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## Superconducting and normal state properties of the systems $\text{La}_{1-x}\text{M}_x\text{Pt}_4\text{Ge}_{12}$ ( $\text{M} = \text{Ce}, \text{Th}$ )

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# Superconducting and normal state properties of the systems $\text{La}_{1-x}\text{M}_x\text{Pt}_4\text{Ge}_{12}$ ( $M = \text{Ce}, \text{Th}$ )

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Electrical resistivity, magnetization, and specific heat measurements were performed on polycrystalline samples of the filled-skutterudite systems  $\text{La}_{1-x}\text{M}_x\text{Pt}_4\text{Ge}_{12}$  ( $M = \text{Ce}, \text{Th}$ ). Superconductivity in  $\text{LaPt}_4\text{Ge}_{12}$  was quickly suppressed with Ce substitution and no evidence for superconductivity was found down to 1.1 K for  $x > 0.2$ . Temperature-dependent specific heat data at low temperatures for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  show a change from power-law to exponential behavior, which may be an indication for multi-band superconductivity in  $\text{LaPt}_4\text{Ge}_{12}$ . A similar crossover was observed in the  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  system. However, the suppression rates of the superconducting transition temperatures,  $T_c(x)$ , in the two systems are quite disparate, indicating a difference in the nature of superconductivity, which is conventional in  $\text{LaPt}_4\text{Ge}_{12}$  and unconventional in  $\text{PrPt}_4\text{Ge}_{12}$ . In comparison, a nearly linear and smooth evolution of  $T_c$  with increasing Th was observed in the  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  system, with no change of the superconducting energy gap in the temperature dependence of the specific heat, suggesting similar types of superconductivity in both the  $\text{LaPt}_4\text{Ge}_{12}$  and  $\text{ThPt}_4\text{Ge}_{12}$  compounds.

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## I. INTRODUCTION

Recently, a new branch of filled skutterudites was discovered with the chemical formula  $A\text{Pt}_4\text{Ge}_{12}$ .<sup>1,2</sup> Several members of this branch were found to exhibit superconductivity with  $A = \text{La}$  and  $\text{Pr}$  exhibiting the highest superconducting transition temperatures,  $T_c \sim 8$  K.<sup>1-3</sup> Considerable attention has been focused on  $\text{PrPt}_4\text{Ge}_{12}$  as it exhibits signs of unconventional superconductivity.<sup>4-10</sup> However, investigations into  $\text{SrPt}_4\text{Ge}_{12}$  and  $\text{BaPt}_4\text{Ge}_{12}$  show that the superconductivity is conventional BCS-type which originates from, and is intrinsic to, the Pt-Ge cages.<sup>1</sup> Furthermore,  $\text{LaPt}_4\text{Ge}_{12}$  was also found to exhibit evidence for conventional BCS-type superconductivity from nuclear magnetic resonance (NMR) and <sup>73</sup>Ge nuclear quadrupole resonance (NQR) measurements.<sup>11,12</sup>

The compound  $\text{CePt}_4\text{Ge}_{12}$  is thought to lie on the border between an intermediate-valence (IV) and a Kondo lattice compound.<sup>11</sup> Initial investigations into  $\text{CePt}_4\text{Ge}_{12}$  revealed a broad maximum in the magnetization  $M(T)$ , which can be a characteristic of intermediate-valence compounds. However, high resolution X-ray absorption spectroscopy measurements indicated that the Ce ions exhibit a temperature-independent valence close to  $\sim 3^+$ .<sup>13</sup> Recent inelastic neutron scattering measurements find a wider quasielastic peak at higher energies, consistent with an IV system, as well as the absence of crystalline electric field effects expected in a Kondo system.<sup>14</sup>

Therefore, we decided to investigate the  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  system to complement our previous study of the  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  system. We anticipated that these two investigations could provide valuable insight into the nature of superconductivity in the Pt-Ge based filled skutterudites. Additionally, studies of  $\text{ThPt}_4\text{Ge}_{12}$  have uncovered signatures of an exotic form of superconductivity from  $\mu\text{SR}$  measurements,<sup>15</sup> power law contributions to specific heat,<sup>16</sup> and a complex Fermi surface from band-structure calculations;<sup>17</sup> these results motivated a parallel study on the system  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$ .

We found that  $T_c$  in  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  is suppressed rapidly and almost linearly with increasing  $x$ , with the onset of superconductivity no longer being observable down to 1.1 K for  $x \geq 0.2$ . In contrast, the onset of superconductivity in  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  persists up to  $x = 0.5$ , and the  $T_c$  vs.  $x$  curve has pronounced positive curvature.<sup>9</sup> In the  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  system, we observed a smooth and continuous change in  $T_c$  vs.  $x$ , which is inconsistent with the behavior that would be expected for the existence of different types of superconducting states;<sup>18,19</sup> i.e., the continuous and smooth behavior of  $T_c$  vs.  $x$  instead suggests that both  $\text{LaPt}_4\text{Ge}_{12}$  and  $\text{ThPt}_4\text{Ge}_{12}$  exhibit the same type of superconductivity.

A change in the temperature-dependence of the specific heat in the superconducting state of  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  is observed; this may be evidence for a crossover from multi-band superconductivity in  $\text{LaPt}_4\text{Ge}_{12}$  to isotropic single-band superconductivity in the  $x > 0$  samples. A similar crossover in the specific heat behavior was observed when Ce was substituted into  $\text{PrPt}_4\text{Ge}_{12}$ , a material with well-established evidence for multi-band superconductivity.<sup>6-9</sup> Specific heat measurements on the system  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  from  $x = 0$  to  $x = 0.2$  did not exhibit a similar change. Taken together with previous studies, it is possible that both  $\text{LaPt}_4\text{Ge}_{12}$  and  $\text{ThPt}_4\text{Ge}_{12}$  are multi-band superconductors.

## II. EXPERIMENTAL DETAILS

Polycrystalline samples of  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  ( $x = 0, 0.05, 0.1, 0.15, 0.2, 0.4, 0.6, 0.80, 1$ ) and  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  ( $x = 0, 0.2, 0.4, 0.6, 0.8, 1$ ) were synthesized in an atmosphere of ultrahigh purity argon by arc-melting in a custom built arc furnace employing a zirconium getter on a water-cooled copper hearth. The starting materials were La ingots (Sigma-Aldrich, 99.9%), Ce rods (Alfa Aesar 3N, EPSI 99.9%), Th pieces, Pt sponge arc-melted into spheres (99.9999+%), and Ge pieces (Alfa Aesar 99.9999+%). The starting materi-

als were weighed out in the molar stoichiometric ratios, arc-melted together, and then flipped over and arc-melted again four more times to promote homogeneity. All samples were heat treated in a sealed quartz tube under an inert atmosphere (200 torr Ar) for 336 hours at 800 °C.

