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Divergent synthesis routes and superconductivity of ternary hydride MgSiH₆ at high pressure

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Dedicated to Prof. Guangtian Zou on the occasion of his 80th birthday

ABSTRACT

We predict a new ternary hydride MgSiH₆ under high pressures, which is a metal with ionic feature and takes on a simple cubic structure with space group *Pm*-3 above 250 GPa. Our first-principles calculations show that the cubic MgSiH₆ is a potential high-temperature superconductor with superconducting transition temperature T_c of ~ 63 K at 250 GPa. Further analysis suggests that phonon softening along mainly Γ -X and Γ -M directions induced by Fermi surface nesting plays a crucial role in the high-temperature superconductivity. Herein, we propose a new method "Triangle Straight-Line Method" which provides a clear guide to determine the specific A+B→D type formation routes for ternary hydrides of Mg-Si-H system and it effectively reveals two divergent paths to obtain MgSiH₆ under high pressures: MgH₂+SiH₄→MgSiH₆ and MgSi+3H₂→MgSiH₆. This method might be applicable to all ternary compounds, which will be very significative for further experimental synthesis.

I. INTRODUCTION

Excitingly theoretical prediction¹ and experimental observations^{2,3} of superconductivity in strongly squeezed solid hydrogen sulfide with high superconducting transition temperature T_c of ~ 200 K have been widely recognized as one of most significant findings in the superconducting field. What's more, these breakthrough discoveries reignite interest to seek possible high temperature superconductors in other hydrogen-dominated compounds. Thus far, a large number of researches are mainly focused on binary hydrides and extensive investigations suggest that high- T_c usually involve with a large hydrogen framework⁴. In these binary hydrogen-rich high- T_c superconductors, doped elements play a role to metallize hydrogen at lower pressures, which is defined as so-called "chemical precompression"⁵, but in fact, hydrogen is mainly responsible for the superconductivity owing to its light atomic mass and high Debye temperature. Based on this essence, some ternary hydrogen storage materials are believed to be candidates as high-temperature superconductors.

Experimentally, Muramatsu *et al.* found that the ternary BaReH₉ transforms into a superconductor with T_c of ~ 7 K above 100 GPa⁶. Theoretically, $Cmc2_1$ phase of Fe₂SH₃ was predicted to be stable at 100 GPa, but its electron phonon coupling (EPC) parameter λ is just 0.30 and that results in a fairly low T_c = 0.3 K at 173 GPa⁷. Recently, Rahm et *al.* predicted that *P4/mmm*-KAuH₂, *I*4-Ba(AuH₂)₂ and *I*4-Sr(AuH₂)₂ which contain AuH₂⁻ molecular units are superconductors with T_c of 0.3, 30 and 10 K at 120 GPa, 1 atm and 1atm, respectively⁸. Earlier, CH₄ molecular unit was found in ternary superconductive *P4/nmm*-MgCH₄ at high pressures⁹.

Silicon (Si) is the next group-IVA element isoelectronic to C. Undoubtedly, someone may argue that Si atom would bond with four H atoms to form SiH₄ molecular units in Mg-Si-H system similar to MgCH₄. However, owing to the larger atomic core of Si than those of C, Si-H bonding is expected to be weaker than that of C-H, which might promote the dissociation of the Si-H bonding and then lead to some completely different crystal structures and novel properties at high pressure. Similarly, a typical example is MH_4 (M = Si¹⁰, Ge¹¹ and Sn¹²) system, where the discrepancies of bonding render substantially different structures and properties.

In addition, high pressure can stabilize some novel and unexpected stoichiometric binary hydrides. For instance, NaH₃, NaH₇ and possible NaH₉ were reported to be synthesized by compressing NaH and H_2^{13} . More intriguingly, our group proposed three different paths to obtain solid H_3S^{14} , *i.e.*, $2H_2S+H_2\rightarrow 2H_3S$, $3H_2S\rightarrow 2H_3S+S$ and $3/2H_2+S\rightarrow H_3S$. Strobel *et al.* have reported that $(H_2S)_2H_2$ (stoichiometric H_3S) can be formed by mixing hydrogen sulfide (H_2S) and hydrogen (H_2) at high pressure¹⁵. Theoretical predictions proposed the H_3S could be the high-pressure decomposition product of $H_2S^{14,16,17}$, which has been confirmed by synchrotron X-ray diffraction experiment³. More recently, H_3S was directly synthesized by combining the molecular hydrogen (H_2) with sulfur (S) at about 50 GPa¹⁸.

