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Ferromagnetism and correlation strength in cubic barium ruthenate in comparison to strontium and calcium ruthenate: a dynamical mean field study

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We present density functional plus dynamical mean field studies of cubic BaRuO₃ using interaction parameters previously found to be appropriate for the related materials CaRuO₃ and SrRuO₃. The calculated variation in transition temperature between the Ba and Sr compounds is consistent with experiment, confirming the assignment of the compounds to the Hund's metal family of materials, and also confirming the appropriateness of the values for the interaction parameters previously estimated and the appropriateness of the single-site dynamical mean field approximation for these materials. The results provide insights into the origin of magnetism and the role of the van Hove singularity in the physics of Hund's metals.

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I. INTRODUCTION

The relation between crystal structure and electronic properties is a fundamental issue in condensed matter and materials physics. Studies of the variation of properties across a family of materials with similar chemical composition and structures can provide insight while the ability to capture the variation in properties is an important test of theoretical methods. In this paper we consider the ARuO₃ pseudocubic ruthenium-based perovskite family of materials, with A=Ca, Sr or Ba. The Sr and Ca compounds have been studied for decades, but BaRuO₃ has been successfully synthesized only relatively recently^{1,2}. The materials crystallize in variants of the ideal ABO₃ cubic perovskite structure and the three choices of A site ion are 'isoelectronic': each donates two electrons to the Ru-O complex and is otherwise electrically inert at the relevant energy scales. All three compounds display correlated electron behavior including large mass enhancements. The Ca material is paramagnetic down to the lowest temperatures measured, while the Sr and Ba materials have ferromagnetic ground states with the transition temperature of the Sr materials rather higher than that of the Ba material. The Ba compound is cubic; in the Sr and Ca materials a GdFeO₃ distortion (rotation and tilt of the RuO₆ octahedra) occurs, with the rotation and tilting angles being larger in the Ca than in the Sr compound. In the Ba compound a van Hove singularity leads to a density of states peak that happens to be very close to the Fermi level. The GdFeO₃ distortion splits and weakens the peak in the Ca and Sr materials; thus comparison of the electronic properties provides insight into the role of the van Hove singularity in the magnetic ordering and correlation physics.

In this paper we present a comparative DFT+DMFT analysis of Ba-, Sr- and CaRuO₃ aimed at gaining understanding of the relation between the degree of octahedral distortion, the correlation strength, and the mag-

netism in this family of compounds. Our work builds on a DFT+DMFT study of CaRuO₃ and SrRuO₃ by Mravlje, Georges and two of us³ which concluded that the pseudocubic ruthenates should be identified as 'Hund's metals' in which the physics is dominated by a slowly fluctuating local moment in the Ru d-shells while Mott physics is of secondary importance⁴. A particular combination of interaction parameters was argued to describe the materials well. In this paper we use the same methods to calculate the ferromagnetic transition temperature and electron self energy for cubic BaRuO₃, fixing the interaction parameters to the values determined previously. We find that the calculated difference in ferromagnetic transition temperature between the Sr and Ba compounds is in good accord with experiment, confirming both the applicability of the density functional plus dynamical mean field methodology to these compounds and the correctness of the interaction parameters. Consideration of the variation of the electron self energy across the series of compounds is shown to lead to insight into the role of the van Hove singularity in the physics of Hund's metals. DFT+DMFT methods have been used to study electron correlation effects in Sr- and CaRuO₃⁵⁻⁸ as well as BaRuO₃^{9,10}, here we present a comparative study of the three ruthenate materials. We will comment on the relation between our work and that of Refs. 9 and 10 below.

The rest of this paper is organized as follows. Section II presents the calculational methodology. Section III presents our main calculated results and section IV provides analysis and interpretation of the transition temperatures. Section V discusses the issue of the relative correlation strengths of the materials. Section VI is a summary and conclusion.

II. CRYSTAL STRUCTURE, ELECTRONIC STRUCTURE AND MANY-BODY MODEL

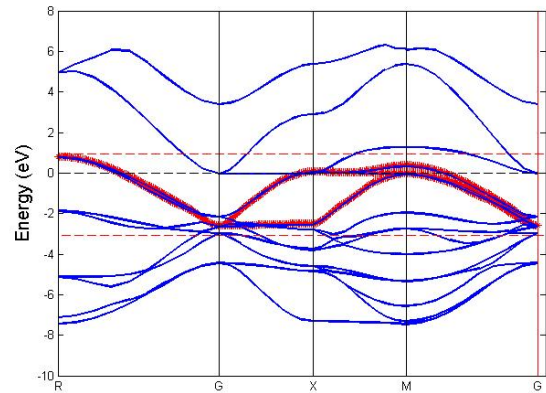
A. Crystal Structures

BaRuO₃ crystallizes in the ideal ABO_3 perovskite structure with bond length 2.003 Å¹. CaRuO₃ and SrRuO₃ crystallize in a $Pnma$ symmetry crystal structure related to the ideal cubic perovskite structure by a GdFeO₃ distortion corresponding to a four-sublattice tilt and rotation of the RuO₆ octahedra. The Ru-O-Ru bond angles of the three compounds are 180° (BaRuO₃), ≈ 163° (SrRuO₃) and ≈ 150° (CaRuO₃)^{11,12}.

