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Vortex-like excitations in the heavy-fermion superconductor CeIrIn₅

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We report a systematic study of temperature- and field-dependent charge (ρ) and entropy (**S**) transport in the heavy-fermion superconductor CeIrIn₅. Its large positive thermopower S_{xx} is typical of Ce-based Kondo lattice systems, and strong electronic correlations play an important role in enhancing the Nernst signal S_{xy} . By separating the off-diagonal Peltier coefficient α_{xy} from S_{xy} , we find that α_{xy} becomes positive and greatly enhanced at temperatures well above the bulk T_c . Compared with the non-magnetic analog LaIrIn₅, these results suggest vortex-like excitations in a precursor state to unconventional superconductivity in CeIrIn₅. This study sheds new light on the similarity of heavy-fermion and cuprate superconductors and on the possibility of states not characterized by an order parameter.

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Typically, a disorder-order phase transition is described within the context of Ginzburg-Landau theory by an order parameter and identified by a spontaneously broken symmetry. From this point of view, a superconducting transition might be special. The order parameter of superconductivity (SC) is expressed by a complex function in the form $\Psi_s(\mathbf{r}) = |\Psi_s(\mathbf{r})| e^{i\theta(\mathbf{r})\mathbf{1}}$. Gauge symmetry is broken after phase coherence is established throughout the system. When the phase stiffness is strong, phase coherence develops *concomitantly* as Cooper pairs form, and the superconducting critical temperature T_c is mainly determined by T^{MF} , the mean-field transition temperature predicted by the BCS theory². In contrast, if the superfluid density is small (e.q. in underdoped cuprates and organic superconductors), the phase stiffness is low, and the phase coherence can be destroyed by short-lived vortex-like excitations. In this situation, bulk SC cannot be realized until the phases of Cooper pairs are ordered, and T^{MF} is simply the characteristic temperature below which pairing becomes significantly local $(T^{MF} \gg T_c)^3$. As learned from the cuprates, states without a well-defined order parameter emerge above T_c and include phenomena such as superconducting phase fluctuations, pre-formed Cooper pairs, and a pseudogap.

The $CeMIn_5$ (M=Co, Rh and Ir) family of tetragonal heavy-fermion compounds is useful platform to investigate the interplay among unconventional SC, antiferromagnetic (AFM) order and spin fluctuations in the vicinity of quantum criticality. The member CeRhIn₅ is an incommensurate antiferromagnet at ambient pressure with Néel temperature $T_N=3.8 \text{ K}^{4,5}$ and can be pressurized into a superconducting state with the highest $T_c \sim 2.2$ K achieved around 2.35 GPa where $T_N(p)$ extrapolates to zero^{6,7}. Textured SC was observed in the region where SC and AFM coexist, characterized by vanishingly small resistivity well above the bulk T_c and the anisotropic resistive $T_c^{\ 8}$, reminiscent of the nematic state observed in cuprates. In this pressure range, nuclear quadrupole resonance (NQR) experiments suggested the presence of a pseudogap that develops above $T_N(P)$ and extrapolates to the maximum in $T_c(P)^9$. Likewise, scanning tunneling spectroscopy revealed a pseudogap that coexists with d-wave SC in CeCoIn₅^{10,11}, and replacing a small amount of In by Cd induces coexisting AFM order and SC in $CeCo(In_{0.99}Cd_{0.01})_5$ where again a transition to zero resistance appears well above the bulk T_c^{12} . Pristine CeIrIn₅ shows filamentary $SC^{13,14}$ at atmospheric pressure with a resistive onset temperature $T_c^{on}=1.38$ K, but a diamagnetic state appears only below $T_c^b \simeq 0.5$ K [This is also illustrated in Fig. 1(a)]. Although no direct evidence of magnetic order has yet been identified, chemical substitutions of Hg/Sn on the In site demonstrate that the SC in CeIrIn₅ is in proximity to an AFM quantum-critical point¹⁵. Careful magnetoresistance and Hall effect studies of CeIrIn₅ found evidence for a precursor state of unknown origin arising near 2 K in the limit of zero field^{16,17}. Though the pressure dependence of the precursor state is unknown, the resistive and bulk $T_{\rm c}$ s approach each other at the maximum in a dome of bulk SC^{18} , suggesting the possibility that the precursor state may be competing with SC. The complex interplay among states in the $CeMIn_5$ superconductors bears strikingly similarities to the cuprates, with pure CeIrIn₅ at atmospheric pressure presenting an opportunity to examine more closely these similarities.