Likewise, pressure could also synthesize some unusual ternary hydrides in Mg-Si-H system. Nevertheless, how to determine synthesis paths for these stable ternary hydrides will be critical because of these rich precursors (*e.g.*, Mg, Si, H₂ MgH₂ and SiH₄, etc.). Once these synthetic paths are identified, they will be very helpful to stimulate further experimental synthesis. In this work, we proposed a method to determine A+B \rightarrow D (reactants A, B and resultant D) type high-pressure formation-route. Moreover, we predicted that the cubic MgSiH₆ (group space *Pm*-3) has a high *T*_c of 63 K at 250 GPa and soft phonon modes play a significant role in superconductivity.

II. COMPUTATIONAL METHODS AND DETAILS

We explored these stoichiometries and crystal structures of Mg-Si-H system at the pressure range of 50-300 GPa by means of evolutionary algorithm and particle swarm optimization algorithm, implemented in the USPEX (Universal Structure Predictor: Evolutionary Xtallography)^{19,20} and CALYPSO (Crystal structure AnaLYsis by Particle Swarm Optimization) $code^{21,22}$, respectively. Both of two methods are very successful in predicting ternary high-pressure crystalline structures^{7,23-25}. Unlike binary compounds, too many structures and stoichiometries need to be considered in complicated ternary hydrides. Therefore, we employed variable-composition prediction method in USPEX to seek possible stoichiometries. Subsequently, we further used CALYPSO and USPEX to research these structures of possible stoichiometries with 1 ~ 4 formula units.

Structural relaxations and calculations of electronic properties were carried out by using the projector augmented-wave potentials²⁶ implemented in the Vienna ab initio simulation VASP code²⁷. 1*s*, $3s^2$ and $3s^23p^2$ configurations were treated as valence electrons for H, Mg and Si, respectively. Exchange-correlation functional was described by adopting the generalized gradient approximation (GGA) of Perdew-Burke-Ernzerhof (PBE)²⁸. For structural searches, a kinetic cutoff energy of 500 eV and Monkhorst-Pack k meshes with grid spacing $2\pi \times 0.05$ Å⁻¹ were found to be sufficient. Furthermore, these selected structures were re-optimized by employing a more precise set of

parameters: a basis set cutoff of 1000 eV and a k-point grid spacing of $2\pi \times 0.03$ Å⁻¹. The high precision parameters ensure the enthalpy converges better than 1meV/atom. The zero-point energy (ZPE) is calculated by using VASP in conjunction with the PHONOPY code²⁹ with 3 × 3 × 3 supercells.

Phonon and incipient electron-phonon coupling (EPC) calculations were performed based on density functional perturbation theory (DFPT)³⁰ through the Quantum-ESPRESSO code³¹. The generalized gradient approximation correction (GGA) of PBE within Norm-conserving pseudopotentials of Troullier-Martins (TM) form³² was tested to be used. The kinetic energy cutoff and the charge density cutoff of the plane wave basis were chosen to be 100 Ry and 400 Ry, respectively. Self-consistent electron density was evaluated by employing $24 \times 24 \times 24$ k mesh. Both phonon and EPC were calculated by using a $6 \times 6 \times 6$ q mesh.

Subsequently, considering the effect of Brillouin zone sampling to EPC³³⁻³⁵, we further used a recently developed Wannier interpolation method³⁶ to recalculate the EPC with fine k and q grids. In the Wannier interpolation calculation, we used the TM norm-conserving pseudopotentials and local density approximation (LDA) exchange-correlation functional to evaluate the Bloch states and the phonon perturbation potentials. The kinetic energy cutoff was tested to choose 100 Ry. A Γ -centered Brillouin-zone mesh of 24 × 24 × 24 mesh was employed to calculate charge density. The phonon was calculated on a Γ -centered 6× 6× 6 mesh. Maximally localized Wannier functions (MLWF) were constructed on a 6× 6× 6 grid of the Brillouin zone with the 1*s*, 2*s* and 3*s* 3*p* orbitals for H, Mg and Si, respectively. Fine electron (60 × 60 × 60) and phonon (30 × 30 × 30) grids were interpolated into the EPC constant with the Wannier90³⁷ and EPW (Electron–Phonon coupling using Wannier functions)³⁸ codes.

