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Semimetallic "Electride Bands" Derived from Interlayer Electrons in Quasi-Two-Dimensional Electride Y_2C

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Two-dimensional (2D) electrides are a new concept material in which anionic electrons are confined in the interlayer space between positively charged layers. We have carried out angle-resolved photoemission spectroscopy measurements on Y_2C , which is a possible 2D electride, in order to verify the formation of 2D electride states in Y_2C . We clearly observe the existence of semimetallic "electride bands" near the Fermi level, as predicted by *ab initio* calculations, which conclusively demonstrates that Y_2C is a quasi-2D electride with electride bands derived from interlayer anionic electrons.

I. INTRODUCTION

Electrides are ionic crystals in which electrons serve as anions^{1,2}. In actual electride materials, anionic electrons may have not only a localized but also a delocalized character, and move easily from void (cavity) to void because of their small mass and small effective radius^{3,4}. Consequently, electrides exhibit a rich variety of intriguing physical properties originating from the delocalized anionic electrons, which makes the electrides novel engineering materials. The breakthrough discovery of the first room-temperature- and air-stable inorganic electride, $[Ca_{24}Al_{28}O_{64}]^{4+.4e^-}$ (C12A7)^{4,5} has opened up a new avenue in the application of electrides, capitalizing on their low work functions, such as their use as electron injection layers in organic light emitting diodes⁶ and as catalysts for ammonia synthesis^{7,8}.

The electronic properties of electrides are expected to depend critically on the topology and dimensionality of the void space confining the anionic electrons. Thus, electrides have recently attracted considerable attention as a new class of low-dimensional materials. However, for many years after their discovery, all the known electrides were found to be either quasi-zero-dimensional $(\text{electrons confined in cages})^5$ or quasi-one-dimensional (electrons confined in filamentary channels)⁹. A recent study has reported the synthesis of the first possible twodimensional (2D) electride, Ca_2N^{10} , and further, the possible existence of 2D electride states in Ca_2N has been supported by *ab initio* calculations^{10,11}. Subsequently, Inoshita et al. have predicted Y₂C as another possible candidate for 2D electrides¹². These materials have a unique layered structure, as shown schematically in Fig. 1(a): One (two) anionic electron(s) per Ca_2N (Y₂C) unit cell ($[Ca_2N]^+ \cdot e^-$ or $[Y_2C]^{2+} \cdot 2e^-$) is (are) confined in the interlayer space between positively charged $[Ca_2N]^+$ ($[Y_2C]^{2+}$) sheets. Relating to the electronic states, electrides are materials in which some electrons occupy void spaces instead of being specifically attached to atoms: Electron occupies the quantized orbital at the void space rather than the atomic orbital, leading to the formation of void quasiatoms (VQAs)¹³. Thus, the meaning of "2D electrides" is that the orbital of VQAs overlap each other in plane, but hardly do along out-of-plane direction owing to the "ionic" nature between VQA layers and positivelycharged layers^{10–12,14}. Also, the in-plane overlapping of VQA orbitals cause the formation of (semi)metallic "electride bands" near the Fermi level $(E_F)^{10-12,14}$.

The crucial issue in the research of 2D electrides is whether or not the material concept is actually realized in Ca₂N and/or Y₂C. In this context, Lee *et al.* have reported detailed transport measurements of singlecrystalline Ca₂N¹⁰. The realization of the material concept of 2D electrides in Ca₂N is supported by two unique behaviors: very high electron mobility even at very high electron concentrations ($\sim 10^{22}$ cm⁻³) corresponding to that for the assumed formula [Ca₂N]⁺·e⁻, and negative magnetic resistivity under the application of magnetic field along the normal to the confined space. These experimental results are fully consistent with *ab initio* calculations. Subsequent studies have also revealed that Ca₂N is a nearly-2D electride^{10-12,14,15}.

