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Influence of the magnetic proximity effect on spin-orbit torque efficiencies in ferromagnet/platinum bilayers

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Abstract

Current-induced spin-orbit torques in Co₂FeAl/Pt ultrathin bilayers are studied using a magnetoresistive harmonic response technique, which distinguishes the dampinglike and fieldlike contributions. The presence of a temperature-dependent magnetic proximity effect is observed through the anomalous Hall and anisotropic magnetoresistances, which are enhanced at low temperatures for thin platinum thicknesses. The fieldlike torque efficiency decreases steadily as the temperature is lowered for all Pt thicknesses studied, which we propose is related to the influence of the magnetic proximity effect on the fieldlike torque mechanism.

Through the spin-orbit interaction (SOI), an electrical current \mathbf{j}_e in a ferromagnet(F)/nonmagnetic metal(N) bilayer results in a torque on the magnetization \mathbf{M} of F[1, 2]. This spin-orbit torque (SOT) may be decomposed into two perpendicular components – a component oriented along $\hat{\mathbf{m}} \times (\hat{\mathbf{m}} \times \hat{\boldsymbol{\sigma}})$ and a component along $\hat{\mathbf{m}} \times \hat{\boldsymbol{\sigma}}$, where $\hat{\boldsymbol{\sigma}} \equiv \hat{\mathbf{j}}_e \times \hat{\mathbf{n}}$ denotes the orientation of the spin current created by the SOI and $\hat{\mathbf{n}}$ defines the unit vector normal to the plane formed by the F/N interface. These are referred to respectively as the dampinglike (DL) and fieldlike (FL) SOTs. Although the microscopic origins of the DL and FL SOTs remain unclear, the DL contribution has been widely interpreted using N bulk spin-Hall effect (SHE) diffusion models[2–5], and the FL contribution attributed to the F/N interfacial SOI[1, 4]. Amin and Stiles [6] have recently emphasized that this interpretation is overly simplistic, showing that the interfacial SOI and the SHE in the N layer may both produce FL *and* DL torques depending on the interface details. Unfortunately, the interfacial parameters used in spin diffusion models are not easily measured, and it remains an experimental challenge to separately identify the origins of the DL and FL torques. Also, in bilayers where interface scattering is dominant, a conventional normal-to-interface spin diffusion length becomes difficult to define. Furthermore, magnetic proximity effects (MPE) at F/N interfaces have been widely reported[7–10], yet how the MPE influences SOTs is unknown.

In this article, we report a decrease in the FL and DL torques per unit current density (hereafter referred to as SOT efficiencies) at low temperature in $\text{Co}_2\text{FeAl}/\text{Pt}$ bilayers. In the same bilayers, a temperature-dependent MPE is revealed through magnetoresistance (MR) measurements. The FL SOT efficiency is suppressed by nearly a factor of 4 at 20 K with respect to room temperature for all Pt thicknesses studied, which we propose is related to the increasing influence of the MPE exchange field on the F/N interface Rashba spin accumulation. Meanwhile, the DL SOT efficiency monotonically increases with decreasing Pt thickness and closely tracks the Pt resistivity as temperature is varied. Within the Pt SHE diffusion model, the latter observation may be described by either the intrinsic SHE or spin backflow processes, between which we cannot differentiate.

The F/N bilayers used in this study were grown on $\text{MgO}(001)$ substrates by molecular-beam epitaxy (MBE). Prior to F growth, an *in-situ* MgO buffer was grown by e-beam evaporation on prepared MgO substrates in order to bury residual carbon and improve surface morphology. The F layer is the Heusler compound Co_2FeAl (CFA) with thick-

