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Energy confinement and thermal boundary conductance effects on short-pulsed thermal ablation thresholds in thin films

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For this work, single-pulse ablation mechanisms of ultra-fast laser pulses (25 ps) were studied for thin gold films (65 nm) on an array of substrates with varying physical properties. Using time-domain thermoreflectance (TDTR), the interfacial properties of the thin film systems are measured; in particular, the thermal boundary conductance. We find that a often used, and widely accepted equation describing threshold fluences of homogeneous bulk targets breaks down at the nanoscale. Rather than relying solely on the properties of the ablated Au film, the ablation threshold of these Au/substrate systems is found to be dependent on the measured thermal boundary conductance; we additionally find no discernible trend between the damage threshold and properties of the underlying substrate. These results are discussed in terms of diffusive thermal transport and the interfacial bond strength.

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I. INTRODUCTION

Ablation, from a thermodynamic standpoint, is the pro-20 cess of evaporative material removal when a critical temper-21 ature is reached. However, laser-induced ablation has be-55 22 come a general term referencing any laser-induced mass re- 56 23 moval, with expected ejection mechanisms ranging from non-57 24 thermal, photomechanical spallation [1-3] to a thermally-58 25 driven vaporization process [4, 5]. This mixture of mecha-59 26 nisms and definitions has clouded the current understanding of 60 27 the basic heat transport processes that drive material ablation 61 28 [1, 3, 6], especially when considering thin films and nanocom-29 posites. On the nanoscale, the high densities of inclusions, de-63 30 fects and interfaces can lead to thermal transport properties in 64 31 materials that can be drastically varying from those intrinsic 65 32 to their respective bulk phases [7, 8]. Thus, an understanding ₆₆ 33 of the heat transport processes that drive material ablation in 67 34 nanosystems is lacking; this lack of understanding is ampli-35 fied by the aforementioned ambiguities in the role of diffusive 69 36 thermal transport and thermal resistance in bulk materials dur-70 37 ing laser ablation. 38 71

Diffusive heat transport generally drives ablation processes 72 39 in materials when the characteristic energy deposition time 73 40 (i.e., pulse width, t_p) is much greater than the electron-phonon 74 41 equilibration time (τ_{ep}) [1]. In this temporal regime, the elec- 75 42 trons and lattice are in equilibrium during the majority of the 76 43 laser pulse absorption; thus, the assumption of $T_e \sim T_i$ is valid, 77 44 45 where T_e is the electron temperature and T_i is the ion tempera-78 ture. In this "thermal ablation" regime [1], thermal expansion 79 46 limits the ablation threshold, hence defining the condition that 80 47 the absorbed laser energy must be fully converted into the en- 81 48 ergy of the broken bonds in some thickness defined by a ther- 82 49 mal penetration depth of the pulse ($\delta_T = (\alpha t_p)^{1/2}$, where α is α 50 the thermal diffusivity). In this regime, the thermal ablation 84 51 threshold, which determines the onset of the material removal 85 52 process, follows the well known $\sqrt{t_p}$ pulse width dependence 86 53

$$F_T \approx \frac{(\alpha t_p)^{1/2} \varepsilon_b n_a}{A},\tag{1}$$

where ε_b is the atomic binding energy, n_a is the number density of atoms in the target, and A is the absorptivity of the material.

The threshold fluence given in Eq. 1 is derived by performing a basic energy balance with the absorbed laser pulse and the heat equation used to describe diffusive thermal transport in a homogeneous material [1]. This threshold applied to thin films and nanosystems is thus questionable, as previously mentioned, the heterogeneity induced from interfaces and inclusions can lead to thermal transport properties to be vastly different from that of the homogeneous bulk phase [7, 8]. For example, when film thickness approaches δ_T , interfaces and boundaries adjacent to these thin films can pose significant thermal resistance that impede heat flow out of locally heated volumes in thin films. Indeed, this finite thermal boundary conductance, $h_{\rm K}$, can represent a limiting thermal resistance in a wide array of thin films and nanosystems [10-13]. Furthermore, for thermal ablation conditions (i.e., when $t_p >> \tau_{ep}$, as previously mentioned), thermal diffusion could be dominated by the thermal boundary conductance as opposed to the thermal properties of the film or substrate. For example, characteristic time scales associated with the interfacial temperature drop [14] driven by $h_{\rm K}$ are estimated as $\tau_{\rm int} = Cd/h_{\rm K}$, where C and d are the heat capacity and film thickness of the thin film material [15]. For a homogeneously heated Au film where $d \approx 100$ nm (the ballistic penetration depth of electrons after laser irradiation in Au is ~ 100 nm) [16], the time scale necessary for complete diffusion of energy across an Au film on a substrate is ~ 5 ns, assuming $h_{\rm K}$ is ~ 50 MW m⁻² K⁻¹ [17– 19]. Thus in the regime where this timescale is two orders of magnitude greater than laser deposition time (e.g., when using picosecond pulses), the thermal energy deposited by the laser

pulse would be intially confined in the volume of the film.139 87 As thermal ablation processes occur up to nanosecond times140 88 scales [20] and are greatly affected by the ablated material's141 89 temperature [6], energy diffusion, limited by the interfacial₁₄₂ 90 thermal resistance, would be expected to play a role in such₁₄₃ 91 processes in thin films. 144 92

