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Charged defects in two-dimensional semiconductors of arbitrary thickness and geometry: formulation and application to few-layer black phosphorus

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Abstract

Energy evaluation of charged defects is tremendously important in two-dimensional (2D) semiconductors for the industrialization of 2D electronic devices because of its close relation with the corresponding type of conductivity and its strength. While the method to calculate the energy of charged defects in single-layer one-atom-thick systems of equilateral unit cell geometry has been recently proposed, few-layer 2D semiconductors are more common in device applications. As it turns out, one may not apply the one-layer formalism to multi-layer cases without jeopardizing accuracy. Here, we generalize the approach to 2D systems of arbitrary cell geometry and thickness and use the few-layer black phosphorus (BP) to illustrate how defect properties, mainly group-VI substitutional impurities, are affected. Within the framework of density functional theory, we show that substitutional Te (Te_P) is the best candidate for *n*-type doing, and as the thickness increases, the ionization energy is found to decrease monotonically from 0.67 eV (monolayer) to 0.47 eV (bilayer) and further to 0.33 eV (trilayer). While these results show the ineffectiveness of the dielectric screening at the monolayer limit, they also show how it evolves with increasing thickness, whereby setting a new direction for the design of 2D electronics. The proposed method here is generally suitable to all the 2D materials regardless of their thickness and geometry.

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Introduction

Two-dimensional (2D) materials are promising candidates for future highperformance electronics and optoelectronics due to their intriguing properties [1-8]. One of the prerequisites for achieving this goal is to understand the properties of defect. This is not only because that native defects and unintentional impurities are usually unavoidable in real sample and can strongly affect the physical properties of materials but also because intentional doping is a primary means to control n- or p-type conductivity, which is a key ingredient for the design of optoelectronic devices [9-12]. This has prompted theoretical development of methods to study ionization energies (IE) or charged energies of defects in monolayer materials to overcome the drawback of energy divergence accompanied with the use of a conventional *jellium* approach [13,14]. Due to reduced dimensionality and screening, defects usually introduce deep (i.e., close to midgap) levels in such materials [13,15,16]. However, the levels are found to be shallower when the monolayer material is placed in a dielectric environment such as on a substrate, which can strongly screen the Coulomb interaction between charges [15]. This suggests that controllable electrical conductivity should be easier to obtain in few-layer systems. Moreover, few-layer 2D materials or a monolayer on substrate is more practical in electronic devices instead of a freestanding monolayer [5,17-22]. Therefore, understanding defects in few-layer 2D materials is a significant goal for the fundamental understanding low-dimensional electronics. One possibility to tackle the physics of defects in multilayer could be the use of a supercell with extremely large vacuum size to mimic that the few layer is still thin enough compared to this vacuum size and the application of the existing monolayer formalism [13]. However, such calculations are usually prohibitive due to the associated computational cost. Thus, it is essential to update the formalism of IE of defects in 2D materials for systems with more than one layer under the condition of limited vacuum size.

In this work, we derive a general formalism of charged energies based on Ref. [13] for not only one-atom-thick systems of unilateral geometry such as hexagonal boron nitride but also 2D systems of arbitrary thickness and geometry including one-molecule-

thickness [such as MoS_2 and black phosphorus (BP)], few-layer-thick, 2D systems on a substrate, as well as surfaces and interfaces. We apply this approach to calculate the IE of phosphorus vacancy (V_P) and substitutional group-VI impurities (O_P , S_P , Se_P , and Te_P) in BP from monolayer up to trilayer. Due to the increased screening in thick layers, the IE of Te_P is reduced from 0.67 eV for monolayer (ML-BP) to 0.47 eV for bilayer (2L-BP), and to 0.33 eV for trilayer (3L-BP). The results show that shallow dopants are more practical and easier to obtain in few-layer BP, and most likely in other few-layer 2D semiconductors as well.

