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Disorder-driven topological phase transition in Bi_2Se_3 films

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Abstract: Topological insulators (TI) are a phase of matter that host unusual metallic states on their surfaces. Unlike the states that exist on the surface of conventional materials, these so-called topological surfaces states (TSS) are protected against disorder-related localization effects by time reversal symmetry through strong spin-orbit coupling. By combining transport measurements,

angle-resolved photo-emission spectroscopy and scanning tunneling microscopy, we show that there exists a critical level of disorder beyond which the TI Bi_2Se_3 loses its ability to protect the metallic TSS and transitions to a fully insulating state. The absence of the metallic surface channels dictates that there is a change in material's topological character, implying that disorder can lead to a topological phase transition even without breaking the time reversal symmetry. This observation challenges the conventional notion of topologically-protected surface states, and will provoke new studies as to the fundamental nature of topological phase of matter in the presence of disorder.

It has been known since the 1950s that disorder alone can localize electrons and drive metals into an insulating state¹. Such disorder-driven localization effects are enhanced in 2-dimensions (2D)^{2,3}. This is exemplified by the surface states that form on the boundary of non-topological insulators, which are especially susceptible to localization effects by an arbitrarily small level of disorder. In contrast, the novel 2D, Dirac-like topological surface states (TSS) that emerge at the surface of a 3-dimensional (3D) topological insulator (TI) are predicted to be robust to disorder that preserves time-reversal symmetry, in that they should remain metallic⁴⁻⁶. So far, experimental efforts to probe the extent of topological protection have been limited to controlling spin-orbit-coupling strength through elemental substitution⁷⁻¹¹ and thickness control in the ultrathin regime of 3D TIs¹²⁻¹⁴, where the reduced dimensionality and the overlap of the top and bottom surface wavefunctions are found to compromise the topological protection even without intentional disorder. However, despite theoretical efforts¹⁵⁻¹⁷, the very fundamental question of whether (and how) disorder can drive 3D TIs beyond topological protection remains elusive in real TI materials.

In this work, we address this very issue, by creating the TI Bi_2Se_3 films with intentional disorder. As summarized in Table 1, TI phases are generically required to be metallic because of the gapless TSS, whereas metallic nature alone is *not sufficient* to confirm the non-trivial topology because a topologically trivial bulk metal is also metallic, and, therefore, confirmation of a material to be a TI requires other probes such as angle-resolved photo-emission spectroscopy (ARPES). In contrast, however, the material

being insulating *is sufficient* to confirm that it is not a TI because a TI is guaranteed to have a metallic surface state⁵. This allows us to show that there exists a critical level of disorder, beyond which the topological Bi₂Se₃ transitions into a fully insulating topologically-trivial state. This is achieved by co-depositing Bi and Se onto Al₂O₃ substrates at room temperature (~20 °C). At this unusually low growth temperature, rather than being topological and thus metallic, these films are found to be insulating due to the formation of strongly disordered Bi₂Se₃ nanocrystals.

To achieve the highest quality single-crystal (referred to herein as low-disorder) Bi₂Se₃ films, the optimum growth temperature on Al₂O₃ is ~200 – 300 °C^{18–21}, which gives the adsorbed Bi and Se atoms sufficient surface mobility to diffuse and find an optimal location to crystallize and form single crystals¹⁸. However, as the deposition temperature is decreased to room temperature and the surface mobility of adatoms decreases, they begin to accumulate in a less coherent manner forming highly disordered nanocrystalline (high-disorder) grains of Bi₂Se₃. Further, the disorder can be partially reduced by post-growth annealing of the high-disorder film above 72 °C; these films, which we refer to as an intermediate-disorder state, are found to rearrange structurally to a lower disorder state. Altogether, it is found that three different disorder regimes of Bi₂Se₃ are accessible — for more growth details, see Supplemental Information.

