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Impact of Uniaxial Pressure on Structural and Magnetic Phase Transitions in Electron-Doped Iron Pnictides

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We use neutron resonance spin echo and Larmor diffraction to study the effect of uniaxial pressure on the tetragonal-to-orthorhombic structural (T) and antiferromagnetic (AF) phase transitions in iron pnictides BaFe2−xNixAs2 (x = 0, 0.03, 0.12), SrFe1.97Ni0.03As2, and BaFe2(As0.65P0.35)2. In antiferromagnetically ordered BaFe2−xNixAs2 and SrFe1.97Ni0.03As2 with TN and TS (TS ≤ TN), a uniaxial pressure necessary to detwin the sample also increases TS. Smears out the structural transition and induces an orthorhombic lattice distortion at all temperatures. By comparing temperature and doping dependence of the pressure induced lattice parameter changes with the elastoresistance and nematic susceptibility obtained from transport and ultrasonic measurements, we conclude that the in-plane resistivity anisotropy found in the paramagnetic state of electron underdoped iron pnictides depends sensitively on the nature of the magnetic phase transition and a strong coupling between the uniaxial pressure induced lattice distortion and electronic nematic susceptibility.

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I. INTRODUCTION

The parent compounds of iron pnictide superconductors such as BaFe2As2 and SrFe2As2 exhibit a tetragonal-to-orthorhombic structural transition at Tc followed by development of collinear antiferromagnetic (AF) order along the a-axis of the orthorhombic lattice below TN [left inset in Fig. 1(a) and TN ≈ 245 K]. Upon electron-doping via partially substituting Fe by Co or Ni to form BaFe2−xTxAxAs2 (T = Co, Ni), the nearly coupled structural and magnetic phase transitions in BaFe2As2 become two separate second order phase transitions at TS and TN (TS > TN) that decrease in temperature with increasing x7–10. On the other hand, the coupled first order structural and magnetic phase transitions in SrFe2As24, while decreasing in temperature with increasing x in SrFe2−xTXAOx, remain coupled first order transitions leading up to superconductivity11.

Because the structural and magnetic phase transitions in BaFe2−xTxAxAs2 and SrFe2−xTxAxAs2 occur below room temperature, iron pnictides in the orthorhombic AF ground state will form twin domains with AF Bragg peaks appearing at the in-plane (±1, 0) and (0, ±1) positions in reciprocal space [right inset in Fig. 1(a)]9. To probe the intrinsic electronic properties of these materials, one can apply uniaxial pressure along one axis of the orthorhombic lattice to obtain single domain samples12–15. Indeed, transport measurements on uniaxial pressure detwinned electron-doped BaFe2−xTxAxAs2 (T = Co, Ni) reveal in-plane resistivity anisotropy in the AF state that persists to temperatures above the zero-pressure TN and TS12–15. On the other hand, similar transport measurements on uniaxial pressure detwinned SrFe2−xTxAxAs2 (T = Co, Ni) indicate vanishingly small resistivity anisotropy at temperatures above the zero pressure coupled TN and TS16–18. Figure 1(b) compares temperature dependence of the resistivity anisotropy [defined as ∆ρ = (ρb − ρa)/(ρb + ρa), where ρa and ρb are resistivity along the a and b axis of the orthorhombic lattice, respectively] obtained under 20 MPa uniaxial pressure for BaFe2As2, BaFe1.97Ni0.03As2, SrFe1.97Ni0.03As2, and SrFe2As2. Consistent with earlier works12–18, we find that resistivity anisotropy is much larger in BaFe2As2 and BaFe1.97Ni0.03As2 at temperatures above TN.

Although resistivity anisotropy in the paramagnetic state of the iron pnictides under applied uniaxial pressure suggests the presence of an electronic nematic phase that breaks the in-plane fourfold rotational symmetry (C4) of the underlying tetragonal lattice19–24, much is unclear about the microscopic origin of the in-plane resistivity anisotropy and electronic nematic phase25–38. Since neutron scattering experiments reveal that uniaxial pressure necessary to detwin the sample also increases TN of the system, the observed in-plane resistivity anisotropy above the zero pressure TN and TS may arise from the increased TN and intrinsic anisotropic nature of the collinear AF phase39,40. Furthermore, while it is generally assumed that the uniaxial pressure for sample detwinning has negligible effect on the lattice parameters of the iron pnictides12–15, the precise effect of uniaxial pressure on structural distortion of these materials is unknown. From neutron extinction effect measure-
ments, a uniaxial pressure is suggested to push structural fluctuations related to the orthorhombic distortion to a temperature well above the zero-pressure value of $T_N$, similar to the effect on the resistivity anisotropy $^{12-15}$. To understand the microscopic origin of the in-plane resistivity anisotropy in the paramagnetic state $^{12-15}$, it is important to establish the effect of a uniaxial pressure on the magnetic and structural phase transitions of BaFe$_2$-$x$Ni$_x$As$_2$ and SrFe$_2$-$x$T$_2$As$_2$, and determine if the electronic anisotropy in the paramagnetic tetragonal phase of iron pnictides is intrinsic $^{42,43}$, or entirely due to the symmetry breaking uniaxial pressure applied to the materials $^{44,45}$. It is also important to deduce what role the nature of the AF transition plays in the nematic susceptibility $^{17,25,26,38}$ and how the latter depends on the uniaxial pressure.

