N , the similar observation is caused by quasi-degeneracy of two different magnetic orders.

The picture of PQ order being quasi-degenerate with BC order also implies that a small external perturbation can tilt the balance in the stability of the two orders. Indeed, it was found that the large magnetic moment on interstitial iron in $\text{Fe}_{1+y}\text{Te}_{0.62}\text{Se}_{0.38}$ induces short-range spin arrangements resembling the PQ order⁵³, suggesting excess interstitial iron in Fe_{1+y}Te would similarly favor PQ over BC order locally. This view is consistent with the observation that BC order is destabilized with increasing excess iron²⁶.

To summarize, our polarized neutron scattering results in $\text{Fe}_{1.07}\text{Te}$ point to the presence of both transverse spin waves associated with BC order and a continuum of isotropic excitations likely associated with short-range PQ order. This provides evidence for the quasi-degeneracy between the short-range PQ order and the long-range BC order and, thereby, the strongly frustrated nature of local-moment magnetism in the iron chalcogenides. Our findings underscore the importance of electron correlations to the magnetism and superconductivity in the iron-based materials.

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