Figure 1(a-c) show high-angle annular dark-field scanning transmission electron microscopy (HAADF-STEM) images for films with the different disorder states. The low-disorder sample is clearly single-crystalline with the c-axis orientated out-of-plane. In contrast, the high-disorder state is composed of ~5 nm size grains that are randomly oriented. Finally, the intermediate-disorder sample is composed of nearly c-axis oriented domains with grain size of ~100 nm. X-ray photoemission spectra (XPS) for the Se 3d and Bi 4f in Fig. 1(d-e), respectively, show that despite this large rearrangement, the local chemical environment remains that of Bi₂Se₃²², regardless of the level of disorder. Further, as shown in Fig. 1(f), X-ray diffraction (XRD) measurements indicate a clear change in crystal structure from one with small wide peaks, for the highly disordered films, to the clear c-axis quintuple layer (QL, 1 QL ≈ 0.95 nm) structure for the intermediate (and low) disorder films, which is indicative of the common rhombohedral Bi₂Se₃

phase — a well-known TI. For high disorder films, however, the small peaks are identified as an orthorhombic form of Bi_2Se_3 ^{23,24}, which is also known to be a TI²⁵; the broadness of the peaks and the lack of preferred orientation implies that this phase is composed of disordered nanocrystals, which is consistent with the HAADF-STEM images above. Altogether, HAADF-STEM, XPS and XRD show that all the films are composed of Bi_2Se_3 phases at the nanoscale that are known TIs, but, as we will see below, the level of disorder manifests dramatically in the electronic properties.

Figure 2(a-c) shows resistance versus temperature measurements for low, intermediate and high disorder films, respectively. The resistance for both low- and intermediate-disorder films decreases with decreasing temperature, which is indicative of metals. For the high-disorder state, however, the room temperature resistance is three orders of magnitude larger, and the resistance quickly increases with decreasing temperature to a point where it becomes immeasurably large below ~ 150 K: in other words, it is an insulator. As shown in Tab. 1, the observation of the insulating behavior directly indicates that the high-disorder phase is non-topological. If the sample were topological, the interface with vacuum (or air) should have metallic surface states. Therefore, the very fact that the high-disorder Bi_2Se_3 is not metallic implies that it is non-topological. However, the insulating nature and the lack of long-range-order (due to small randomly oriented grains) precludes (see Supporting Information) other probes such as ARPES and scanning tunneling microscopy (STM) from proving the trivial topology of this state, which makes transport measurements the only (but still sufficient) probe showing that the highly disordered state of Bi_2Se_3 is non-topological.

In contrast to the insulating phase, the observation of metallic transport shown in Fig. 2(a-b) is not sufficient to confirm the topological nature of these states. This is due to the fact that carriers can be transported through the bulk, through the TSS or through both. Therefore, other probes are required to confirm whether a metallic system is topological or not. Fig. 2(d-e) show ARPES measurements for low- and intermediate-disorder phases, respectively. For the low-disorder film, the bulk band and the Dirac-like TSS are clearly visible, which confirms that the sample is topological. For the intermediate-disorder films, however, the spectrum is diffuse and much broader with noticeable suppression of the intensity at

the Dirac point, and, thus, inconclusive regarding the topology of this sample. The beam size for APRES experiments performed here is large ($> 100 \mu\text{m}$) compared to the nanoscale microstructure of the films in this study. Therefore, the smearing of the spectrum in Fig. 3(e) may be due to the superposition of grains with disparate electronic structures.

To understand how the local electronic properties affect the macroscale properties measured by transport and ARPES, Fig. 2(g-l) shows local topographical maps and tunneling spectroscopy for low- (STM), intermediate- (STM), and high-disorder (atomic force microscopy) films, respectively. In Fig 2(g-i) there is a clear difference in surface morphology between different levels of disorder, and are consistent with the STEM and XRD data shown in Fig. 1. The low-disorder sample shows clear large quintuple layer (QL, the minimum unit of Bi_2Se_3) terraces typical of epitaxial Bi_2Se_3 . The intermediate-disorder film shows both ordered QL step terraces and disordered areas. In contrast, there are not any long-range crystalline features visible on the high-disorder sample in Fig. 2(i), which is consistent with the STEM image in Fig. 1(c). Further, scanning tunneling spectroscopy (STS) measurements enable probing the electronic structure in a spatially resolved way. Fig. 2(j-k) show STS measurements for low- and intermediate-disorder samples, respectively. For the low-disorder sample the differential conductance, dI/dV , decreases with negative bias, until it reaches a minimum around -0.4 eV , at which point it again starts to increase. This is typical of the Dirac surface band as observed many times before²⁶. For the intermediate-disorder sample, the STS spectrum from the terraced area is nominally identical to the low-disorder STS data. This indicates that there exists TSS and, at least locally, the material is topological. However, the more disordered regions in Fig. 2(h) was so insulating that STS spectrum was not measurable. This suggests that either the more disordered region does not contain TSS (non-topological) or the TSS exists below vacuum- Bi_2Se_3 interface in this region. This observation shows that the intermediate-disorder sample may be phase-segregated into topologically trivial and non-trivial regions. It is worth noting that despite the similarities between the transport properties between the low-disorder and intermediate-disorder samples, their ARPES and STM (STS) data are vastly different. This is in fact easy to understand considering that transport properties are dominated by the most conducting paths of the

sample as far as the conducting paths are contiguous throughout the sample, whereas ARPES requires long-range crystalline order and STM (STS) probes local properties.