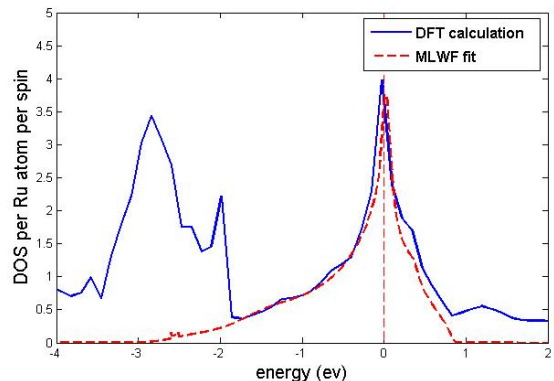
B. Background electronic structure

We computed band structures for BaRuO₃ using the experimental atomic positions and the non-spin-polarized Generalized Gradient Approximation as implemented in VASP^{13–16} with energy cutoff 400 eV and k-mesh as large as 11 × 11 × 11 to verify convergence. (Figure 1 is based on this mesh. The rest of our results are obtained from a k-mesh of 5 × 5 × 5 to obtain the hopping terms for the DMFT calculation). We then extract the near Fermi surface t_{2g} derived bands via a fit to maximally localized Wannier Functions (MLWF)^{17,18} derived from t_{2g} orbitals of Ru atom using the WANNIER90 code¹⁹ with an energy window from −3 eV to 1 eV (The interface between VASP and WANNIER90 is used for this MLWF projection.) For the cubic Ba material the application is straightforward. For the GdFeO₃-distorted Ca and Sr materials we use the band structure data calculated in Ref. 3 (obtained by QUANTUM ESPRESSO²⁰) and the procedure outlined in the same reference to find a Wannier basis adapted to the local orientation of each octahedron. We have checked that the Wannier function projection is similar if the VASP code is used instead of QUANTUM ESPRESSO for band structure calculation for Ca- and SrRuO₃.

Figure 1 shows the near Fermi surface band structure of BaRuO₃ and the Wannier fit to the t_{2g} symmetry states. The Wannier and VASP bands are almost indistinguishable. We observe that the t_{2g} bands identified by the Wannier procedure overlap slightly in energy with other bands both at the lower end of the t_{2g} bands ($E \approx -2.5$ eV) and very near the Fermi level. The overlap issue is much less severe in the Sr system and does not occur at all in the Ca system³ because the GdFeO₃ distortion in those compounds leads to narrower bands that are better separated in energy. The cubic structure of BaRuO₃ means that straightforward symmetry considerations enable us to distinguish the t_{2g} bands from the other states. At energy $E \approx -2.5$ eV, the overlap is with oxygen p -derived bands. The overlap occurs near the zone center [Γ point - denoted by G in Fig. 1(a)] where there is a sharp symmetry distinction between the states so identification of bands is unambiguous. The other



(a)



(b)

FIG. 1. (Color online) (a) Near Fermi level energy bands of cubic perovskite BaRuO₃. Lighter lines (blue on-line) are DFT bands. Heavier lines (red on-line) are MLWF fits to the t_{2g} -derived near Fermi level orbitals using an energy window extending from −3 eV to 1 eV (dashed red line). (b) Total density of states per Ru atom for BaRuO₃: solid lines (blue on-line) DFT results; dashed lines (red on-line) MLWF fit. The Fermi level is at energy $\omega = 0$.

states near and above the Fermi level are determined by a five band Wannier analysis (not shown) to be of Ru e_g origin. Inclusion of beyond-band theory interactions will increase the crystal field splittings, pushing these e_g -derived bands farther from near Fermi surface region of interest. We neglect the e_g - and oxygen p -derived bands henceforth.

C. Many-body physics

To treat the many-body physics of BaRuO₃ we follow Ref. 3 and use the one-shot density functional plus dynamical mean field method, in which an effective Hamiltonian for the frontier t_{2g} -derived bands is defined as

$$H = H_{\text{kin}} + H_{\text{onsite}}, \quad (1)$$

with H_{kin} obtained by projecting the DFT Hamiltonian onto the Wannier bands discussed above and setting the chemical potential to ensure that these bands contain four electrons per Ru.