III. RESULTS AND DISCUSSION

A. Determination of stable stoichiometries and divergent synthesis routes

Different from binary system, there are some potential difficulties in predicting the stable stoichiometries of ternary hydrides. Above all, we have to consider a great deal of stoichiometries to construct convex hull and then choose stable structures. However, obviously, it is unrealistic to get all stable Mg-Si-H stoichiometries. In order to reduce computational costs and attain precise search ranges, we used variable-composition prediction method by taking into account a little bit of Mg, Si, but

massive H. For each stoichiometry, the maximum atomic numbers of every species were restricted to less than 4 for magnesium (Mg), 4 for silicon (Si) and 16 for hydrogen (H), which means total stoichiometres are 403, including 256 tri-hydrides, 128 binary hydrides, 16 Mg-Si alloys, and the rest 3 elements (*i.e.*, Mg, Si and H). Treating Mg, Si and H as fundamental search blocks, we undertook the variable-composition predictions and the generalized trigonal high-pressure phase diagrams are depicted in Fig. 1. Although the initial searching pressure is 50 GPa, the Fig. 1 is constructed from 200 GPa, because dynamically unstable or nonmetallic feature for three phases (*R*-3*m*, *Pm*-3 and *C*2/*m*) of MgSiH₆ below 200 GPa, which will be discussed later.

As is shown in Fig. 1, for elemental solids located on three vertexes of triangle, we predicted a *bcc* Mg, a *fcc* Si and a C2/*c* H from 200 to 300 GPa, in excellent agreement with previous reports³⁹⁻⁴¹. For binary system, we predicted 8 different stoichiometries located on three sides (Mg-H, Si-H and Mg-Si) of triangle *i.e. P*6₃/*mmc*-MgH₂, *Cmcm*-MgH₄, *R*-3-MgH₁₂, *P*-1-MgH₁₆, SiH₄, *Fm*-3*m*-Mg₃Si, *P6/mmm*-Mg₂Si and *P4/mmm*-MgSi. These predicted binary Mg-H system compounds (see more detailed Fig. S1 in Supplementary Materials (SM)) accord with literature⁴². Silane (SiH₄) falls on Si-H side and its high-pressure phase consists with that in literature¹⁰. For Mg-Si system, at ambient pressure, Mg₂Si is the only stable compound⁴³. In this Mg-Si-O system²³, *P6/mmm*-Mg₂Si was reported to be the only stable binary compound above 0.5 TPa. However, our predictions suggest that Mg₃Si, Mg₂Si and MgSi locate on Mg-Si side from 200 to 300 GPa (Fig. S2) and their crystal structure information can be found in SM (Fig. S3 and Table S1). Furthermore, calculations on thermodynamics, mechanics and dynamics demonstrate that they are stable (Table S2 and Fig. S4). All of these reported stable elemental solids and binary compounds on three vertexes and sides of triangles, respectively, were also found in our work, demonstrating that our results are credible and these chemical species are suitable as high-pressure reactants.

Except for elemental solids and binary compounds, we predicted 7 ternary hydrides Mg₃SiH, MgSiH, MgSiH₂, MgSiH₃, MgSiH₄, MgSiH₆, and Mg₂SiH₈ from 200 to 300 GPa located inside of the triangle depicted in Fig. 1 and their crystal structure information can be also found in Fig. S5 and Table S3. Obviously, these ternary hydrides can be obtained by directly compressing Mg, Si and H. Besides, it could exist others synthesis routes to obtain ternary hydrides due to abundant precursors (stable elemental solids and binary compounds). Some possible formation-routes types for ternary hydrides can be summarized: A+B+C→D; A+B→D; A+B→D+E; A+B→D+E+F; A→B+C and A→B+C+D types etc., where the left of arrows are/is the reactant(s) and the resultant(s) on the right.