To the best of our knowledge, this effect of thermal confine-145 93 ment during thermal ablation conditions has never been exper-94 imentally and systematically investigated, leaving a large void 95 in the understanding of how Eq. 1 applies to thin film sys-146 96 tems for predicting ablation thresholds. Qualitatively, in this 97 temporal regime where the deposited laser energy is confined147 98 in the thin films due to a thermal boundary resistance at the148 99 film/substrate interface, it would be expected that lower ap-149 100 plied fluences would be necessary for ablation to occur, as less150 101 energy from the absorbed laser pulse is necessary for equiva-151 102 lent power densities in a thin films compared to its bulk coun-152 103 terpart. Thus, in this regime with increasing interface conduc-153 104 tances, thermal energy is better coupled to the substrate, and¹⁵⁴ 105 the ablation threshold should correspondingly increase. 155 106

An additional consideration in applying Eq. 1 to thin films¹⁵⁶ 107 lies in the binding energy terms, ε_b , as the interatomic cohe-157 108 sion forces of a pure material are not the only forces present in158 109 the thin film on substrate system. This is evident throughout¹⁵⁹ 110 literature [21–23] for laser ablation in liquids; the overlying¹⁶⁰ 111 liquid layer mechanically confines the system and becomes161 112 an additional force that the spalled material must overcome,162 113

thus leading to an increase in the relative ablation threshold 114 for that material. In this context, for thin films, the binding 115 energy term must also be related to the interfacial bonding en-116 vironment between the film and the substrate as the film must 117 overcome the work of adhesion at this interface. Note, this in-163 118 terfacial bond strength can be intimately related to the thermal₁₆₄ 119 boundary conductance across solid/solid interfaces [10, 24-165 120 291. 121

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This work seeks to elucidate the role of diffusive thermal₁₆₇ 122 transport mechanisms during short-pulse laser ablation of thin₁₆₈ 123 films. When the film thickness approaches the length and time₁₆₉ 124 scales associated with energy diffusion, thermal boundary re-170 125 sistances are expected to influence the ablation threshold of_{171} 126 a material. In this work, we experimentally demonstrate the₁₇₂ 127 failure of Eq. 1 for predicting the ablation threshold for thin₁₇₃ 128 films. By obtaining the ablation threshold of gold thin films₁₇₄ 129 deposited on various substrates with varying thermal bound-175 130 ary conductances across the Au/substrate interfaces, we find₁₇₆</sub> 131 that the thermal confinement within the film controls both the₁₇₇ 132 damage threshold and the heat-affected zone. 133 178

II. METHODS

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II.A Sample fabrication

We conducted the thermal ablation threshold and thermal185 136 boundary conductance measurements on 65 nm Au films on₁₈₆ 137 different substrates with varying interfacial resistances. The187 138

Au films were electron-beam deposited on fused silica (SiO_2) , silicon, nickel, titanium, sapphire (Al₂O₃, and copper substrates; all substrates were purchased from MTI corporation. Prior to deposition, the substrates are rinsed with acetone, ethanol, and methanol then subsequently dried with nitrogen gas. Note, no efforts to remove native oxides on certain substrates were undertaken.

II.B. Picosecond laser ablation

The single-pulse ablation threshold experiments utilized a 25 picosecond Nd:YAG laser operating at its fundamental wavelength of 1064 nm as shown in Fig. 1a. The beam size is experimentally determined with the knife-edge method for both air and liquid environments. We also use the beam waist, ω_0 , as a fitting parameter during threshold measurements for confirmation of the spot size at the target surface; the two methods are in good agreement for bulk targets. In the case of our thin films, as discussed in detail later, we find that the bestfit value for the beam-waist increases with increasing thermal boundary conductance. This phenomenon is attributed to inplane thermal diffusion during the ablation process. The thermal ablation threshold for these 25 picosecond pulses is determined in each Au/substrate system by measuring the induced damage area as a function of incident laser fluence. The results are then fit to [30]