ness $t_F = 1.2$ nm, grown by MBE at a substrate temperature of 200° C by codeposition
 of individual elemental sources in ultrahigh vacuum (UHV). Reflection high energy elec-
 tron diffraction (RHEED) monitored during CFA growth confirmed a 45° rotated orien-
 tation $\text{CFA}\langle 110 \rangle \parallel \text{MgO}\langle 100 \rangle$. X-ray diffraction (XRD) measurements conducted on
 thicker 4 and 30 nm MgO/CFA samples confirm a single phase of (001) oriented CFA
 while the presence and relative peak area of the (002) reflection confirms at least B2 or-
 dering. The samples were cooled to room temperature before capping with Pt, which
 was grown using e-beam evaporation in UHV. The Pt grew epitaxially and was (001) ori-
 ented with $\text{Pt}\langle 100 \rangle \parallel \text{CFA}\langle 110 \rangle$, as confirmed by RHEED and XRD. An *in-situ* shad-
 owmask technique was used to achieve four different Pt cap thicknesses (t_N) on the same
 MgO/CFA(1.2 nm) underlayer. Two growths, one with $t_N = 1, 2, 3, 4$ nm and the other with
 $t_N = 5, 6, 7, 8$ nm, were used in this study. After Pt capping, samples were removed from
 UHV and exposed to atmosphere for subsequent processing. Vibrating sample magnetome-
 try was used to measure the CFA(1.2 nm) saturation magnetization $M_s = 800 \pm 100$ emu/cm³
 at room temperature. The saturation magnetic field of the anomalous Hall effect (AHE) at
 300 K matched $4\pi M_s$ within uncertainty. Therefore, the AHE saturation field was used to
 infer the temperature dependence of M_s , which increased from 850 emu/cm³ at 300 K to
 1050 emu/cm³ at 10 K. Ferromagnetic resonance (FMR) measurements were performed
 at room temperature on a companion MgO/CFA(1.2 nm)/Pt(7 nm) bilayer, for which
 Kittel formula[11] fits of the FMR field for rf excitation frequencies from 4-20 GHz re-
 vealed a cubic in-plane anisotropy $K_1 = -6 \times 10^3$ J/m³ with magnetic easy axes along
 $\text{CFA}\langle 110 \rangle (\text{MgO}\langle 100 \rangle)$.

The bilayers were patterned into Hall bars by photolithography and Ar⁺-ion milling, and
 Ti/Au vias and bonding pads were subsequently deposited. The Hall bar width was 10 μm .
 A magnetoresistive second harmonic (2ω) response technique similar to that discussed in
 Refs. [4, 12, 13] was employed to measure the SOT efficiencies. The DL and FL effective
 fields H_{DL} and H_{FL} result in 2ω Hall resistances due to the anomalous Hall effect (AHE) and
 planar Hall effect (PHE), respectively. An applied magnetic field was rotated 360° in the
 sample plane, and the angular dependence of the 2ω Hall resistance was fit to extract H_{DL}
 and H_{FL} . Magnetothermoelectric effects[14], which can contribute to 2ω resistances, were
 carefully taken into account. See the Supplemental Material[15] for a detailed description
 of the measurement geometry and fitting procedure. The dimensionless SOT efficiency is

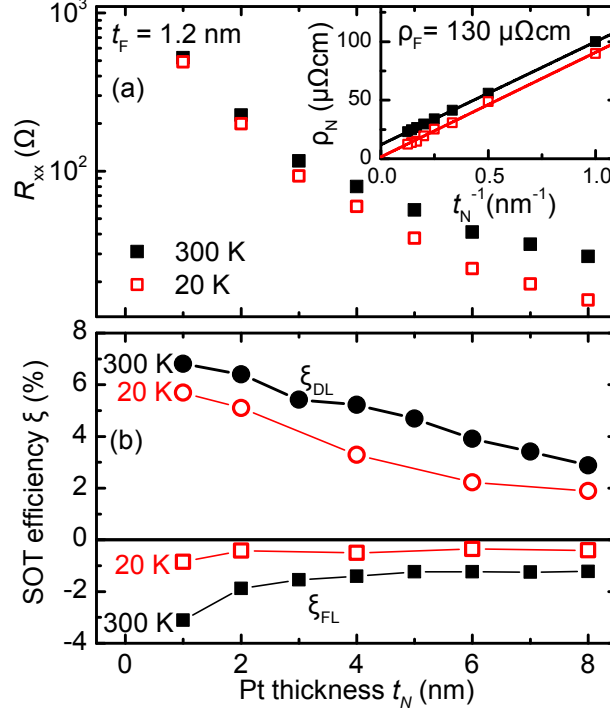


FIG. 1. (a) The bilayer square resistance for all Pt thicknesses. The solid black squares are 300 K data and open red squares are 20 K data. In the inset, the Pt resistivity is plotted vs. the inverse of the Pt thickness. The intercepts of the solid lines correspond to the bulk resistivity of Pt. In (b), the SOT efficiencies ξ_{DL} (circles) and ξ_{FL} (squares) are shown for different Pt thicknesses at 300 K (black solid symbols) and 20 K (red open symbols). The lines connect data points. For all data the CFA thickness is 1.2 nm.

given by[16]

$$\xi_{DL(FL)} \equiv \frac{M_s t_F H_{DL(FL)}}{(\hbar/2e) j_N^e}, \quad (1)$$

where e is the electron charge, \hbar is Planck's constant, and j_N^e is the current density in the N layer.