In this paper, we use neutron resonance spin echo (NRSE) $^{46,47}$ and Larmor diffraction $^{48}$ to study the effect of uniaxial pressure on the structural and magnetic phase transitions in electron doped iron pnictides BaFe$_{2-x}$Ni$_x$As$_2$ with $x = 0, 0.03, 0.12^{9,10}$ and SrFe$_{1.97}$Ni$_{0.03}$As$_2$ $^{18}$, and in the iso-valently doped BaFe$_2$(As$_{0.7}$P$_{0.3}$)$_2$ $^{49}$. While the underdoped BaFe$_{1.97}$Ni$_{0.03}$As$_2$ ($T_N = 109$ K and $T_s = 114$ K) exhibits a second-order AF transition below $T_s$, SrFe$_{1.97}$Ni$_{0.03}$As$_2$ has coupled first-order and magnetic phase transitions at $T_N = T_s \approx 175$ K $^{50}$. The electron doped BaFe$_{1.88}$Ni$_{0.12}$As$_2$ ($T_c = 18.6$ K) and iso-valently doped BaFe$_2$(As$_{0.7}$P$_{0.3}$)$_2$ ($T_c = 30$ K) have a paramagnetic tetragonal structure at all temperatures without static AF order. Figure 1(c) summarizes the key experimental result of the present work, where the temperature dependences of the uniaxial pressure induced orthorhombic lattice distortion $\delta(P = 20 \text{ MPa}) - \delta(P = 0 \text{ MPa})$ are determined using neutron Larmor diffraction for BaFe$_2$As$_2$, BaFe$_{1.97}$Ni$_{0.03}$As$_2$, SrFe$_{1.97}$Ni$_{0.03}$As$_2$, and BaFe$_{1.88}$Ni$_{0.12}$As$_2$ [we defined the lattice distortion $\delta = (a - b)/(a + b)$ with $a$ and $b$ being the orthorhombic lattice parameters]. Remarkably, the magnitude of our determined structural nematic susceptibility $\delta \delta / \delta P \propto \delta(P) - \delta(0)$ in Figure 1(c) is comparable in all three materials that have a structural phase transition, unlike the very different values of the resistivity anisotropy displayed in Figure 1(b). Comparing these results with those of the elastoresistance and nematic susceptibility obtained from transport $^{20,23,24}$ and from elastic shear modulus/ultrasound spectroscopy measurements $^{38,51,52}$, we conclude that the resistivity anisotropy in the paramagnetic phase of the iron pnictides depends sensitively on whether the underlying magnetic phase transition is first or second order. We also find a strong coupling between the uniaxial pressure induced lattice distortion and the electronic nematic susceptibility, and have to be cautious in directly relating resistivity anisotropy to the nematic order parameter in the iron pnictides.

II. RESULTS

A. Experimental Results

Our experiments were carried out using conventional thermal triple-axis spectrometer PUMA and three axes spin echo spectrometer (TRISP) at the Forschungsneu-
FIG. 2: (Color online) (a) Magnetic order parameters at $Q = (1,0,1)$ for the zero ($P = 0$) and uniaxial pressured ($P \sim 15$ MPa) BaFe$_{1.97}$Ni$_{0.03}$As$_2$. $T_N$ is 109 K for an unpressured sample (blue diamonds). Upon applying uniaxial pressure of $P \sim 15$ MPa, the $T_N$ is enhanced to 118 K and the sample becomes 100% detwinned as seen by PUMA and TRISP measurements. (b) The energy line width (Half-Width-at-Half-Maximum, $\Gamma$) of the magnetic Bragg peak $Q = (1,0,1)$ measured by NRSE using TRISP for BaFe$_{1.97}$Ni$_{0.03}$As$_2$. The blue and red dashed lines indicate $T_N$ in $P = 0$ and 15 MPa uniaxial pressure, respectively. The slight larger errors of $\Gamma$ near $T_N$ is due to low statistics data.

tronquelle Heinz Maier-Leibnitz (MLZ), Garching, Germany. The principles of NRSE and Larmor diffraction are described elsewhere.$^{50}$ Single crystals of BaFe$_{2-x}$Ni$_x$As$_2$, SrFe$_{2-x}$Ni$_x$As$_2$, and BaFe$_2$(As$_{0.7}$P$_{0.3}$)$_2$ were grown by self-flux method as described before.$^{49,51}$

We define the momentum transfer $Q$ in the three-dimensional reciprocal space in Å$^{-1}$ as $Q = Ha^* + Kb^* + Le^*$, where $H$, $K$, and $L$ are Miller indices and $a^* = 2\pi/|a|$, $b^* = 2\pi/|b|$, $c^* = 2\pi/|c|$ with $a \approx b \approx 5.6$ Å, and $c = 12.96$ Å for BaFe$_{2-x}$Ni$_x$As$_2$. In this notation, the AF Bragg peaks should occur at $(\pm 1, 0, 0)$ and $(0, \pm 1, 0)$ positions in reciprocal space of a completely detwinned sample [right inset in Fig. 1(a)]. For neutron scattering experiments, single crystals are aligned in either the $[H, K, H + K]$ or $[H, K, 0]$ zone.

