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# Spin-orbit coupling fluctuations as a mechanism of spin decoherence

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We discuss a general framework to address spin decoherence resulting from fluctuations in a spin Hamiltonian. We performed a systematic study on spin decoherence in the compound  $K_6[V_{15}As_6O_{42}(D_2O)] \cdot 8D_2O$ , using high-field Electron Spin Resonance (ESR). By analyzing the anisotropy of resonance linewidths as a function of orientation, temperature and field, we find that the spin-orbit term is a major decoherence source. The demonstrated mechanism can alter the lifetime of any spin qubit and we discuss how to mitigate it by sample design and field orientation.

#### I. INTRODUCTION

In solid-state systems, interactions between electronic spins and their environment are the limiting factor of spin phase lifetime, or decoherence time. Important advances have been recently realized in demonstrating long-lived spin coherence via spin dilution<sup>1-6</sup> and isolating a spin in non-magnetic cages<sup>7</sup>, for instance. The presence of a lattice can be felt by spins through orbital symmetries and spin-orbit coupling. An isolated free electron has a spin angular momentum associated with a g-factor  $g_e = 2.00232$  but in general, spin-orbit coupling changes the g-factor by the admixture of excited orbital states<sup>8</sup> into the ground state. In this Letter, we demonstrate that fluctuations in the spin-orbit interaction can be a significant source of spin decoherence. We present a general theoretical framework to obtain noise spectrum. The method is applied to fluctuations of the long-range dipolar interactions and we observe how the spin-orbit term is modulating the induced decoherence. The model describes spin dilution and thermal excitations effects as well. Experimentally, we analyze shape and orientation anisotropy of ESR linewidths of the molecular compound  $K_6[V_{15}^{IV}As_6^{III}O_{42}(D_2O)] \cdot 8D_2O$  or  $V_{15}$ . This system has shown spin coherence at low temperatures<sup>5,9</sup> and interesting out of equilibrium spin dynamics due to phonon bottlenecking<sup>10,11</sup>. However, the details of the spin decoherence are still not fully understood. In the case of diluted or molecular spins, little evidence has been brought up to now on the role of spin-orbit coupling on spin coherence time. This study elucidates this decoherence mechanism and how to mitigate its effect.

## II. FLUCTUATIONS IN SPIN HAMILTONIAN

The  $V_{15}$  cluster anions form a lattice with trigonal symmetry containing two clusters per unit cell<sup>12</sup>. Individual molecules have fifteen  $V^{IV}$  s=1/2 ions arranged into three layers, two non-planar hexagons sandwiching a triangle (see Fig. 1a). Exchange couplings between the spins in the triangle and hexagons exceed 100 K<sup>13,14</sup> and at low temperatures this spin system can be modeled as

a triangle of spins 1/2. The spin Hamiltonian is, as discussed in Supplemental Material<sup>15</sup> (SM) Section I:

$$\mathcal{H}_{st} = \mathcal{H}_0 + \mathcal{H}_J + \mathcal{H}_{DM} \tag{1}$$

where  $\mathcal{H}_0$  describes the Zeeman splitting in an external field  $\vec{B}_0$ ,  $\mathcal{H}_J$  is the symmetric exchange term, and  $\mathcal{H}_{DM}$  is the anti-symmetric Dzyaloshinsky-Moriya (DM) term (see<sup>16</sup> for a detailed formulation).  $\mathcal{H}_{st}$  eigenvalues are shown in Fig. 1(b) and are used to calculate resonant field positions  $B_{res}$  of the ESR spectra through the method of first moments<sup>16</sup>. As shown in Fig. 1(b), the ground state of the total molecular spin  $\vec{S}$  is S = 3/2 for large enough  $\vec{B}_0$ . In this case, dipolar interactions between total molecular spins in the crystal are described by:

$$\mathcal{H}_d = \frac{3\mu_0}{8\pi} S^2 \mu_B^2 \sum_{p:q \neq p} g_p(\theta) g_q(\theta) \frac{\left(1 - 3\cos^2\phi_{pq}\right)}{d_{pq}^3}$$
 (2)

where  $\mu_0$  is the vacuum permeability,  $\mu_B$  is the Bohr magneton,  $\theta$  is the angle between  $\vec{B}_0$  and the z axis (z is  $\bot$  to triangle plane and is also the symmetry c axis of the molecule),  $d_{pq}$  is the distance between two molecules located at sites p and q,  $g_{p,q}(\theta) = \left(g_a^2 \sin^2 \theta + g_c^2 \cos^2 \theta\right)^{1/2}$ ,  $g_{c,a}$  are the g-tensor components parallel and perpendicular to the z axis,  $\phi_{pq}$  is the angle between  $\vec{S}$  at site p and  $\vec{d}_{pq}$ . Due to local fluctuations of the g-factor, as discussed below,  $g_p$  and  $g_q$  are distinct quantities.