The bilayer square resistances R_{xx} are summarized in Fig. 1(a) for all Pt thicknesses at temperatures of 300 K and 20 K. The inset of Fig. 1(a) shows the Pt resistivity, which is a strong function of thickness due to diffuse surface scattering[17]. The F and N layers are treated as parallel resistances to account for the current shunted through F and determine j_N^e in the denominator of Eq. 1. See the Supplemental Material[15] for a detailed discussion of the shunting model and the method used to extract the Pt and CFA resistivities from R_{xx} . The CFA resistivity extracted from the shunting model is $130 \mu\Omega\text{cm}$, which is similar to

92 resistivities we measure for thicker 5 and 10 nm CFA films capped with AlOx. For the 5 and
 93 10 nm CFA films, resistivities are $\rho \simeq 100 \mu\Omega\text{cm}$ with residual resistivity ratios $\text{RRR} \simeq 1.1$,
 94 and we have also measured the AHE resistivity $\rho_{AHE} \simeq 0.6 \mu\Omega\text{cm}$. For these CFA films
 95 we find ρ_{AHE} decreases as temperature is decreased, with a trend close to $\rho_{AHE} \propto \rho^2$. In
 96 contrast, for the CFA(1.2 nm)/Pt bilayers we observe an increase in the AHE resistance
 97 R_{AHE} and anisotropic MR R_{AMR} at low temperatures for thin Pt thicknesses. (R_{AHE} is
 98 defined by the expression $R_{xy} = R_{AHE}m_z + R_H$, with m_z denoting the out-of-plane magne-
 99 tization component and R_H the ordinary Hall effect resistance, and $R_{AMR} \equiv (R_{xx}^{\parallel} - R_{xx}^{\perp})/2$
 100 with the parallel and perpendicular superscripts denoting the orientation of the current and
 101 saturated magnetization.) Figure 2 summarizes the temperature and Pt thickness depen-
 102 dence of R_{AHE} and R_{AMR} by plotting these MRs vs. R_{xx} , in which temperature is the
 103 implicit variable. The temperature was varied between 10 K (low R_{xx}) and 300 K (high
 104 R_{xx}). (See the Supplemental Material[15] for example magnetic field sweeps used to extract
 105 R_{AHE} and R_{AMR} , and for an alternative representation of the data shown in Fig. 2 in which
 106 temperature is indicated explicitly.)

107 The increase in the (extraordinary, or anomalous[18]) MR observed at low temperatures in
 108 Fig. 2 is due to the MPE. Because of current shunting through the F in metallic F/N bilayers,
 109 MR-based studies of the MPE have typically been relegated to ferromagnet insulator/Pt
 110 bilayers[8, 19–21]. However, the MR behavior shown in Fig. 2 as temperature is decreased
 111 cannot be attributed to shunting through F. Given F RRR values near unity, F shunting
 112 alone results in a measured $R_{MR} \propto R_{xx}^2$ [15]. In fact, the trends of both R_{AHE} and R_{AMR}
 113 consistently show excess MR at low temperature compared to the $R_{MR} \propto R_{xx}^2$ trend drawn
 114 on Fig. 2, indicating an additional MPE MR contribution at low temperature. Furthermore,
 115 for the 1 and 2 nm Pt bilayers, both AHE and AMR resistances *increase* as the temperature
 116 decreases. For the 1 nm Pt bilayer R_{AMR} increases by a factor of 3 from 300 K to 10 K,
 117 in stark contrast to the F shunting prediction of a 12% decrease over the same temperature
 118 range. In fact, the bilayer $R_{AMR} > 0$ is opposite in sign to that measured on 5 nm CFA
 119 films with Al capping layers, highlighting the influence of the Pt layer on the AMR.