Fig. 2(m) shows a phase diagram summarizing the results for the evolution of a TI phase with increasing disorder. Under the Z_2 TI paradigm, all non-magnetic insulators can be grouped into either topological insulators, which are guaranteed to have metallic surface states, or trivial insulators, whose surface states are not guaranteed to be metallic. According to this classification, the disordered insulator phase studied here should belong to the trivial insulator. However, it should be noted that disorder itself is a non-specific property, covering a broad range of material states that interrupts the real-space periodicity of the underlying lattice in combination of point, linear, or planar defects. The question is then: what specific aspect of disorder drives a TI to a trivial insulating state? In our present case the disorder is in the form of decreasing grain size with random orientation, which ultimately must be the driver that changes the material's global topology.

It is well known that near a phase transition small local fluctuations in disorder can dramatically shift the global ground state. This has long been studied from percolation theory near a metal-insulator phase transition²⁷, electron-hole phase segregation near the Dirac point in graphene²⁸, to fluctuating anti-ferromagnetism that may stabilize high-temperature superconductivity²⁹. The Z_2 classification scheme should be no exception, and must be sensitive to local disorder³⁰. Our present study shows that topological-percolation most likely drives the observed phase transition from a TI to a non-TI, and, therefore, the transition cannot be considered abrupt in the disorder phase space. As STM shows, in the intermediate-disorder sample the material is phase-segregating into regions with and without gapless surface states, while globally the material remains sufficiently well connected as to remain metallic. As disorder is further increased with grain sizes reducing from ~100 nm to ~5 nm scale, non-topological regions grow and topological regions shrink, and eventually the materials become globally insulating when the metallic topological islands are sufficiently surrounded by small trivially insulating grains. Such a combination of topological-disorder and percolation likely plays an important role even in other topological transition materials such as $(\text{Bi}_{1-x}\text{In}_x)_2\text{Se}_3$ ^{8,31,32}. Still, with percolation aside, it remains an open

question what drives the local disordered regions to a net-insulating, non-topological state as their grain size decreases. Instead of attempting to provide a definite answer to this question, below we present a simple physical picture as a guide to future studies.

The transition away from the TI phase observed here likely comes down to a combination of the size of the grains, their random orientation with respect to each other, and the details of the interfaces. Considering the grain size, it is well known that making a TI film thinner than a critical thickness ($\sim 4\text{-}5\text{ nm}$)¹² opens a gap at the Dirac point, and hence, drives the TI into a trivial state. This results from the TSSs on the top surface hybridizing with the TSS on the bottom surface since they have opposite spin direction. In terms of finite thickness, the small grain size of the high-disorder film is similar to the 4-5 nm critical thickness. This should, however, not compromise the topological properties of the material because finite thickness effects should only occur at the interface of a TI and non-TI when the TI is below this critical thickness.

The grain boundaries are composed of random crystallographic surfaces and how this affects the long range properties of the materials is not clear. As the grains are made smaller, the reciprocal lattice vector loses meaning and energy bands flatten, with the k -dependent band structure being replaced by a conglomeration of local molecular orbitals. Defining a Z_2 topological invariant only relies on the presence of an energy gap, and does not require k -space being well defined³³. Reducing the size of crystalline grains, however, is well known to only increase the energy gap due to quantum confinement effect, which should not cause a global band inversion requisite for a TI-to-non-TI phase transition. This then prompts the question of how the systematic increase in crystalline disorder kills the global topological invariant as observed here. To better answer this question, future explorations into the materials properties that control grain size will be required; this will provide a means to explore the nature of the transition from a topological insulator to a disordered trivial insulator in a continuous way. Altogether, the current study raises the challenging theoretical and experimental questions as to how to define and probe topological nature of disordered materials.

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Captions

Table 1. The relationship between transport properties being metallic or not and the material being topological or not. If a material is metallic, then it could be topological or non-topological. However, if a material is insulating then it cannot be topological because a topological material is guaranteed to have a metallic surface state.