From electrical (ρ) and thermoelectric (**S**) transport measurements in CeIrIn₅ and a comparison to its non-4f counterpart LaIrIn₅, we identify signatures of vortexlike excitations well above T_c^{on} (T_c^b). These findings suggest the existence of a pseudogap-like state where Cooper pairs start to form locally at a temperature well above T_c^{on} , but phase coherence among pairs is destroyed by thermally activated vortex-like excitations, pointing to a common framework for the physics of such states in both heavy-fermion and cuprate¹⁹.

Single crystalline CeIrIn₅ was grown from an indium flux method¹³. The crystal was pre-screened by both resistivity and magnetic susceptibility measurements to ensure the absence of free In. Thermoelectric measurements were carried out by means of a steady-state technique. A pair of well calibrated differential Chromel-Au_{99,93%} Fe_{0.07%} thermocouples was used to measure the temperature gradient. Upon a thermal gradient $-\nabla T \| \mathbf{x}$ and a magnetic field $\mathbf{B} \| \mathbf{z}$, both thermopower signal $S_{xx} = -E_x/|\nabla T|$ and Nernst signal $S_{xy} = E_y/|\nabla T|$ were collected by scanning field at fixed temperatures. The same contact geometry also was used to measure electrical resistivity (ρ_{xx}) and Hall resistivity (ρ_{yx}). Both electrical and thermal currents were applied along the **a**axis, and the magnetic field was parallel to **c**. The same measurements were performed on the non-magnetic analog LaIrIn₅ for comparison. We adopt the sign convention as Ref.²⁰, which defines a *positive* Nernst signal for vortex motion^{21,22}.



FIG. 1. (Color online) (a) Temperature dependence of ρ_{xx} (blue), χ_{ac} (green) and S_{xx} (red) of CeIrIn₅, showing $T_c^{on}=1.38$ K and $T_c^b=0.5$ K. (b) Comparison of $S_{xx}(T)$ for CeIrIn₅ and LaIrIn₅.

In the presence of a temperature gradient $-\nabla T$, an electric field **E** and a magnetic field **B**, the total current density is $\mathbf{J}=\boldsymbol{\sigma}\cdot\mathbf{E}+\boldsymbol{\alpha}\cdot(-\nabla T)$, where $\boldsymbol{\sigma}$ is the conductivity tensor, and $\boldsymbol{\alpha}=\frac{\pi^2k_B^2T}{3q}\frac{\partial\boldsymbol{\sigma}}{\partial\varepsilon}|_{\varepsilon=\varepsilon_F}$ (k_B is Boltzman constant, q is charge of carriers, ε_F is chemical potential) is the Peltier conductivity tensor²³. In an equilibrium state without net current, the Boltzman-Mott transport equation deduces the thermoelectric tensor

$$\mathbf{S} = \boldsymbol{\alpha} \cdot \boldsymbol{\sigma}^{-1} = \boldsymbol{\alpha} \cdot \boldsymbol{\rho}. \tag{1}$$

We start with the temperature dependence of thermopower $S_{xx}(T)$ as shown in Fig. 1(b). $S_{xx}(T)$ of LaIrIn₅ is positive at room temperature and changes sign near 150 K, characteristic of the expected multi-band behavior²⁴. In contrast, $S_{xx}(T)$ of CeIrIn₅ is positive in the full temperature range between 0.3 K and 300 K, displaying a pronounced maximum at around 25 K with the magnitude reaching 76 μ V/K. This peak in $S_{xx}(T)$ is associated with the onset of Kondo coherence²⁵. These features are consistent with a Ce-based Kondo lattice in which the strong hybridization between 4f- and conduction-electrons forms a Kondo resonance with the density of states $N(\varepsilon)$ asymmetric with respect to $\varepsilon_F^{26,27}$ (see below). At low temperatures, $S_{xx}(T)$ shows a small kink at $T_c^{on} = 1.38$ K, but drops sharply at 0.7 K and tends to saturate below $T_c^b=0.5$ K [cf Fig. 1(a)]. Down to the lowest temperature of 0.3 K, however, $S_{xx}(T)$ still remains finite. We attribute this non-vanishing S_{xx} in the bulk superconducting state to the low T_c^b of CeIrIn₅: even

a small temperature gradient may generate ungapped quasiparticles that contribute transport entropy.