The linewidth of ESR signals can be significantly affected by exchange interactions. In V<sub>15</sub> the intramolecular couplings are large and the exchange narrowing effect<sup>17</sup> collapses the  $(2I+1)^{15}$  resonances (I=7/2for  $^{51}$ V) into one and it also acts to average out fluctuations related to  $\mathcal{H}_{st}$ . This leaves fluctuations in  $\mathcal{H}_d$  as being the major contributor to spin decoherence.

There are three possible sources of fluctuation in Eq.(2), the first being the geometrical factor  $(1-3\cos^2\phi_{pq}) d_{pq}^{-3} = R_{pq}(t)$  since both  $d_{pq}$  and  $\phi_{pq}$  can fluctuate (here, t represents time). This case is described by Bloembergen  $et~al.^{18}$  (Nuclear Magnetic Resonance case) and Kubo and Tomita<sup>17</sup> (ESR case). If  $R_{pq}(t)$  fluctuates randomly, its correlation function decays exponentially  $\langle R(t)R(0)\rangle = R^2 + r^2 \exp(-t/\tau_{dip})$  with a

Fourier spectrum:

$$J_R(\nu) = \sqrt{\frac{2}{\pi}} r^2 \frac{\tau_{dip}}{1 + 4\pi^2 \nu^2 \tau_{dip}^2}$$
 (3)

where R is an average value of the geometric term  $\sum_{p\neq q} R_{pq}$ , r is an average size of R(t)'s fluctuations and the correlation time  $\tau_{dip}$  is a characteristic of the random motion. This result is described generally by Atherton <sup>19</sup> and can be applied to any stationary random function that is independent of the time origin. The inverse square of the decoherence time  $T_2$  is proportional to  $\int J_R(\nu) d\nu^{17,18}$ . Therefore, the decoherence rate depends directly on r:  $1/T_2 \propto r$ .

Another fluctuation source comes from thermal excitations to different  $S_Z$  states of  $\vec{S}$ , where Z axis is  $\parallel \vec{B}_0$ , which defines the second moment of a resonance line<sup>20–22</sup> (potential fluctuations between different spin states in low fields has been studied as well<sup>9</sup>):  $\langle S_Z(t)^2 S_Z(0)^2 \rangle = S_Z^4 + KU(T) \exp(-t/\tau_s)$ , where  $\tau_s$  is the thermal correlation time and KU(T) a term studied by Kambe and Usui<sup>21</sup>. It is shown that the fluctuations Fourier spectrum is proportional to a temperature dependent factor:

$$KU(T) = \langle S_Z^2 \rangle_T - \langle S_Z \rangle_T^2 = S^2 \frac{d}{dy} B_s(y)$$
 (4)

where  $B_s(y)$  is the Brillouin function,  $y = T_Z S/T$ ,  $T_Z = h f_0/k_B$  ( $f_0$  is the microwave excitation frequency), and S = 3/2 is the total spin state. KU(T) has thus a similar role to  $r^2$  in Eq. (3). This formulation is valid above the ordering temperature which is  $\sim 0.01 \text{ K}^{23}$  for  $V_{15}$ .

The dipolar term  $\mathcal{H}_d$  serves as an excellent platform to study fluctuations of  $g(\theta)$ . Its value away from  $g_e$  is due to the spin-orbit interaction and it is given by<sup>8</sup>:

$$\mathbf{q} = q_e \mathbf{I} - 2\lambda \mathbf{\Lambda} \tag{5}$$

where g is the g-tensor (diagonal  $[g_a, g_a, g_c]$  for  $V_{15}$ ), I is the unit matrix,  $\lambda$  is the spin-orbit coupling constant and  $\Lambda$  is a tensor defined in terms of the matrix elements of the orbital angular momentum  $\mathbf{L}$ . In general terms,  $\Lambda$  is the coupling between the ground and excited orbitals divided by their energy separation. Relative fluctuations with an average size  $\xi = \delta(\lambda \Lambda)/(\lambda \Lambda)$  (assumed isotropic) can be induced by crystal and molecular vibrations. In particular, Raman measurements on  $V_{15}^{24}$  discussed below, show a broad distribution of the vibration modes. Fluctuations of excited orbitals and thus of  $\Lambda$  can generate broad virtual transitions since those orbitals are mixed with the ground orbital state. The resultant fluctuation in the g-factor can be written as:

$$\delta g(\theta) = \xi \left( g(\theta) - g_e \right). \tag{6}$$

Assuming  $g(\theta)$  is a stationary function with small temporal random fluctuations and that magnetic and orbital fluctuations are uncorrelated in first approximation, the