We first discuss the effect of uniaxial pressure on the collinear AF order in BaFe$_{2-x}$T$_x$As$_2$. In previous neutron scattering work on BaFe$_{2-x}$Co$_x$As$_2$, the Néel temperature ($T_N$) was found to be pushed to higher temperature under uniaxial strain field, forming a broader magnetic transition.$^{39,40}$ Moreover, it seems that the increase in $T_N$ depends on the annealing condition.$^{41,54}$ Although the $T_N$ enhancement was attributed to uniaxial strain aligned fluctuating magnetic domains, the effect of uniaxial pressure on the ordered moment remains elusive and the nature of the $T_N$ enhancement is still under debate.$^{40,41,54}$

By aligning single crystals in the $[1,0,1] \times [0,1,1]$ scattering plane,$^{41}$ we were able to determine $T_N$, detwinning ratio, as well as the ordered moment of the system under zero and finite uniaxial pressures. Figure 2(a) shows temperature dependence of the $(1,0,1)$ and $(0,1,1)$ magnetic scattering intensity for BaFe$_{1.97}$Ni$_{0.03}$As$_2$ obtained using PUMA [left axis in Fig. 2(a)] and TRISP (right axis). The two sets of data are in excellent quantitative agreement with each other. Under the applied uniaxial pressure of $P \sim 15$ MPa, the Néel temperature increases from $T_N \approx 109$ K ($P = 0$) to $T_N \approx 118$ K. The magnetic scattering intensity [Fig. 2(a)] in the $(1,0,1)$ peak becomes approximately twice as large as in the twinned sample, whereas the $(0,1,1)$ peak vanishes, suggesting that the sample is completely detwinned and the applied uniaxial pressure does not significantly affect the ordered moment.

To test whether the $T_N$ increase is an intrinsic feature of the system, we note that the magnetic order parameter under uniaxial pressure has a round tail around $T_N$,$^{39,40}$ suggesting that the $T_N$ enhancement could arise from enhanced slow spin dynamics (critical scattering) under inhomogeneous uniaxial strain field and cannot be resolved by conventional triple-axis neutron diffraction due to its coarse energy resolution ($\Delta E \approx 0.3 – 1$ meV). To clarify the nature of the increase in $T_N$, we have measured the energy line-width ($\Gamma \geq 0$, [see Fig. 2(b)]) of the quasielastic scattering for magnetic reflection $(1,0,1)$ using high energy resolution ($\Delta E \approx 1$ µeV) NRSE at TRISP.$^{55}$ As seen in Figure 2(b), the $\Gamma$ at all measured temperatures is resolution limited, indicating that the increase in magnetic scattering intensity below $T_N \approx 118$ K is elastic ($\Gamma \leq 1$ µeV), and an intrinsic nature of the system.

To determine the effect of uniaxial pressure on the tetragonal-to-orthorhombic phase transition in iron pnic- tidies, we carried out neutron Larmor diffraction experiments capable of measuring minor change of lattice spacing $d = 2\pi/|Q(H, K, L)|$ and its spread $\Delta d$ with a resolution better than $10^{-4}$ in $\Delta d/|d|$ [inset in Fig. 3(a)]. We focus on $(4,0,0)$ and $(0,4,0)$ nuclear Bragg reflections corresponding to a $d$-spacing $d \approx a/4$, which we measured in BaFe$_{2-x}$Ni$_x$As$_2$ ($x = 0, 0.03, 0.12$), SrFe$_{1.97}$Ni$_{0.03}$As$_2$, and BaFe$_2$(As$_{0.7}$P$_{0.3}$)$_2$ both on freshly prepared samples (uniaxial pressure $P = 0$) and under uniaxial pressure ($P \approx 10, 20$ MPa). Figure 3 shows the temperature and pressure dependence of the $d$ spread for these samples. The $d$ spread is characterized by the FWHM (Full-Width-Half-Maximum) of the lattice spacing distribution $f(\Delta d/d)$, which is assumed to be Gaussian distribution.$^{50}$ The diamonds in Figure 3(a) show temperature dependence of the FWHM for BaFe$_2$As$_2$ at zero pressure. Similar to BaFe$_{1.97}$Ni$_{0.03}$As$_2$,$^{45}$ temperature dependence of FWHM follows a Curie-Wiess form and peaks around the zero-pressure value of $T_N \approx T_s$. Upon application of a uniaxial pressure $P \approx 20$ MPa, the magnitude of FWHM increases at all temperatures and now peaks at an enhanced $T_N = 144$ K [Fig. 3(a)].