Powder X-ray diffraction (XRD) measurements were performed using a Bruker D8 X-ray diffractometer with a Cu  $K_\alpha$  source. Four-wire electrical resistivity measurements were performed from 300 K down to  $\sim 1.1$  K in a pumped  $^4\text{He}$  Dewar. Magnetization measurements were performed between 300 K and 2 K in a Quantum Design Magnetic Property Measurement System (MPMS) equipped with a 7 T superconducting magnet. Specific heat measurements were performed down to 1.8 K using a Quantum Design Physical Property Measurement System (PPMS) DynaCool. The heat capacity measurements employed a standard thermal relaxation technique.

### III. RESULTS

Rietveld refinements were performed on the powder XRD patterns for each sample using GSAS<sup>20</sup> and EXPGUI.<sup>21</sup> Displayed in Fig. 1(a) is an XRD pattern for  $\text{La}_{0.4}\text{Ce}_{0.6}\text{Pt}_4\text{Ge}_{12}$ , representative of the XRD patterns observed for values of  $x$  throughout both the  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  and  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  systems. The blue line is the experimental XRD pattern and the red tick marks below locate the  $2\theta$  positions of the expected Bragg reflections for the refined filled-skutterudite crystal structure. The cubic filled-skutterudite crystal structure (space group  $Im\bar{3}$ ) was observed over the entire range of  $x$  for both series. As is commonly observed in the Pt-Ge based skutterudites,<sup>2,7,8,11,14,22,23</sup> small impurity phases of Ge and/or  $\text{PtGe}_2$  (at most up to  $\sim 5\%$  by mass) were detected in the samples. Figures 1(b) and (c) display the lattice parameter,  $a$ , for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  (blue circles) and  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  (teal pentagons) with dashed lines serving as guides to the eye. The system  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  exhibits a linear decrease of  $a$  as  $x$  increases with the end members exhibiting  $a$  values of 8.618 Å for  $x = 0$  and 8.615 Å for  $x = 1$ . The plot of  $a$  vs.  $x$  for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  shows a sudden increase in  $a$  of about 0.3% at  $x = 1$ . This may be because the XRD measurements for the sample with  $x = 1$  were made using a different X-ray diffractometer. Another possible explanation for the larger  $a$  value for the sample with  $x = 1$  is that there is a known sample dependence in the Pt-Ge based filled skutterudites; reported values for  $a$  of  $M\text{Pt}_4\text{Ge}_{12}$  ( $M = \text{La, Pr, Nd, Ce}$ ) differ by roughly 0.5%.<sup>2,11</sup>

The electrical resistivity,  $\rho(T)$ , measured in zero applied magnetic field, is displayed for the series  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  in Fig. 2(a) and  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  in Fig. 2(b). The system  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  exhibits an overall increase in  $\rho(T)$  with increasing  $x$ , except for  $x = 1$  at low temperature which exhibits a large decrease below 150 K. The overall shape of  $\rho(T)$  exhibits the behavior of a simple metal, while at higher temperature, it has a negative curvature. This type of  $\rho(T)$  behavior is often observed in the Ce-based filled skutterudites such as  $\text{CeFe}_4\text{Sb}_{12}$ .<sup>24</sup> However, for  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$ ,  $\rho(T)$

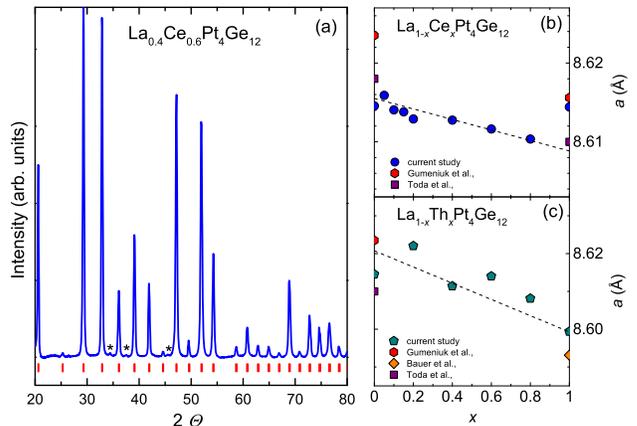


FIG. 1: (Color online) (a) Powder X-ray diffraction pattern for a representative sample of  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  ( $x = 0.6$ ) where the blue line represents the intensity vs.  $2\theta$  and the red tick marks locate the  $2\theta$  positions of the expected Bragg reflections for the refined filled-skutterudite crystal structure. Black asterisks indicate Bragg reflections associated with a  $\text{Ge/PtGe}_2$  impurity phase. The lattice parameter,  $a$ , is plotted for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  in panel (b) and for  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  in panel (c). The dashed lines are guides to the eye. The  $a$  vs.  $x$  data for both  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  and  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  obey Vegard's law, except for  $x = 1$ , in  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ , where  $a$  has a larger value (see text). The  $a$  values for  $\text{LaPt}_4\text{Ge}_{12}$ ,  $\text{CePt}_4\text{Ge}_{12}$ , and  $\text{ThPt}_4\text{Ge}_{12}$  are plotted for comparison.

does not exhibit any clear trend with increasing  $x$ , possibly due to uncertainties in the measurement of the geometrical factors of the resistivity samples. Plotted in Fig. 2(c) are the scaled  $\rho(T)$  data for the system  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  such that the slopes,  $d\rho/dT$ , are identical to  $d\rho/dT$  for  $\text{LaPt}_4\text{Ge}_{12}$  at high temperature. The scaled  $\rho(T)$  data clearly show that additional electron scattering associated with the  $4f$  electrons is introduced by Ce substitution. In contrast, when the same procedure is performed on the  $\rho(T)$  data for  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$ , displayed in Fig. 2(d), the scaled  $\rho(T)$  data collapse onto a single curve, suggesting that Th substitution does not introduce any additional mechanisms for scattering electrons. The intrinsic differences in the  $\rho(T)$  curves in Fig. 2(b) are due to differences in lattice scattering (electron-phonon scattering depends on the Debye temperature,  $\Theta_D = 220$  K,<sup>13</sup> in the Bloch-Grüneisen formula), and the non-monotonic trend of the unscaled  $\rho$  at 300 K may be a consequence of errors in estimating the geometrical factor for the  $x = 0.4, 0.6, 0.8$  samples.