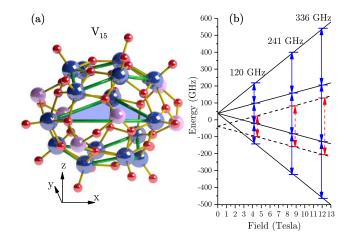


FIG. 1. (Color online) (a) Ball-and-stick representation of  $V_{15}$  (V ions in blue). The x axis is along one side of the triangle while the z axis is perpendicular to the triangle plane and represents the c axis of the crystal unit cell. (b) Level diagram of the three spin model in field ||z|, with positions of the three experimental frequencies shown. Dashed lines show the S=1/2 doublets with the red dashed arrows indicating those transitions. Lines show the S=3/2 quartet with blue arrows indicating the transitions; the resonance fields are averaged in the first moment calculation of  $B_{res}$  at a given frequency.

correlation function of a fluctuating  $\mathcal{H}_d(t)$  is:

$$G_d(t) = \langle \mathcal{H}_d(t)\mathcal{H}_d(0) \rangle$$
  
=  $\alpha^2 \langle g(t)g(0) \rangle^2 \langle S_Z^2(t)S_Z^2(0) \rangle \langle R(t)R(0) \rangle$  (7)

where  $\langle g(t)g(0)\rangle = g(\theta)^2 + (\delta g(\theta))^2 \exp(-t/\tau_g), \ \tau_g$  is the correlation time of g-factor fluctuations, and  $\alpha = \frac{3\mu_0\mu_B^2}{8\pi}$ . A corresponding  $J_d(\nu)$  gives the Fourier spectrum of the fluctuations, as in Eq. 3.  $G_d(t)$  can be written as the sum of four terms (see SM Section II for details):  $G_0$  which is a constant ,  $G_g(t) \propto g(\theta)^4$ ,  $G_\delta(t)$  which is temperature indepedent and  $G_T(t)$  which is temperature dependent.

In absence of g-factor fluctuations, the resulting Fourier spectrum is defined only by  $G_g(t)$  and for neglible r (less important in solids at low temperatures) the term  $G_g(t) \approx \alpha^2 g(\theta)^4 R^2 K U(T) e^{-\frac{t}{\tau_s}}$  is as in  $^{21}$ . A temperature dependence of the linewidth  $\propto K U(T)$  is similar to observations done with Fes  $^{25-27}$ , nitrogen-vacancy color centers in diamond  $^{28}$  while other studies seem to confirm the proportionality to the g-factor  $^{29,30}$ . If the g-value does fluctuate then all three terms  $G_{g,\delta,T}$  represent sources of decoherence, with  $G_{\delta}+G_{T}$  given by:

$$G_{\delta}(t) + G_{T}(t) \approx \alpha^{2} R^{2} \left[ S^{4} + KU(T) \right] \times \left[ 2g(\theta)^{2} \delta g^{2}(\theta) e^{-\frac{t}{\tau_{g}}} + \delta g^{4}(\theta) e^{-\frac{2t}{\tau_{g}}} \right].$$
 (8)

Because  $1/T_2^2$  is  $\propto \int J_d(\nu)d\nu$ , an important consequence is that one can combine different decoherence sources by summing their effect (each term i) as follows:  $\frac{1}{T_2^2} \approx \sum_i \frac{1}{T_{2i}^2}$ , similar to the well-known fact that the sum of uncorrelated variances is equal to the total variance.

Additionally, the weight of each term in the sum depends on, or can be tuned with, the field angle  $\theta$  through g and  $\delta g$ . Here we show that for  $V_{15}$ , the anisotropy of the decoherence time is explained by fluctuations  $\delta g$ , as shown in Eq. 8, amplified by spin thermal fluctuations KU(T).

#### III. EXPERIMENTAL DATA

Continuous-wave ESR measurements at 120, 241, and 336 GHz are performed using the quasioptical superheterodyne spectrometer at the National High Magnetic Field Laboratory<sup>31,32</sup>, with a sweepable 12.5 T superconducting magnet (homogeneity of  $10^{-5}$  over 1 cm<sup>3</sup>). Sample temperature can be varied from room temperature down to 2.5 K. A single crystal of regular shape (as in<sup>16</sup>) of volume  $\lesssim 0.1 \text{ mm}^3$  was positioned on a rotating stage allowing for continuous change of the angle  $\theta$  between  $\vec{B}_0$  and the c axis of the molecule following the procedure described in 16. The homogeneity of the magnet compared to the size of the crystal allows us to ignore  $\vec{B}_0$  as a source of broadening. The applied fields are above 4 T, past the crossing of the S=1/2 doublet and S = 3/2 quartet, such that the ground state of the system is in the S = 3/2 quartet (see Fig. 1(b)).