FIG. 2. (Color online) (a) Field dependence of S_{xx} of CeIrIn₅ at selected temperatures. (b) and (c) display $\rho_{xx}(B)$ and $\rho_{yx}(B)$, respectively.

Figure 2(a) displays isothermal field dependence of S_{xx} at various temperatures. For all temperatures, the magneto-thermopower is positive. One important feature of $S_{xx}(B)$ is a valley in the vicinity of zero field. As temperature decreases, this valley deepens and evolves into a cusp when $T \leq 3$ K. At 0.3 K, S_{xx} is small at B=0 but recovers when the field is larger than 1.6 T. With the field dependencies of ρ_{xx} and ρ_{yx} shown in Fig. 2(b) and (c), respectively, it is reasonable to attribute this small transport-entropy state to a SC state. The cusp in $S_{xx}(B)$ occurring near 3 K is indicative of the loss of transport entropy well above T_c^b . The critical field recovering a normal state, however, is much smaller than that determined from $\rho_{xx}(B)$ [Fig. 2(b)] and $\rho_{yx}(B)$ [Fig. 2(c)]. Systematic analysis of $\rho_{xx}(B)$ and $\rho_{yx}(B)$ by Nair *et al.*^{16,17} showed that the modified Kohler's scaling $[\Delta \rho_{xx}(B)/\rho_{xx}(0) \propto \tan^2 \theta_H$, where $\theta_H = \arctan(\rho_{yx}/\rho_{xx})$ is the Hall angle] breaks down prior to T_c^{on} , the region where we observe a large Nernst effect (see below). Similar phenomenon was observed in $CeCoIn_5$ and $CeRhIn_5$ under pressure²⁸, as in cuprates, and is reminiscent of a pseudogap-like precursor state²⁹.

In Fig. 3 we present the field dependence of the Nernst signal S_{xy} , the off-diagonal term of the thermoelectric tensor **S**. $S_{xy}(B)$ is both negative and linear in B at 20 K. The magnitude of $S_{xy}(B)$ decreases with decreasing T and changes sign near 15 K [Fig. 3(a)]. The nonlinearity of $S_{xy}(B)$ becomes pronounced and the value of S_{xy} rapidly increases with decreasing T. At 2 K, S_{xy} reaches 7 μ V/K when B is 9 T. We will see that such a large S_{xy} , even larger than that in the vortex-liquid state of cuprates^{21,22}, is mainly due to the Kondo effect, albeit the vortex-like excitation contribution is also non-negligible. A large Nernst effect also has been seen



FIG. 3. (Color online) Nernst signal S_{xy} of CeIrIn₅ as a function of B at selected temperatures. (a), $0.3 \le T \le 2.0$ K; (b), $2 \le T \le 20$ K.

in other Kondo-lattice compounds, like $CeCoIn_5^{30-32}$, $CeCu_2Si_2^{33}$, $URu_2Si_2^{34}$ and SmB_6^{35} . In CeIrIn₅ S_{xy} starts to drop when T is lower than 2 K but remains positive down to 0.3 K, the base temperature of our measurements [Fig. 3(b)]. At 0.3 K, which is below T_c^b , $S_{xy}(B)$ increases slowly at small field but much more rapidly near 1.8 T. It is likely that this 1.8 T magnetic field defines a melting field B_m above which the vortex solid melts into a vortex-liquid state. A large number of vortices start to move in response to a temperature gradient and this results in the abrupt increase in $S_{xy}(B)$. Similar results also have been seen in other type-II superconductors, like $cuprates^{21,22}$ and $CeCoIn_5^{31}$. This vortex-lattice melting field disappears immediately when T exceeds T_c^b , e.g. 0.55 K as shown in Fig. 3(b). This implies that a welldefined Abrikosov- lattice of vortices only exists in the bulk superconducting state of CeIrIn₅.