120 Briefly, we discuss the relevance of the recently-discovered spin-Hall MR (SMR) effect[22–
 121 25] to our MR measurements. The conventional AMR effect[18] magnitudes summarized in
 122 Fig. 2 were obtained by performing the measurement in a geometry such that the SMR
 123 effect is absent, similar to Ref. [22]. See the Supplemental Material[15] for the details of

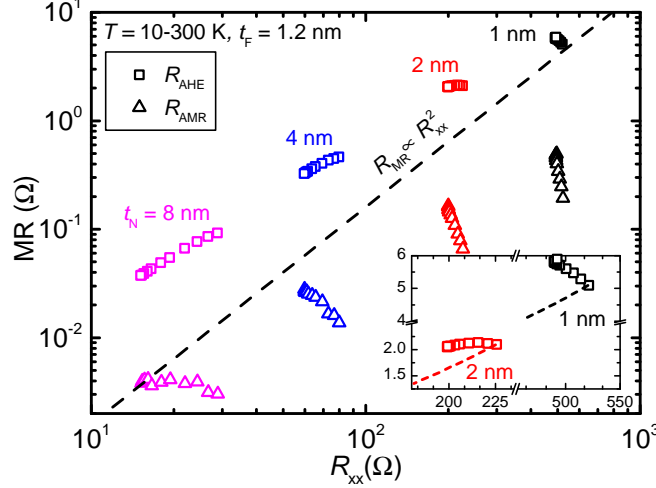


FIG. 2. Summary of R_{AHE} (squares) and R_{AMR} (triangles) vs. R_{xx} for the different bilayers which are labeled by the Pt thickness. Temperature is an implicit variable, and the minima and maxima of R_{xx} correspond to 10 and 300 K, respectively, for all bilayers except the 1 nm Pt bilayer, in which R_{xx} shows a small upturn below 20 K. The dashed lines indicate $R_{MR} \propto R_{xx}^2$, which is expected for MR originating from F shunting alone. The inset magnifies the AHE data for the 1 and 2 nm Pt bilayers. See Fig. 5 in the Supplemental Material[15] for an alternative representation in which temperature is indicated explicitly, and details on how R_{AHE} and R_{AMR} were measured.

the measurement geometry used to differentiate R_{AMR} from SMR effects. (We do observe a SMR-like MR of magnitude $\Delta R_{xx}/R_{xx} \sim 10^{-3}$, but these effects are not the focus of this letter.) It has been reported that the SMR effect in N may give rise to an AHE-like transverse resistance (SH-AHE)[23, 26, 27]. In comparison to Refs. [23, 26], however, in our bilayers R_{AHE} is a factor of 10-100 times larger. Furthermore, given that we observe SMR magnitudes $\sim 10^{-3}$, we expect the SH-AHE magnitude (R_{xy}/R_{xx}) to be of order $10^{-4} - 10^{-5}$ [27], much smaller than the AHE we observe.

The temperature-dependent AHE and AMR behaviors we observe are in good agreement with literature reports of a low-temperature MPE in F/Pt bilayers[8, 9, 20, 28], although quantitative parameters such as the magnetic moment density or MPE layer thickness are not easily extracted from these measurements. Although few experimental papers directly discuss the influence of the MPE on SOT efficiencies, Lim *et al.* [28] have commented that the MPE at a F/Pt interface may affect spin-dependent transport significantly through enhanced transverse dephasing processes in the MPE Pt volume. The distinguishing experimental

feature is expected to be the temperature dependence, because the MPE is enhanced at low temperatures. To study the influence of the MPE on the SOT efficiencies, we have performed the ξ_{DL} and ξ_{FL} harmonic response measurement from 300 K to 20 K, the results of which are summarized in Fig. 1(b). Both the DL and FL components are detected for all Pt thicknesses, with ξ_{FL} having opposite sign and smaller magnitude than ξ_{DL} . The signs of ξ_{DL} and ξ_{FL} are in agreement with measurements reported for CoFe/Pt bilayers[30]. In Fig. 1(b), it is clear that ξ_{FL} is strongly suppressed at low temperature for all thicknesses, while ξ_{DL} shows only modest suppression. The SOT efficiencies are plotted vs temperature in Fig. 3.