For the  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  and  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  series, the  $\rho(T)$  data are well described by  $\rho(T) = \rho_0 + AT^2$  up to  $\sim 250$  K<sup>2</sup> in Fig. 3 (c) and (d), indicating that both systems exhibit Fermi liquid behavior.  $A$  is a fitting parameter and  $\rho_0$  is the residual resistivity. The insets in Fig. 2(a) and (b) plot the residual resistivity ratio (RRR) as a function of  $x$  for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  and  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$ , respectively, where the RRR is defined as  $\rho_{300}/\rho_0$ , where  $\rho_{300}$  is the value

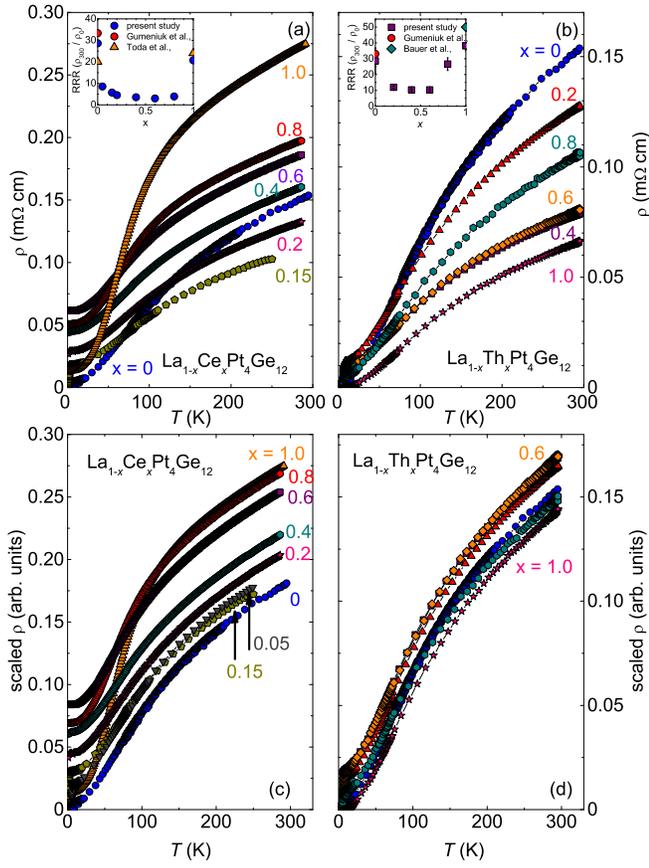


FIG. 2: (Color online) (a) Electrical resistivity,  $\rho$ , vs. temperature  $T$  for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ . The electrical resistivity at high temperature is enhanced with increasing Ce concentration. The inset displays the residual resistivity ratio RRR ( $\rho_{300}/\rho_0$ ) vs.  $x$  for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  (blue circles for this work), plotted as a function of  $x$ . The ratio exhibits a parabolic behavior with a minimum RRR = 3 for  $x = 0.6$ . (b)  $\rho$  vs.  $T$  for  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  which tends to exhibit an overall decrease of  $\rho$  with increasing  $x$ . The RRR vs.  $x$  is displayed in the inset for  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  (purple squares) with the minimum RRR = 10 at  $x = 0.6$ , similar to the parabolic behavior observed in  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ . (c) Scaled  $\rho(T)$  data for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  such that the high temperature slope  $d\rho/dT$  matches the high temperature  $d\rho/dT$  of  $\text{LaPt}_4\text{Ge}_{12}$ . (d) Scaled  $\rho(T)$  data for the  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  system. The curves appear to collapse onto a single curve.

of  $\rho$  at 300 K. The RRR vs.  $x$  exhibits a parabolic shape with the minimum at  $x = 0.6$  for both  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  (RRR = 3) and  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  (RRR = 10), close to the predicted minimum for simple alloys at  $x = 0.5$ .

There are clear drops in  $\rho(T)$  at  $T_c$ . To determine  $T_c$ , the ratio  $\rho(T)/\rho_{10}$ , where  $\rho_{10}$  is  $\rho(T = 10 \text{ K})$  (a representative value of  $\rho(T)$  in the normal state) was plotted vs.  $T$  in Fig. 3(a) and (b) for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  and  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$ , respectively.  $T_c$  was defined as the temperature where  $\rho(T)/\rho_{10} = 0.5$  and the width of the transition was characterized by the temperatures where  $\rho(T)/\rho_{10} = 0.9$  and  $0.1$ . For  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ ,  $T_c$  is rapidly suppressed

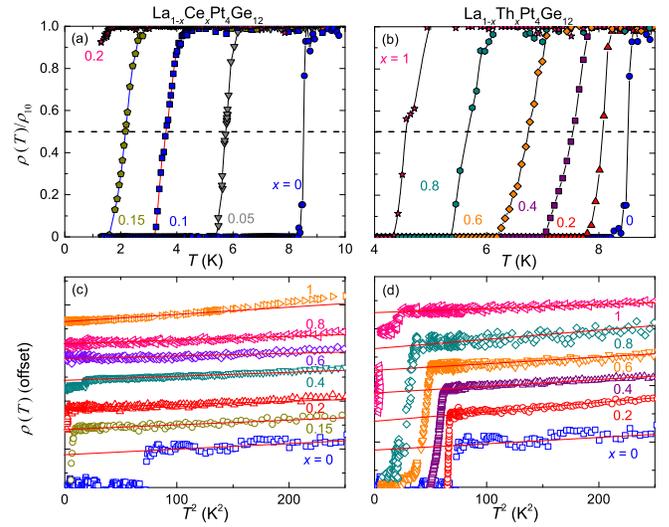


FIG. 3: (Color online) The electrical resistivity normalized by  $\rho$  at  $T = 10 \text{ K}$ ,  $\rho(T)/\rho_{10}$ , vs.  $T$  for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  in (a) and  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  in (b). The superconducting critical temperature  $T_c$ , where  $T_c$  is defined as  $\rho(T)/\rho_{10} = 0.5$ , for both systems decreases with increasing  $x$ . Measurements down to 1.1 K reveal that the onset of superconductivity is observable up to  $x = 0.2$  for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ . The  $T_c$  for  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  decreases almost linearly with  $x$ , with the lowest value of  $T_c = 4.5 \text{ K}$  observed for  $x = 1.0$ , close to the reported value.<sup>3,16</sup> Selected  $\rho$  vs.  $T^2$  data for (c)  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  and (d)  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  with offsets for visual clarity. Linear fits of  $\rho(T) = \rho_0 + AT^2$  were performed up to roughly  $250 \text{ K}^2$ .