In this work, $A+B\rightarrow D$ type formation-route is mainly concerned. Herein, we propose a new method to judge the specific synthesis pathways for ternary hydrides. Namely, if a straight line connected any two stable species A and B (elements or compounds) passes through another ternary hydride C, proving that the ternary hydride C might be synthetized by this two species A and B. We call this method as "Triangle-Straight Line Method" (TSLM) in the following text. Based on this method, it can be clearly seen that Mg₃SiH is obtained by combining Mg₃Si alloy and elemental H (blue line in Fig. 1). MgSiH_n (n=1, 2, 3, 4) could be synthetized by combining MgSi alloy with different concentrations of hydrogen (red line in Fig. 1). Intriguingly, two different color lines (red and green) intersect at MgSiH₆, indicating that it could be synthetized by two substantially different synthesis routes, *i.e.*, MgH₂ + SiH₄ \rightarrow MgSiH₆ and MgSi + 3H₂ \rightarrow MgSiH₆. Likewise, purple and green lines intersecting at Mg₂SiH₈ suggests that it could be also obtained via 2MgH₂+SiH₄ and Mg₂Si+4H₂. We do emphasize that some other binary or ternary stoichiometres are possibly attained by extending the search range or adding atomic numbers, but it needs more computational costs.

To verify the reasonability of the above-mentioned TSLM, we performed fixed-composition predictions by considering 5 different stoichiometres (*i.e.*, Mg₃SiH₁₀, Mg₂SiH₈, MgSiH₆, MgSi₂H₁₀, MgSi₃H₁₄) with MgH₂ and SiH₄ treated as precursors. The enthalpies of formation for candidate stoichiometries with respect to dissociation into MgH₂ and SiH₄ at 200 to 300 GPa are calculated and depicted in Fig. 2 (a)-(c). It is found that both MgSiH₆ and Mg₂SiH₈ locate on tielines from 200 to 300 GPa, indicating they are thermodynamically stable and could be synthesized by mixing MgH₂ and SiH₄, proving that TSLM is an effective method to determine the specific synthesis route for ternary hydrides of Mg-Si-H system. Owing to the most negative formation enthalpies, MgSiH₆ can be synthesized more easily than Mg₂SiH₈ in principle. Mg₃SiH₁₀, MgSi₂H₁₀ and MgSi₃H₁₄ are off the tielines, indicating they are thermodynamically unstable.

In addition, we carried out another fixed-composition prediction to verify the TSLM by taking into account 8 different stoichiometres (*i.e.*, MgSiH, MgSiH₂, MgSiH₃, MgSiH₄, MgSiH₅, MgSiH₆, MgSiH₇ and MgSiH₈) with respect to decompose into MgSi alloy and elemental H. As depicted in Fig. 2(d), except for MgSiH₅, MgSiH₇ and MgSiH₈, other stoichiometres fall on convex hull at 200 GPa. With increasing pressure, MgSiH₄ deviates distinctly tieline and become unstable at 250 GPa shown in Fig. 2(e). Further compressed to 300 GPa (Fig. 2 (f)), MgSiH₃ separates from tieline. Notably, in the

process of pressurization, $MgSiH_6$ is always on the convex hull, indicating it remains thermodynamically stable from 200 to 300 GPa. The above results show that MgSi can combine with one, two, three, four and six H atoms at different pressures to form ternary MgSiH, MgSiH₂, MgSiH₃, MgSiH₄ and MgSiH₆, respectively, demonstrating that our TSLM is reasonable.

Herein, it can be found that the TSLM is very useful in determining $A+B\rightarrow D$ type high-pressure fomation routes for ternary hydrides of Mg-Si-H system. It might be also applicable to all ternary compounds, which is very significant and helpful for further experimental synthesis. Notably, there may exist other pathways to obtain ternary MgSiH₆, such as $A+B+C\rightarrow MgSiH_6$ type listed in Table S4 (SM), and others ternary compounds Mg₃SiH, MgSiH, MgSiH₂, MgSiH₃, MgSiH₄ and Mg₂SiH₈ might also exhibit some excellent properties (include superconductivity) at stable pressures, but these exceed our discussion scope.

B. Structural characteristics and electronic properties of cubic MgSiH₆

For MgSiH₆, three energetically competing phases *R*-3, *C*2/*m* and *Pm*-3 were found via our structural predictions. The crystal structures and lattice parameters of *R*-3, *C*2/*m* and *Pm*-3 MgSiH₆ are shown in Fig. S6 and Table S5, respectively. Without considering zero-point energy (ZPE), we found that *R*-3 phase is the thermodynamically more stable than other two phases below 113 GPa (Fig. 3). But the *R*-3 phase is dynamically unstable (Fig. S7). Above 113 GPa, *C*2/*m* phase become the more stable phase until 275 GPa, then it transforms to *Pm*-3 phase. The *C*2/*m* phase exhibit nonmetallic feature until the highest pressure 275 GPa (Fig. S8).