Figure 4(a) shows the temperature dependence of the Nernst coefficient $\nu_N \equiv S_{xy}/B$. Here, the solid symbols are obtained at B=9 T, and the open symbols represent the initial slope of $S_{xy}(B)$ as $B\rightarrow 0$. In both definitions, ν_N above T_c^{on} is large and sign-changes near 15 K. It is well known that for a single-band, non-superconducting and non-magnetic metal, the Nernst signal is vanishingly small, due to so-called Sondheimer cancellation³⁶,

$$S_{xy} = \rho_{xx} \alpha_{xy} - S_{xx} \tan \theta_H. \tag{2}$$

A large Nernst effect has been observed in: (i) multi-band systems such as $NbSe_2^{37}$ in which the ambipolar effect violates Sondheimer cancellation; (ii) phase slip due to vortex motion in type-II superconductors, as in underdoped



FIG. 4. (Color online) (a) Temperature-dependent Nernst coefficient ν_N of LaIrIn₅ and CeIrIn₅. For CeIrIn₅, the open symbols are the initial slopes of $S_{xy}(B)$ as $B \rightarrow 0$. (b) and (d) show the separation of $\rho_{xx}\alpha_{xy}$ from S_{xy} at T=6 K for CeIrIn₅ and LaIrIn₅, respectively. (c) Off-diagonal Peltier coefficient α_{xy} as a function of B at selected temperatures. (e) Contour plot of $\alpha_{xy}(B,T)$, with the resistively determined $B_{c2}(T)$ shown in the lower left corner. The black dash line is the boundary where $\alpha_{xy}=0$.

cuprates^{21,22}; (iii) ferromagnets like CuCr₂Se_{4-x}Br_x in which $S_{xy}(B)$ scales to magnetization M(B), known as anomalous Nernst effect³⁸; (iv) Kondo-lattice systems, like CeCu₂Si₂, in which an enhanced ν_N is determined by asymmetry of the on-site Kondo scattering rate³³.

We can exclude the anomalous Nernst effect in CeIrIn₅ because $S_{xy}(B)$ does not scale with the magnetization, which is essentially a linear function of B (data not shown). From the negative Hall resistivity $\rho_{yx}(B)$ shown in Fig. 2(c), we also rule out a substantive contribution from skew scattering because, as discussed in Refs.^{28,39}, it generates a *positive* anomalous Hall effect for Ce ions.

To study a possible multiband contribution to the Nernst signal of CeIrIn₅, we performed the same measurements on the non-4f counterpart LaIrIn₅. According to quantum oscillation measurements and density func-

tional theory (DFT) calculations, LaIrIn₅ is electron-hole compensated^{24,40}, and a large Nernst effect is possible³⁷. The Nernst signal of LaIrIn₅, however, is surprisingly both negative and linear in *B* [see Fig. 4(d) for instance], and most importantly, the Nernst coefficient remains small between 0.3 K and 20 K [Fig. 4(a)]. This demonstrates that a multiband effect does not play an important role in LaIrIn₅. Compared with LaIrIn₅, CeIrIn₅ has a somewhat larger Fermi surface due to a partially itinerant 4*f*-band²⁴, electron-hole compensation is relatively unbalanced, and, therefore, a multiband contribution to the Nernst signal of CeIrIn₅ is expected to be even weaker.

To better understand the origin of a large Nernst effect in CeIrIn₅, we separate $\rho_{xx}\alpha_{xy}$ from the total Nernst signal S_{xy} [cf Eq. (2)]. As an example, we show S_{xy} , $\rho_{xx}\alpha_{xy}$ as well as $-S_{xx}\tan\theta_H$ at 6 K in Fig. 4(b). As seen, $-S_{xx}\tan\theta_H$ is the dominant contribution to S_{xy} . In a Kondo-lattice system, strong electronic correlations build up a resonance in the density of states near the chemical potential ε_F , and the scattering rate $(1/\tau)$ is now mainly determined by the very narrow, renormalized 4f-bands, *i.e.* $N_f(\varepsilon)$. As a result, the thermopower, given by Eq. (3), becomes large⁴¹

$$S_{xx} \propto \frac{\partial \ln \tau}{\partial \varepsilon} \propto -\frac{\partial \ln N_f(\varepsilon)}{\partial \varepsilon}|_{\varepsilon=\varepsilon_F}$$
 (3)

due to an asymmetric $N_f(\varepsilon)$ and is reflected in data plotted in Fig. 1(b). This asymmetry of on-site Kondo scattering also enters S_{xy} through the term $-S_{xx} \tan \theta_H$ and gives rise to the large Nernst effect in CeIrIn₅ and other Kondo-lattice systems as well^{30,31,33,35}.