Figure 3(b) shows similar data for SrFe$_{1.97}$Ni$_{0.03}$As$_2$,
FIG. 3: (Color online) Temperature dependence of FWHM of $\Delta d/d$ in several iron pnictides obtained from neutron Larmor diffraction experiments\textsuperscript{20}. (a) Temperature dependence of $\Delta d/d$ in FWHM for the (4, 0, 0) Bragg reflection of BaFe$_2$As$_2$ at $P = 0$ and 20 MPa. The solid line above $T_N$ is a fit using Curie-Weiss formalism [FWHM($T$) = $A/(T-T_1)+B$, where $A, B$, and $T_1$ are fitting parameters]. (b) Similar data for SrFe$_{1.97}$Ni$_{0.03}$As$_2$. The vertical blue and red dashed lines in (a) and (b) mark the $T_N$ of the sample at zero and finite pressure, respectively. (c) Similar data for BaFe$_{1.97}$Ni$_{0.03}$As$_2$, where the vertical green and blue dashed lines mark $T_N$ and $T_s$, respectively, at zero pressure. The open green and yellow squares mark measurements of FWHM under zero pressure (fresh) at the (4, 0, 0) and (0, 4, 0) Bragg peaks, respectively. The pink solid circles are identical measurements under $P \approx 10$ MPa uniaxial pressure on (4, 0, 0). The solid green diamonds are data after uniaxial pressure is released. The vertical red dashed line indicates the peak position of the FWHM under $P = 10$ MPa. (d) Temperature dependence of FWHM in $\Delta d/d$ for BaFe$_2$As$_2$ at $P = 0$ MPa (solid green circles), BaFe$_{1.88}$Ni$_{0.12}$As$_2$ at $P = 0$ (solid green diamonds) and 14 MPa (solid red circles), where there are coupled strong first order structural and AF phase transitions at $T_N = T_s = 175$ K\textsuperscript{11}. Compared with BaFe$_2$As$_2$, where the AF phase transition is weakly first order and structural transition is second order\textsuperscript{5}, the AF and structural transition induced changes in FWHM are much smaller and confined to temperatures close to $T_N \approx T_s$ in SrFe$_{1.97}$Ni$_{0.03}$As$_2$ [Fig. 3(b)]. Under a uniaxial pressure $P \approx 20$ MPa, however, both the FWHM and $T_N$ increase dramatically with solid lines showing Curie-Weiss fits to the data. For BaFe$_{1.97}$Ni$_{0.03}$As$_2$, application of a $P \approx 10$ MPa uniaxial pressure transforms temperature dependence of the FWHM, which forms a broad peak above the zero-pressure value of $T_s$. Upon releasing the uniaxial pressure [$P$ released, filled green diamonds in Fig. 3(c)], the system goes back to the original unpressed fresh state.

Figure 3(d) compares temperature dependence of the FWHM for electron overdoped BaFe$_{1.88}$Ni$_{0.12}$As$_2$ and BaFe$_2$(As$_0.7$P$_{0.3}$)$_2$, where both materials are in the paramagnetic tetragonal state without static AF order. The weak temperature dependence of FWHM in these materials suggests that the large temperature dependence of FWHM in AF ordered BaFe$_2$As$_2$ ($x = 0, 0.03$) and SrFe$_{1.97}$Ni$_{0.03}$As$_2$ is due to a strong magnetoelastic coupling. Although application of a $P \approx 14$ MPa uniaxial pressure on BaFe$_{1.88}$Ni$_{0.12}$As$_2$ increases the absolute value of FWHM, it is still weakly temperature dependent [Fig. 3(d)].

To further demonstrate the impact of uniaxial pressure on the tetragonal-to-orthorhombic structural transition in BaFe$_{2-x}$Ni$_x$As$_2$ ($x = 0, 0.03, 0.12$) and SrFe$_{1.97}$Ni$_{0.03}$As$_2$, we compare in Figure 4 temperature dependence of the lattice parameters along the orthorhombic $a$ and $b$ axis directions under zero and finite uniaxial pressure. We first discuss results for BaFe$_{2-x}$Ni$_x$As$_2$ with $x = 0$ [Fig. 4(a), 4(b)] and 0.03 [Fig. 4(c) and 4(d)]. At $P = 0$, the lattice parameters have $a = b$ at temperatures above $T_s$ (tetragonal phase) and decrease linearly with decreasing temperature [open diamonds and hexagons in Fig. 4(a) and 4(c)]. Upon application of a uniaxial pressure, the system becomes orthorhombic at all temperatures and the orthorhombic structural transition becomes a crossover [filled diamonds and hexagons in Fig. 4(a) and 4(c)]. Figures 4(b) and 4(d) show temperature dependence of the lattice orthorhombicity $\delta = (a - b)/(a + b)$ at different uniaxial pressures for $x = 0$, and 0.03, respectively. For unpressed fresh samples ($P = 0$), and after the pressure has been released, the tetragonal structure becomes orthorhombic below $T_s$ and the AF order below $T_N$ further enhances the lattice orthorhombicity\textsuperscript{5}. Upon applying the uniaxial pressure $P \approx 10, 15,$ and 20 MPa, the temperature dependence of the lattice orthorhombicity becomes remarkably similar to that of the $B_{2g}$ elastic constants and nematic susceptibility of BaFe$_{2-x}$As$_2$ obtained from transport\textsuperscript{23,24} and elastic shear modulus/ultrasound spectroscopy measurements\textsuperscript{18,31,32}, respectively.
B. Theoretical Ginzburg–Landau analysis