As usual in studies of transition metal oxides, the interaction Hamiltonian is taken to be site-local and to have the rotationally invariant Slater-Kanamori form²¹. We use the version appropriate⁴ for intra- t_{2g} orbitals, since these are the primary focus of this work

$$\begin{aligned}
H_{\text{on-site}} = & U \sum_{\alpha} n_{\alpha\uparrow} n_{\alpha\downarrow} + (U - 2J) \sum_{\alpha \neq \beta} n_{\alpha\uparrow} n_{\beta\downarrow} + \\
& + (U - 3J) \sum_{\alpha > \beta, \sigma} n_{\alpha\sigma} n_{\beta\sigma} + \\
& + J \sum_{\alpha \neq \beta} (c_{\alpha\uparrow}^{\dagger} c_{\beta\downarrow}^{\dagger} c_{\alpha\downarrow} c_{\beta\uparrow} + c_{\alpha\uparrow}^{\dagger} c_{\alpha\downarrow}^{\dagger} c_{\beta\downarrow} c_{\beta\uparrow}),
\end{aligned} \quad (2)$$

where α, β are orbital indexes, σ is the spin index and U and J are screened interaction parameters appropriate for calculations restricted to the t_{2g} -derived correlated subspace. We set $U = 2.3$ eV and $J = 0.35$ eV as proposed for the Ca and Sr materials in Ref. 3 and solved the impurity model using the hybridization expansion variant of the continuous-time quantum Monte Carlo (CT-HYB) solver as implemented in the Toolbox for Research on Interacting Quantum Systems (TRIQS) library^{22,23}.

The momentum integral needed to obtain the on-site Green's function for the DMFT loop is via Gaussian quadrature using 30^3 k points for BaRuO₃ and 26^3 k points for Sr- and CaRuO₃; the number of k -points is chosen to be large enough to capture the main features of the density of states.

III. RESULTS

A. Density of states

Figure 2 shows the density of states of the three materials, projected onto the Wannier functions corresponding to the Ru t_{2g} orbitals of interest here. We see that the Ba compound has the largest bandwidth (≈ 3.6 eV) and exhibits a near Fermi level density of states peak arising from a van Hove singularity. The GdFeO₃ distortion reduces the bandwidth and by splitting the van Hove singularity reduces the near Fermi level DOS. The Sr compound has bandwidth of ≈ 3.0 eV. The Ca material has a larger amplitude GdFeO₃ distortion and a correspondingly smaller bandwidth (≈ 2.6 eV) and larger splitting of the van Hove peak.

B. Magnetic transition temperature

To determine the magnetic transition temperatures we applied small fields H to the Ru t_{2g} orbitals, measured the resulting t_{2g} spin polarization m in the converged

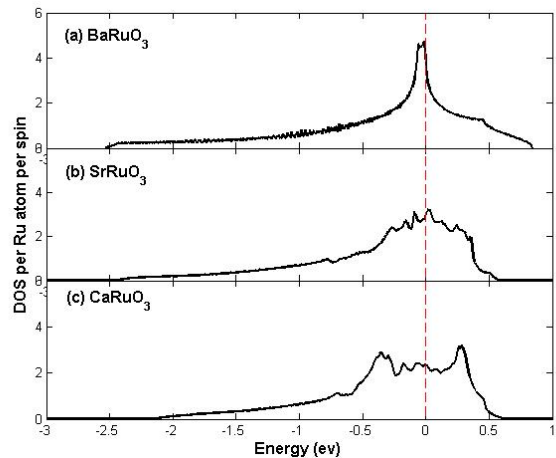


FIG. 2. (Color online) t_{2g} projected near Fermi surface density of states for BaRuO₃, SrRuO₃ and CaRuO₃, obtained from Wannier fit to calculated band structure. Vertical red dashed line indicates the Fermi level.

DMFT solution, and plotted m^2 against H/m for different H and temperature T . We find that our calculated m fits the Arrott form²⁴

$$m^2 = \frac{1}{B} \frac{H}{m} - \frac{A}{B} (T - T_c) \quad (3)$$

very well, and the temperature at which the extrapolated $H/m = 0$ value of m^2 vanishes provides a good estimate of the transition temperature. To confirm the result we extended the DMFT solution to the ferromagnetic phase and plotted m^2 against temperature. The form of the Arrott plots and the agreement between these and the value calculated from the m^2 vs T plot also confirms that the transition is second order. In the dynamical mean field approximation used here the transition is mean field, experimental measurements on BaRuO₃ reveal non-mean-field exponents² indicating the importance of fluctuations which would lower the transition temperature relative to the mean field estimate.