We note that $-S_{xx} \tan \theta_H$ surpasses S_{xy} when B is larger than 7.3 T at 6 K, and this leads to a sign change in $\rho_{xx}\alpha_{xy}$ [Fig. 4(b)]. Figure 4(c) shows the field dependent α_{xy} at various temperatures. Due to a large contribution from asymmetric Kondo scattering in $S_{xy}(B)$, $\alpha_{xy}(B)$ clearly differs from $S_{xy}(B)$ and, therefore, more intrinsically describes the off-diagonal thermoelectric response. $\alpha_{xy}(B)$ is negative and linear in B at 20 K. As T decreases, an anomalous positive term gradually appears on top of the negative linear background. Similar behavior was observed in CeCoIn₅ and was interpreted as a signature of phase-slip events caused by the passage of individual vortices³¹. To compare, we show $\rho_{xx}\alpha_{xy}$ at 6 K for LaIrIn₅ in Fig. 4(d). As expected, the unusual behavior is absent in LaIrIn₅ where there is only a small negative $\rho_{xx}\alpha_{xy}$.

It is reasonable to write α_{xy} in the form³¹

$$\alpha_{xy} = \alpha_{xy}^n + \alpha_{xy}^s,\tag{4}$$

where α_{xy}^n is the contribution from normal quasiparticles and α_{xy}^s represents an anomalous term stemming from vortex excitations. The positive $\alpha_{xy}(B)$ manifests that vortex motion dominates the quasiparticle term. We summarize these results in a contour plot of $\alpha_{xy}(B, T)$ in Fig. 4(e). Below the $\alpha_{xy}=0$ boundary near 8 K, vortex-like excitations contribute and become most pronounced in the "island" region below 4 K. These temperature scales are qualitatively different from those in $CeCoIn_5$ in which Nernst effect develops at very low temperature near a field-induced quantumcritical point³². We also note that the temperature dependence of α_{xu}^s/B in CeIrIn₅ cannot be reproduced even approximately by assuming that it arises from Gaussian superconducting fluctuations (data not shown) which seems successful in describing the Nernst effect for optimally-doped and overdoped cuprates but not underdoped ones⁴². Taking $T_c^{on}=1.38$ K in simulation, the calculated α_{xu}^s/B by Gaussian model is an order of magnitude smaller than the observed values. These findings suggest that local Cooper pairs start to form at a temperature well above T_c^{on} and that phase coherence among them is destroyed by thermally activated vortexlike excitations. We estimate the phase-order temperature (above which the phase coherence is destroyed), $T_{\theta}^{max} \sim 4$ K, if we adopt Emery's model³ to CeIrIn₅ with lattice parameter c=7.515 Å¹³ and superconducting penetration depth $\lambda(0) \sim 10^4$ Å⁴³. The ratio $T_{\theta}^{max}/T_c^b \sim \hat{8}$ (or $T_{\mu}^{max}/T_{c}^{on}\sim 2.9$) is significantly smaller than that of conventional superconductors $(10^2 \sim 10^5)$ but is comparable to that of underdoped high- T_c cuprates (<10)³ whose phase stiffness is soft. Perhaps not coincidentally, T_{θ}^{max} is comparable to the estimated zero-field temperature of a precursor state found in magnetotransport^{16,17}. The filamentary nature of SC^{14} also would imply a dilute superfluid density, which renders the phase fluctuations possible in CeIrIn_5^3 . Finally, we note that the specific heat (C/T) of CeIrIn₅ deviates from a $-\log T$ dependence below $\sim 2-4$ K where it rolls over to a weaker (nearly constant) temperature dependence⁴⁴. On a similar temperature scale, ¹¹⁵In nuclear spin-lattice relaxation rate $(1/T_1)$ also shows a weak inflection at around 6 K⁴⁵. These evolutions prior to T_c suggest formation of a partial gap in $N(\varepsilon)$ that is in parallel with ungapped heavy quasiparticles. Whether these behaviors are the consequences of a possible pseudogap or correlated with the formation of local Cooper pairs is still an open question and requires further investigation.

Thermoelectric measurements in combination with charge transport in the heavy-fermion superconductor CeIrIn₅ indicate the formation of an unusual state above T_c that is reminiscent of cuprate physics. By separating the off-diagonal Peltier coefficient α_{xy} from S_{xy} , we find that α_{xy} becomes positive and greatly enhanced at the temperatures well above T_c . Compared with the nonmagnetic analog LaIrIn₅, these results suggest vortexlike excitations in a precursor state of CeIrIn₅. This work sheds new light on bridging the similarity between heavy-fermion and cuprate superconductors and is a step towards uncovering the mechanism of the unconventional superconductivity in the CeMIn₅ family compounds.

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