ESR spectra at temperatures T = 4-60 K for  $\vec{B}_0 \parallel$  and  $\perp$  to c-axis ( $\theta = 0^{\circ}, 90^{\circ}$  respectively) show a Lorentzian (homogenous) lineshape. Representative spectra with Lorentzian and Gaussian fits are shown in Fig. 2(a) for comparison. The temperature dependence of the linewidth is shown in Fig. 2(c) for three microwave frequencies  $f_0$ . Compared to measurements made at lower fields<sup>33</sup>, where the ground state is in the S = 1/2 doublet, the linewidths are  $\sim 10$  times narrower. Plotted is the full width at half maximum (FWHM) of the Lorentzian fits vs  $T/f_0$  to underline that the temperature dependent mechanism of decoherence in the system qualitatively follows the temperature behavior predicted by KU(T) plus a temperature independent contribution, essential in the low T limit [Eq. (8)]. Note the absence of linewidth increase with frequency (or field) which excludes a static distribution of the q-factor. Additionally, there is no hyperfine structure visible in the spectra (exchange narrowing) since the 3d electrons of V interact with the nuclei of several other V ions due to the large exchange couplings  $(\sim 10^2 \text{ K})$  within the molecule. Due to these properties of the measured line width and shape, we can estimate  $T_2$  to be the inverse of the FWHM.

There are two distinct curves in Fig. 2(c), dependent on the orientation of  $\vec{B}_0$ . To probe this orientation dependence, the linewidth is measured as a function of  $\theta$ , see Fig. 2(b). The narrowest linewidth occurs when  $\theta = 0^{\circ}$  ( $\vec{B}_0 \parallel c$  axis) while the largest occurs at  $\theta = 90^{\circ}$  ( $\vec{B}_0$  in the triangle plane). This implies more decoherence the further  $g(\theta)$  gets from  $g_e$  since  $g(0^{\circ}) = g_c \approx 1.98$  and  $g(90^{\circ}) = g_a \approx 1.95$ . The fact that the width is largest (smallest) when  $g(\theta)$  is minimum (maximum) rules out

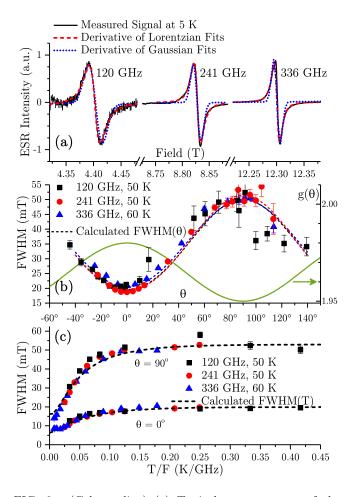


FIG. 2. (Color online) (a) Typical measurements of the derivative of the absorption  $\chi''$  at 120 GHz, 241 GHz and 336 GHz with derivative of Gaussian (blue dotted line) and Lorentzian fits (red dashed line). (b) FWHM of Lorentzian fits as a function of field angle  $\theta$  measured at three frequencies: 336 GHz (blue triangles), 241 GHz (red circles) and 120 GHz (black squares) The dashed lines are calculated widths as a function of  $\theta$ ; the agreement shows the predicted correlation between decoherence rate and  $g_e - g(\theta)$ . In contrast, the green line (right axis) shows the opposite angular behavior of calculated  $g(\theta)$ , leading to  $G_g \ll G_\delta + G_T$  (see text). (c) FWHM of Lorentzian fits vs temperature/frequency for the 3 studied frequencies. Dashed lines are calculated FWHM(T) for  $\theta = 0^{\circ}$  and  $90^{\circ}$ .

exchange narrowing being the cause of this anisotropy since it would require a linewidth  $\propto (1+\cos^2\theta)^{17}$ , as in the case of  $\mathrm{CsCuCl_3}^{34}$ . To rule out an angular effect of the dipolar field distribution, we measured the FWHM( $\theta$ ) on a sample of irregular shape at 240 GHz and 60 K. Although the shape-dependent coefficients R and r must be different, the same behavior is observed as in Fig. 2b (see SM Section III B for details). We can thus focus on the terms  $G_{g,\delta,T}$  as source of fluctuations.