Results are shown in Fig. 3 and confirm a transition temperature for BaRuO₃ of $T_c \approx 0.012$ eV ~ 140 K. This transition temperature is to be compared to the calculated value $T_c \approx 0.017$ eV ~ 200 K for SrRuO₃ and the absence of ferromagnetism in CaRuO₃ obtained using the same methods and the same interaction parameters³. Bearing in mind that mean field approximations such as DMFT overestimate transition temperatures, we consider that the findings are in good agreement with experimental results on this family of materials where CaRuO₃ is not magnetically ordered to the lowest temperatures studied, SrRuO₃ has a Curie temperature $T_c \approx 160$ K²⁵ and BaRuO₃ has $T_c \approx 60$ K¹.

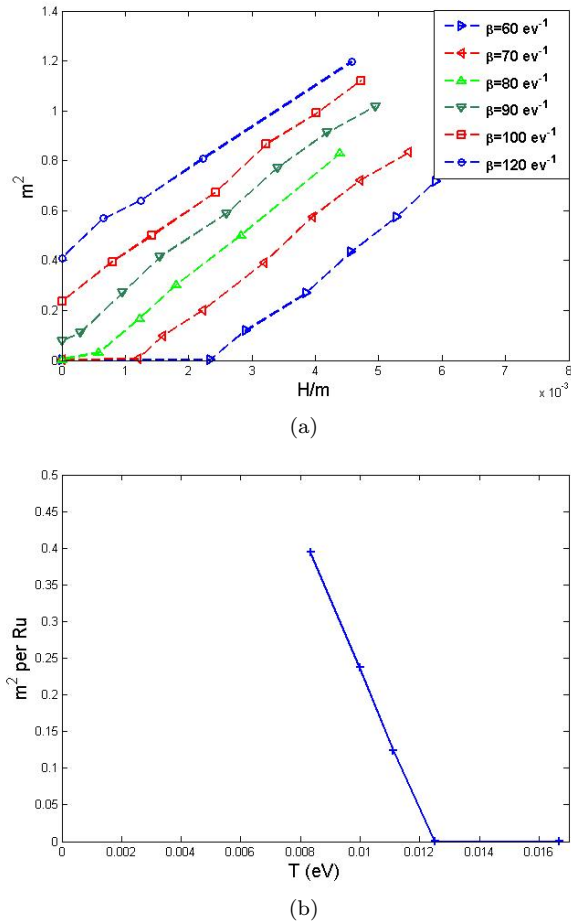


FIG. 3. (Color online) (a) Square of calculated magnetization m^2 of BaRuO_3 plotted against ratio of applied field H divided by magnetization m at $U = 2.3 \text{ eV}$, $J = 0.35 \text{ eV}$ and temperatures indicated. (b) m^2 calculated at $H = 0$ plotted against temperature.

C. Self Energies

To better understand the differences in physics between the compound we present in Fig. 4 the imaginary part of the Matsubara self energies for the three compounds, calculated using the interaction parameters given above at temperature $T = 0.0025 \text{ eV}$. In the Sr and Ca materials the octahedral rotations lead to small differences between the self energies corresponding to different local orbitals. As the differences between orbitals are not of interest here we present results averaged over all three orbitals. We further restrict our calculations to paramagnetic phases, because the onset of ferromagnetism dramatically changes the self energies. From Fig. 4(a) we see that for $\omega_n > 0.5 \text{ eV}$, the Ca compound (smallest bandwidth) has the largest magnitude of the self energy and the Ba compound (largest bandwidth) has the smallest. This variation between compounds is consistent with the ‘‘Mott’’ picture in which the key parameter is the ratio of an interaction strength to a bandwidth. However

