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Probing the Pu^{4+} Magnetic Moment in PuF_4 with ¹⁹F NMR Spectroscopy

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Abstract

The magnetic fields produced by Pu^{4+} centers have been measured by ¹⁹F NMR spectroscopy to elucidate the Pu–F electronic interactions in polycrystalline PuF₄. Spectra acquired at applied fields of 2.35 and 7.05 T reveal a linear scaling of the ¹⁹F lineshape. A model is presented that treats the linebroadening and shifts as due to dipolar fields produced by Pu valence electrons in localized non-interacting orbitals. Alternative explanations for the observed lineshape involving covalent Pu–F bonding, superexchange interactions, and electronic configurations with enhanced magnetic moments are considered.

I. INTRODUCTION

Soon after the synthesis of the first transuranic elements, Seaborg proposed that the actinide elements were 5f analogs of the lanthanide (4f) series, as implied by the placement of the actinide row below the lanthanide row in the Periodic Table.¹ Heavy actinides have indeed been found to behave similarly to the lanthanides, but at plutonium there is a discontinuity whereupon lighter actinide elements exhibit physical and chemical properties more closely associated with transition metals.^{2–4} These trends suggest that Pu is the pivotal element to study for insights on the electronic structure of the actinide series.

Valence electrons in 4f and 5f shells, unlike lower angular momentum orbitals, may display atomic ("localized") or band-like ("itinerant") character depending on the degree of hybridization with electrons of neighboring atoms. This duality underlies many phenomena unique to lanthanide and actinide compounds such as extremely slow conduction electrons with large mass renormalization ("heavy fermions"),⁵ unusual quadrupolar (or higher) magnetic ordering,⁶ and unconventional superconductivity.^{7–10} The complexity of the electronic structure of Pu is illustrated by a recent study of δ -Pu, wherein a theory involving a novel fluctuating valence ground state was developed to describe the lack of magnetism.¹¹

To better understand the behavior of electrons in Pu, comparisons of compounds with isostructural lanthanide counterparts are instructive. One such system is PuF_4 ,^{12,13} which has both lanthanide and other actinide analogs.¹⁴ In spite of their simple stoichiometry, actinide tetrafluorides AnF_4 exemplify the difficulties of relating f-electron configurations to observed properties. The metal is coordinated to eight fluorine atoms in the structure of the tetrafluoride compounds (Fig. 1), and thus these cannot be straightforwardly portrayed as a lattice formed by ions with formal charges (An^{4+}) $(F^-)_4$. The number of electrons per unit cell is even, suggesting that PuF_4 is a band insulator, but to our knowledge this prediction has not been confirmed. Previous magnetic susceptibility measurements indicate a paramagnetic system consistent with a 5f⁴ configuration.¹⁵ Specific heat data reveal no sign of ordering down to 10 K,¹⁶ despite a substantial antiferromagnetic coupling among the Pu moments, as evidenced by the Curie-Weiss temperature of $\Theta = 290$ K.¹⁵ X-ray photoelectron spectroscopy measurements in isostructural UF₄ showed some covalent character for the felectrons¹⁷ even though the magnetic susceptibility obeys Curie-Weiss behavior consistent with local moment paramagnetism.¹⁸

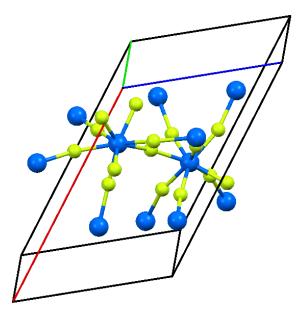


FIG. 1. Monoclinic crystal structure of PuF_4 illustrating the coordination of Pu (blue) with eight fluorine atoms (green) and the near linearity of the Pu-F-Pu bridges.

The possibility of probing f-electrons through their interactions with nuclear spins makes nuclear magnetic resonance spectroscopy (NMR) an appealing approach for investigating the magnetism of actinide compounds. While NMR investigations in strongly correlated electron materials often focus on the temperature dependence of Knight shifts and relaxation times,¹⁹ lineshapes of NMR signals from ligand nuclei can also be used to infer details on the electronic configuration of paramagnetic metal centers surrounding the ligand.²⁰ Actinide and lanthanide tetrafluorides, with their high density of the NMR-favorable ¹⁹F isotope, are attractive for such experiments.