In the discussion that follows below, we propose a mechanism by which the MPE may suppress ξ_{FL} at low temperature, in which we attribute the DL SOT to the Pt SHE, and the FL SOT to the CFA/Pt interface Rashba effect. This causal distinction is well-motivated for F/Pt bilayers[1, 3–5], and is supported by the qualitatively different trends we observe in ξ_{DL} and ξ_{FL} as Pt thickness and temperature are varied. In principle, the CFA/MgO interface may also possess a Rashba interaction, however as Pt thickness is increased, a diminishing fraction of the current is shunted through the CFA layer. Because the ξ_{FL} data shown in Fig. 1(b) plateaus for large Pt thickness *when normalized by Pt current density*, the Pt and CFA/Pt interface give the dominant sources of SOTs. An alternative explanation of the FL SOT in F/N bilayers invokes the N SHE and a nonzero imaginary component of the interface mixing conductance $\text{Im}(G_{\uparrow\downarrow})$, which has been supported by recent measurements involving light-metal spacer layers[31–33]. We will return to a discussion of our SOT measurements in the context of the SHE- $\text{Im}(G_{\uparrow\downarrow})$ interpretation near the end of this article.

First, we discuss the ξ_{DL} measurements summarized in Fig. 1(b). DL SOT efficiencies in F/N bilayers are typically interpreted through fits to the N SHE spin diffusion model[5, 34], the hallmark of which is an increase in ξ_{DL} with increasing N thickness, saturating at a thickness set by the spin diffusion length. Because ξ_{DL} in our samples *decreases* monotonically with increasing Pt thickness, any naïve model would imply that a corresponding spin diffusion length is less than ~ 1 nm. Although the data may be interpreted by invoking a spin diffusion length less than 1 nm, the value itself does not have real physical significance given that it is smaller than the momentum scattering length, which in this limit is set by the film thickness. In Fig. 3, the right ordinate is used to compare ξ_{DL} to Pt resistivity as the temperature is varied. We see that ξ_{DL} tracks ρ_{Pt} closely: for small

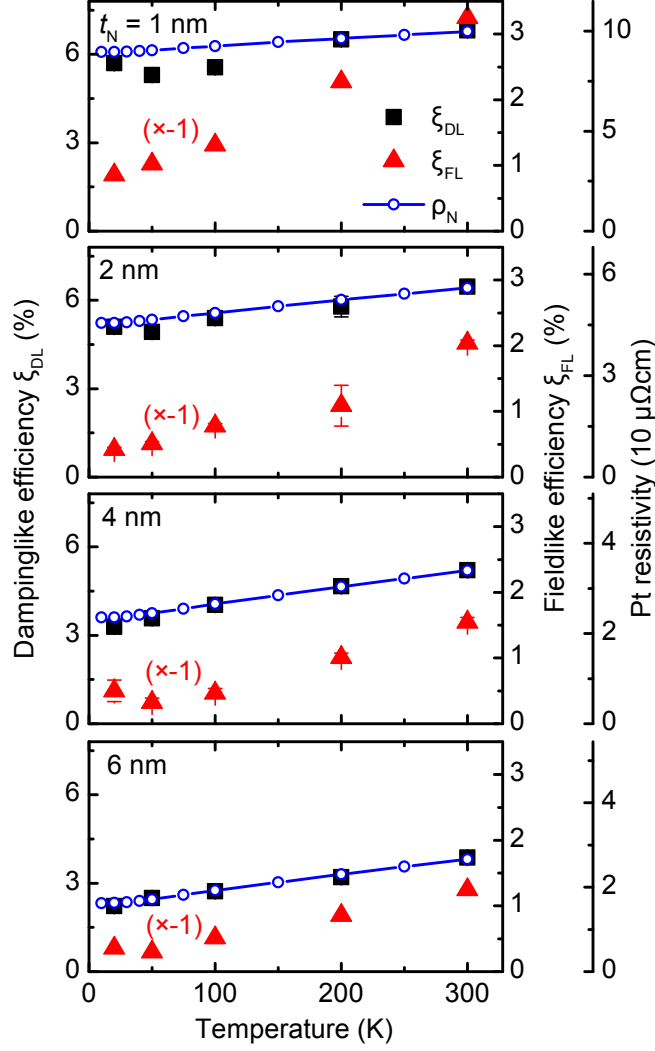


FIG. 3. The temperature dependence of the SOT efficiencies, ξ_{DL} (black squares, left ordinate) and ξ_{FL} (red triangles, right ordinate 1) for the 1, 2, 4, and 6 nm Pt bilayers as indicated on the figure. The ξ_{FL} data has been scaled by a factor of -1 . The error bars represent the standard errors. The Pt resistivity is shown (right ordinate 2) as the blue open circles, and the lines connect data points.