Method and Formulation

The calculations were performed using the density functional theory (DFT) [23,24] with the Perdew-Burke-Ernzerhof approximation for the exchange-correlation functional [25], as implemented in the Vienna Ab-initio Simulation Package (VASP) [26,27]. Note that while advanced functionals could yield more accurate results [28,29], the methodology developed here is independent of the choice of functionals. The cutoff energy for the plane wave basis was 520 eV. The 3×2×1 Monkhorst-Pack mesh grid was used for *k*-point sampling and spin polarization was included. All atoms were relaxed until the Hellman-Feynman forces on individual atoms are less than 0.02 eV/Å. For charged defects, a homogenous counter charge (i.e., the *jellium* background) was used to maintain charge neutrality [9,30,31].

The formation energy of a defect α of charge q is given by [32],

$$\Delta H_{f}(q,d) = E(q,d) - E(host) + \sum_{i} n_{i} \mu_{i} + q \left(\varepsilon_{VBM} + \varepsilon_{F}\right)$$

$$= \Delta E(q,d) + \sum_{i} n_{i} \mu_{i} + q \left(\varepsilon_{VBM} + \varepsilon_{F}\right)$$
(1)

where $\Delta E(q,d)$ is the total energy difference between the supercell with defect d, E(q,d), and the perfect supercell, E(host), n_i is the number of atoms exchanged when the defect is created, μ_i is the chemical potential of each of the atoms exchanged, and ε_F is the Fermi energy with respect to the valence band maximum (VBM) of the host material, ε_{VBM} . The defect transition energy is defined by the Fermi energy at which two different charge

states (q'and q) of the same defect d have the same formation energy $\Delta H_f(q,d) = \Delta H_f(q',d)$. Namely,

$$\varepsilon(q/q') + \varepsilon_{VBM} = \left[\Delta E(q,d) - \Delta E(q',d) \right] / (q'-q)$$
(2)

A donor ionization energy, which evaluates the ability of defect to produce free carriers, is defined by $\varepsilon(+/0)$ with respect to the conduction band minimum (CBM), ε_{CBM} , whereas an acceptor ionization energy is defined by $\varepsilon(0/-)$ with respect to VBM.

The scheme leads to an energy error of $\delta E \propto \sqrt[1]{\sqrt[3]{V}}$ for 3D materials, which means gradually converged energies with increasing cell size, but encounters a divergence with increasing vacuum size for charged defects for 2D materials [13,14]. The divergence originates from the long-range Coulomb interaction between charged defects and the compensating *jellium* charge. This difficulty is resolved by an extrapolation of the asymptotic IE expression provided in Ref. [13],

$$IE(S, L_Z) = IE_0 + \frac{\alpha}{\sqrt{S}} + \frac{q^2}{24S\varepsilon_0} L_Z = IE_0 + \frac{\alpha'}{L_s} + \frac{q^2}{24L_s^2\varepsilon_0 sin\theta} L_Z$$
 (3)

where IE_0 is the converged (converged with respect to variable cell size) ionization energy and L_s is the in-plane equilateral cell size, i.e., $L_s = L_x = L_y$, $S = L_s^2 sin\theta$ is the surface area with θ being the angle between L_x and L_y , and L_z is the vertical cell size. This method has been shown to work well for defects in monolayer boron nitride [13]. However, direct application of Eq. (3) does not adequately describe the asymptotic behavior of two dimensional systems with certain thickness, such as 3L-BP studied here.

Eq. (3) is derived in Ref. [13], from a formal expansion of the calculated ionization energy in a power series of $L_x(L_y = \gamma L_x)$ and L_Z , namely (for a more general expression, L_s is replaced by L_x here),

$$IE(L_x, L_Z) = \sum_{i,j=-\infty}^{\infty} c_{i,j} L_x^i L_Z^j$$
(4)

By taking three separate physical limits, (1) L_x and L_y are fixed , $L_Z \rightarrow \infty$; (2)