with increasing  $x$ , with only the onset of superconductivity observed for  $x = 0.2$  from measurements down to 1.1 K. In the system  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$ ,  $T_c$  is also suppressed with increasing  $x$ , from 8.3 K for  $x = 0$  down to 4.5 K for  $x = 1$ . Th substitution suppresses  $T_c$  less rapidly than Ce substitution; however, this is not surprising since its  $5f$  electron shell is empty so that Th is nonmagnetic and  $\text{ThPt}_4\text{Ge}_{12}$  exhibits superconductivity. In contrast,  $\text{CePt}_4\text{Ge}_{12}$  exhibits no ordered state down to 50 mK.<sup>11,13,25</sup>

Magnetization divided by magnetic field,  $M/H$ , vs.  $T$  data for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  are shown in Fig. 4(a) where the  $M(T)/H$  data were scaled by a factor of 1000 for clarity.  $M(T)/H$  exhibits Curie-Weiss behavior above 200 K for all  $x$  and passes through a broad maximum around 80 K, followed by an upturn as  $T \rightarrow 0 \text{ K}$ . The deviations from Curie-Weiss behavior, manifested by the broad maxima, could be an indication of either intermediate-valence (IV) behavior of Ce or Kondo lattice behavior.<sup>2</sup> The broad maxima become smaller in amplitude and width as the peak position shifts to lower temperatures with decreasing  $x$ , as seen in Fig. 4(c). This behavior may suggest that the local Kondo temperature,  $T_K$ , also decreases with decreasing  $x$  and that the  $4f$  electrons are well localized at high temperatures. If  $T_K$  arises from the fully trivalent  $\text{Ce}^{3+}$ , then La substitution would weaken the Ce-Ce interactions, which would suppress the broad maxima as well as  $T_K$ . However, it should be noted that this behavior dif-

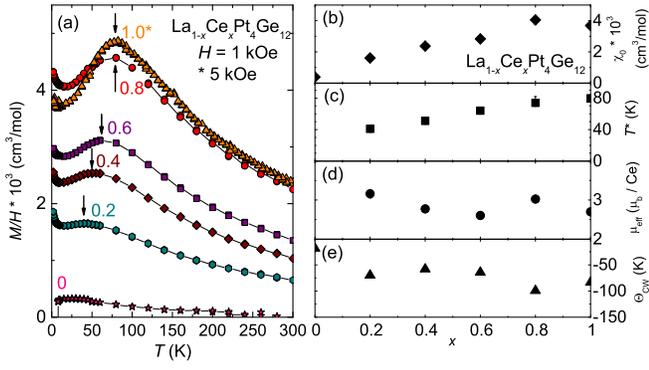


FIG. 4: (Color online) (a) Magnetization divided by applied magnetic field,  $M/H$ , vs.  $T$  from 300 K down to 2 K for the  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  system. The magnetic susceptibility,  $\chi(T) = M(T)/H$ , increases with increasing  $x$ , exhibiting an almost 10-fold increase between  $x = 0$  and  $x = 1.0$ . (b) The low temperature magnetic susceptibility,  $\chi_0$ , plotted as a function of  $x$ .  $\chi_0$  was determined by extrapolating  $M(T)/H$  data to  $T \rightarrow 0$  K while ignoring the small upturns observed at the lowest temperatures; these were determined to be due to small amounts of paramagnetic impurities. (c)  $T^*$ , the temperature where the broad maximum in the  $M/H$  vs.  $T$  data is centered as indicated by the black arrows in panel (a), plotted vs.  $x$ . The local maximum is possible evidence for either intermediate valence Ce or Kondo lattice behavior.  $T^*$  shifts to higher temperatures with increasing  $x$ , up to 80 K at  $x = 1$ , consistent with reported literature for  $\text{CePt}_4\text{Ge}_{12}$ .<sup>11</sup> The effective magnetic moment  $\mu_{eff}$  and Curie-Weiss temperature  $\theta_{CW}$  were determined from Curie-Weiss fits performed on the inverse  $M/H$  data in the temperature range 200-300 K and are plotted vs.  $x$  in (d) and (e), respectively.

fers from that observed for La substitution into the compound  $\text{CeRu}_4\text{Sb}_{12}$ , where the broad maximum in  $M(T)$  does not shift in temperature with increasing La concentration.<sup>26</sup> The small upturns in  $M(T)/H$  as  $T \rightarrow 0$  K do not scale with  $x$ , making the upturns more likely due to small amounts of paramagnetic impurities, as described in previous literature,<sup>9,10,27</sup> instead of being a signature of non-Fermi liquid behavior.<sup>28</sup> Both  $\chi_{300}$ ,  $M(T)/H$  at 300 K, and  $\chi_0$ ,  $M(T)/H$  as  $T \rightarrow 0$  K, are enhanced with increasing  $x$ .  $\chi_{300}$  increases from  $\sim 0$   $\text{cm}^3/\text{mol}$  for  $x = 0$  to  $2.3 \times 10^{-3}$   $\text{cm}^3/\text{mol}$  for  $x = 1$ .  $\chi_0$  was determined by extrapolating  $M(T)/H$  as  $T \rightarrow 0$  K from data at temperatures above those where the broad upturns are observed. As can be seen in Fig. 4(b),  $\chi_0$  increases with increasing  $x$ , exhibiting an almost 10-fold increase from  $\chi_0 = 0.39 \times 10^{-3}$   $\text{cm}^3/\text{mol}$  for  $x = 0$  up to  $\chi_0 = 3.69 \times 10^{-3}$   $\text{cm}^3/\text{mol}$  for  $x = 1$ .