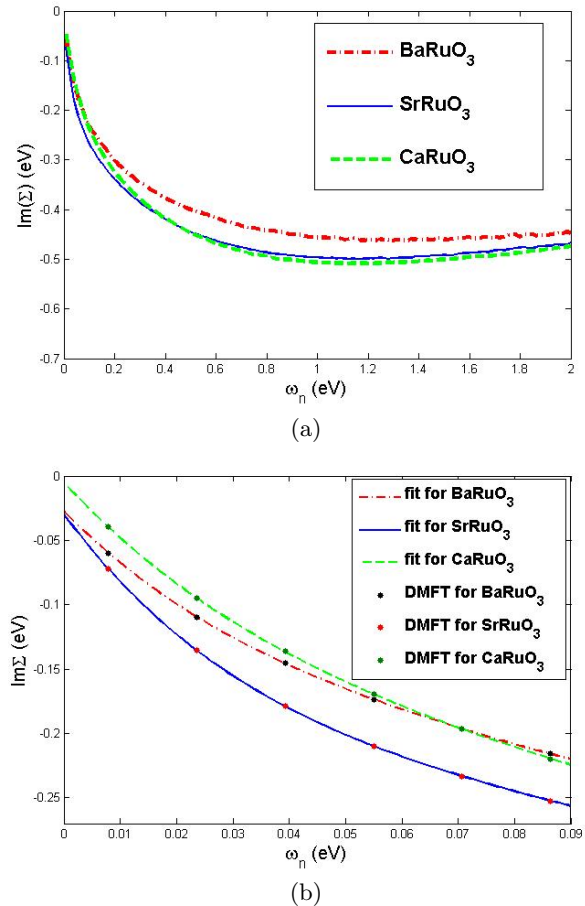


FIG. 4. (Color online) (a) Imaginary part of orbitally averaged self energy of CaRuO_3 (dashed lines, green on-line), SrRuO_3 (solid line, blue on-line) and BaRuO_3 (dash-dotted line, red on-line) calculated in the paramagnetic state at $T = 0.0025 \text{ eV}$ with $U = 2.3 \text{ eV}$ and $J = 0.35 \text{ eV}$. (b) Expanded view of low frequency region. The dots are the DMFT results and the curves are from the fourth order polynomial fit of the last six points of $\text{Im}\Sigma(i\omega_n)$.

we see from panel b of Fig. 4 that at low frequency the curves cross. For $\omega \lesssim 0.4 \text{ eV}$ the self energy for the Sr compound becomes larger in magnitude than that for the Ca compound while for $\omega \lesssim 0.07 \text{ eV}$ the self energies for the Ca and Ba materials cross. We expect that at even lower temperatures the self energies for the Ba and Sr materials will cross. This behavior suggests that the very low frequency and temperature limits of the self energy are controlled by the near Fermi level density of states, which is largest for the Ba material and smallest for the Ca material, rather than by the bandwidth²⁶.

IV. ANALYSIS

In this section we analyze the calculated variation of transition temperature across the material families. We begin our analysis by considering the Stoner (Hartree-

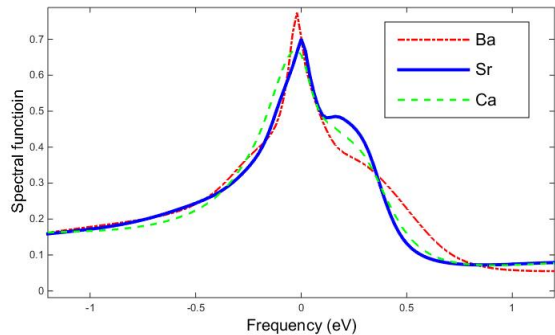


FIG. 5. (Color online) Momentum-integrated orbitally averaged electron spectral function computed as described in the text at temperature $T = 0.025$ eV. The short-dashed line (red on-line) is for BaRuO₃, the solid line (blue on-line) is for SrRuO₃ and the long-dash line (green on-line) is for CaRuO₃.

Fock) criterion for magnetism. In its simplest form²⁷, the Stoner criterion relates the onset of magnetism to the product of an interaction and the Fermi surface density of states. Assuming an orbital-independent magnetization $m = \sum_{\alpha} (n_{\alpha\uparrow} - n_{\alpha\downarrow})/3$, we find that the change in interaction energy (expectation value of H_{onsite} , Eq. (2)) is

$$\delta E_{\text{interaction}} = -3(U + 2J) \left(\frac{m}{2}\right)^2. \quad (4)$$

For small m , the kinetic energy cost is

$$\delta E_{\text{kinetic}} = 3 \frac{m^2}{4N_0}, \quad (5)$$

where N_0 is the density of states per orbital per spin, averaged over all orbitals. Thus the Stoner criterion for the multi-orbital situation considered here is

$$(U + 2J)N_0 > 1. \quad (6)$$

Inspection of Fig. 2 shows that the values of N_0 are ~ 1.2 eV⁻¹, ~ 0.97 eV⁻¹ and ~ 0.78 eV⁻¹ for BaRuO₃, SrRuO₃ and CaRuO₃ respectively. The Stoner criterion therefore indicates, in clear contradiction to experiment and to our calculated results, that all three materials should be ferromagnetic, and that the ferromagnetism should be strongest in the Ba material. This discrepancy suggests that beyond mean-field many-body effects may be important.