$$D^2 = 2\omega_0^2 ln(\frac{F}{F_{\rm th}}) \tag{2}$$

where both ω_0 , the beam waist, and F_{th} , the ablation threshold are used as free parameters to the best-fit, while D is the diameter of the ablation area and F is the applied fluence and are experimentally measured. The ablation measurements were performed in both air and water environments; in the liquid environment, the target was submerged in 15 mm of pure DDI water utilizing a flow cell, as described in [22, 31], to avoid scattering with pre-existing nanoparticles. The subsequent damage area was measured using dark-field optical microscopy which matches the damage areas measured via scanning electron microscopy. This method of measuring damage areas has been shown to provide similar and accurate results to other methods of determining damage and ablation thresholds [32]. It should be noted that our ablation 'crater' depth is limited to the thickness of our films and there is no visible damage to the substrates in values used for the threshold measurements; we emphasize the lack of visible damage to the substrate in our measurements, as there may be underlying microstructure alteration and formation of defects not observable in our microscopy characterization. Further, we find redeposition of ablated material on the substrate surface, indicitive of droplet formation. This finding implies that at least one mechanism leading to thermal ablation in this work is phase explosion; the possibility of this phase-transformation occurring simultaneous to other ejection processes is discussed later.



Figure 1. a) A schematic of the experimental set-up for the ablation threshold experiments. The Au/substrate sample is placed in a liquid cell for threshold measurements in water. b) A schematic of the experimental set-up for our TDTR measurements. c) A schematic of the computational domain representing a thin film (red and yellow atoms) on a substrate (blue atoms) described by the Lennard-Jones potential.

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III.C. Time-domain thermoreflectance

For measurement of the interfacial thermal resistance, we²²⁵ 189 utilize a two-color TDTR scheme, as described in more de-226 190 tail elsewhere [33-35] and graphically depicted in Fig. 1b.Our²²⁷ 191 TDTR system is centered around a Spectra Physics Tsunami²²⁸ 192 Ti:Sapphire oscillator, emanating ~90 fs, 800 nm (center²²⁹ 193 wavelength with 10.5 nm bandwidth) pulses at an 80 MHz²³⁰ 194 repetition rate. The output of the oscillator is split into pump²³¹ 195 and probe paths. The pump, after passing through an electro-232 196 optical modulator and a second-harmonic generation crystal,233 197 is converted to a modulated pulse train of 400 nm pulses;²³⁴ 198 in this work, we modulate the pump train at 8.8 MHz. The²³⁵ 199 probe pulses are mechanically delayed to known time inter-236 200 vals relative to the pump pulse. We monitor the in-phase²³⁷ 201 and out-of-phase voltages from the reflected probe pulses at²³⁸ 202 the frequency of the pump modulation frequency with a lock-239 203 in-amplifier. These lock-in signals are related to the surface²⁴⁰ 204 temperature of the Au film, and are related to the thermal₂₄₁ 205 properties of the samples, including the Au/substrate thermal₂₄₂ 206 boundary conductance [15, 36–38]. The in-phase data is fit₂₄₃ 207 208 to a thermal model where the thermal boundary conductance₂₄₄ is our free parameter [33, 39, 40]; the thermal conductivity of_{245} 209 the film and substrate are obtained from literature values [41-246 210 43] and the film thicknesses are determined from profilometry₂₄₇ 211 measurements. The measured thermal boundary conductance₂₄₈ 212 and associated error is obtained from measuring five spots on₂₄₉ 213 the film. 214 250

II.D. Molecular dynamics simulations

To explore the nanoscopic mechanisms responsible for²⁵⁵ dictating thin film damage, we perform molecular dynam-²⁵⁶ ics (MD) simulations on representative thin films with vary-²⁵⁷ ing boundary conditions with the region defined by substrate²⁵⁸ atoms. For our MD simulations, we employ the widely₂₅₉ used 6-12 Lennard Jones (LJ) potential, $U(r) = 4\varepsilon[(\sigma/r)^{12} - _{260}$ $(\sigma/r)^6]$, where U is the interatomic potential, r is the inter-₂₆₁ atomic separation, and σ and ε are the LJ length and energy parameters, respectively. The cutoff distance is set to 2.5σ (for computational efficiency) with the time step for all simulations set to 0.1 fs. As we are interested in understanding the effects of TBC on the damage area in thin films in general, the use of LJ potential is sufficient to provide qualitative insight. For the thin films, the length and energy parameters are modeled for argon with σ_s =3.405 Å and ε_s =10.3 meV and the atoms are placed in an fcc structure with a lattice constant of $a_0=1.56\sigma$. The substrate atoms are also placed in an fcc lattice with the same lattice constant, and the energy and length parameters are set to σ_s =3.405 Å and ε_s =10.3 meV, respectively. To mimic a weakly bonded interface, the film-substrate energy parameter is set to $\varepsilon_{f-s}=2.6$ meV, whereas, for the strongly bonded interface, $\varepsilon_{f-s}=10.3$ meV. The sizes of the computational domains are $30a_0 \times 30a_0 \times 20a_0$ with periodic boundary conditions applied in all directions. The mass for all atoms is set to 40 g mol⁻¹.