It can be also noted that the enthalpy of C2/m phase (23.96522 eV/f.u) is slightly lower than that of Pm-3 phase (24.00464 eV/f.u) at 250 GPa, as listed in Table S6. However, it is well known that the zero-point energy (ZPE) is essential in determining structural stability of hydrogen-rich compounds, especially for where the energy difference between phases is very small. The ZPE can be defined as,

$$E_{ZPE} = \frac{1}{2} \sum_{q,v} \hbar \omega_{q,v} \tag{1}$$

where v indicates a phonon branch at wave vector q; $\omega_{q,v}$ is the frequency at wave vector q in the zone. In the formula (1), E_{ZPE} is proportional to $\omega_{q,v}$, which means some soft phonon modes (to be discussed in section C) might induce a lower E_{ZPE} . Since the *Pm*-3 phase is dynamically unstable at 200 GPa (Fig. S9), we calculated its ZPE from 250 GPa. The calculated ZPE of *Pm*-3 phase (2.13403 eV/f.u) is lower than that of C2/m (2.35285 eV/f.u) at 250 GPa (see Table S6). Once the ZPE is included, the total energy of *Pm*-3 phase become lower than that of C2/m phase from 250 to 300 GPa (inset of Fig. 3), meaning *Pm*-3 is more stable than C2/m at this pressure range. Obviously, ZPE essentially lowers the stable pressure of *Pm*-3 MgSiH₆ at least 250 GPa or even lower. Therefore, it can be found that phonon softening affects the ZPE, and further reduces the pressure points of phase transition between competing C2/m and *Pm*-3 phases.

Divergent synthesis routes produce same MgSiH₆ adopting a simple cubic structure with group space *Pm*-3 at 250 GPa. As is depicted in Fig. 4(a), in cubic MgSiH₆, the center and vertex of simple cubic lattice are occupied by Si and Mg atom, respectively. Moreover, all equivalent H atoms form chains arranging along directions of axis. This structure is extremely similar to binary A15-type hydride AlH₃⁴⁴ (Fig. 4(b)). The structural similarity can be explained from alternative perspective by analyzing elemental mass and Pauling electronegativity. From the vibrational view, the atomic mass (M) is an anticipated major factor in dynamic equation, and corresponding values of Mg, Al, and Si are 24.31, 26.98 and 28.09 a.m.u, respectively. Obviously, two M_{Al} is closed to $M_{Mg}+M_{Si}$, which could somewhat guarantees the dynamical stability of system by replacing 2 Al atoms with Mg and Si atoms. By analysis of Pauling electronegativity, we found that the effect of 2 Al atoms can be completely displaced by Mg + Si, because the electronegativity of Al is closed to a half of Mg+Si. More importantly, in *Pm*-3*n* Al₂H₆ (AlH₃ can be written as Al₂H₆), all H atoms form a sublattice and 2 Al atoms provide 6 electrons to stabilize structural framework. In similar H sublattice of *Pm*-3 MgSiH₆, Mg and Si replace 2 Al to offer same amount of electrons.

The electronic band structure and density of electronic states (DOS) of MgSiH₆ at 250 GPa are calculated and shown in Fig. 4(c). The energy band structure characterizes the metallic character with bands overlapping at Fermi level. It is clearly seen that a steep conduction band crosses Fermi level along Γ -R-M direction and forms an "electron pocket" around R points. Simultaneously, two flat valence bands appear in the vicinity of Fermi level along X-M direction. The "flat band-steep band" concurrently occurring in MgSiH₆ indicates that it may be a good high temperature superconductor⁴⁵. Although MgSiH₆ takes on a similar crystalline structure with AlH₃, the band structure dependence on pressure is essentially different from that of AlH₃. The band structures of MgSiH₆ are not dramatically changed from at 250 to 300 GPa. However, with increasing pressures, AlH₃ exhibits an anti-metallization behavior⁴⁶. Besides, it can be found that H atoms provide significant contributions to DOS at Fermi level $N(\varepsilon_F)$, which is very similar with some binary hydrogen-dominated high- T_c

superconductors⁴. High $N(\varepsilon_F)$ usually means a large EPC strength⁴⁷. Fig. 4(d)-(e) show the electron localization function (ELF) of MgSiH₆ and no electron localization is found between Mg-H and Si-H, indicating the ionic nature of system. Note that there are no molecular units in MgSiH₆, which is different from the CH₄ units-contained MgCH₄⁹.