However, the term  $G_g(t)$  is  $\propto g(\theta)^4$ , in clear contrast with the observation that the FWHM and  $g(\theta)$  have opposite angular dependences (see Fig. 2b and also SM Sec-

tion IIIA). This is the essential property of the V<sub>15</sub> compound, which makes it particularly suitable to study the effect of spin-orbit fluctuations. Therefore, this opposite angular behavior provides evidence that  $\delta g(\theta) \neq 0$  and the terms  $G_{\delta,T}(t)$  must be considered while  $G_g(t)$  can be discarded. One can argue that geometrical fluctuations in solids at low temperatures are very small  $(r \ll R)$  and lattice fluctuations are mostly influencing the relaxation time  $T_1$   $(\tau_s \gg \tau_g)$  making  $G_g \approx \text{constant}$  at the time scale of the decoherence time.

Since  $G_d(t) \approx G_\delta(t) + G_T(t)$  and  $1/T_2^2 \propto \int J_d(\nu)^{17,18}$  the linewidth square can be modeled by the following fit function (see SM Section II for details):

$$\Delta^{2} = [S^{4} + KU(T)] \times \times [2a^{2}g(\theta)^{2}(g(\theta) - g_{e})^{2} + A^{2}(g(\theta) - g_{e})^{4}]$$
 (9)

where A and a are fit parameters. The procedure is detailed in SM Section IV; it allows to calculate the angular dependence FWHM( $\theta$ ) by using only two data points,  $\Delta(0^{\circ})$  and  $\Delta(90^{\circ})$ , as shown in Fig. 2(b) (dashed lines).

To analyze the temperature dependence of the linewidth shown in Fig. 2(c), we solve for A and a at all available temperatures and frequencies (see SM Section IV B for details). Above 10-20 K, the values stabilize at  $A \sim 100$  GHz and  $a \sim 3.2$  GHz. At lower temperatures, the values decrease by almost half, indicating a small decrease in  $\xi$  and/or a slowing down in the fluctuations time  $\tau_q$ . These temperature trends A(T) and a(T) are estimated by an exponential saturation (see SM Fig. 4 for details), with decay constants of 3.6 K and 11 K for A(T)and a(T) respectively. With no other adjustments, the calculated linewidth is in very good agreement with the experimental data, as shown with dashed line in Fig.2(c). On the low end of  $T/f_0$  one observe a residual value of the linewidth, which includes the effects of other decoherence sources (such as the nuclear spin bath<sup>35</sup>), although it can be well described by Eq. 9.

The outcome of the fit procedure can be used to estimate the size of spin-orbit fluctuations (see SM Section IV C) leading to an order of magnitude for  $\xi \sim 10^{-2}$ . This corresponds to a fluctuation  $\delta g/g \sim 10^{-4}$ , too small to result in directly measurable fluctuations of the Zeeman splitting. Note that for V<sub>15</sub>, a large spin-orbit fluctuation is supported by previous Raman measurements<sup>24</sup>

showing a very broad signal in the region of  $\sim 500~\rm cm^{-1}$  corresponding to vibrations of oxygen bridges between V ions. The observed broad distribution of the modes can induce very fast virtual transitions to excited coupled states and, as a consequence, spin decoherence.

#### IV. CONCLUSION

Our study provides insight on how to mitigate the effects of spin-orbit fluctuations. It is evident from Eqs. (6) and (7) that the g-tensor should be as close as possible to  $g_e$ . In molecular compounds this can be achieved by engineering the ligands type since local symmetry affects the diagonal values of the g-tensor of a magnetic ion. Aside from material design by chemical methods,  $J_d(\nu)$  can be minimized by applying the magnetic field at a specific angle  $\theta$ . For V<sub>15</sub>, this would be  $\theta = 0$  for which the decoherence time reaches several nanoseconds. This time can reach  $\sim 400$  ns by reducing R in  $J_d(\nu)$  via dilution in liquid state, thus allowing the observation of Rabi oscillations and spin-echoes<sup>5</sup>. The methodology presented here can be important for the diluted spin systems as well, since long range interactions are still present and can carry modulations due to q-factor fluctuations. Potential examples are transition metals such as Cr<sup>5+</sup>:K<sub>3</sub>NbO<sub>8</sub><sup>2</sup>) or some lanthanide monomers doped into insulating lattice such as Hf:LuPO<sub>4</sub><sup>36</sup> or La:CaF<sub>2</sub><sup>37</sup>. The results extend to any solid-state system where spin-orbit coupling leads to quantum effects, independent of system dimensionality.

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