Initially the computational domains are equilibrated under the Nose-Hoover thermostat [44], and the number of atoms, volume and temperature of the simulation are held constant followed by the NPT integration, which is the isothermalisobaric ensemble with the number of particles, pressure and temperature of the system held constant for a total of 1.5 ns at 0 bar pressure and 70 K temperature. To melt a region of the thin film, we heat the atoms contained in a cylindrical area in the center of the thin film at a temperature of 300 K (under the NVT ensemble, with the number of particles, volume and temperature held constant) for a total of 1 ns after equilibration, while the NVT integration at a temperature of 70 K is simultaneously applied to the rest of the computational domain; note, the melting temperature of LJ argon is 87 K [45]. A schematic of the computational domain is shown in Fig. 1c, where the red atoms represent the thin film, the yellow atoms represent the melted region in the thin film and the blue atoms represent the substrate.

After we melt the cylindrical region in the thin film, the atoms in the thin film region are allowed to equilibrate under the NVE integration, which is the microcanonical ensemble

with the number of atoms, volume and the energy held con-262 stant, while the substrate atoms are simulated under the NVT 263 integration. We monitor the melted regions of the computa-264 tional domains with the varying boundary conditions between 265 the film and the substrate atoms to shine more light on the 266 influence of the different mechanisms that dictate diffusive 267 damage of thin films. The results of these simulations are dis-268 cussed in detail in the following section. 269

III. RESULTS AND DISCUSSION

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Figure 2a shows the measured thermal ablation threshold 271 values for the various Au films as a function of substrate ther-272 mal conductivity. The lack of substrate dependence suggests 273 that the thermal properties of the substrate are not primary 274 factors dictating the different ablation thresholds in the thin 275 Au films; note, we find a similar lack-of-trend is found in 276 the thermal ablation threshold as a function of substrate ef-277 fusivity. Furthermore, even if a general monotonic decrease 278 trend could be gleaned from Fig. 2a, these data would suggest 279 that the faster in which heat is being transferred away from 280 the heat-affected zone and into the bulk of the substrate heat 281 sink, the lower the ablation threshold, which is counterintu-282 itive from a simple energy balance argument. This suggests 283 another energy diffusion mechanism must be limiting the ab-284 lation threshold in these films on substrate systems. 285

As we discussed previously, due to the typical times scales 286 of thermal diffusion, we hypothesize that the thermal bound-287 ary conductance, $h_{\rm K}$, at the Au/substrate interface imposes 288 the limiting resistance that will dictate thermal ablation of the 289 Au films under these conditions. We plot the thermal abla-290 tion threshold in ambient conditions as a function of mea-291 sured $h_{\rm K}$ for the various Au/substrate interfaces in Fig. 2b. 292 We find that the ablation threshold of these systems scales 293 linearly with their respective thermal boundary conductances 294 as shown in Fig. 2b, supporting our hypothesis that $h_{\rm K}$ at 295 the film/substrate interface can influence the thermal abla-296 tion threshold more directly than the substrate thermal proper-297 ties. The measured thermal boundary conductances agree well 298 with previously reported values for various Au/substrate inter-299 faces [17–19, 27, 35]. The thermal boundary conductance is³¹⁵ 300 a diffusive thermal resistance that is well known to impact the³¹⁶ 301 overall heat transport in thin films and nanosystems. Thus, our317 302 data suggest that thermal ablation thresholds in this picosec-318 303

ond regime are related to the heat transport mechanisms that³¹⁹
 underpin the diffusive thermal resistance at the film/substrate³²⁰
 interface.

In the "bulk" limit of ablation thresholds, previous exper-322 307 imental [22] and computational [1] works have determined₃₂₃ 308 threshold values for bulk Au targets through numerous meth-324 309 ods, with reasonable agreement at 0.210 J cm⁻² and 0.245₃₂₅ 310 J cm⁻², respectively, in ambient conditions; the experimen-326 311 tal value was reported as slightly lower than theory due to a327 312 roughened surface, leading to an enhancement in photon ab-328 313 sorption [22, 46]. Under these circumstances, Eq. 1 is valid₃₂₉ 314





0.5

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a)

Figure 2. a) Measured ablation thresholds of Au films as a function of the associated substrate's thermal conductivity. b) The thermal ablation thresholds as a function of the measured thermal boundary conductance between Au films and the labeled substrates. The gray bar represents range of previously reported values for the 'bulk' ablation threshold of Au in air [1, 22].

as only the properties of a pure substance must be considered (in particular, a constant thermal diffusivity and cohesion energy can be assumed). Thus, in the limit where interfacial resistances are large and thus confine thermal energy to the volume of the thin film, the ablation threshold approaches the previously measured bulk damage threshold.