One possibility is that inelastic scattering broadens the density of states peak. We present in Fig. 5 the local spectral function (many-body density of states) $A(\omega)$ calculated by using maximum entropy methods to analytically continue the self energy²⁸ and then inserting the result into the Green function, via

$$A(\omega) = \text{Im} \int d^3k \text{Tr} \left[\omega + \mu - \hat{H}_{\text{kin}}(k) - \hat{\Sigma}(\omega) \right]^{-1} \quad (7)$$

We see that many-body effects substantially reduce the Fermi level density of states of the Ba and Sr materials and slightly reduce that of the Ca material. However, even if we use the many-body density of states, all three materials are predicted by the Stoner criterion to be ferromagnetic and the Ba material is still predicted to have the strongest magnetism. We therefore conclude that some parameter other than the value of the Fermi-level density of states is important. A possible explanation was suggested by Kanamori²⁹ and investigated in detail for a single band Hubbard model by Vollhardt, Ulmke and coworkers³⁰⁻³², and later by two of us in the context of vanadate perovskites³³. A key issue identified by this work was a strongly skewed density of states, with a peak close to a band edge. In the work of Refs.³⁰⁻³³, less than half-filled bands were considered, and ferromagnetism was strongest if the Fermi level and density of states peak were close to the lower band edge. In the present situation the band is more than half filled and we expect that ferromagnetism would be strongest if the peak were close to the upper band edge.

To investigate this possibility we constructed a family of model system densities of states, all of which have the same bandwidth as SrRuO₃ but with the van Hove peak at the Fermi level as in BaRuO₃. The densities of states differ in the positions of the upper band edge E_U relative to the Fermi level E_F which we label by $\alpha = (E_U - E_F)/(E_U^0 - E_F^0)$, where the superscript 0 indicates the values for BaRuO₃ with only the bandwidth rescaled to the SrRuO₃. Several members of this family are shown in Fig. 6(a) (note the Fermi level is always at the DOS peak).

For each of these systems we solved the DMFT equations and computed the transition temperatures, finding $T_c \sim 0.033$ eV for $\alpha = 0.76$, ~ 0.025 eV for $\alpha = 0.86$, ~ 0.018 eV for $\alpha = 1.0$ which should be compared to $T_c \sim 0.0125$ eV for BaRuO₃. The results show that simply rescaling the bandwidth of BaRuO₃ ($\alpha = 1.0$) increases the T_c to the value $T_c \sim 0.018$ eV calculated for SrRuO₃. A further increase occurs if the the DOS peak is moved towards the upper band edge. Moving the DOS peak closer to the upper band edge also increases the calculated magnetization [see Fig. 6(b)].

We therefore conclude that ferromagnetic transition temperature is controlled by three factors: the DOS at the Fermi level (Stoner theory²⁷), the DOS peak position with respect to the band edge (Kanamori, Vollhardt and others²⁹⁻³³), and the bandwidth. CaRuO₃ has no ferromagnetism because the strong lattice distortion leads to the splitting of the DOS peak and thus results in small magnitude of DOS at the Fermi level. BaRuO₃, despite of a large DOS peak, has larger bandwidth and the DOS peak position farther from the upper band edge than SrRuO₃, explaining the higher T_c of SrRuO₃. As seen in Fig. 6, adjusting the DOS shape of BaRuO₃ to have similar bandwidth and DOS peak position as SrRuO₃ will give the Curie temperature much larger than that of SrRuO₃.