thicknesses ($t_N = 1, 2 \text{ nm}$), where the Pt RRR is small, the temperature dependence of ξ_{DL} is weak, whereas for large thicknesses ($t_N = 6, 8 \text{ nm}$), where the RRR is larger, ξ_{DL} has a more pronounced temperature dependence. The observation that $\xi_{DL} \propto \rho$, if interpreted through the SHE diffusion model, is consistent with the intrinsic (or possibly side-jump) SHE scaling reported for Pt[5, 35, 36]. However, spin backflow could also result in a similar phenomenology, as $\xi_{DL} \propto 2G_{\uparrow\downarrow}/(G_N + 2G_{\uparrow\downarrow})$ where $G_N \equiv (\rho\lambda)^{-1}$ and $G_{\uparrow\downarrow}$ is the F/N

177 interface spin-mixing conductance[37]. Spin backflow is significant for Pt, due to the rela-
 178 tively low resistivity and short spin diffusion length. From a fitting point-of-view, we cannot
 179 constrain enough parameters to distinguish between these two explanations for the $\xi_{DL} \propto \rho$
 180 observation. Furthermore, we caution that when the SHE diffusion model parameters (SH
 181 ratio, spin diffusion length, N spin resistance) vary with N resistivity, all of the models
 182 become poorly constrained.

183 We now turn to discussing the temperature dependence of the FL SOT efficiency, which
 184 is shown in Fig. 3. For all thicknesses, the magnitude of ξ_{FL} decreases by a factor nearly of 4
 185 from 300 K to 20 K, in contrast to ξ_{DL} , for which the temperature dependence simply follows
 186 the Pt resistivity. A similar behavior of ξ_{FL} has been observed in annealed CoFe/Pt[16]. We
 187 believe that the decrease in ξ_{FL} as temperature decreases is due to the increased MPE at
 188 low temperatures. The FL component of the SOT originates from the exchange interaction
 189 between a Rashba-induced spin accumulation in N and the F magnetization[38, 39]. In Fig.
 190 4(a), the Rashba spin accumulation is drawn transverse to the magnetization to illustrate
 191 the maximal torque configuration in absence of the MPE. However, for nonzero MPE, the
 192 Rashba spin accumulation generated at the interface transverse to \hat{m} rapidly precesses about
 193 and is dephased by the inhomogeneous MPE exchange field, as is illustrated in Fig. 4(b).
 194 Perhaps counter-intuitively, at low temperatures where moments in N and F are strongly
 195 coupled, ξ_{FL} decreases because the exchange interaction extends into N and destroys the
 196 spin accumulation responsible for the FL SOT. We note that, in principle, the anisotropic
 197 nature of the proposed dephasing process may modify the angular dependence of the FL SOT
 198 contribution harmonic response measurement. This modification is discussed at length in the
 199 Supplemental Material[15]. Unfortunately, within the fitting uncertainty of our measurement
 200 we cannot resolve if these modifications are reflected in our data. In any case, any small
 201 modification to the angular dependence of the FL SOT harmonic response does not alter our
 202 critical observation (*i.e.*, the suppression of the FL SOT at low temperatures). The physics
 203 of the MPE suppression of the FL SOT may not be captured by existing models, which
 204 assume an interface delta function exchange coupling between the F and N moments[40, 41]
 205 rather than a spatially nonuniform MPE exchange interaction extending a finite thickness
 206 into N. We note that in some cases[33, 42, 43] the FL SOT has been observed to increase with
 207 temperature in bilayers with Ta and W as the N metal, which are not believed to support
 208 MPEs. It is not clear if the FL SOTs presented in Refs. [33, 42, 43], and their temperature-