 L_z is fixed, L_x and $L_y \rightarrow \infty$; and $(3)L_x$, L_y and $L_z \rightarrow \infty$, the power expansion can be substantially reduced to,

$$IE(L_{x}, L_{z}) = \dots + \frac{1}{L_{z}^{2}} \left(\dots + \frac{c_{-2, -2}}{L_{x}^{2}} + \frac{c_{-1, -2}}{L_{x}} + c_{0, -2} \right) + \frac{1}{L_{z}} \left\{ t \ln(L_{x}) + c_{0, -1}' + \frac{c_{-1, -1}'}{L_{x}} + \dots \right\}$$

$$+ \left(\dots + \frac{c_{-2, 0}}{L_{x}^{2}} + \frac{c_{-1, 0}}{L_{x}} + c_{0, 0} \right) + L_{z} \left(\frac{c_{-2, 1}}{L_{x}^{2}} \right)$$

$$(5)$$

Eq. (3) is then arrived at by requiring that $L_Z >> L_x >> 1$. While the requirement that $L_Z >> L_x$ is physically clear, it is not quite clear in which cases the largeness of L_x (or L_Z for that matter) enables the dropping of terms proportional to $\frac{1}{L_x}$, $\frac{1}{L_x^2}$, etc. To gain a better understanding of which terms need to be kept for practical calculations, we revisit limit (1) in the more general situation of a charged defect in a dielectric slab of finite thickness.

In this limit of $L_Z \to \infty$ at fixed L_x and $L_y = \gamma L_x$, the system can be considered as a charged slab with area S and thickness $2d_0$ in a uniform *jellium* background, see Fig. 1.

One may integrate the energy density $\frac{1}{2} \mathbf{E}^2 \varepsilon_{\perp} \varepsilon_0$ where $|E| = \frac{q|z|}{2S\varepsilon_{\perp}\varepsilon_0} \left(\frac{1}{d_0} - \frac{2}{L_z}\right)$

$$\left(-d_{0} < z < d_{0}\right) \text{ and } \frac{1}{2} \mathbf{E}^{2} \varepsilon_{0} \text{ where } \left|E\right| = \frac{q}{2S\varepsilon_{0}} \left(1 - \frac{2|z|}{L_{z}}\right) \left(-\frac{L_{z}}{2} < z < -d_{0}, \ d_{0} < z < \frac{L_{z}}{2}\right) \text{ to }$$

obtain the total electrostatic energy:

$$E_{total} = \frac{q^{2}}{24S\varepsilon_{0}} \left[\left(L_{Z} - 4d_{0} \right) - 2d_{0} \left(1 - \frac{1}{\varepsilon_{\perp}} \right) \right] + \frac{q^{2}d_{0}^{3}}{3S\varepsilon_{0}} \left(\frac{1}{\varepsilon_{\perp}} - 1 \right) \frac{1}{L_{Z}^{2}} + \frac{q^{2}d_{0}^{2}}{4S\varepsilon_{0}} \left(2 - \frac{4}{3\varepsilon_{\perp}} \right) \frac{1}{L_{Z}}$$
(6)

where ε_0 is vacuum dielectric constant (i.e., the absolute dielectric constant as the relative dielectric constant of vacuum is 1) and ε_{\perp} is the out-of-plane dielectric constant (relative dielectric constant) of the 2D material (see the Appendix for details). As $S = L_x \times L_y \times sin\theta = \gamma L_x^2 sin\theta$, we find

$$E_{total} = \frac{q^2}{24\gamma L_x^2 \varepsilon_0 sin\theta} \left[\left(L_z - 4d_0 \right) - 2d_0 \left(1 - \frac{1}{\varepsilon_\perp} \right) \right] + \frac{q^2 d_0^3}{3\gamma L_x^2 \varepsilon_0 sin\theta} \left(\frac{1}{\varepsilon_\perp} - 1 \right) \frac{1}{L_z^2} + \frac{q^2 d_0^2}{4\gamma L_x^2 \varepsilon_0 sin\theta} \left(2 - \frac{4}{3\varepsilon_\perp} \right) \frac{1}{L_z}$$

$$(7)$$

From this limit, IE should be dominated by the L_Z^n term, $n \in [-2,1]$. Here, we explicitly see that as the thickness of the slab $(2d_0)$ increases, the energy has greater contributions from L_Z^2 and L_Z^1 which vanish in the strictly 2D limit $(L_Z \to \infty)$. Also, worth noting is the presence of term $\infty d_0/L_x^2$ in Eq. (7). While this is an idealized system, we see that the thickness of the slab plays an important role as the appropriate physical distance to which we should compare L_x and L_Z . Hence, Eq. (3) is expected to be valid when $L_Z >> L_x >> d_0$.