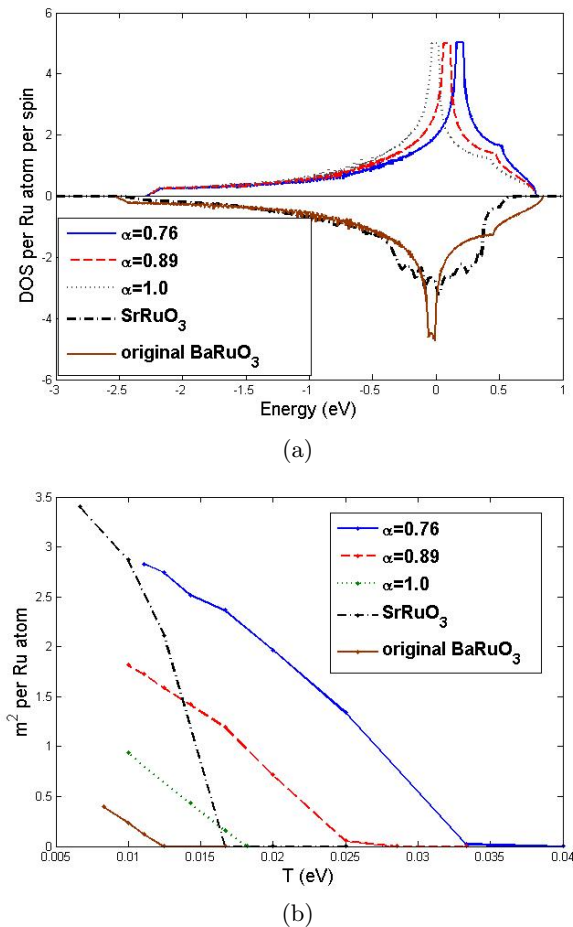


FIG. 6. (Color online) (a) The plot of noninteracting density of states: positive half panel: BaRuO₃ DOS with bandwidth rescaled to be the same as that of SrRuO₃ and DOS peak position shifted towards the upper band edge. The Fermi level is located at the DOS peak position. The case $\alpha = 1$ corresponds to the BaRuO₃ DOS with bandwidth scaled to the SrRuO₃. The negative half panel: original DOS for BaRuO₃ and SrRuO₃. (b) m^2 vs. T for three typical designed DOS, the original BaRuO₃ and SrRuO₃.

V. SELF ENERGIES AND CORRELATION STRENGTH

The electron correlation strength is a generally important issue for electronically active materials, and the issue is of particular significance in the theory of Hund's metals, where one may consider both the ratio of an interaction parameter to the bandwidth, and the ratio of an interaction parameter to the near Fermi level density of states^{3,4}. BaRuO₃ highlights this issue, as this material has both the largest bandwidth and the largest Fermi level density of states.

The correlation strength may be parametrized by the value of the imaginary part of the self energy. From Fig. 4 we see that over the broad energy range, the Ca material has the largest self energy magnitude as expected

from its smallest bandwidth. In the low energy range, the self energy curves cross and SrRuO₃ has the largest self energy magnitude. At lower temperatures we expect that the low frequency self energies of the BaRuO₃ and SrRuO₃ would cross and BaRuO₃ self energy become the largest.

To analyze the self energy in more detail we fit the lowest six Matsubara points to a fourth order polynomial

$$Im\Sigma(\omega_n) = \sum_{p=0}^4 s_p \omega_n^p. \quad (8)$$

where s_0 is the residual scattering rate and s_1 is an estimate for $Re[d\Sigma/d\omega]|_{\omega_n \rightarrow 0}$ which, within the single-site DMFT approximation, yields the mass enhancement via

$$\frac{m^*}{m} \approx 1 - \frac{dIm(\Sigma(i\omega_n))}{d\omega_n} \Big|_{\omega_n \rightarrow 0} \approx 1 - s_1. \quad (9)$$

Two tests of whether the system is in the Fermi liquid regime (so that $1 - s_1$ provides a good approximation to the mass enhancement) are that $s_0 \ll Im\Sigma(\omega_n = \pi T) \approx s_1 \pi T$ and that the slope defined from the lowest two Matsubara points is in good agreement with the slope defined from the higher order polynomial fit. The low frequency data and the fitted curves are shown in Fig. 4(b). Table I shows the first two coefficients along with the percent difference between s_1 and the slope defined from the lowest two Matsubara points. We see that for all materials the slopes computed in two different ways agree at the 25-30% level, indicating that the calculations have at least reached the edge of the Fermi liquid regime. However, for the Sr and Ba materials the intercept (residual scattering rate) is still about 50% of the value at the lowest Matsubara frequency, suggesting that these compounds have not quite reached the Fermi liquid regime, so the properties would evolve further as the temperature is lowered.

At $T = 0.0025$ eV the mass enhancement of SrRuO₃ is about 6.9 while for CaRuO₃ and BaRuO₃ it is about 5.5, although as noted for the Sr and Ba compounds the mass enhancement may evolve further as the temperature is lowered. The differences we see between the wide-range and low frequency self energies are consistent with previous work and suggest (in agreement with previous work)

TABLE I. Intercept s_0 and slope s_1 obtained from fourth order fit to orbitally averaged $Im\Sigma$ computed at $T = 0.0025$ eV and the relative difference Δ in percentage of the slope s_1 obtained from the fitting and from the lowest two Matsubara points. Δ is defined as the difference between the two slope values divided by s_1 value from the fitting.

	s_0	s_1	$s_1 \pi T$	m^*/m	Δ
BaRuO ₃	-0.02734	-4.508	-0.0354	5.508	30%
SrRuO ₃	-0.02974	-5.929	-0.0466	6.929	32%
CaRuO ₃	-0.00508	-4.765	-0.0374	5.765	26%