To understand the temperature dependence of the pressure-induced lattice orthorhombicity described in Figs. 4(b) and 4(d), we consider the Ginzburg-Landau free energy formalism used in previous works\textsuperscript{20,38}:

\[
F[\varphi, \delta] = F_0 + \frac{a}{2}(T - T_0)\varphi^2 + \frac{B}{4}\varphi^4 + \frac{C_{66,0}}{2}\delta^2 - \lambda\delta\varphi - P\delta,
\]

where the electronic nematic order parameter \( \varphi \) is coupled linearly to the orthorhombic lattice distortion \( \delta \). It then follows that (see appendix\textsuperscript{56})

\[
\delta = (\lambda\langle \varphi \rangle + P)/C_{66,0},
\]

where \( C_{66,0} \) is the bare elastic constant that has no strong temperature dependence and \( P \) is the conjugate uniaxial pressure (stress)\textsuperscript{38,41,50–52}. In the absence of the elasto-nematic coupling (\( \lambda = 0 \)), the nematic susceptibility \( \chi_\varphi = 1/[a(T - T_0)] \) is characterized by the Curie-Weiss temperature \( T_0 \). Upon considering the coupling between the nematic order parameter \( \varphi \) and the structural lattice distortion \( \delta \) (or equivalently, the elastic shear strain \( \varepsilon_6 \)), the elastic susceptibility takes on the form\textsuperscript{20,38}:

\[
\frac{d\delta}{dP} = \frac{1}{C_{66,0}} \frac{T - T_0}{T - T_s^{CW}}
\]

with the renormalized nematic transition temperature \( T_s^{CW} = T_0 + a^2/(aC_{66,0}) \) that is increased compared to the bare Curie-Weiss temperature \( T_0 \). The pressure-induced lattice distortions in Figs. 4(b) and 4(d) can be well described by the Curie-Weiss functional form\textsuperscript{50}. Therefore, uniaxial pressure induced orthorhombic lattice distortion and its temperature dependence in underdoped iron pnictides indeed arises from the coupling of the uniaxial-pressure induced lattice distortion \( \delta \) with the nematic susceptibility, it would be interesting to determine the effect of similar uniaxial pressure on the electron overdoped sample, where the resistivity anisotropy is known to be much weaker\textsuperscript{14}. Figures 4(e) and 4(f) summarize the outcome of the neutron Larmor diffraction experiments on uniaxial pressure BaFe\textsubscript{1,88}Ni\textsubscript{0,12}As\textsubscript{2}, which is tetragonal \( (a = b) \) and non-magnetic at all temperatures in zero pressure\textsuperscript{10}. Figure 4(e) shows temperature dependence of the lattice parameter changes along the \( a \)-axis \( (\Delta a/a) \) and \( b \)-axis \( (\Delta b/b) \) under a uniaxial pressure of \( P \approx 14 \) MPa. For comparison, the thermal contraction of aluminum is also shown\textsuperscript{56}. Figure 4(f) shows the temperature dependence of the orthorhombic lattice distortion \( \delta \), which reveals a clear anomaly at \( T_c \), consistent with ultrasonic spectroscopy measurements\textsuperscript{51,52}. While the applied uniaxial pressure induces orthorhombic lattice distortion at 230 K, the magnitude of the lattice distortion, \( \delta \approx 1.1 \times 10^{-4} \), is about 5 times smaller than that of BaFe\textsubscript{2}As\textsubscript{2} and BaFe\textsubscript{1,97}Ni\textsubscript{0,03}As\textsubscript{2} at 230 K. On cooling to 20 K, \( \delta \) in BaFe\textsubscript{1,88}Ni\textsubscript{0,12}As\textsubscript{2} increases to \( 2 \times 10^{-4} \), while \( \delta \) in BaFe\textsubscript{2}As\textsubscript{2} and BaFe\textsubscript{1,97}Ni\textsubscript{0,03}As\textsubscript{2} becomes \( 2.5 \times 10^{-3} \) near \( T_s \) [Fig. 4(b) and 4(d)], an order of magnitude larger than that of the electron overdoped compound.

To understand how a uniaxial pressure affects the first order nature of the structural and magnetic phase transitions in SrFe\textsubscript{1,97}Ni\textsubscript{0,03}As\textsubscript{2}, we compare in Fig. 4(g) and 4(h) temperature dependence of the lattice parameters and orthorhombicity under the zero and finite uniaxial pressure. At zero pressure, the first order nature of the structural transition is clearly seen in hysteresis of temperature dependence of the lattice parameters and distortion [Fig. 4(g) and 4(h)]. Upon application of \( P \approx 20 \) MPa uniaxial pressure, the lattice orthorhombicity no longer displays the first order transition at \( T_s \), but instead becomes a crossover, similar to that observed in the undoped and underdoped BaFe\textsubscript{2−x}Ni\textsubscript{x}As\textsubscript{2} [see Figs. 4(b) and 4(d)].