II. EXPERIMENTAL

A. Sample description

The PuF₄ sample used here was drawn from a stock of powder produced at the U.S. D.O.E.'s Hanford Site Plutonium Finishing Plant.²¹ Plutonium and americium isotope contents were measured in triplicate by thermal ionization mass spectrometry and gamma spectrum analysis (Table I). The NMR sample (mass = 581 mg) was doubly contained in robust nested capsules made with PEEK (OD = 7.5 mm). The ¹⁹F NMR background of the

PEEK capsules was negligible in comparison to the PuF₄ signal. *Caution:* Plutonium-239 is an alpha emitter (specific activity = 2.30×10^9 Bq/g) that presents both radioactivity and toxicity hazards. All sample manipulations were performed in the Radiochemical Processing Laboratory, which is a U.S. Department of Energy Category 2 nuclear facility located at the Pacific Northwest National Laboratory.

TABLE I. Plutonium isotope distribution in the PuF_4 NMR sample. The ²⁴¹Am content was found by gamma spectral analysis to be 0.0050 m/m relative to ²³⁹Pu.

Isotope	Mass fraction normalized to total Pu		
	GEA^{a}	$\mathrm{TIMS^{b}}$	
²³⁸ Pu	ND^{c}	0.0001	
²³⁹ Pu	0.9339	0.9416	
²⁴⁰ Pu	0.0656	0.0576	
²⁴¹ Pu	0.0004	0.0005	
242 Pu	ND^{c}	0.0002	

^a GEA: gamma energy analysis.

^b TIMS: thermal ionization mass spectrometry.

^c ND: not detected.

B. Spectroscopy

Data were acquired at ambient temperatures with 2.35 and 7.05 Tesla superconducting magnets, corresponding to ¹⁹F Larmor frequencies of 93.62 and 282.41 MHz, respectively. Both instruments were equipped with Redstone consoles from Tecmag, Inc. The ¹⁹F NMR frequency scale was referenced with 0.01 M NaF dissolved in 1.0 M NaClO₄(aq) at room temperature.²² Radiofrequency (rf) field amplitudes (B_1) were calibrated with nutation experiments on a concentrated NaF(aq) solution.

A two-pulse solid echo experiment²³ and a 16 step phase cycle²⁴ were used to detect the PuF_4 ¹⁹F signal. Refocusing times for the echo were 8-12 μ s. The inhomogeneously broadened PuF_4 ¹⁹F resonance was recorded in a piecewise fashion by stepping the spectrometer carrier frequency across the entire spectral region. The signal intensity at each frequency was obtained by integrating the Fourier transform of the echo signal. The output of the rf amplifier was monitored and adjusted as needed to provide a constant field amplitude at each frequency step of the spectrum. The spectrum was measured with several B_1 field amplitudes ranging between 0.1 to 0.9 mT in the rotating frame. Signal intensities were greater with increased B_1 fields, but the overall lineshape was unchanged, and no sign of power broadening was observed.

Spin-lattice relaxation times (T_1) were determined by the saturation recovery method. Fig. 2 shows the integrated NMR signal intensity as a function of the magnetization recovery time, measured in the 2.35 T field. A two-step recovery is observed. A slow recovery signal appears within a 200 kHz range around the ¹⁹F Larmor frequency, and can be assigned to diamagnetic fluorinated parts in the housing and circuit of the probe. The T_1 of this signal was found to be more than 100 times longer than the $T_1(\sim 1 \text{ ms})$ of the second relaxation process, which we assign to PuF₄. The measured relaxation time of PuF₄ varied by less than 14% over the entire frequency range and was found to be the same at both fields. Because of the disparity in relaxation times, the background signal could be selectively attenuated by applying a saturating pulse train and delaying acquisition of the echo transient by a time long compared to the PuF₄ T_1 but short relative to the background signal recovery time.