On the other hand, as regards the possible 2D electride Y_2C , transport, x-ray photoemission spectroscopy, and magnetic susceptibility measurements have been carried out only for polycrystalline samples of Y_2C^{16} . However, such experiments can at best be considered as indirect probes of electronic structures, although these results appear to be consistent with *ab initio* calculations. In order to credibly prove that this material is indeed a 2D electride (in which anionic electrons are confined two-

dimensionally in the interlayer space and consequently "electride bands" are formed near E_F), it is necessary to directly probe the electronic band structure.

In this Letter, we provide experimental evidence that Y_2C is indeed a quasi-2D electride having semimetallic band structures by using angle-resolved photoemission spectroscopy (ARPES). As shown in Fig. 1, the existence of mobile anionic electrons in the interlayer space has a one-to-one correspondence with the formation of "electride bands" near E_F as per band-structure calculations. That is, the direct observation of these electride bands near E_F is the direct proof of the realization of the (quasi-) 2D electride states in Y_2C . In the study, we clearly observed that electron and hole electride bands exist near E_F , and that these semimetallic bands form Fermi surfaces (FSs), as predicted by ab *initio* calculations^{12,16}. Furthermore, the observed band structure is in good agreement with the results of ab initio calculations. This agreement between the theoretical and experimental results clearly demonstrates that Y_2C is a quasi-2D electride having semimetallic electride bands crossing E_F .

II. EXPERIMENTAL AND CALCULATION METHODS

Single crystals of Y_2C were grown by the floating zone method under an argon pressure of 0.4 MPa. The details of the growth conditions and characterizations are described elsewhere¹⁷. Since Y_2C is highly reactive with ambient oxygen and water vapor, the samples were affixed to the ARPES holder with a silver conductive epoxy adhesive in a purified Ar-filled glove box and then moved to an ultrahigh vacuum (UHV) chamber for ARPES measurements with the use of a specially designed transfer vessel.

ARPES measurements were carried out using horizontally polarized synchrotron radiation light at the BL-2A MUSASHI beam line of the Photon Factory, KEK. The samples were cleaved in situ under a UHV of $\sim 10^{-8}$ Pa at a low temperature of ~ 20 K. As shown in Fig. 2(a), the low-energy electron diffraction (LEED) pattern exhibits a hexagonal arrangement of spots corresponding to the reciprocal lattice of the $R\overline{3}m$ space group^{18,19}, thus indicating the obtainment of a clean and well-ordered Y₂C surface. For the present ARPES study, soft x rays (SX) with a large probing depth were used to probe the intrinsic electride states because the anionic electron layer is expected to lie buried below the top $[Y_2C]^{2+}$ layer. The sample temperature during the ARPES measurements and the total energy resolution were set to 20 K and 200 meV at a photon energy $(h\nu)$ of around 400 eV, respectively.

We carried out density-functional electronic structure calculations of Y_2C with the generalized gradient approximation (GGA) of the exchange-correlation functionals. Two different methods were employed:

(1) the full-potential linearized augmented plane wave (FLAPW) method, as implemented in the all-electron band structure calculation package $(ABCAP)^{20}$ and (2)the projector augmented wave (PAW) method using a plane wave basis set, as implemented in the Vienna *ab initio* simulation package $(VASP)^{21-24}$. We used the Perdew-Burke-Ernzerhof (PBE)²⁵ and Perdew and Wang $(PW91)^{26}$ GGA potentials for (1) and (2), respectively. In the FLAPW calculations, the cutoff energies were set to 163 eV and 653 eV for the wave functions and charge/potential, respectively, and momentum (k-)integration was carried out in the conventional (hexagonal) Brillouin zone (BZ) using a $12 \times 12 \times 4$ Γ -centered mesh. For the PAW calculations, the plane waves were cut off at 800 eV, and integration over the primitive (rhombohedral) BZ was performed with a $17 \times 17 \times 17$ Γ -centered mesh. The structure was relaxed using the PAW method until the force acting on each ion became less than 0.7 meV/Å. The optimized structure was used for FLAPW calculations. The band structures obtained by the two methods were in excellent agreement with each other.