Curie-Weiss law fits were performed on the  $M(T)/H$  data between 200 and 300 K for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ ; this temperature range was used because the broad maxima in  $M(T)/H$  made fitting to lower temperatures inappropriate. The effective magnetic moment  $\mu_{eff}$  and Curie-Weiss temperature  $\theta_{CW}$  for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  were determined using the relation  $M(T)/H = C_0/(T - \theta_{CW})$ , where  $C_0 = \mu_{eff}^2 N_A / 3k_B$ ,  $N_A$  is Avagadro's number, and  $k_B$  is Boltzmann's constant. The values we obtained for  $\mu_{eff}$  and  $\theta_{CW}$  are plotted in Fig. 4(d) and Fig. 4(e), respectively.  $\mu_{eff} = 2.67 \mu_B/\text{Ce}$  for  $x$

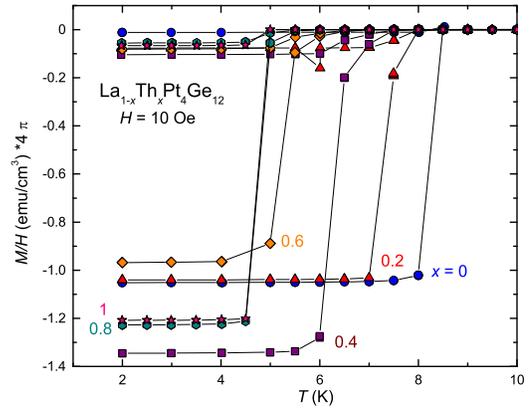


FIG. 5: (Color online) Magnetization divided by magnetic field plotted as  $4\pi M/H$  vs.  $T$  for  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  from 2-10 K in an external magnetic field  $H = 10$  Oe. The superconducting critical temperature,  $T_c$ , decreases as  $x$  increases, from 8 K for  $x = 0$  down to 4.3 K for  $x = 1$ . The nearly unity value of  $|4\pi M/H|$  is evidence for bulk superconductivity throughout the  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  series.

$= 1$ , which is slightly larger than the predicted value of  $2.54 \mu_B$  for the  $\text{Ce}^{3+}$  electronic configuration using Hund's rules; the limited temperature range for the Curie-Weiss fits, caused by the broad maximum, is possibly responsible for the disparity between the measured and calculated  $\mu_{eff}$  values. The effective moment,  $\mu_{eff}$ , increases slowly with decreasing  $x$  and exhibits values close to the free ion values derived from Hund's rules, reaching  $3.16 \mu_B/\text{Ce}$  for  $x = 0.2$ . The Curie-Weiss temperature  $\theta_{CW} = -83$  K of  $\text{CePt}_4\text{Ge}_{12}$  has a magnitude about twice as large as the value originally reported ( $\theta_{CW} = -39.2$  K),<sup>13</sup> and within the scatter of the data, remains nearly constant with a value of  $-80$  K throughout the entire series.

$M(T)/H$  measurements were performed for  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  samples in an applied magnetic field  $H = 10$  Oe to determine  $T_c$  and the superconducting volume fraction,  $v$ , as can be seen in Fig. 5. The superconducting volume fraction,  $v$ , was estimated using the equation  $M(T)/H \times d = v$ , where  $M(T)/H$  is in units of  $\text{emu}/\text{mol}$  and  $d$  is the molar density of the compound in units of  $\text{mol}/\text{cm}^3$ .  $T_c$  for  $\text{LaPt}_4\text{Ge}_{12}$  is 8 K, and it is suppressed with increasing  $x$  down to 4.3 K for  $x = 1$ , consistent with reported literature for the end-member compounds.<sup>2,3</sup> The volume fraction,  $v$ , is consistently near -1 for all  $x$ . This is evidence that the sample completely expels magnetic fields and is consistent with bulk superconductivity.

Specific heat divided by temperature,  $C(T)/T$ , vs.  $T$  plots for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  ( $x = 0, 0.05, \text{ and } 0.1$ ) and for  $\text{La}_{0.8}\text{Th}_{0.2}\text{Pt}_4\text{Ge}_{12}$  are displayed in Fig. 6(a).  $T_c$  was determined from idealized equal entropy conserving constructions about the specific heat jump associated with superconductivity as seen for  $\text{La}_{0.95}\text{Ce}_{0.05}\text{Pt}_4\text{Ge}_{12}$  in the inset of Fig. 6(a). In  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ ,  $T_c$  was rapidly suppressed with increasing  $x$ , from  $T_c = 8.3$  K for  $x = 0$  down to  $T_c = 3.2$  K for  $x = 0.1$ . For  $\text{La}_{0.8}\text{Th}_{0.2}\text{Pt}_4\text{Ge}_{12}$ , only a small decrease in  $T_c$  was observed, shifting down to  $T_c = 7.3$  K.

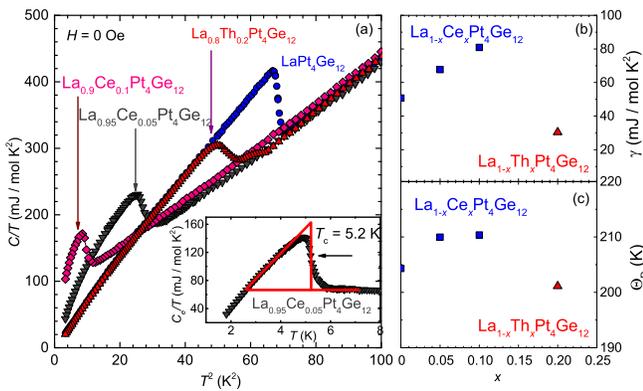


FIG. 6: (Color online) (a) Specific heat divided by temperature  $C(T)/T$  vs.  $T^2$  for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  ( $x = 0, 0.05, \text{ and } 0.1$ ) and  $\text{La}_{0.8}\text{Th}_{0.2}\text{Pt}_4\text{Ge}_{12}$  down to 2 K in zero magnetic field. The superconducting critical temperature  $T_c$  is suppressed with increasing  $x$ , with Ce substitution having a more pronounced effect than Th substitution.  $T_c$  values were determined from idealized equal entropy constructions fitted to the electronic contribution to specific heat,  $C_e/T$ , as shown in the inset for  $\text{La}_{0.95}\text{Ce}_{0.05}\text{Pt}_4\text{Ge}_{12}$ . Linear fits were performed on the  $C/T$  data plotted vs.  $T^2$  in the lowest temperature regions in the normal state to determine the Sommerfeld coefficient,  $\gamma$ , and the Debye temperature,  $\Theta_D$ ; these quantities are plotted in (b) and (c), respectively.