The primary mechanisms driving laser ablation of thin films is typically discussed in terms of delamination and ejection of condensed material due to thermo-mechanical effects at the interface [47, 48]. Though, even in the case of laser-induced forward transfer (LIFT), previous experimental works using picosecond pulses have shown the process to follow melting dynamics in fashion similar to that of nanosecond melting of thin films [49]. Furthermore, as shown by numerous computational works, at higher fluences, phase explosion (or

an analogous phase-transformation such as explosive boiling, 330 whereby the material is transformed into a metastable liquid 331 state) occurs and is the primary mechanism for material ejec-332 tion [23, 50, 51]; a mechanism occurring independent of the 333 ablated materials thickness. As our threshold measurements 334 are derived from a fit to Liu's equation over a large span of ap-335 plied fluences, it is likely that a complex mix of these dynam-336 ics occurs within the heated volume simultaneously, poten-337 tially dependent on fluence. This is further supported by two 338 observations of the damaged region: Redeposition of ablated 339 material and delamination of the surrounding film. Droplet 340 formation during ablation, a consequence of explosive boil-341 ing or phase explosion, is known to lead to redeposition of 342 such droplets on the target surface, which we observe in our 343 microscopy images. Furthermore, we find delamination out-344 side the area in which material is ejected, indicating that a 345 thermomechanical mechanism occurs simultaneous to phase 346 explosion. Nonetheless, regardless of mechanism, as Eq. 1 347 is derived from a basic energy balance, the binding term, ε_b , 348 references the energy necessary to overcome some adhesive 349 force. Typically, this term implicitly references the binding 350 energy between two atoms within a material (i.e., atomic dis-351 integration). In a thin film system, the interfacial atoms have 352 some adhesive force between the film and substrate, which 353 can be overcome. During a gas-phase transformation, these 354 interfacial atoms would play less of a role, making the bind-386 355 ing energy a more negligible term, as the disintegration en-387 356 ergy in the bulk of the film would be the dominant adhe-388 357 sive force to be overcome for the material's ablation thresh-389 358 old. This does not imply the interface is to be neglected;390 359 should heat be efficiently dissipated into the substrate, the Au³⁹¹ 360 film could rapidly drop below the temperature necessary for³⁹² 361 the phase-transformation, and remain adhered in condensed³⁹³ 362 phase. On the contrary, should mechanical spallation be the³⁹⁴ 363 primary ejection mechanism, one would expect the interfacial395 364 adhesion to be the dominating term, as it is the weakest en-396 365 ergy to overcome, and the bulk of the film would spall once397 366 reached. As discussed later, the measured value of thermal³⁹⁸ 367 boundary conductance is known to be related to both phonon³⁹⁹ 368 mismatch at the interface as well as interfacial bonding. Thus,400 369 the TBC reflects both dissipation rate and adhesion of the film.401 370 To study this hypothesis in more detail, we repeat the abla-402 371

tion threshold experiments on the same Au/substrate systems403 372 while submerged in 15 mm of DI water, as depicted by the⁴⁰⁴ 373 open circles in Fig. 3. The thermal ablation thresholds are405 374 higher for the Au films when submerged in liquid as compared406 375 to the air experiments, but only for the Au/substrate systems407 376 with the highest $h_{\rm K}$'s; in other words, as the thermal boundary₄₀₈ 377 conductance is lowered (resistance is increased), the presence409 378 of the liquid on the Au has a reduced effect. In the limit of₄₁₀ 379 Au/Si (lowest $h_{\rm K}$), the liquid layer does not affect the abla-411 380 tion threshold. This further supports our discussion regard-412 381 ing diffusive heat transport across the nanoscale interfaces as413 382 the underlying mechanisms affecting thermal ablation. The414 383 addition of the liquid layer, and resulting Au/water interface415 384 conductance, creates an additional parallel path for thermal₄₁₆ 385



Figure 3. Ablation thresholds against the thermal boundary conductance in air (black squares) and liquid (open circles) environments, where the Au/liquid interface is assumed to have a thermal boundary conductance of 50 ± 30 MW m⁻² K⁻¹; as the liquid provides a parallel path for thermal transport, the Au/water interfacial conductance can be summed with the measured Au/substrate interface.