Figure 1. Structural and chemical comparison of disordered Bi_2Se_3 thin films with various levels of disorder. (a-c) High-angle annular dark-field scanning transmission electron microscopy images for films with low-, intermediate- and high-disorder, respectively. The low-disorder one (a) shows fully single crystalline ordering and the intermediate one shows some grain boundaries with ~ 100 nm grain sizes but with still mostly c-orientation. On the other hand, the high-disorder film (c) is composed of ~ 5 nm crystalline grains (outlined by dashed lines) without any preferential orientations. (d-e) X-ray photoemission spectra show that the Se-3d (d) and Bi-4f (e) levels are independent of the level of disorder. (f) X-ray diffraction data show that the high-disorder films is composed of orthorhombic Bi_2Se_3 disordered grains, whereas intermediate- and high-disorder are formed of rhombohedral Bi_2Se_3 phase with dominant c-orientation: note the crystal orientation indices.

Figure 2. Electrical transport, and spectroscopy measurements as a function of disorder strength (Low-disorder: left column, intermediate-disorder: center column, and high-disorder: right column). (a-c) Resistance versus temperature. (d-f) Angle-resolved photoemission spectroscopy (ARPES). ARPES for the high disorder sample is not possible due to lack of long range crystalline order, combined with its insulating behavior. (g-i) Surface topography. The low-disorder and intermediate-disorder were performed with scanning tunneling microscopy ($V_B = -2$ V, $I_T = 5$ pA), whereas, due to the highly insulating properties, the high-disorder case was performed with atomic force microscopy. (j-k) Scanning tunneling spectroscopy, taken from X-marked regions of (g) and (h). For the intermediate-order sample, STS was not possible in the more disordered regions away from the X-mark. STS for the high-disorder

sample was not possible due to its insulating behavior. (m) A phase diagram summarizing the electronic phase as a function of disorder.

Tab. 1 (single column)

	Insulating	Metallic
Topological	×	✓
Non-topological	✓	✓

Figure 1. (double column)

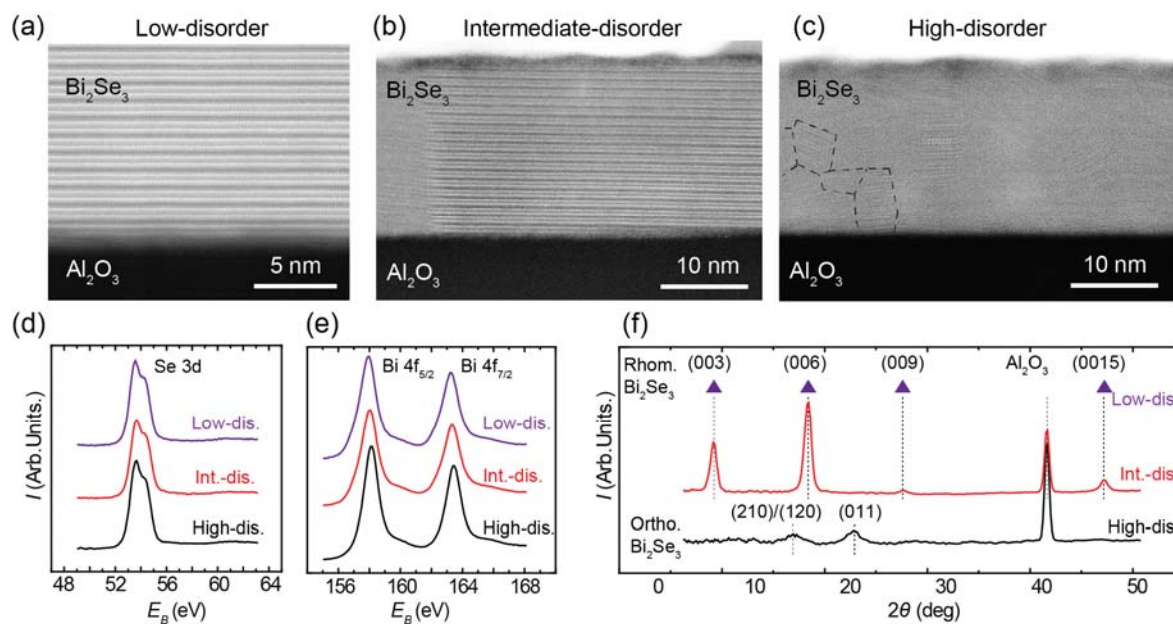


Figure 2. (single column)