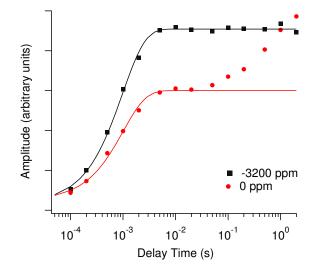


FIG. 2. Integrated ¹⁹F NMR signal intensities vs. delay time for PuF_4 measured at 2.35 T. Measurements at the two indicated frequencies in the inhomogeneously broadened line shape are shown, along with fits to a single exponential recovery function.

III. RESULTS AND DISCUSSION

Fluorine-19 NMR spectra acquired in a stepped frequency mode as described above appear in Fig. 3. Spectral data are presented in accordance with the recommendation of the IUPAC,²⁵ which specifies line positions in terms of a scaled shift from the signal of a reference compound

$$\delta = \frac{\nu - \nu_{\rm R}}{\nu_{\rm R}} \times 10^{6}$$
$$= \frac{\sigma_{\rm R} - \sigma}{1 - \sigma_{\rm R}} \times 10^{6}, \tag{1}$$

where ν and $\nu_{\rm R}$ represent the NMR frequencies of the sample and reference nuclei, respectively, and σ refers to the absolute shielding parameter (in ppm). The position of the ¹⁹F resonance of hydrated F⁻ on the shift scale having CFCl₃ as the reference compound is -125.0 ppm.²⁶

The anisotropic local magnetic fields giving rise to the experimental spectra in Fig. 3 were modeled by a second rank Cartesian tensor with principal values δ_{xx} , δ_{yy} , and δ_{zz} , which are proportional to the applied field and can be extracted from the ¹⁹F lineshapes by fitting the experimental points to the function^{27,28}

$$\delta = \delta_0 + \frac{1}{2}\delta_1 \left[\left(3\cos^2\theta - 1 \right) - \eta \sin^2\theta \cos 2\phi \right],\tag{2}$$

where δ_0 , δ_1 , and η are defined according to the standard expressions

$$\delta_0 \equiv \frac{1}{3} \left(\delta_{xx} + \delta_{yy} + \delta_{zz} \right)$$
$$\delta_1 \equiv \delta_{zz} - \delta_0,$$
$$\eta \equiv \frac{\delta_{yy} - \delta_{xx}}{\delta_1},$$

with $|\delta_{zz} - \delta_0| \geq |\delta_{xx} - \delta_0| \geq |\delta_{yy} - \delta_0|$, and θ and ϕ are the longitudinal and azimuthal angles, respectively, describing the orientation of the principal axis system of the tensor with respect to the applied field \mathbf{B}_0 . The δ_{jj} obtained from the fit of Eq. (2) to the experimental data appear in Table II. Two fits were performed, one in which δ_{xx} , δ_{yy} , and δ_{zz} were allowed to vary freely, and another in which the shift tensor was forced to be axially symmetric as proposed by Gabuda et al. for the isostructural compound UF₄.²⁹ The non-axial function was statistically superior to the axial function in modeling the spectra, even accounting for the extra adjustable parameter in the former. A spectrum comparable in appearance

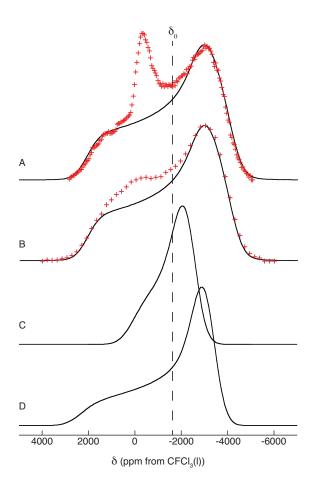


FIG. 3. Fluorine-19 spectra of PuF₄(s). Experimental spectral intensities were measured as a function of the spectrometer carrier frequency at magnetic fields of 7.05 T (A) and 2.35 T (B), and are indicated by red crosses. Solid curves in A and B are fits of the function in Eq. (2) to the experimental data; non-fitted features centered at ~ 0 ppm are from residual ¹⁹F background signal. Simulated spectra were computed with models that assume 5f⁴ (C) and 5f³ 6d¹ (D) Pu electronic configurations (*vide infra*); these spectra have been centered at the same isotropic shift frequency as A and B ($\delta_0 = -1620$ ppm) symbolized by the dashed line. Note that at fixed field, energy increases from right to left on the δ scale.