Assuming that the application of the modest uniaxial pressure \( P \approx 20 \) MPa can be considered in the linear-response regime\textsuperscript{45}, we can estimate the elastic susceptibility from the finite difference \( \delta P \propto \Delta(\delta) = \delta(P = 20 \) MPa) − \( \delta(P = 0) \) and compare it among the different compounds in the iron pnictide family. Figure 1(c) compares temperature dependence of \( \delta(P = 20 \) MPa) − \( \delta(P = 0) \) for BaFe\textsubscript{2−x}Ni\textsubscript{x}As\textsubscript{2} (\( x = 0, 0.03, 0.12 \)) and SrFe\textsubscript{1,97}Ni\textsubscript{0,03}As\textsubscript{2} normalized for \( P = 20 \) MPa. For AF ordered BaFe\textsubscript{2−x}Ni\textsubscript{x}As\textsubscript{2} (\( x = 0, 0.03 \)) and SrFe\textsubscript{1,97}Ni\textsubscript{0,03}As\textsubscript{2}, the magnitudes of the pressure-induced lattice orthorhombicity are similar in the paramagnetic phase and vanish rapidly upon entering into the AF ordered state. Furthermore, the \( \delta(P = 20 \) MPa) − \( \delta(P = 0) \) decreases for the iron pnictides with reduced \( T_N \), and are much smaller for BaFe\textsubscript{1,88}Ni\textsubscript{0,12}As\textsubscript{2}.

III. DISCUSSION

It is well known that the effect of increasing electron-doping in BaFe\textsubscript{2−x}T\textsubscript{z}As\textsubscript{2} is to suppress the static AF order and to eliminate the low-temperature lattice orthorhombicity\textsuperscript{7–10}. At zero pressure, BaFe\textsubscript{2}As\textsubscript{2} first exhibits a second-order structural transition from the high-temperature paramagnetic tetragonal phase to a paramagnetic orthorhombic phase at \( T_s \), followed by a discontinuous further orthorhombic structural distortion and weakly first order AF phase transition at \( T_N \) (\( T_N < T_s \)) due to magnetoelastic coupling\textsuperscript{5}. Upon Ni-doping in BaFe\textsubscript{2−x}Ni\textsubscript{x}As\textsubscript{2}, the structural and magnetic phase transitions are gradually separated and suppressed [Fig. 1(a)], and become second order in nature\textsuperscript{7–10}. Upon application of a uniaxial pressure, the \( C_4 \) rotational symmetry of the tetragonal lattice is broken. Since the tetragonal-to-orthorhombic symmetry of the under-
FIG. 4: (Color online) Temperature dependence of the a and b lattice parameters and orthorhombicity $\delta$ under different uniaxial pressure conditions ($P = 0$ fresh, $\sim 10$, $\sim 15$, $\sim 20$ and 0 released MPa) for BaFe$_{2-x}$Ni$_x$As$_2$ ($x = 0, 0.03, 0.12$) and SrFe$_{1.97}$Ni$_{0.03}$As$_2$. (a) Temperature dependence of the a and b under $P = 0$ and 20 MPa uniaxial pressure for BaFe$_2$As$_2$. (b) Temperature dependence of $\delta$ under different uniaxial pressure ($P = 0$ fresh, $\sim 20$, and 0 released MPa). The vertical blue dashed line marks the $T_N/T_s$. (c) Temperature dependence of the lattice parameters a and b at $P = 0$ and 15 MPa for BaFe$_{1.97}$Ni$_{0.03}$As$_2$. (d) Temperature dependence of $\delta$ under different uniaxial pressure ($P = 0$ fresh, $\sim 10$, $\sim 15$ and 0 released MPa). The open red diamonds and green hexagons are obtained by lattice thermal expansion measurements under uniaxial pressure. The pink squares are measurements of an unpressurized fresh sample, while blue circles are obtained after releasing $P \approx 10$ MPa uniaxial pressure. The blue circles and two pink squares below $T_s$ are from zero pressure Larmor diffraction measurements. The pink squares above $T_s$ are obtained from thermal expansion measurements. The vertical arrow marks $T_s = 18.6$ K and the solid lines are guides to the eye. (e) Temperature dependence of the a and b for BaFe$_{1.88}$Ni$_{0.12}$As$_2$. The lattice thermal expansion of aluminum is plotted as a reference. The vertical arrow marks $T_N = 18.6$ K and the solid lines are guides to the eye. (f) Temperature dependence of the orthorhombic lattice distortions calculated from (c). (g) Temperature dependence of the a and b lattice parameters for SrFe$_{1.97}$Ni$_{0.03}$As$_2$ under $P = 0$ fresh, 20 and 0 (released) MPa. (h) Temperature dependence of $\delta$ for the same pressure condition. The solid curves in (b), (d), (f), and (h) are fits using a Curie-Weiss functional form.
lying lattice can only be broken once, $T_s$ will become a
crossover regardless the magnitude of the applied pressure,
as our findings in Figs. 3 and 4 corroborate. The same conclusion
holds for SrFe$_{1.97}$Ni$_{0.03}$As$_2$ where the first-order structural transition becomes a crossover [see Figs. 4(g) and 4(h)]. Therefore, both BaFe$_{2-x}$Ni$_x$As$_2$
and SrFe$_{1.97}$Ni$_{0.03}$As$_2$ under uniaxial pressure can only exhibit AF phase transition. We note that our measurements and theoretical Landau–Ginzburg analysis do
not rely on the microscopic nature of the nematic order parameter $\varphi$. In particular, they apply equally well to
the so-called Ising spin nematic scenario$^{25-29}$ or the
orbital order interpretation of nematicity$^{30-36}$. In fact, the
ferro-orbital order $\varphi_{\text{orb}} = \langle n_{xz} - n_{yz} \rangle$ is always linearly
coupled$^{26,36}$ to the Ising spin nematic order parameter $\varphi_{\text{spin}} = \langle S_z \cdot S_{i+x} - S_z \cdot S_{i+y} \rangle$, so the orbital order is
generically present whenever $\varphi_{\text{spin}} \neq 0$, although there
are theoretical indications that the converse is not always
true. In other words, the orbital order can exist in the
absence of static AF order$^{36}$, as is known to be the case in FeSe$^{37-39}$. In either case, the application of external uniaxial
stress renders the nematic transition a crossover, so
that the lattice distortion $\delta$ and consequently $\varphi$ are both
finite above the zero-stress value of $T_s$. In this light,
the electronic anisotropy seen in the magnetic torque$^{21}$
and scanning tunneling microscopy$^{43}$ measurements above $T_s$
without explicit external uniaxial pressure is likely due to
intrinsic local strain in these materials which breaks the
$C_4$ rotational symmetry of the paramagnetic tetragonal
phase. Indeed, local strain-induced effect has recently
been observed in free standing BaFe$_{2}$As$_2$ above $T_N$ and
$T_s$.$^{60}$