C. Phonon softening, Fermi surface nesting and superconductivity

To ensure the structural stability of MgSiH₆ at high-pressure, mechanics and the lattice dynamics was tested at 250 GPa. The strain energy of a mechanically stable crystal must be positive, namely, the matrix of elastic constants (C_{ij}) should be positive. The simple mechanical stability criteria of a cubic phase is given by $C_{11} > 0$, $C_{44} > 0$, $C_{11} > |C_{12}|$ and $(C_{11} + 2C_{12}) > 0^{48}$. In the cubic phase of MgSiH₆, the $C_{11} = 777.98$, $C_{44} = 226.1$ and $C_{12}=432.8$ GPa, and they satisfy mechanical stability criteria, demonstrating MgSiH₆ is mechanically stable at 250 GPa. The phonon band structure and the projected density of states (PHDOS) at 250 GPa is depicted in Fig. 5. The presence of no any imaginary frequency in the phonon spectra indicates the dynamical stability of cubic phase (Fig. 5(a)). Owing to discrepancy of atomic mass, these vibrational modes can be divided into two major regions. As is depicted in Fig. 5(b), the low-frequency vibrational modes below about 645 cm⁻¹ is dominated by heavier Mg and Si atoms, and the high-frequency region is mainly associated with H atomic vibration modes. It is found that the positions and values of peaks in PHDOS derived from Mg and Si atoms are very similar, which is ascribed to similar atomic masses and positions.

A prominent feature in the phonon dispersion is the presence of soft phonon modes mainly concentrated in two regions. The lowest acoustic vibration mode (branch 1) undergoes softening along Γ -X and the seventh vibration mode softens along Γ -X and Γ -M (Fig. 5(a)). To clearly elucidate this reason of phonon softening, we investigated the Fermi surface nesting in the cubic MgSiH₆ by applying the nesting function

$$\xi(Q) = \frac{1}{N} \sum_{\vec{k},i,j} \delta(\varepsilon_{\vec{k},i} - \varepsilon_F) \delta(\varepsilon_{\vec{k} + \vec{Q},j} - \varepsilon_F) , \qquad (2)$$

where $\varepsilon_{k,i}$ is the Kohn-Sham eigenvalue and *i*, *j* are the indices of energy bands, *N* is the number of *k* points, and ε_F is the Fermi energy. To calculate the $\zeta(Q)$, we used the density function of normal distribution (*i.e.*, Gaussian function) to replace the δ function with broadening of 0.01. The large value of nesting function $\zeta(Q)$ for a vector *Q* vividly describes high probability for parallel portions of the Fermi surface nested by a *Q*. Fig. 6(a) shows the $\zeta(Q)$ along high-symmetry lines Γ -X-M-R- Γ -M. For Γ

point, its $\xi(Q)$ represents entire Fermi surface nests into itself, which has no actual physical meaning. The $\xi(Q)$ quantitatively describe two sharp peaks along Γ -X and Γ -M directions, demonstrating that strong Fermi surface nesting occurs at these directions. Not coincidentally, it can be observed from Fig. 5(a) that the regions of phonon softening correspond to the nesting directions, strongly indicating phonon softening is induced by Fermi surface nesting. Furthermore, this quantitatively calculation on $\xi(Q)$ can be proved by observing the contour of Fermi-surface, as depicted in Fig. 7. Peaks in $\xi(Q)$ along Γ -X direction are related to nesting vectors along the k_x , k_y and k_z axis (Fig. 7(a)). Peaks along Γ -M direction correspond to the obvious Fermi surface nesting depicted in Fig. 7(b).

To explore the superconductivity of MgSiH₆, we investigated the EPC parameter λ by two ways. Based on density functional perturbation theory (DFPT), we used QE with the coarse $6 \times 6 \times 6$ q-mesh and obtained the $\lambda = 0.956$ at 250 GPa. In order to attain the more precise EPC parameter λ , the more accurate electron-phonon interaction matrix elements depending on the number of k and q points should be calculated with more dense k-mesh and q-mesh. Therefore, the EPW was used to compute λ with fairly dense k-mesh ($60 \times 60 \times 60$) and q-mesh ($30 \times 30 \times 30$) (see section II). Nonetheless, we found the value of λ from EPW calculation is 0.943, which is closed to that from QE, indicating both of two ways are reasonable in estimating EPC. Calculation reveals a large $\lambda = 0.96$ or 0.94, suggesting the electron phonon coupling is fairly strong.