For the case of 3L-BP however, with $d_0 = 0.66$ nm (thickness $2d_0$), neglecting quadratic terms in L_x , even with a lateral dimension of 4 nm would constitute ignoring terms ~ 120 meV in the ionization energy. Furthermore, simultaneously requiring $L_Z >> L_x$, would drastically increase computational time. In order to obtain a tractable method for dealing with defects in this systems, we include in the fitting of the ionization energy terms which are up to quadratic in length, where we truncate the series as follows:

$$IE(L_{x}, L_{z}) = \frac{c_{0,-2}}{L_{z}^{2}} + \frac{c(L_{x})}{L_{z}} + \left(\frac{c_{-2,0}}{L_{x}^{2}} + \frac{c_{-1,0}}{L_{x}} + IE_{0}\right) + L_{z}\left(\frac{c_{-2,1}}{L_{x}^{2}}\right)$$
(8)

where $c(L_x)$ contains the logarithmic divergence L_x from Eq. (5), $c(L_x) = t \ln(L_x) + c_{0,-1}' + \frac{c_{-1,-1}'}{L_x}$ and $IE_0 = c_{0,0}$ (as $L_x, L_Z \to \infty$, only $c_{0,0}$ survives and thus $c_{0,0}$ equals to IE_0). Instead of directly fitting all parameters simultaneously in Eq. (8), we define

$$\overline{\overline{IE(L_x, L_Z)}} = IE(L_x, L_Z) - \frac{c_{0,-2}}{L_Z^2} - \frac{c(L_x)}{L_z} - L_Z \left(\frac{c_{-2,1}}{L_x^2}\right) = \frac{c_{-2,0}}{L_x^2} + \frac{c_{-1,0}}{L_x} + IE_0$$
(9)

 $\overline{\overline{IE(L_x,L_z)}}$ consists of terms of $IE(L_x,L_z)$, L_z^{-2} , L_z^{-1} , and L_z^{-1} , and it also equals to the

coefficient of the L_Z^0 term (right hand side of the equation). Their specific values can be obtained by fitting calculated $IE(L_x,L_Z)$ with increasing vacuum size L_Z at different L_x . Then IE_0 is obtained as the intercept of $\overline{IE(L_x,L_Z)}$ at $1/L_x \to 0$. Therefore, the difficult problem of taking the limits of $L_x \to \infty$ and $L_Z \to \infty$ is transformed into a simpler problem of finding the intercept of $\overline{IE(L_x,L_Z)}$. The results obtained using this way, denoted by method 1, are shown in Fig. 3(a-c) which will be detailedly discussed below. While this method gives consistent results, the number of calculations involved are laborious, which has motivated us to investigate a more approximate method to determine the ionization energy.

In practical application, the requirement of large L_Z is much easier to obtain than that of large L_x , as it only involves increasing the vacuum dimension, instead of the number of atoms. If we maintain $L_Z >> L_x$, we can drop the $\frac{1}{L_Z}$ and $\frac{1}{L_Z^2}$ terms from Eq. (8) which then reduces to:

$$IE(L_x, L_Z) = \frac{c_{-2,0}}{L_x^2} + \frac{c_{-1,0}}{L_x} + IE_0 + L_Z \left(\frac{c_{-2,1}}{L_x^2}\right)$$
(10)

In order to obtain a more practical expression, which reduces the amount of computation required, we can approximate the value of the coefficient $c_{-2,0} = \frac{q^2}{24\gamma\varepsilon_0 sin\theta} \left[-4d_0 - 2d_0 \left(1 - \frac{1}{\varepsilon_\perp} \right) \right] \text{ from the ideal case presented in Eq. (7),}$

obtaining

$$IE(L_x, L_Z) = \frac{c_{-1,0}}{L_x} + IE_0 + \frac{q^2}{24\gamma L_x^2 \varepsilon_0 sin\theta} \left[\left(L_Z - 4d_\theta \right) - 2d_\theta \left(I - \frac{I}{\varepsilon_\perp} \right) \right]$$

$$(11)$$

which also includes the value of $c_{-2,1} = \frac{q^2}{24\gamma\varepsilon_0 sin\theta}$ which is known exactly. When

compared with Eq. (3) where
$$L_{z}$$
 is the vacuum size, $L_{z}^{'} = (L_{z} - 4d_{\theta}) - 2d_{\theta} \left(1 - \frac{1}{\varepsilon_{\perp}}\right)$ in Eq.