The key finding of the present work is that undoped BaFe$_{2}$As$_2$, as well as BaFe$_{1.97}$Ni$_{0.03}$As$_2$ and
SrFe$_{1.97}$Ni$_{0.03}$As$_2$ all exhibit similar magnitudes of the
pressure-induced lattice orthorhombicity [Fig. 1(c) and
Fig. 4] and FWHM of $\Delta d/d$ near $T_N$ (Fig. 3). This
indicates that these samples experience similar strain field
under nominally similar applied uniaxial pressure, thus
suggesting that the doped Ni impurities do not play an
important role in determining the strain field inside the
sample. Theoretically, the electronic anisotropy of the
iron pnictides is expected to couple linearly to the lattice
orthorhombicity $\delta^{26-29}$, as captured by the effective
Landau free energy in Eq. (1). The Curie-Weiss like
temperature dependence of the uniaxial pressure in-
duced lattice distortion [Fig. 1(c)] is consistent with the
temperature dependence of the nematic susceptibility $d\delta/dP$ in Eq. (3) and agrees with the results of
Young’s modulus measurements$^{38}$. This gives us confi-
dence that in the effective Landau description$^{39}$, the
uniaxial pressure-induced lattice distortion $\delta$ has a com-
ponent proportional to the electronic nematic order pa-
parameter $\varphi$ via Eq. (2), where one expects $\delta \propto \varphi$ in zero
pressure ($P = 0$). Since $\delta$ has similar magnitude in
BaFe$_{2}$As$_2$, BaFe$_{1.97}$Ni$_{0.03}$As$_2$, and SrFe$_{1.97}$Ni$_{0.03}$As$_2$ (see Fig. 4), one would also expect comparable values of $\varphi$
in all three compounds. So if one uses the resistivity
anisotropy $\Delta \rho = (\rho_{x} - \rho_{y})/(\rho_{x} + \rho_{y})$ as a proxy for the
nematic order parameter, as has been widely used in the
literature$^{12,20,23,24}$, how does one then explain the resistivity
anisotropy differences in BaFe$_{2-x}$T$_x$As$_2$.$^{14}$ and a
much smaller resistivity anisotropy above $T_N$ [Fig. 1(b)]
in SrFe$_{2-x}$T$_x$As$_2$ family of materials$^{38,42}$. The bare value
of the elastic shear modulus $C_{66,0}$ that enters Eq. (20) has
no strong temperature dependence$^{38}$ and from the
Curie-Weiss fits of the nematic susceptibility to Eq. (24),
we find it to be roughly the same in all three compounds,
$C_{66,0} \approx 50$ GPa$^{39}$. The only remaining un-
known variable is the elasto-nematic coupling constant $\lambda$,
which could be material-dependent but not temperature-
dependent.$^{20,38}$ It is thus very challenging to explain
the qualitatively different temperature dependence of the
resistivity anisotropy in BaFe$_{1.97}$Ni$_{0.03}$As$_2$ [monotonic,
blue diamonds in Fig. 1(b)] from that in BaFe$_{2}$As$_2$ and
SrFe$_{1.97}$Ni$_{0.03}$As$_2$ [both non-monotonic, with a max-
imum at or just below $T_s$]. One possible explanation for
the non-monotonic temperature dependence of the resid-
itivity anisotropy, recently proposed in the context of
FeSe$^{61}$, is to assume a temperature dependent coefficient of
proportionality between $\Delta \rho$ and $\varphi$:

\[
\Delta \rho(T) = \Upsilon(T) \varphi(T),
\]

such that $\Upsilon(T)$ tends to zero as $T \to 0$, whereas $\varphi(T)$ is expected to increase monotonically below $T_s$ as
the temperature is lowered (consider for instance the mean-field result $\varphi(T) \propto \sqrt{T_s - T}$ for the second order phase transition).