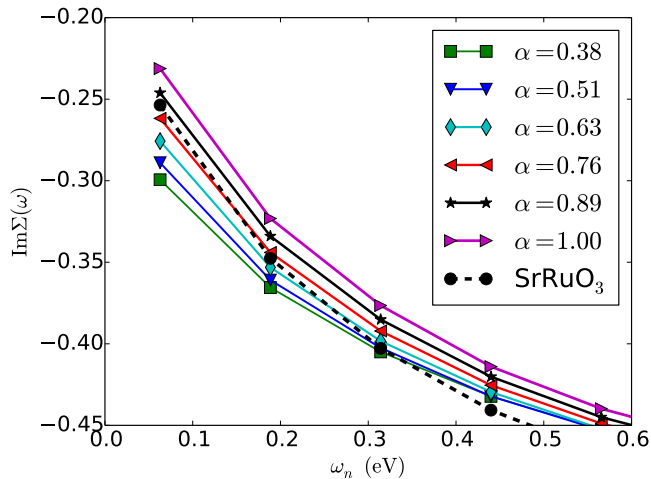


FIG. 7. (Color online) Imaginary part of the self energy for model calculation with DOS peak position (represented by the dimensionless parameter α) varying. SrRuO₃ self energy (circle dashed black line) is also showed for reference. Temperature is fixed at $T = 0.02$ eV. Results are obtained for paramagnetic order.

that in Hund's metals the low frequency mass enhancement is more sensitive to the Fermi level density of states than to the overall bandwidth²⁶. However, the BaRuO₃ results show that one needs to go to extremely low temperatures before the density of states effect dominates.

To gain more insight into the relative importance of different factors in the density of states we have computed the mass enhancements for the model DOS shown in Fig. 6(a). Figure 7 shows the results for self energy at $T = 0.02$ eV (computed in the paramagnetic state). There is a systematic increase in correlation strength at low frequency as α decreases, implying a stronger Hund's effect when the DOS peak position gets closer to the upper band edge. This increase in the effective mass is consistent with the increase in T_c and suggests that the importance of the Hund's coupling is determined not only by the Fermi level density of states but also by the breaking of particle-hole symmetry.

VI. CONCLUSION

In this paper we have presented single-site dynamical mean field calculations of the ferromagnetic transition temperature and electronic self energy of cubic BaRuO₃. We used interaction parameters $U = 2.3$ eV and $J = 0.35$ eV obtained for CaRuO₃ and SrRuO₃ in previous work³ which place the material far from the Mott insulating regime and firmly in the Hund's metal regime. We compared the results to those previously obtained on GdFeO₃-distorted SrRuO₃ and CaRuO₃. In good qualitative agreement with experiment, the calculated ferromagnetic transition temperature of BaRuO₃ is positive, but substantially lower than that of SrRuO₃.

This agreement provides strong evidence that the single-site dynamical mean field approximation is a reasonable description of the ruthenate materials and suggests that the interaction parameter regime identified for the Sr and Ca materials is correct.

A very recent theoretical study using an almost identical formulation of the DFT+DMFT methodology studied BaRuO₃, considering a range of U and J values and focusing on the self energy and local susceptibility in the paramagnetic phase¹⁰. Where parameter values overlap, the results of Ref. 10 for the self energy are in agreement with those presented here. These authors argued, on the basis of a comparison to the fluctuating moment measured at high temperatures, that a value $J = 0.5$ eV is more appropriate than the $J = 0.35$ eV considered here. This issue deserves further investigation, but we note that according to Ref. 3 this value of J would predict a ferromagnetic ground state for CaRuO₃. The other work⁹ studied BaRuO₃ using a slightly different implementation of DFT+DMFT in which the correlated orbitals were defined as atomic-like d orbitals and the model was defined over a much wider energy range. The parameters chosen in this study were such as to lead to weaker correlation effects (self energies smaller by a factor of ~ 2 than those found here). Extending our analysis of trends across material families to a wider range of parameters and to the wide-band implementation of DFT+DMFT are important issues that might be addressed in future work.

The relation between the non-interacting (band theoretic) density of states and many-body materials properties is a fundamental and important question in condensed matter physics. A striking feature of the band theory density of states of BaRuO₃ is a strong van Hove peak very close to the Fermi level. We find that proximity of the van Hove peak to the Fermi level does not by itself drive dramatic correlation effects at the temperature and energy scales accessible to us. The non-monotonic variation of transition temperature with GdFeO₃ rotation amplitude indicates that important features of the magnetism are controlled by features beyond the value of the Fermi-level density of states, in particular the bandwidth and distance from the DOS peak to the upper band edge. This finding is in agreement with previous work²⁹⁻³³. We also see that even at the lowest frequency the magnitude of the self energy of BaRuO₃ is less than that of SrRuO₃, indicating that Hund's metal correlations also are sensitive not only to the Fermi level density of states but also to additional structures in the density of states farther from the Fermi surface.

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