Linear fits using the equation  $C(T)/T = \gamma + \beta T^2$  were performed on the specific heat data from the lowest temperature in the normal state up to temperatures as high as linear fits were possible to determine the Sommerfeld coefficient,  $\gamma$ , and Debye temperature,  $\Theta_D$ . The coefficient of the phonon contribution to the specific heat,  $\beta$ , is related to  $\Theta_D$  by the relation  $\Theta_D = [1944 \times (n/\beta)]^{1/3}$  K where  $n = 17$  is the number of atoms in the formula unit. The electronic contribution to specific heat,  $\gamma$ , exhibits a moderate increase with initial Ce substitution where  $\gamma = 50$  mJ/mol K<sup>2</sup> for  $x = 0$  and reaches 80 mJ/mol K<sup>2</sup> for  $x = 0.1$ , close to the reported values of  $\gamma \sim 100$  mJ/mol K<sup>2</sup> for  $\text{CePt}_4\text{Ge}_{12}$ .<sup>9,13</sup> Thorium substitution results in a slight suppression of  $\gamma$ , where  $\gamma = 30$  mJ/mol K<sup>2</sup> for  $\text{La}_{0.8}\text{Th}_{0.2}\text{Pt}_4\text{Ge}_{12}$ , as shown in Fig. 6(b).  $\Theta_D$  appears to be insensitive to Ce or Th substitution, fluctuating less than 5% from  $\Theta_D = 204$  K for  $x = 0$ , as seen in Fig. 6(c).

Interestingly, negative curvature was observed in the  $C/T$  vs.  $T^2$  data as  $T \rightarrow 0$  K for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  with  $x \geq 0.05$ . To investigate this behavior, the electronic contribution to the specific heat,  $C_e(T)$ , was determined by subtracting the phonon contribution from  $C(T)/T$  and plotting as  $\log(C_e(T))/\gamma T_c$  vs.  $T_c/T$  in Fig. 7(a) for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  and (b) for  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$ . The data sets were offset for clarity. The solid lines represent fits to each data set. For  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ ,  $C_e(T)$  for the samples with  $x = 0.05$  and  $x = 0.1$  is well described by an exponential temperature dependence of the form  $be^{-(\Delta/T)}$ , where  $b$  is a fitting parameter and  $\Delta$  represents the superconducting energy gap. Best fit values for  $b$  were roughly 9.8 and 7.3 for  $x = 0.05$  and  $x = 0.1$ , respectively. The best fit values were  $\Delta/T_c = 1.52$  and 1.38 for  $x = 0.05$ , and  $x = 0.1$ , respectively; the val-

ues of  $\Delta/T_c$  could vary depending on the fitting range,<sup>30</sup> the exponential behavior, however, is still evidence for BCS superconductivity. Attempts to fit  $C_e(T)$  data for  $x = 0$  with the function  $be^{-(\Delta/T)}$  were unsuccessful. However, fits using a power-law function of the form  $cT^n$ , where  $c$  is a fitting parameter, were found to describe  $C_e(T)$  vs.  $T$  for  $x = 0$  very well, where  $n = 2.5$ . The change from  $cT^n$  to  $be^{-(\Delta/T)}$  temperature dependencies may be explained by a transition from a multi-band superconductor to a single-band isotropic  $s$ -wave superconductor.  $C_e(T) \sim T^n$  behavior is also expected for superconductors with nodes in the energy gap with  $n = 2$  for line nodes and  $n = 3$  for point nodes,<sup>29</sup> while  $C(T) \sim e^{-(\Delta/T)}$  behavior is expected for single-band isotropic  $s$ -wave superconductors. It should be noted that this type of analysis based on the temperature-dependence of the specific heat is believed to be valid at low-temperatures (i.e.  $T \ll T_c$ )<sup>29,30</sup>. However, our results, including the change of the temperature-dependence of the specific heat and the rapid initial suppression of  $T_c$ , are quite similar to those observed in the  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  system<sup>9</sup>; this matter has been further investigated by a recent study of the low-temperature specific heat, confirming a crossover in the superconducting gap structure.<sup>31</sup> Combining these factors, we believe that the change in the temperature-dependence of the specific heat is very likely intrinsic to  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ . Non-integer values of  $n$  can be due to the contributions to specific heat from multiple superconducting gaps, as was observed in  $\text{PrPt}_4\text{Ge}_{12}$ .<sup>8</sup> Our results suggest that multiband superconductivity may also occur in  $\text{LaPt}_4\text{Ge}_{12}$  as  $C(T)$  for this compound varies as  $T^{2.5}$  for  $T < T_c$ , which is consistent with a recent tunnel-diode-oscillator (TDO) and transverse-field muon-spin rotation (TF- $\mu$ SR) spectroscopy measurements on  $\text{LaPt}_4\text{Ge}_{12}$ , suggesting marginal two-gap superconductivity in  $\text{LaPt}_4\text{Ge}_{12}$ .<sup>32</sup> A non-integer value of  $n$  for Ce substitution may indicate that the system has been driven to single-band conventional superconductivity. The  $cT^n$  behavior of  $\text{LaPt}_4\text{Ge}_{12}$  was preserved with  $n = 2.4$  for  $\text{La}_{0.8}\text{Th}_{0.2}\text{Pt}_4\text{Ge}_{12}$ .

#### IV. DISCUSSION

The  $T_c$  vs.  $x$  curve for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  (blue symbols), derived from  $\rho(T)$ ,  $M(T)/H$ , and  $C(T)$ , is shown in Fig. 8. Dashed lines in the figure are guides to the eye. The  $T_c$  vs.  $x$  curve for  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  (red symbols) reported in Ref. [9] is also shown for comparison. Displayed in the inset is the  $T_c$  vs.  $x$  curve for  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$ . In  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ , the initial rate of suppression of  $T_c$ ,  $(dT_c/dx)_{x=0} = -0.4$  K/at. % Ce, is much larger in magnitude than  $(dT_c/dx)_{x=0} = -0.04$  K/at. % Th for  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$ . Because of the positive curvature of  $T_c$  vs.  $x$  in  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ , we were only able to approximate  $(dT_c/dx)_{x=0}$  for  $x \leq 0.1$  which yields  $(dT_c/dx)_{x=0} \sim -0.4$  K/at. % Ce, close to the value obtained for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ . The series  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  was found to exhibit a rapid and almost linear suppression of  $T_c$  with increasing Ce concentration, which extrapolated to 0 K near  $x \approx 0.2$ . While Ce substitution at low  $x$  produces a similar depression of  $T_c$  for both  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$