(11) here may be considered as an effective vacuum size. Then IE_0 can be obtained in the same way as that proposed in Ref [13]. Note that IE_0 obtained in this way should be a function of the threshold of L_Z , denoted by L_Z^T , at which the terms of L_Z^{-2} and L_Z^{-1} are considered to be negligible, namely, $IE_0\left(L_Z^T\right)$. $IE_0\left(L_Z^T\right)$ approaches the actual one at $L_Z^T\to\infty$, so the real IE_0 can be deduced by making $1/L_Z^T\to0$. Since the term of L_Z^{-2} and L_Z^{-1} diverge faster and faster with increasing thickness $2d_0$ considering the ratio of $2d_0/L_Z$, L_Z^T should become larger with increasing thickness. This way to get actual IE_0 is denoted by method 2.

Two kinds of native defects (vacancy and interstitial) and four kinds of substitutional impurities (O, S, Se, and Te) are calculated here. In addition to Te substitution, the IEs for other defects in ML-BP are all obtained by Eq. (11) with $L_Z^T = 4$ nm in this study. For Te substitution which is adopted to explore the dielectric effect in few-layer BP, the IEs in ML-BP, 2L-BP, and 3L-BP are all calculated using method 1 [Eq. (9)] and method 2 [Eq. (11)]. The dimensions of the supercell size are 4×4 , 5×5 , 6×6 for $L_x\times L_y$, and (2 nm – 5 nm), (2.5 nm- 8 nm), and (3 nm – 8.5 nm) for L_Z in ML-BP, 2L-BP, and 3L-BP respectively. It should be noted that in our formulation $\gamma = L_y/L_x$ must remain unchanged during the extrapolation.

Results and Discussions

Figures 2(a)-(f) show the optimized atomic structures of native defects and substitutional impurities in ML-BP. Their formation energies, as a function of Fermi energy, are shown in Fig. 2(g). The native defects here include phosphorus vacancy (V_P) and interstitial (P_i). As most BPs show p-type conductivity in the laboratory [4,5,33-35], four substitutional group-VI elements (O_P , S_P , S_P , and S_P) are considered here to explore the possibility of n-type conductivity. For S_P , the top layer S_P atom, originally bonded to the vacant S_P atom in bottom layer, goes down in position to form fourfold coordination. In spite of that, the formation energy of neutral S_P (= 1.96 eV) is still the

largest. For P_i , the foreign P atom can bond to three host P atoms so its energy is relatively low. V_P and P_i are acceptors with deep transition energies at ε_{VBM} + 0.36 and + 0.48 eV, respectively. The group-VI elements, S, Se, and Te, on the other hand, favor twofold coordination, which leaves one dangling bond (DB) in the top-layer P. Hence, they are all donors. While the formation energy follows the trend, Te > Se > S, the donor levels at ε_{CBM} – 0.67, – 0.69, and – 0.74 eV get deeper due to the increase of localization of P DB. Oxygen is somewhat an exception as the formation energy for charge neutral O_P is negative now at -0.72 eV due to its exceptionally large electronegativity, which is reminiscent of the fact that BP is very easily oxidized by air. Due to the significantly increased localization of the P DB in O_P , the donor level also drops significantly, 0.11 eV below the VBM.

In view of the above results, the best candidate for n-type doping of ML BP are Tep ($\varepsilon_{CBM} - 0.67$ eV). However, these levels are still too deep to supply sufficient amount of carriers for electronic applications. (With a more accurate theoretical band gap, the situation is expected to only getting worse since the functional used here is known to systematically underestimate the band gap [36,37].) The depth here mainly comes from the weak screening of 2D semiconductors, leading to a stronger effective Coulomb attraction between opposite charges, compared to behavior in bulk material [15]. The screening, however, should get stronger as the layer thickness increases. For the clarity of discussion and for simplicity, in our study, defects are kept at the bottom of the first layer as in Fig. 2. Altering defect positions are expected to alter numerical results but not the conclusion.