transport out of the Au film. In Fig. 3, an additional thermal boundary conductance of 50 \pm 30 MW m $^{-2}$ K $^{-1}$ is assumed for the Au/liquid interface [40, 52, 53]. As can be seen, the lower values for $h_{\rm K}$ (higher resistances at the Au/substrate interface), such as Au/Si, the additional thermal pathway is not large enough to drastically affect this threshold, and it does not deviate far from the theoretical minimum value found in previous literature [22]. Though the nominal value of ablation threshold for Au on Si substrates appears independent of environment, the large error associated with both the measured threshold and previous measurements of thermal boundary conductance at a solid/water interface leaves the possibility of it being within the linear range found in the solid/solid interfacial conductances. Additionally, although they can not be accounted for in error bars, phenomena leading to damage outside of thermal effects should be considered during ablation in a liquid environment. For example, cavitation and plasma confinement are hypothesized to lead to secondary erosion effects during laser ablation in liquids [22].

Furthermore, given the relatively modest increase in pressure with the addition of water on the Au surface (~150 Pa), we do not believe this change in thermal ablation threshold upon liquid submersion is due to an increase in mechanical confinement from the additional pressure. While an increase in ablation threshold has been observed during laser ablation in liquids [22, 50] due to mechanical confinement of the spalled material, previous work by Losego *et al.* [27] has shown that pressures on the order of MPa are necessary for spallation to occur for 80 nm Au films. This suggests orders of magnitude more pressure from the liquid addition would be necessary to impact the thermal ablation threshold if the liquid ⁴¹⁷ was mechanically confining the thermally excited Au.

As an additional experiment to support our assertion that 418 the thermal boundary conductance at the Au/substrate inter-419 face is the limiting factor impacting thermal ablation thresh-420 olds, we considered the measured damage area of the Au films 421 on the different substrates, as shown in Fig. 4. The dam-422 age area trends inversely to thermal boundary conductance 423 (i.e., higher damage areas for the Au/substrate samples with 424 lower $h_{\rm K}$ at a set fluence). In the time scale of the diffu-425 sive damage (i.e., nanoseconds [54]), competing thermal dif-426 fusion processes are occurring, namely, diffusion across the 427 Au/substrate interface and in-plane thermal diffusion in the 428 Au film. A reduction in thermal boundary conductance pro-429 motes increased in-plane diffusion of the deposited energy, 430 which leads to an increase in damaged area. This hypoth-431 esis is further supported by the increasing best-fit value of 432 the beam waist, ω_0 , with increasing thermal boundary con-433 ductance as shown in Fig. 4. As Eq. 2 is derived for one-434 dimensional transport, a fitted value larger than the experi-435 mental beam-waist would be expected should lateral transport 436 begin to play a substantial role in the ablation process. In the 437 original derivation of Eq. 2, Liu found sound agreement be-438 tween the measured area of a laser-induced amorphous region 439 and the incident laser-energy profile, indicating negligible lat-440 eral thermal transport during picosecond-laser-induced phase₄₇₃ 441 transformations [30]. As we find the beam waist in his inter- $_{474}$ 442 polation model to deviate from the experimentally-measured₄₇₅ 443 beam waist, which is held constant during the ablation ex_{-476} 444 periments, this further supports our posit regarding a thermal₄₇₇ 445 boundary conductance-limiting thermal ablation threshold in₄₇₈ 446 these films. For example, at a set fluence, one would expect₄₇₉ 447 that a larger beam waist results in a lower effective fluence,480 448 thus decreasing the damage area at a constant incident power;481 449 this is equivalent to a constant beam waist with power dissi-482 450 pated from the thin film to a supporting substrate due to en-483 451 hanced cross-plane thermal transport. 452 484

Given this, it is evident that Eq. 1 cannot accurately be ap-485 453 plied to nanosystems and thin films without modification of₄₈₆ 454 various terms; the threshold is very clearly dependent on the₄₈₇ 455 thermal boundary conductance present at the film interface.488 456 Thus, we turn our discussion now to the underlying nanoscale489 457 heat transport mechanisms that are impacting thermal ablation490 458 of thin films, which will lead to the necessary understanding491 459 required for future studies to derive thin film equivalents of₄₉₂ 460 Eq. 1. Thermal transport across a thin film and its underly-493 461 ing substrate, and hence the measured $h_{\rm K}$, can be influenced₄₉₄ 462 by numerous factors, which has been reviewed in detail in495 463 previous works [10, 12]. Most notably in relation to our ther-496 464 mal ablation data, we focus on the following three factors that₄₉₇ 465 can drive changes in thermal boundary conductance: i) lattice₄₉₈ 466 temperature, ii) phonon spectrum mismatch and iii) interfacial₄₉₉ 467 bonding. 468

i) Temperature: Assuming elastic phonon scattering at the₅₀₁
 Au/substrate interface [55–59], the phonon thermal bound-₅₀₂
 ary conductance from the Au film to the substrate will follow₅₀₃
 temperature trends similar to that of the lattice heat capac-₅₀₄