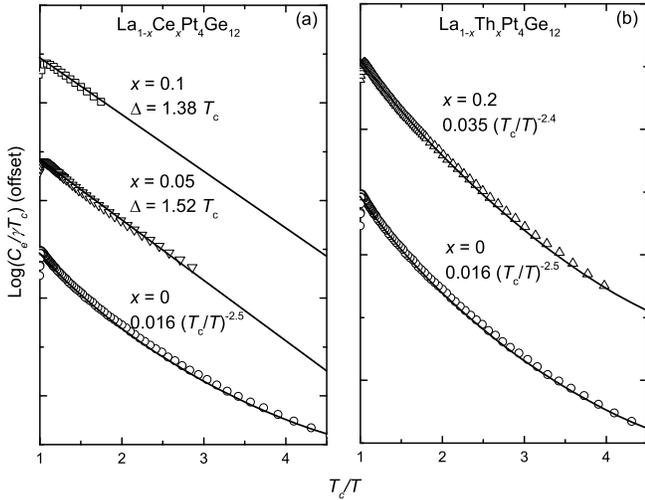


FIG. 7: (Color online) (a) and (b) The electronic contribution to specific heat plotted as  $\log(C_e/\gamma T_c)$  vs.  $T_c/T$  for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  and  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$ , respectively. The data sets were offset for clarity. For the  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  samples, the specific heat data are well described by an exponential temperature dependence of the form  $e^{-\Delta/T}$ , which is the expected behavior for an isotropic superconducting energy gap. However, the  $\text{LaPt}_4\text{Ge}_{12}$  and  $\text{La}_{0.8}\text{Th}_{0.2}\text{Pt}_4\text{Ge}_{12}$  data exhibit a power-law  $T^n$  temperature dependence where  $n \sim 2.5$ . This result may be consistent with multi-band superconductivity.

and  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ , at higher Ce concentrations, the  $T_c$  vs.  $x$  curve for  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  develops strong positive curvature and appears to extrapolate to 0 K at  $x \approx 0.4$ , roughly twice the value of  $x$  where  $T_c$  vanishes for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ .

The  $T_c$  vs.  $x$  curves for the  $\text{Ln}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  ( $\text{Ln} = \text{La}, \text{Pr}$ ) systems shown in Fig. 8 reveal that the rate of depression of  $T_c$  with Ce concentration is similar for the two systems, both of which have values of  $T_c \approx 8$  K at  $x = 0$ , for  $x \lesssim 0.1$ , and is significantly weaker for  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  than  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  for  $0.1 \lesssim x \lesssim 0.2$ . This reveals that the Ce substituents produce stronger superconducting electron pair breaking in the  $\text{LaPt}_4\text{Ge}_{12}$  compound, in which the electronic correlations are relatively weak and the superconductivity is conventional,<sup>11,12</sup> than in the  $\text{PrPt}_4\text{Ge}_{12}$  compound, where the electronic correlations are stronger and the superconductivity is unconventional (e.g., superconductivity breaks time-reversal symmetry).<sup>4-10</sup> Since the  $\text{CePt}_4\text{Ge}_{12}$  end member compound is also a correlated electron system,<sup>11</sup> the electronic correlations associated with the Ce solutes apparently have a stronger pair breaking effect on the conventional superconductivity exhibited by the  $\text{LaPt}_4\text{Ge}_{12}$  parent compound than on the unconventional superconductivity displayed by the  $\text{PrPt}_4\text{Ge}_{12}$  parent compound. The shapes of the  $T_c$  vs.  $x$  curves for the  $\text{Ln}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  ( $\text{Ln} = \text{La}, \text{Pr}$ ) systems are reminiscent of metallic host metals that exhibit conventional superconductivity containing transition metal, lanthanide, and actinide solute ions with partially-filled  $d$ - or  $f$ -electron shells in which the normal ground state at superconducting temperatures is nonmagnetic.<sup>33</sup> In these systems, a characteristic tem-

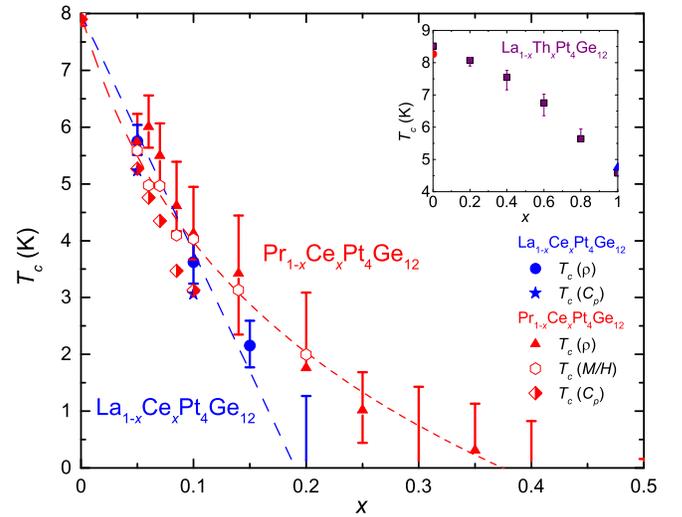


FIG. 8: (Color online) Plots of the superconducting transition temperature,  $T_c$  vs. Ce concentration,  $x$ , for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  (blue symbols) and, for comparison,  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  (red symbols) (Ref. [9]). The dashed lines are guides to the eye. The suppression of  $T_c$  with increasing  $x$  for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  is greater than in  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ . Whereas the  $T_c$  vs.  $x$  curve for  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  is nearly linear, the  $T_c$  vs.  $x$  curve for  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  exhibits positive curvature. Shown in the inset is the  $T_c$  vs.  $x$  curve for  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  (purple squares). The response of  $T_c$  with increasing  $x$  is smooth and continuous. The reported  $T_c$  values for  $\text{LaPt}_4\text{Ge}_{12}$  (Ref. [13]) and  $\text{ThPt}_4\text{Ge}_{12}$  (Ref. [3]) are added as a red circle and blue triangle for reference.