Figures 3(a)-(c) show the $IE(L_x,L_Z)$ of Te_P in ML-BP, 2L-BP, and 3L-BP, respectively. In ML-BP, the $IE(L_x,L_Z)$ is nearly in linear divergence with increasing L_Z at fixed L_x , which means that the terms of L_Z^{-2} and L_Z^{-1} do not play a major role in the energy divergence. However, they indeed do that in 2L-BP and 3L-BP where the energies deviate from linear divergence at small L_Z . The intercepts at $1/L_x \rightarrow 0$ of $\overline{IE(L_x,L_Z)}$

denote the real ionization energies, IE_0 , which become shallower with increasing layer thickness: e.g., 0.67 eV, 0.47 eV, and 0.33 eV for ML-BP, 2L-BP, and 3L-BP, respectively. As shown in Fig. 3(d), IE_0 is also obtained with method 2 [Eq. (11)]. In this way, the terms of L_Z^{-2} and L_Z^{-1} in Eq. (8) are ignored at L_Z^T (threshold of L_Z , at which the terms of L_Z^{-2} and L_Z^{-1} are ignored) and IE_0 is dependent of L_Z^T , i.e., $IE_0(L_Z^T)$. Direct extrapolation of the linear dependence in $1/L_Z^{T}$ of $IE_0\left(L_Z^{T}\right)$ yields the actual value IE_0 (orange arrows in Fig. 3(d)), being 0.67 eV, 0.43 eV, and 0.37 eV for ML-BP, 2L-BP, and 3L-BP, respectively. The results are well consistent with that obtained with method 1. Note that the decreasing ionization energies is not only a result of the up/down shifts of the VBM/CBM, but also a result of weakened Coulomb attraction due to increased dielectric screening. Though both methods perform well, the first one needs more calculation resource than the second one since the latter only requires the calculation of three or four points for the linear extrapolation. Moreover, the slope of the linear dependence is extremely small for thin films and become larger with increasing thickness. This means that the value of $IE_0(L_z^T) - IE_0(L_z^T)$ is minimal for thinnest limitation. Fig. 3 (d) shows that indeed this is the case for monolayer here, with energy difference between $IE_0\left(L_Z^T=2.5 \text{ nm}\right)$ and $IE_0\left(L_Z^{T'}\to\infty\right)$ is less than 0.04 eV. Therefore, sensible results can be obtained for monolayer at one appropriate L_Z^T without the need for linear extrapolation.

The thickness-dependent IE₀ is consistent with the calculated defect/impurity charge distributions, shown in Fig. 4 (a-c) along the in-plane (X and Y) and out-of-plane (Z) directions, for example, for Te_P. They show consistently that, with an increasing layer thickness, the spatial charge distributions of the gap states induced by the substitutional Te become more delocalized. One can see this from the in-plane charge distribution in Fig. 4 (a-b) where there is a significant reduction at the Te site especially between ML to 2L. Likewise, there is also a significant increase at the tail region away from the Te. Although the increase may look small, taking into account the geometric factor of R², where R being the distance to Te indicates that the effect should be on par with that in the center, since the total number of electrons for each state is conserved. One can also see

this from the out-of-plane charge distribution in Fig. 4 (c) where the tail extends into the second layer noticeably for 2L and 3L, but not for ML. One can also see a similar but less dramatic effect in charge contour plot in Fig. 4 (d). It appears that in terms of the charge distribution, the most significant effect is between ML and 2L, which is consistent with the decreasing tendency of ionization energy.

In summary, while Ref. [13] laid the foundation for first-principles determination of charged defects in monolayer 2D materials using the standard jellium background approximation, it requires a generalization of the approach to cases which are mostly used in the practical electronic devices, i.e. few/multi-layer 2D semiconductors instead of monolayer, a layer of 2D material on a substrate, and surfaces/interfaces. It also requires a generalization to systems of arbitrary geometry and hence with less symmetry requirement in the method. These are carried out here. The method here is general and suitable for all the 2D materials with arbitrary thickness and geometry. With the generalized approach, the dopability of 2D and quasi-2D materials, which is crucial for their application in electronic and optoelectronic devices, can be evaluated by the calculation of ionization energy. Application to black phosphorus, in particular, to substitutional Te (Te_P, the most promising candidate for *n*-type doing) in few-layer BP reveals that enhanced screening indeed exists and can reduce the Coulomb attraction between opposite charges to result in the dopant wavefunction delocalization as well as shallower levels. The ionization energy of Te_P decreases by nearly half in 3L-BP (0.33) eV) in comparison with that in ML-BP (0.67 eV). These results further suggest that for 2D applications, single layer materials may not always be the best choice but few-layer materials can offer the most balanced properties for novel electronic and optoelectronic applications.