and slightly narrower in width has been observed for UF₄ ($\sim 3 \text{ mT}$, corresponding to 4920 ppm).²⁹

Absolute shielding parameters can be ascertained from the shifts in Table II using data from Hindermann and Cornell, who reported a value of $\sigma_0 = +188.7$ ppm for liquid CFCl₃ based on a calculated shielding of $\sigma_0 = +410.0$ ppm for HF(g).^{30,31} The principal values of the shielding tensor computed in this way from the non-axial shift tensor are (in ppm)

	ppm from $CFCl_3(l)$			
	δ_{xx}	δ_{yy}	δ_{zz}	η
Axial	-3489	-3489	2118	0.00
Non-axial	-4078	-2900	2118	0.32

TABLE II. Fitted shift parameters for PuF_4 ¹⁹F spectra. Spectra calculated with the non-axial tensor appear in Figs. 3A and 3B. The model spectra were convolved with a Gaussian function (FWHM = 1100 ppm) as part of the fitting process.

 $(\sigma_{xx}, \sigma_{yy}, \sigma_{zz}) = (4267, 3089, -1929);$ adjustments can be readily made through addition or subtraction of a constant offset as improved estimates of $\sigma_0(\text{CFCl}_3)$ become available.³²

The shifts and lineshapes of the observed spectra in Fig. 3 are determined by the cumulative effects of 19 F- 19 F dipolar couplings, the chemical shift, and hyperfine couplings to unpaired electrons at the metal. The contribution of the homonuclear dipolar interaction to the 19 F linewidth was evaluated using C⁺⁺ computer programs written with object code from the GAMMA simulation environment.³³ These calculations reveal an inhomogeneous broadening of <40 kHz from the dipolar coupling with powder averaging, consistent with nearest neighbor F–F distances of 2.6 – 2.8 Å. This interaction is small relative to the overall linewidth, and moreover, is field independent in magnitude, contrary to the observation of a linear scaling of the experimental spectra with respect to the field. Its effects can evidently be neglected at the magnetic fields considered in this work.

Chemical shift tensors for PuF_4 have not been reported, but ¹⁹F data are available for the isostructural compound CeF_4 ,³⁴ which has a tetravalent metal center with an ionic radius close to Pu^{4+} . Magnitudes of the chemical shift anisotropies (CSA) of the seven fluorine sites in CeF₄ average 385 ppm, which is an order of magnitude smaller than the anisotropies indicated by Table II. The effects of the chemical shift tensor will also be ignored.

The NMR shifts of nuclei interacting with paramagnetic d- or f-electron centers have been discussed in detail by Shulman and Jaccarino.²⁰ Gabuda et al.²⁹ and Martel et al.³⁵ have proposed that the field dependent anisotropic hyperfine shifts in paramagnetic tetravalent actinide systems can be approximated as a dipolar field produced by localized, unpaired

electrons at the An^{4+} sites

$$H_{\rm F} = \sum_{j=1}^{N} \frac{\langle \mu_j \rangle}{r_j^3} \left(3\cos^2\theta_j - 1 \right),\tag{3}$$

where r_j is the distance between the fluorine nucleus and the center, θ_j is the angle between the electronic-nuclear vector and the applied field direction, and the sum is over N nearby paramagnetic centers. The parameter $\langle \mu_j \rangle$ is the magnetic moment of the *j*th paramagnetic center, which in the limit of short electronic relaxation times can be approximated by its thermodynamic average.²⁰ To estimate the magnitude of the hyperfine field $H_{\rm F}$, $\langle \mu_j \rangle$ was calculated for a 5f⁴ configuration according to