III. RESULTS AND DISCUSSION

Before discussing the ARPES results, we explain the vital difference in the electronic structures of the two types of electrides, nitrides (Ca₂N) and carbides (Y₂C) in terms of the band-structure calculation. Since the oxidation numbers of Ca and N are +2 and -3, respectively, Ca₂N has one excess electron per unit cell [Ca₂N]⁺·e⁻, which is two-dimensionally confined in the interlayer space and forms a half-filled interlayer (electride) band. As a result of the nearly 2D nature of the anionic electrons confined in the interlayer space, the FS, which is mainly derived from the *metallic* electride band near E_F , is located at the BZ center and is highly cylindrical. That is, Ca₂N is a nearly-2D electride metal^{10-12,14}.

While the oxidation numbers of Y and C (+3 and -4, respectively) indicate that Y_2C has two excess electrons per unit cell $[Y_2C]^{2+} \cdot 2e^-$ and is therefore a band insulator, our *ab initio* calculations reveal that Y_2C is a semimetal: An almost fully occupied hole-like electride band and a slightly occupied electron-like electride band overlap each other near E_F , as shown in Fig. 1(b). Here, the size of the circles in Fig. 1(b) indicates the interlayer probability of the calculated eigenstates, i.e., the probability that the electron is found inside a sphere of radius 1.7 Å at the interstitial site between Y_2C layers. Note the strong interlayer (electride) character of the two semimetallic bands near E_F . The FSs for the two bands are located near the BZ boundary and are shaped as rugged cylinders (not shown), thereby reflecting the rather three-dimensional (3D) nature of the anionic electrons of Y_2C over those of $Ca_2N^{10-12,14,16,27}$. Thus, according to the band-structure calculation, Y₂C is a quasi2D electride^{28–30} having semimetallic band structures.

In order to directly observe the electride band near E_F as evidence of the realization of quasi-2D electride states in Y₂C, we performed ARPES measurements. Figure 2(b) shows an experimental out-of-plane FS obtained by plotting the ARPES intensity at E_F in the ΓZFL plane for varying excitation photon energies. A meandering FS derived from the electron band is clearly observed at the BZ boundary, following the periodicity of the rhombohedral BZ. As can be observed in Fig. 2(b), the overall shape of the observed FS is in excellent agreement with the results of our calculation. The observed strong modulation in the FS along the momentum perpendicular to the surface (k_z) strongly suggests the increased 3D character of the electride states in Y₂C in comparison with those in Ca₂N¹⁰.

The observation of k_z -modulation in the FS indicates that the present SX-ARPES clearly reveals a bulk electronic structure in Y_2C . This means that the large probing depth of the SX-ARPES enables us to examine the buried anionic electrons in the positively charged layer [see Fig. 1(a)]. Therefore, we next measured the in-plane FS at a constant photon energy by varying the emission angle; the corresponding results are shown in Figs. 2(c)and (d). The FS mapping acquired at $h\nu = 400 \text{ eV}$ and 440 eV traces the spherical surface of the k-space through the high-symmetry L and F points [each profile in the ΓZFL plane is shown as an orange line in Fig. 2(b)], respectively. Therefore, these FS maps could be exactly compared with the band-structure calculation only around the L and F points because the FS maps shown in Figs. 2(c) and (d) represent the projections of the spherical surface on the corresponding $k_x - k_y$ plane. The observed electron FSs around the L and F points are in good agreement with the corresponding prediction of the theoretical calculations. On the other hand, the topology of the hole FSs that are predicted to be located around the B1 and Q points are not clearly resolved in the FS maps, probably because of the matrix element effect, although the hole band crossing E_F itself is observed in the ARPES spectra²⁸.