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APPENDIX: CALCULATION OF ε_{\perp} FOR THE 2D MATERIAL WITH A CERTAIN THICKNESS

The calculated Dielectric constant in VASP for a supercell with L_z can be approximated by an average of the dielectric constant for the 2D material with thickness $2d_0(\varepsilon_\perp)$ and that for the vacuum region (with thickness L_z-2d_0) [16], namely,

$$\varepsilon_{\perp}^{ave} = \frac{2d_0\varepsilon_{\perp} + (L_Z - 2d_0) \times 1}{L_Z}$$

Here, ε_{\perp} is the relative dielectric constant we needed for the 2D material (the vertical scope from the top atom to the bottom atom) and the relative dielectric constant of vacuum is 1. The expression can change to,

$$\varepsilon_{\perp}^{ave} = \frac{2d_{\scriptscriptstyle 0}\varepsilon_{\scriptscriptstyle \perp} + \left(L_{\scriptscriptstyle Z} - 2d_{\scriptscriptstyle 0}\right)}{L_{\scriptscriptstyle Z}} = 1 + \frac{1}{L_{\scriptscriptstyle Z}} \Big[2d_{\scriptscriptstyle 0}\left(\varepsilon_{\scriptscriptstyle \perp} - 1\right) \Big] = 1 + \frac{1}{L_{\scriptscriptstyle Z}} k$$

As such, the ε_\perp^{ave} is inversely proportional to L_Z with a slope k. We can get the ε_\perp via the fitting slope k, i.e. $\varepsilon_\perp = 1 + \frac{k}{2d_0}$.

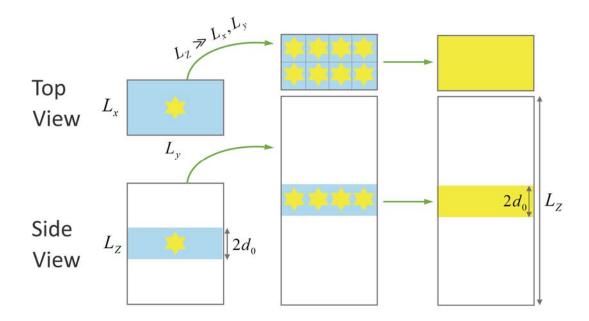


Figure 1. (color online) A schematic illustration of the asymptotic limits of a charged defect (yellow star) in a 2D system (light-blue) with thickness ($2d_0$) and none-equilateral unit-cell geometry ($L_x \neq L_y$) for the limit of $L_Z >> L_x, L_y$.

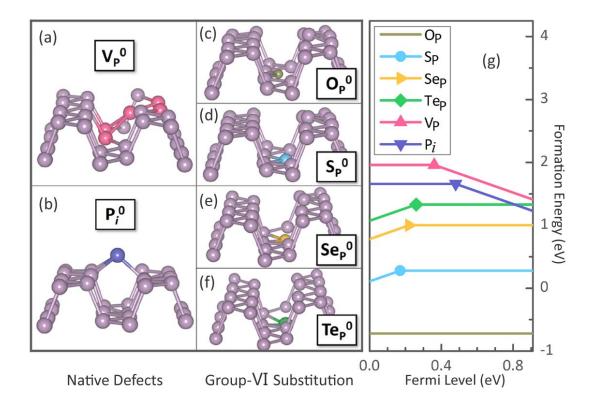


Figure 2. (color online) (a)-(f) Optimized atomic structures of native defects, V_P and P_i , and substitutional group-VI impurities, O_P , S_P , S_P , S_P , and S_P , in ML-BP. (g) Their formation energy as a function of Fermi energy within the calculated GGA band gap of 0.91 eV. Each P atom has three nearest-neighbor (nn) P atoms. In (a), the out-of-plane nn P of the vacant P atom in the bottom layer forms chemical bonds with its two in-plane nn P. Five P atoms are significantly relaxed due to this rebonding and they are all marked in pink. In (b)-(f), interstitial P and substitutional O, S, Se, and Te are marked in purple, tawny, light blue, yellow, and green, respectively.