$$\langle \mu_j \rangle = g\mu_B J B_J(H,T),\tag{4}$$

using the appropriate Brillouin function B_J .³⁶ The value obtained ($\langle \mu_j \rangle = 0.038 \ \mu_B$, corresponding to a hyperfine field of ~3.5 mT at B = 7.05 T, T = 300 K, with $g_J = \frac{3}{5}$ and J = 4) is found to be in good agreement with experimental susceptibility at 300 K in the dilute limit of a Th_{1-x}Pu_xF₄ ($0 \le x \le 1$) solid solution.^{37,38} Note that the susceptibility per Pu⁴⁺ in pure PuF₄ is about 40% smaller than in the dilute compound. The calculated average moment was then used to compute H_F for each of the seven crystallographically distinct fluorine sites, with the sum carried out over the two nearest Pu⁴⁺ centers, which range between 2.230 and 2.354 Å in distance from fluorine atoms. Using these anisotropic fields, orientationally averaged powder ¹⁹F spectra were independently calculated for the seven sites and summed, weighted by the multiplicity of each F site within the unit cell, with the result shown in Fig. 3C. The program created for the spectral simulations utilized GAMMA object code for the computation of the nuclear spin dynamics.³³

As seen in Fig. 3C, the simulated spectrum for the 5f⁴ configuration predicts a smaller linewidth than was observed experimentally, suggesting that the fluorine local magnetic fields have been underestimated. The magnitude of the computed hyperfine dipolar field can be increased by assuming an alternative electronic configuration for Pu⁴⁺ with a larger magnetic moment. For example, the 5f³ 6d¹ configuration, with $g_J = \frac{8}{11}$ and $J = \frac{9}{2}$, gives $\langle \mu_j \rangle = 0.084 \ \mu_B$ including the 6d¹ spin in an applied field of 7.05 T and T = 300 K. In contrast to 5f⁴, the prediction for the 5f³ 6d¹ configuration appears to overestimate the magnitude of the local field (Fig. 3D), which implies that an admixture of the two configurations would lead to better agreement. In particular, a linear combination of 80% (5f³ 6d¹) and 20% (5f⁴), corresponding to a moment $\langle \mu_j \rangle = 0.075 \ \mu_B$, is consistent with the experimental linewidth. This value is also close to the moment calculated for the 5f² configuration assumed for UF₄²⁹ and would explain the similar widths of the experimental spectra in the two compounds. However, a different value of the effective moment is determined from magnetic susceptibility measurements. In fact, PuF₄ appears to have a slightly larger effective moment $\mu_{\text{eff}} = g\sqrt{J(J+1)}\mu_B$ than expected for a 5f⁴ configuration ($\mu_{\text{eff}} = 2.90 \ \mu_B$ instead of 2.68 μ_B)¹⁵ but this would correspond to at most a 23% 5f³ 6d¹ admixture. A similar discrepancy has been reported for UF₄, in which the moment of the electronic configuration (5f²) differs from the effective moment indicated by magnetic susceptibility data.¹⁸ Alternatively, superexchange type antiferromagnetic correlations between Pu local moments mediated by the fluorine ligands may enhance the hyperfine field to the magnitudes implied by the ¹⁹F NMR line widths.

A purely dipolar coupling of the F nuclei to localized f-electrons has no isotropic component, and therefore cannot account for a non-zero absolute shielding of the ¹⁹F NMR line. The shielding observed here for PuF_4 can be estimated from the experimental ¹⁹F spectra using results from Hindermann and Cornell³⁰ to be +1809 ppm. X-ray photoelectron spectra (XPS) show evidence of a significant delocalization of one of the two 5f electrons in UF_4 ,¹⁷ and an admixture of $4f^{0}5d^{1}$ and $4f^{1}$ configurations in CeF₄.³⁹ No similar experiments have been reported in PuF₄ but covalency in the Pu–F bonds and mixed valency in this compound can be expected to induce non-zero isotropic shifts in PuF₄ and related actinide tetrafluorides.

IV. CONCLUSION

Fluorine-19 NMR spectra reveal that local magnetic fields in PuF_4 and UF_4 are similar, despite the former having nominally four valence electrons and the latter two. Analyses that assume purely localized 5f⁴ (for PuF_4) and 5f² (for UF_4) electron configurations for the metal centers systematically underestimate the magnitudes, shifts, and anisotropy of the hyperfine field as measured by the ¹⁹F NMR linewidths. Plausible modifications of the hyperfine interaction that could account for the enhanced field are admixture of higher energy electron configurations, hybridization of f-electron density with ligand orbitals, and inclusion of superexchange effects.

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