The spectral function $\alpha^2 F(\omega)$ and the integrated EPC parameter λ as a function of frequency are shown in Fig. 6(b). It is found that the low-frequency and high-frequency contribute 45% and 55% to total EPC λ , respectively. Herein, it is noted that the low-frequency provides a very important contributions to EPC, which is significantly different from some binary H₂ units contained hydrides^{11,12,49-51} and recently fashionable H₃S¹. As will be discussed later, the important difference is relation with soft phonons of low-frequency. The superconducting critical temperature T_c can be evaluated by using the Allen-Dynes modified McMillan equation⁵²

$$T_{c} = \frac{\omega_{\log}}{1.2} \exp[-\frac{1.04(1+\lambda)}{\lambda - \mu^{*}(1+0.62\lambda)}],$$
(3)

where coulomb pseudopotential μ^* with 0.10 ~ 0.13 is appropriate for hydrogen-rich compounds. For λ < 1.5, this equation can provide a highly accurate value of T_c . As is listed in Table S7, using the calculated $\lambda = 0.96$ and the logarithmically averaged phonon frequency $\omega_{log} = 973.81$, we predicted the T_c of MgSiH₆ to reach a high value 53~63 K with $\mu^*= 0.10~0.13$ at 250 GPa. The T_c is relatively high

in those reported ternary hydrides.

To explore the dependence of the superconductivity on soft phonon modes, we extend calculations on two aspects. On one hand, we calculated these mode-resolved electron phonon coupling constants $\lambda_{q,v}$ projected on phonon spectra, as depicted in Fig. 5 (a). $\lambda_{q,v}$ is the weight function to evaluate overall EPC parameter λ which can be expressed as

$$\lambda = \sum_{q,\nu} \lambda_{q,\nu} w_{q,\nu}, \tag{4}$$

where q, v are phonon vector and the index of mode, respectively, and $w_{q,v}$ is the weight of each q point in the first Brillouin-zone (BZ). It is clearly seen that $\lambda_{q,v}$ is particularly enhanced in these regions of phonon softening (Fig. 5(a)), suggesting soft phonon modes boost the EPC strength, which explains why the low-frequency provides important contributions to EPC. On the other hand, we performed a calculation on the evolution of superconductivity by simulating Al₂H₆ (AlH₃) to be gradually substituted to MgSiH₆ at 250 GPa. In order to ensure the stability of structure, we used a Si atom to replace an Al atom to form the Pm-3 AlSiH₆. Subsequently, the other Al atom is substituted by Mg atom to form the Pm-3 MgSiH₆. For three high-pressure crystal structure (i.e., Pm-3n Al₂H₆, Pm-3 AlSiH₆ and Pm-3 MgSiH₆) at 250 GPa, they are dynamically stable without displaying any negative frequency (see Fig. S10 and S11). Besides, for Al_2H_6 and $AlSiH_6$, no phonon softening is observed in phonon spectra. Fig. 8(a) shows some crucial parameters involved with superconductivity. The electronic DOS at Fermi level $N(\varepsilon_F)$ of MgSiH₆ (3.91 states/Spin/Ry/cell) is comparable with that of isostructural AlSiH₆ (4.11 states/Spin/Ry/cell). However, owing to these soft phonon modes, the EPC strength of MgSiH₆ ($\lambda = 0.96$) is obvious larger than that of AlSiH₆ ($\lambda = 0.54$). By contrary, soft phonon modes render MgSiH₆ to produce the lower ω_{log} (973.81 K) than those of Al₂H₆ (1301.11 K) and AlSiH₆ (1370.07 K). Therefore, it can be summarized that soft phonon modes synchronously play two opposite role in predicting the superconductivity. On one aspect, phonon softening does boost the EPC strength. However, on the other aspect, these soft phonon modes evidently suppress the ω_{log} . In the Allen-Dynes modified McMillan equation, T_c is the balanced results of λ and ω_{log} . Fig. 8(b) shows the pressure evolution of some important parameters involved with superconductivity of MgSiH₆. It is clearly seen that, as a consequence of pressurization, phonon tends to harden and ω_{log} raises, but EPC parameter λ decreases. The reduction of T_c indicates that the λ dominates the superconductivity. It is very obvious that MgSiH₆ is a phonon-mediated high temperature superconductor and T_c has a weak

dependence on pressure with a coefficient (dT_c/dP) of -0.21 K/GPa.