Figure 4. Observed damage areas of each Au/substrate system at a fluence of ~ 0.94 J cm⁻² and the beam-waist value obtained from fitting to Eq. 2. With increasing thermal resistance at the interface, there is an increase in in-plane thermal diffusion, leading to larger damage areas and deviation of Liu's interpolation model [30].

ity of Au. In other words, the thermal boundary conductance will be relatively constant above the Debye temperature of Au $(\sim 165 \text{ K})$. Due to the relatively weak mechanical bond at the Au/substrate interface (especially given the fact that we make no effort to remove native oxides on some of the substrates) [18, 27, 35], we do not expect inelastic processes to dominate the measured $h_{\rm K}$ across these interfaces [26, 60]. Furthermore, on these thermal ablation time scales, we do not expect hot electron-interface or substrate coupling to play a role, as the time scale for this excited electron-phonon processes has been shown to only influence heat transport within a few picoseconds after laser heating [35, 61-63]. Along these lines, previous works have shown that after electron-phonon equilibration following pulse excitation, which takes place within a few picoseconds in Au, the thermal boundary conductance is dominated solely by phonon interaction between the film and substrate [35, 59, 64]. Thus, even though these thermal boundary conductance measurements have not been extended to the high-temperature regime representative of when thermal ablation occurs, it is unlikely the trend in $h_{\rm K}$ vs. substrate would shift. Therefore, we surmise that the trends in $h_{\rm K}$ shown in Fig. 2 to be representative of the phonon resistance mechanisms influencing thermal ablation. To understand the underlying phonon coupling that influences our measured thermal ablation thresholds, we now focus our discussion on the role of phonon spectrum mismatch and interfacial bonding effects.

ii) Phonon spectrum mismatch: To a decent first approximation, the phonon energy transmission across solid interfaces can be related to the spectral overlap of the phonon densities of states between the film and substrate [11, 17, 65]. This could indeed be the limiting factor in our thermal abla-



Figure 5. Thermal boundary conductance plotted as a function of the Au/substrate cutoff frequency ratios determined by phonon dispersion plots obtained in literature.

tion measurements, which is apparent in the trends in Fig. 5, 505 which plots the thermal boundary conductance across the var-506 ious Au/substrate interfaces vs. ratio of phonon cutoff fre-507 quencies between Au and the substrate ($\omega_{Au}^{max}/\omega_{Substrate}^{max}$). In 508 general, $h_{\rm K}$ scales as the phonon spectra between the Au and 509 substrate become better overlapped, which his consistent with 510 several prior works [66, 67]. However, as we discuss below 511 with regards to the mechanical coupling at the Au/substrate 512 interface, we can not rule out changes in the bonding environ-513 ment. 514

iii) Interfacial bonding: The influence of interfacial bond-515 ing on thermal boundary conductance has been well studied 516 [10, 12, 24, 28, 68–71], and previous works have reported on₅₃₉ 517 bonding effects at Au/substrate interfaces [18, 19, 27]. In gen-540 518 eral, the thermal boundary conductance across interfaces can541 519 be influenced by both the phonon spectrum overlap (discussed₅₄₂ 520 above) and the interfacial bonding. Most notably, Losego et₅₄₃ 521 al. [27] demonstrated a direct relationship between the ther-544 522 mal boundary conductances across Au/self assembled mono-545 523 layer/quartz interfaces and interfacial pressure determined via546 524 laser spallation experiments. This would suggest that the ther-547 525 mal ablation threshold in our measurements are a measure of₅₄₈ 526 interfacial bonding, which directly impacts the measured ther-549 527 mal boundary conductance. 528 550

Clearly, based on our discussion of ii and iii above, wessi 529 can not distinguish between the roles of interfacial bonding552 530 and phonon spectrum overlap on the origin of the substrate553 531 dependence of thermal ablation thresholds in the thin Au⁵⁵⁴ 532 films. Thus, to gain more insight into the nanoscopic mech-555 533 anisms driving thermal ablation in these thin films, we con-556 534 duct molecule dynamics simulations. The parameters of these557 535 simulations are discussed in detail in Section II.D. These sim-558 536 ulations are utilized as toy models to explore the individual⁵⁵⁹ 537 roles of the previously mentioned factors involved in the role560 538



Figure 6. Top view of the computational domains with atoms colored according to their centrosymmetry parameter for the (a) weakly bonded and (b) strongly bonded interfaces.