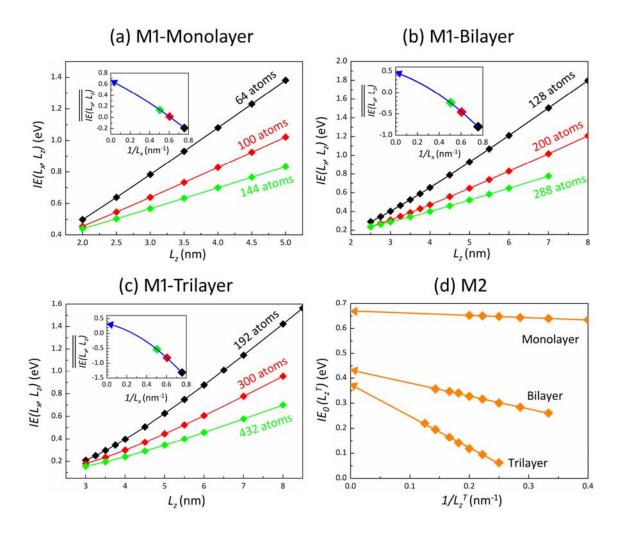


Figure 3. (color online) (a)-(c) Method 1(M1): Ionization energies of Te_P at different lateral dimensions (4×4, 5×5, 6×6 for $L_x \times L_y$) as a function of L_z in ML-BP, 2L-BP, and 3L-BP respectively. The insets show the value of $\overline{IE(L_x,L_z)} = \frac{c_{-2,0}}{L_x^2} + \frac{c_{-1,0}}{L_x} + IE_0$ as a function of $1/L_x$. The actual ionization energies IE_0 s are indicated by blue arrows. (d) Method 2(M2): $IE_0(L_z^T)$ of Te_P as a function of $1/L_z^T$ (L_z^T , threshold at which the terms of L_z^{-2} and L_z^{-1} are ignored) in ML-BP, 2L-BP, and 3L-BP respectively. The real ionization energies IE_0 s are indicated by orange arrows. M1 and M2 mean that ionization energies are calculated with method 1 [Eq. (9)] and method 2 [Eq. (11)], respectively.

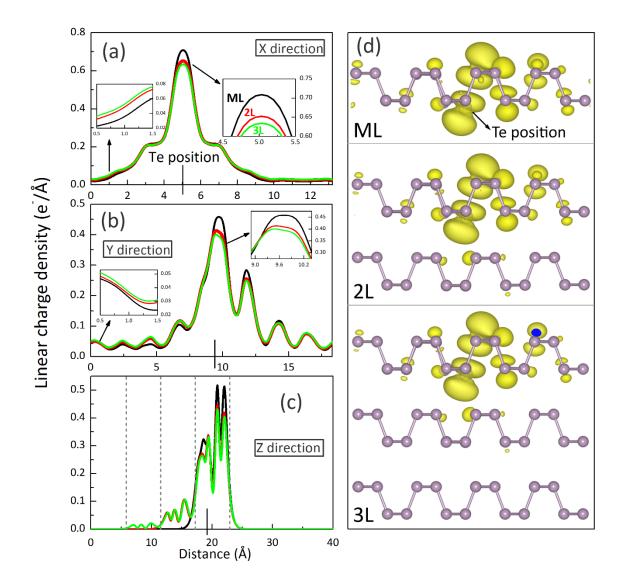


Figure 4. (color online) Non-averaged linear charge density (passing Te_P) along the inplane (a) X and (b) Y and (c) out-of-plane Z directions in ML-BP, 2L-BP, and 3L-BP, respectively. Vertical solid line marks the position of the Te impurity. Dotted lines in (c) denote the physical boundary of each P layer. (d) Charge contour plots with an isosurface $=8\times10^{-4}$ e/Å³.

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