For investigating the electronic structures and their correspondence with the theoretical calculations in detail, we measured the energy-band dispersion along the representative high-symmetry lines. Figures 3(b) and 4(b) show the band dispersions determined by ARPES along the Z-F-Z and B-Z-B directions [along the orange line in the BZ shown in Figs. 3(a) and 4(a)], respectively. It is clear that electron and hole electride bands exist near E_F , leading to the formation of a small electron and hole pockets around the F and B points, which are more clearly seen in the ARPES spectra shown in Figs. 3(c) and 4(c), respectively. According to the calculations, the highly dispersive bands around 1.5–2.5 eV mainly consist of the C 2p orbital, while the dispersive bands in the energy range from near- E_F to around 1 eV are mainly derived from the anionic electrons in the interlayer space. As a result of the considerable

hybridization between the electride band near E_F and Y 4d states above E_F , semimetallic electride bands are formed near E_F . Although there is a quantitative discrepancy between the experiment and calculation around the F points (which we discuss in detail later), the overall band structures observed by ARPES are in good agreement with theoretically predicted band structures. Consequently, these results indicate that Y₂C is most evidently a quasi-2D electride having semimetallic electride bands derived from anionic electrons confined in the interlayer space.

Next, we discuss the possible influence of certain surface states characteristic of electrides. A recent study has reported the observation of metallic band structures in Ca₂N via ARPES using surface-sensitive vacuum ultraviolet light 31 . In this study, the size of the FS determined by ARPES is considerably smaller than that predicted theoretically. Based on their observations, the authors have argued that the reduction in the size of the FS originates from the shift of the chemical potential due to the depletion of anionic electrons on the cleaved surface. In contrast, in the present study, the size of the FS estimated from ARPES, as well as the width of the electride band, are in good agreement with the theoretical predictions, strongly suggesting that the present ARPES using bulk-sensitive SX is nearly free from the influence of the surface states characteristic of electrides. These results suggest that ARPES with a large probing depth is necessary to reveal the intrinsic bulk electronic structures of electrides.

Finally, we discuss the observed quantitative discrepancy in the electride band of Y₂C between the experiment and calculation. The good agreement of the bandwidth between the two strongly suggests that the electronelectron correlation among interlayer electrons is as negligibly weak in Y_2C as in Ca_2N^{31} . Although the overall band structure is well described by the GGA calculation, a slight quantitative discrepancy is observed at the F point: In the experiment, the bottom of the electron band appears to touch the top of the hole band, while the two bands overlap in the calculations. This discrepancy may arise from a somewhat inaccurate positioning of the Y 4d bands by GGA. In fact, GGA+U and hybrid functional (HSE06) calculations (not shown) predict an upward shift of the Y 4d bands when compared with that for GGA, reducing the band overlap at the F point and bringing the theoretical predictions closer to our experimental results.

The semimetallicity in Y₂C, together with hybridization, albeit weak, with the Y 4d bands, results in a rather heavy in-layer effective mass in the vicinity of E_F and a strong peak in the density of states at E_F^{27} . Therefore, this non-trivial band structure may give rise to interesting physical properties. For example, it is predicted that Y₂C is close to a Stoner-type ferromagnetic instability, which is induced by interlayer electrons rather than the *d* electrons of Y²⁷. In fact, the actual value of the magnetic susceptibility is still in question^{16,17} because

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there are strong sample-to-sample variations, which can be attributed to the complex phase diagram of the Y– C system. Considering the unique semimetallic band structure, there is a possibility that the intriguing physical properties of Y₂C originate from the delicate balance between the electron and hole electride bands near E_F . Thus, further investigations of the detailed electronic structures and their relation to the physical properties of Y₂C, as well as other 2D electrides, are required.

In summary, we carried out ARPES measurements on Y_2C to test whether or not it is a 2D electride. We clearly observed semimetallic "electride bands" near E_F via ARPES, as predicted from *ab initio* theoretical calculations. Furthermore, these band dispersions were in good agreement with the results of the calculations. The good agreement between theory and experiment proves that Y_2C is a quasi-2D electride having a semimetallic