IV. CONCLUSION

In summary, we performed first-principles calculations to investigate the high-pressure crystal structures and superconductivity of Mg-Si-H system. We put forward a new method to determine the specific synthesis routes of ternary hydrides. This method reveals that the stoichiometric MgSiH₆ can be obtained by two different A+B \rightarrow D formation ways at high pressure: MgH₂+SiH₄ \rightarrow MgSiH₆ and MgSi+3H₂ \rightarrow MgSiH₆. MgSiH₆ exhibits a *Pm*-3 symmetry and primary ionic feature, which was predicted to possess a large EPC parameter and high superconducting transition temperature of 63 K at 250 GPa. Soft phonon modes induced by the Fermi surface nesting have been found to be very effective to enhance the EPC, playing important role in superconductivity. Our work suggests that high temperature superconductivity can be achieved in ternary hydrides under high pressures. The current work could provide helpful and clear guidance for further experimental synthesis for ternary hydrides under high pressure.

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Figures

- FIG.1. (Color online) Trigonal phase diagrams of Mg-Si-H system at 200, 250 and 300 GPa, respectively. Solid symbols denote stable stoichiometries. Four different color lines stand for different synthesis routes for ternary hydrides.
- FIG. 2. (Color online) (a), (b) and (c) the formation enthalpies of Mg-Si-H compounds with respect to decomposition into MgH₂ and SiH₄ at different pressures. (d), (e) and (f) the enthalpies of formation with respect to decomposition into MgSi alloy and H at different pressures. These solid lines stand for the convex hull, and solid symbols locating on convex hull represent stable stoichiometries. Open symbols connected by dashed lines indicate unstable species.
- FIG. 3 (Color online) The enthalpies per formula unit of *R*-3 and *C*2/*m* phases as a function of pressure, referenced to *Pm*-3 phase of MgSiH₆. Illustration: the enthalpies of *R*-3 and *C*2/*m* relative to *Pm*-3 phase with the zero-point motion corrections from 250 to 300 GPa.
- FIG. 4. (Color online) (a), (c), (d) and (e) some perspectives of *Pm*-3 MgSiH₆ at 250 GPa. (a) Crystal structure. The lattices parameters are a = 2.851 Å with H at 6g (0.255, 0.500, 0.00), Mg at 1b (0.500, 0.500, 0.500) and Si at 1a (0.000, 0.000, 0.000). (b) Crystal structure of *Pm*-3n AlH₃.
 (c) The electronic band structure and density of electronic states (DOS) of MgSiH₆. The electron localization function (ELF) of Mg-H (d) and Si-H (e) planes.
- FIG. 5. (Color online) Phonon band structure (a) and projected density of states (PHDOS) (b) of *Pm*-3 MgSiH₆ at 250 GPa. These red solid circles with black borders overlapping with band show mode-resolved electron phonon coupling constants $\lambda_{q,v}$ and the sizes of circles are proportional to EPC strength.
- FIG. 6. (Color online) Some planes for MgSiH₆ at 250 GPa. (a) The calculated nesting function $\xi(Q)$ along some special Q trajectories. The calculation employs 5225 k points and 658350 k+Q points to attain their respective energy eigenvalues. (b) The Eliashberg phonon spectral function $\alpha^2 F(\omega)$ and the electron-phonon integral λ .

- FIG. 7. (Color online) Fermi surface for MgSiH₆ at 250 GPa. (a) Three dimensional (3D) Fermi surface calculated with 60 × 60 × 60 k-mesh. (b) 2D Fermi surface along Γ-X and Γ-M directions calculated with 216000 k points. The solid line represents the boundary of first Brillouin Zone and possible nesting vectors in (b) are indicated by dashed lines.
- FIG. 8. (Color online) (a) EPC parameter (λ) , the phonon frequency logarithmic average (ω_{log}) in kelvin (K), the electronic DOS at Fermi level $N(\varepsilon_F)$ in states/Spin/Ry/cell, and superconducting transition temperature T_c ($\mu^*= 0.1$) in kelvin (K) for Pm-3n Al₂H₆, Pm-3 AlSiH₆ and Pm-3 MgSiH₆ at 250 GPa. (b) The pressure evolution of λ , ω_{log} , $N(\varepsilon_F)$ and T_c ($\mu^*= 0.1$) for MgSiH₆ at selected pressures.









Fig.3