Figure 7. (a) Phonon density of states for atoms representing the thin film system and the atoms representing the substrates with 40 (black) and 280 (red) g mol⁻¹. (b) Top view of the computational domains with atoms colored according to their centrosymmetry parameter for the case where the substrate atoms have a prescribed mass of 280 g mol⁻¹. The better spectral overlap between the thin film region and the substrate atoms with a mass of 280 g mol⁻¹ ensures that $h_{\rm K}$ is higher compared to the case where the substrate atoms have a lower mass.

of interfacial thermal transport on diffusive damage of thin films. To visualize the defected region in the computational domain after melting the region in the thin film and allowing the structure to evolve under the various ensembles, we make use of the centrosymmetry parameter, which is a measure of the local lattice disorder around an atom [72]. For an atom on an fcc lattice site, surrounded by the 12 nearest neighbor atoms on a perfect lattice, the centro-symmtry parameter will be zero, while for defects and dislocations, the centrosymmetry parameter will be high. We color the atoms based on this criteria (where the most blue atoms are described by a centro-symmetry parameter that is for a perfect lattice position and the red atoms represent a highly defected atom). Figure 6 shows the top surface of the thin film for a weakly bonded (Fig. 6a) and the strongly bonded (Fig. 6b) interfaces at 150 ps after melting. As is clear, for the weakly bonded case, the defected region is larger compared to the strongly bonded case, which is qualitatively in line with our experimental results on the measured damage area of Au films on different substrates. This suggests that the interfacial bonding (and therefore, the $h_{\rm K}$) can influence the damaged area in thin films.

To understand the relative effect of increasing $h_{\rm K}$ on the de-

fected area, while the interfacial bonding is set to that of thesi 561 strongly bonded case, we increase the mass of the substrate612 562 atoms to 280 g mol⁻¹. This effectively shifts the spectrum of 563 the phonon density of states (DOS) of the substrate atoms to 564 lower frequencies and increases the overlap between the DOS 565 of the thin film (as shown in Fig. 7a). Note, increasing the 566 mass of the atoms from 40 g mol⁻¹ to 280 g mol⁻¹ reduces the⁶¹³ 567 thermal conductivity. However, the better spectral overlap be $_{615}^{614}$ 568 tween the thin film and the substrate region for the case where $\frac{1}{616}$ 569 the substrate atoms have a prescribed mass of 280 g mol⁻¹ en-₆₁₇ 570 571 sures that $h_{\rm K}$ is increased [26]. Figure 7b shows the top view₆₁₈ of the computational domain with the atoms colored accord-619 572 ing to their centrosymmetry parameter. The defected area for⁶²⁰ 573 the computational domain with the better spectral overlap is⁶²¹ 574 greatly reduced compared to the case with the lower $h_{\rm K}$ in $^{622}_{623}$ 575 Fig. 6a and Fig. 6b. 576 624

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V. CONCLUSION

In conclusion, the thermal ablation threshold in metal $thin_{abla}^{629}$ 578 films is found to be dependent on the interfacial thermal re-579 sistance of the system. While our results suggest thermal₆₃₂ 580 confinement in the thin film is the primary ablation mech-633 581 anism for picosecond laser pulses of thin films, it is likely634 582 that changes in interfacial bonding are also playing a role in635 583 the obtained threshold values. For weakly bonded systems in636 584 our simulations, the defected area surrounding the melted re_{637}^{637} 585 gion is larger compared to that of a strongly bonded system, 586 which is qualitatively in line with our experimental results on₆₄₀ 587 the measured damage area of Au films on different substrates.641 588 This suggests that the interfacial bonding (and therefore the642 589 $h_{\rm K}$) can influence the damaged area in thin films. Further-643 590 more, when the interfacial bond strength is set to that of the⁶⁴⁴ 591 strongly bonded case, we increased $h_{\rm K}$ by shifting the phonon⁶⁴⁵₆₄₆ 592 density of states (DOS) of the substrate to better overlap the $\frac{1}{647}$ 593 DOS of the thin films. The defected area for the computational₆₄₈ 594 domain with better spectral overlap (and therefore larger $h_{\rm K}$)₆₄₉ 595 is greatly reduced compared to the case with the lower $h_{\rm K}$.650 596 While this model finds excellent agreement with our experi-651 597 mental results, where lower thermal boundary conductances⁶⁵² 598 ultimately lead to increased defected regions, ii and iii above⁶⁵³ 599 can not be separated; both interfacial bonding and spectral 600 overlap lead to similar results while the opposite term is held₆₅₆ 601 constant. Additionally, although typically applied for in-situ657 602 measurement of beam-waist where systems are dominated by658 603 1-D transport, we find variation in the waist-parameter in Eq. 2659 604 of Liu's model to provide a relative measure of transverse ther-660 605 661 mal transport for thin-film systems. 606 662

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