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- ¹ J. L. Dye, Science **301**, 607 (2003).
- ² J. L. Dye, Acc. Chem. Res. **42**, 1564 (2009).
- ³ J. L. Dye, Science **247**, 663 (1990).
- ⁴ S. Matsuishi, S. W. Kim, T. Kamiya, M. Hirano, and H. Hosono, J. Phys. Chem. C **112**, 4753 (2008).
- ⁵ S. Matsuishi, Y. Toda, M. Miyakawa, K. Hayashi, T. Kamiya, M. Hirano, I. Tanaka, and H. Hosono, Science **301**, 626 (2003).
- ⁶ K. B. Kim, M. Kikuchi, M. Miyakawa, H. Yanagi, T. Kamiya, M. Hirano, and H. Hosono, J. Phys. Chem. C **111**, 8403 (2007).
- ⁷ M. Kitano, Y. Inoue, Y. Yamazaki, F. Hayashi, S. Kanbara, S. Matsuishi, T. Yokoyama, S. W. Kim, M. Hara, and H. Hosono, Nat. Chem. 4, 934 (2012).
- ⁸ M. Kitano, S. Kanbara, Y. Inoue, N. Kuganathan, P. V. Sushko, T. Yokoyama, M. Hara, and H. Hosono, Nat. Commun. 6, 6731 (2015).
- ⁹ A. S. Ichimura and J. L. Dye, J. Am. Chem. Soc. **124**, 1170 (2002).
- ¹⁰ K. Lee, S. W. Kim, Y. Toda, S. Matsuishi, and H. Hosono, Nature **494**, 336 (2013).
- ¹¹ A. Walsh and D. O. Scanlon, J. Mater. Chem. C 1, 3525 (2013).
- ¹² T. Inoshita, S. Jeong, N. Hamada, and H. Hosono, Phys. Rev. X 4, 031023 (2014).
- ¹³ M.-S. Miao and R. Hoffmann, J. Am. Chem. Soc. **137**, 3631 (2015).
- ¹⁴ T. Tada, S. Takemoto, S. Matsuishi, and H. Hosono, Inorg. Chem. 53, 10347 (2014).
- ¹⁵ C. M. Fang, G. A. de Wijs, R. A. de Groot, H. T. Hintzen, and G. de With, Chem. Mater. **12**, 1847 (2000).
- ¹⁶ X. Zhang, Z. Xiao, H. Lei, Y. Toda, S. Matsuishi, T. Kamiya, S. Ueda, and H. Hosono, Chem. Mater. 26, 6638 (2014).
- ¹⁷ S. Otani, K. Hirata, Y. Adachi, and N. Ohashi, J. Cryst. Growth **454**, 15 (2016).
- ¹⁸ M. Atoji and M. Kikuchi, J. Chem. Phys. **51**, 3863 (1969).
- ¹⁹ J. P. Maehlen, V. A. Yartys, and B. C. Hauback, J. Alloy. Compd. **351**, 151 (2003).

band structure.

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- ²⁰ N. Hamada, K. Terakura, and A. Yanase, J. Phys. F **14**, 2371 (1984); A. Yanase and N. Hamada, J. Phys. Soc. Jpn. **68**, 1607 (1999).
- ²¹ G. Kresse and J. Furthmüller, Phys. Rev. B 54, 11169 (1996).
- ²² G. Kresse and J. Furthmüller, Comput. Mater. Sci. 6, 15 (1996).
- ²³ P. E. Blöchl, Phys. Rev. B **50**, 17953 (1994).
- ²⁴ G. Kresse and D. Joubert, Phys. Rev. B 59, 1758 (1999).
 ²⁵ J. P. Perdew, K. Burke, and M. Ernzerhof, Phys. Rev. Lett. 77, 3865 (1996).
- ²⁶ J. P. Perdew, J. A. Chevary, S. H. Vosko, K. A. Jackson, M. R. Pederson, D. J. Singh, and C. Fiolhais, Phys. Rev. B 46, 6671 (1992).
- ²⁷ T. Inoshita, N. Hamada, and H. Hosono, Phys. Rev. B **92**, 201109(R) (2015).
- ²⁸ See Supplemental Material at [url] for the definition of "quasi-2D" band structures, more detail about FS mapping results for the hole band, and momentum distribution curves for the determination of k_F points.
- ²⁹ G. Grüner, *Density waves in solids* (Perseus publishing, Cambridge, 1994).
- ³⁰ H. P. Hughes and H. I. Starnberg, *Electron Spectroscopies Applied to Low-dimensional Structures* (Kluwer Academic Publishers, Dordrecht, 2000).
- ³¹ J. S. Oh, C.-J. Kang, Y. J. Kim, S. Sinn, M. Han, Y. J. Chang, B.-G. Park, S. W. Kim, B. I. Min, H.-D. Kim, and T. W. Noh, J. Am. Chem. Soc. **138**, 2496 (2016).