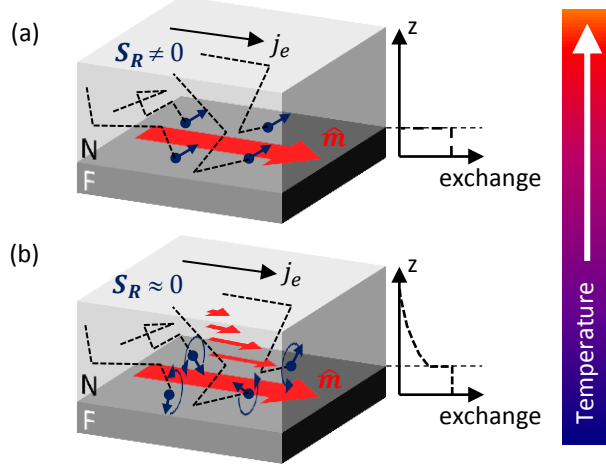


FIG. 4. Illustrations of (a) the Rashba spin accumulation S_R at high temperature in absence of the MPE and (b) MPE order at low temperature which serves to precess and destroy the transverse Rashba spin accumulation. The magnetization \hat{m} and current j_e are indicated with red and black arrows respectively. Right-drifting carriers in N, which make up the current, are drawn as blue arrows (denoting spin accumulation) with black dashed trajectories implying scattering events. Plots of the exchange interaction strength vs. depth coordinate z in the bilayer, which are schematic and not drawn to scale, are included.

dependencies, are due to the same mechanisms as those presented in this article.

In the above discussion, we have attributed the FL SOT to the CFA/Pt interface Rashba effect. We briefly discuss the alternative picture in which the FL SOT arises from the Pt SHE through $\text{Im}(G_{\uparrow\downarrow})$. $\text{Im}(G_{\uparrow\downarrow})$ physically corresponds to incomplete absorption of transverse spin current by the F layer, which can be pictured semiclassically as N spin current reflecting from the F layer with spin precessed through finite phase (rather than complete precessional dephasing). It is believed that $\text{Re}(G_{\uparrow\downarrow}) \gg \text{Im}(G_{\uparrow\downarrow})$, with sizable $\text{Im}(G_{\uparrow\downarrow})$ only occurring for very thin (few-Angstrom) F layers. If we interpret our data in the picture where the FL SOT arises from the Pt SHE through $\text{Im}(G_{\uparrow\downarrow})$, the implication would be that $\text{Im}(G_{\uparrow\downarrow})$ increases as temperature is increased. The same efficient dephasing of spin accumulation transverse to \hat{m} due to the MPE can explain this trend: at low temperature, the extension of the magnetized volume into the Pt[28, 44] suppresses $\text{Im}(G_{\uparrow\downarrow})$ by the increase in the effective F thickness.

We conclude by highlighting an important distinction of the MPE precessional dephasing

process from interface spin-memory loss relaxation processes[45]. For spin-magnetization interactions, angular momentum conservation necessitates that the MPE suppression of the transverse interface spin accumulation represents a transverse spin current sunk into the N MPE magnetization, which should result in a DL torque (as the N magnetization is exchange-coupled to the F magnetization). In the Rashba FL SOT interpretation, this would reflect a transfer of FL SOT to DL Rashba SOT, and in the SHE picture reflect a corresponding increase in $\text{Re}(G_{\uparrow\downarrow})$ as $\text{Im}(G_{\uparrow\downarrow})$ decreases. However, we observe no distinguishable increase in ξ_{DL} at low temperatures. Therefore, we conclude that the MPE suppression of the Rashba spin accumulation generates a much smaller *spin current* than is generated by the SHE, which is consistent with the discussion by Haney *et al.* [40]. In the case of the SHE spin current generated in the bulk of N away from the interface, we expect that the few-Å thick MPE layer extends the effective F/N interface slightly into the Pt but does not influence ξ_{DL} , consistent with SOT-FMR measurements by Zhang *et al.* [46] for Pt thicknesses larger than 1 nm.

In conclusion, we have demonstrated a suppression of the fieldlike SOT efficiency as the MPE increases at low temperature in F/Pt bilayers. The fieldlike SOT is attributed to the Rashba SOT mechanism, which we propose is suppressed in the presence of an MPE exchange field. As a possible alternative, we also outline how the MPE could decrease the imaginary component of the F/N spin-mixing conductance. This identification implies engineering of the MPE may provide a technique to maximize Rashba SOT efficiencies in F/Pt bilayers.

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