perature  $T_0$  associated with spin fluctuations, valence fluctuations, or the Kondo effect separates high temperature local moment behavior, characterized by a Curie-Weiss law, and low temperature nonmagnetic behavior, reflected in a magnetic susceptibility that approaches a finite value as  $T \rightarrow 0$  K. When  $T_0$  is much larger than the  $T_c$  of the superconducting host metal ( $T_{c0}$ ), the initial rate of depression of  $T_c$  can be quite large and have pronounced positive curvature, similar to that observed for  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ . This behavior is well established, and exemplary systems in which it has been observed include the  $\text{Al}_{1-x}\text{Mn}_x$ ,<sup>34</sup>  $\text{Th}_{1-x}\text{Ce}_x$ ,<sup>35</sup> and  $\text{Th}_{1-x}\text{U}_x$ <sup>36</sup> systems, where the Al and Th host metals are conventional superconductors. If one assumes that the temperature at which the magnetic susceptibility of the  $\text{Ln}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  ( $\text{Ln} = \text{La}, \text{Pr}$ ) samples attains a maximum value is of the order of the characteristic temperature  $T_0$ , then these systems are in the limit that  $T_0 \gg T_{c0}$  (e.g.,  $T_0 \sim 50 - 100$  K for both the La- and Pr-based systems). It is tempting to compare the  $T_c$  vs.  $x$  data with theories of superconductivity in host - impurity systems that display the Kondo effect, such as the theory of Müller-Hartmann and Zittartz.<sup>37</sup> However, these theories are based on the host metal being a simple one-band conventional BCS superconductor and for non-interacting paramagnetic impurities. The  $\text{Ln}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  ( $\text{Ln} = \text{La}, \text{Pr}$ ) compounds have complex Fermi surfaces with multiple sheets that apparently lead to multiband supercon-

ductivity,<sup>6-9</sup> large Ce solute concentrations in which the interactions between Ce ions increase with Ce concentration, and conventional superconductivity displayed by the La-based compound<sup>11,12</sup> and unconventional superconductivity exhibited by the Pr-based compound.<sup>4-10</sup>

Previous studies show that  $C(T)$  for  $\text{ThPt}_4\text{Ge}_{12}$  exhibits a  $T^3$  temperature dependence for  $T < T_c$ , which may suggest that there are point nodes in the superconducting energy gap.<sup>16</sup> If this interpretation is correct, the superconductivity exhibited by  $\text{ThPt}_4\text{Ge}_{12}$  could be unconventional. Therefore, chemical substitution between  $\text{ThPt}_4\text{Ge}_{12}$  and  $\text{LaPt}_4\text{Ge}_{12}$ , might be expected to result in a pronounced minimum in  $T_c(x)$  due to competing superconducting phases as was observed in studies of the filled skutterudite system  $\text{PrOs}_{4-x}\text{Ru}_x\text{Sb}_{12}$ ,<sup>18,19,38</sup> Instead, we observe a smooth and continuous  $T_c$  vs.  $x$  curve for  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$ , showing no evidence for competing superconducting phases. One possible explanation for this behavior is that both  $\text{LaPt}_4\text{Ge}_{12}$  and  $\text{ThPt}_4\text{Ge}_{12}$  may be multi-band superconductors, with each band exhibiting conventional BCS superconductivity. Band-structure calculations demonstrate that  $\text{ThPt}_4\text{Ge}_{12}$  exhibits multiple Fermi surface sheets, which is a requirement for multi-band superconductivity.<sup>17</sup> Additionally, the  $T^3$  temperature-dependence of the specific heat was used to suggest point nodes in the energy gap; however, the power-law temperature dependence of  $C(T)$  can also be evidence of multi-band superconductivity, as was suggested for  $\text{PrPt}_4\text{Ge}_{12}$ .<sup>8</sup> With respect to  $\text{LaPt}_4\text{Ge}_{12}$ , band-structure calculations also predict multi-band crossings at the Fermi energy,  $E_F$ .<sup>6</sup> When we combine this with the results from the present study, which show that the specific heat of  $\text{LaPt}_4\text{Ge}_{12}$  displays a power-law temperature-dependence in the superconducting state and that the response of superconductivity in  $\text{LaPt}_4\text{Ge}_{12}$  to Ce substitution is similar to that in the potential multi-band superconductor  $\text{PrPt}_4\text{Ge}_{12}$ ,<sup>6-9</sup> there is mounting evidence for multi-band superconductivity in  $\text{LaPt}_4\text{Ge}_{12}$ . The apparent similarity of the superconducting states of  $\text{LaPt}_4\text{Ge}_{12}$  and  $\text{ThPt}_4\text{Ge}_{12}$  reinforces this possibility. However, further work will be necessary to definitively address the nature of the superconducting energy gap(s) in  $\text{LaPt}_4\text{Ge}_{12}$ .<sup>29,39</sup>

## V. CONCLUDING REMARKS

The  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  and  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  systems were studied by means of electrical resistivity, magnetization, and specific heat measurements. The broad maxima in the  $\chi(T)$  data for  $\text{CePt}_4\text{Ge}_{12}$  were suppressed with increasing La concentrations, both in temperature and amplitude, which may be due to weakening of the Ce-Ce interactions with increasing La concentration. Superconductivity in the  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  system was rapidly suppressed with increasing Ce concentration, with no evidence for superconductivity down to 1.1 K for  $x > 0.2$ . The suppression of  $T_c$  in  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  is significantly more rapid than previously observed in  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ , supporting an interpretation that the superconductivity observed in these two systems is different in nature. Specific heat measurements in the superconducting state of  $\text{La}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$  revealed a change from a power-law to exponential temperature-dependence, similar to the results from a study on  $\text{Pr}_{1-x}\text{Ce}_x\text{Pt}_4\text{Ge}_{12}$ ; this may suggest that, although superconductivity in  $\text{LaPt}_4\text{Ge}_{12}$  is conventional, while it is unconventional in  $\text{PrPt}_4\text{Ge}_{12}$ , both may exhibit a crossover from multi-band superconductivity to single-band superconductivity with Ce substitution. In contrast,  $\text{LaPt}_4\text{Ge}_{12}$  and  $\text{ThPt}_4\text{Ge}_{12}$  appear to exhibit the same type of superconductivity as evidenced by the continuous and smooth behavior of  $T_c$  with increasing  $x$  in  $\text{La}_{1-x}\text{Th}_x\text{Pt}_4\text{Ge}_{12}$  and the power-law temperature-dependence of specific heat in the superconducting state.

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