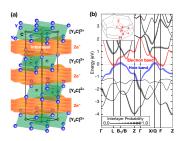


FIG. 1. (a) Crystal structure of Y_2C together with the schematic of the anionic electron layer. Solid thick lines represent the conventional hexagonal unit cell of rhombohedral Y_2C . Ab initio calculations predict that anionic electrons $2e^-$ are confined in the interlayer space between the $[Y_2C]^{2+}$ sheets. (b) Band structure of Y_2C calculated by the PAW method. The interlayer probability, i.e., the probability of the electron being found in the interlayer space, is represented by the size of the filled circles. Semimetallic "electride bands" are formed near E_F . The inset shows the BZ for the rhombohedral lattice of Y_2C together with the symmetry points.



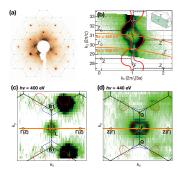


FIG. 2. (a) LEED pattern for a cleaved surface of Y_2C single crystal acquired at an electron energy of 124 eV. Dotted lines represent the hexagonal surface BZ. (b) Out-of-plane FS map in the ΓZFL plane obtained by varying the excitation photon energy from 380 eV to 500 eV. The FS map was obtained by plotting the ARPES intensity within the energy window of ± 100 meV from E_F . The dotted lines indicate the BZ boundaries, while red solid lines indicate the electron FS obtained by FLAPW calculations. The orange lines represent the k-path passing through the L point (at a photon energy of 400 eV) and the F point (at a photon energy of 440 eV). (c), (d) In-plane FS maps acquired at constant photon energies of 400 eV (c) and 440 eV (d) by changing emission angles. Calculated FSs at in-plane $(k_x - k_y \text{ plane})$ crossing the L point $(k_z = 29.5 \ [2\pi/c])$ and the F point $(k_z = 31.0 \ [2\pi/c])$ are superimposed on (c) and (d), respectively. Red and blue lines show electron and hole pockets, respectively.

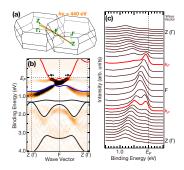


FIG. 3. (a) Measured \mathbf{k} -path passing through the F point in the rhombohedral BZ for which ARPES measurements were carried out at $h\nu = 440$ eV, which corresponds to the orange line in Fig. 2(d). (b) Experimental band structure obtained by plotting the second derivative of the ARPES spectra acquired along the \mathbf{k} -path in (a). The energy bands along the Z-F-Zdirection calculated by the FLAPW method are superimposed by solid lines. Filled triangles indicate the Fermi momentum (k_F) determined by ARPES spectra²⁸. (c) ARPES spectra near E_F and around the F point. Thick red lines indicate the ARPES spectra at k_F .

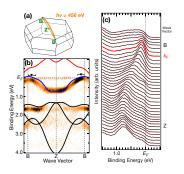


FIG. 4. (a) Measured **k**-path passing through the *B* point of the rhombohedral BZ for which ARPES measurements were carried out at $h\nu = 456$ eV. (b) Experimental band structures obtained by plotting the second derivative of ARPES spectra. Solid lines indicate the energy bands calculated by the FLAPW method along the B-Z-B direction. Filled triangles indicate the k_F points determined by ARPES spectra²⁸. (c) ARPES spectra near E_F and around the *B* point. The thick red line indicates the ARPES spectrum at k_F .