Even with the introduction of $\Upsilon(T)$ in Eq. (4), which
has a meaning of the temperature-dependent scattering
function, it is extremely difficult to explain the much
lower value of $\Delta \rho$ in SrFe$_{1.97}$Ni$_{0.03}$As$_2$ compared to
BaFe$_{2}$As$_2$ and BaFe$_{1.97}$Ni$_{0.03}$As$_2$. In fact, from the
Curie-Weiss fits of the susceptibility data, we estimate the
elasto-nematic coupling constant $\lambda$ to be a factor of $\sim 5$ smaller in SrFe$_{1.97}$Ni$_{0.03}$As$_2$ compared to
BaFe$_{1.97}$Ni$_{0.03}$As$_2$. Given the comparable magnitudes of $\delta$ between the two compounds [see Fig. 4(d) and
4(h)], one would then expect the nematic order parameter $\varphi$ to be a factor of $\sim 5$ greater in SrFe$_{1.97}$Ni$_{0.03}$As$_2$,
to ensure that the left-hand side of Eq. (2) remains of the
same magnitude. And yet the resistivity anisotropy $\Delta \rho \propto \varphi$ paints a diametrically opposite picture, being
much smaller in SrFe$_{1.97}$Ni$_{0.03}$As$_2$.

We propose that a likely resolution of this dilemma lies
in the nature of the magnetic phase transition which we
have so far neglected in our analysis. Indeed, it is well
established that structural and magnetic phase transitions in SrFe$_{2-x}$T$_x$As$_2$ are coupled first order trans-
itions that decrease with increasing $x$ before vanishing
near optimal superconductivity$^{11}$, while electron-
doped BaFe$_{2}$As$_2$ has second order magnetic and struc-
tural phase transitions.$^{7-10}$ Although application of
a uniaxial pressure renders the structural transition a
crossover, the first order nature of the magnetic transi-
tion means a vanishing critical regime with suppressed
low-energy spin fluctuations at temperatures near $T_N$, compared with those of BaFe$_{2-x}$Ta$_x$As$_2$ where the AF phase transition is second order. One expects the scattering of electrons on the magnetic fluctuations, and hence the resistivity, to therefore be smaller in the vicinity of the first-order magnetic transition, as is the case in SrFe$_{2-x}$Ta$_x$As$_2$. We thus conclude that the vanishing resistivity anisotropy above $T_N$ in the uniaxial pressure detwinned SrFe$_{2-x}$Ta$_x$As$_2$ (compared with those of BaFe$_{2-x}$Ta$_x$As$_2$) is likely rooted in the first order nature of the AF phase transition. This is also consistent with the increased paramagnetic resistivity anisotropy on moving from BaFe$_{2}$As$_2$ to BaFe$_{1.96}$Co$_{0.04}$As$_2^{15}$, where the magnetic transition changes from weakly first order to second order$^{5,7,8}$. Similarly, the lack of large resistivity anisotropy in the paramagnetic state of uniaxial pressured Ba$_{1-x}$K$_x$Fe$_2$As$_2$$^{62}$, Ba$_{1-x}$Na$_x$Fe$_2$As$_2$$^{63}$, and Ca$_{1-x}$La$_x$Fe$_2$As$_2$$$^{64}$ is likely due to the first order nature of the paramagnetic to AF phase transition in these materials. The phenomenological Landau theory can be extended to include the coupling between nematicity $\varphi$ and the magnetic order parameter$^{38,50}$, and our theoretical analysis shows$^{50}$ that the resulting uniaxial pressure-induced lattice distortion $\delta(P) - \delta(0)$ reproduces semi-quantitatively the experimental findings in Fig. 1(c).

We conclude that the in-plane resistivity anisotropy found in the paramagnetic state of iron pnictides depends sensitively on the nature of the magnetic phase transition and a strong elasto-nematic coupling between the uniaxial pressure induced lattice distortion and the electronic nematic susceptibility. We caution that while the resistivity anisotropy $\Delta \rho$ and its dependence on the shear strain can be successfully used to extract the quantity proportional to the nematic susceptibility$^{20}$, care should be taken when equating $\Delta \rho$ with the nematic order parameter itself. In particular, the non-monotonic temperature dependence of $\Delta \rho$ and its sensitivity to the nature of the magnetic phase transition remain relatively little explored and deserve further experimental and theoretical studies.

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V. APPENDIX

A. Sample Information

The iron pnictide single crystals used in present study were prepared by self-flux method$^{53}$. The samples have been characterized by resistivity, magnetization, and neutron scattering measurements. Figures 5 and 6 show the basic characterizations of BaFe$_{1.97}$Ni$_{0.03}$As$_2$ and SrFe$_{1.97}$Ni$_{0.03}$As$_2$ samples, respectively. The basic characteristics of the BaFe$_{2}$As$_2$ and BaFe$_{1.88}$Ni$_{0.12}$As$_2$ samples can be found elsewhere$^{41,53}$.

FIG. 5: (Color online) (a) Temperature dependence of the magnetic susceptibility under ZFC and FC cases for BaFe$_{1.97}$Ni$_{0.03}$As$_2$. (b) Temperature derivative of the magnetic susceptibility, showing clearly the structural and magnetic phase transitions. (c) Temperature dependence of the magnetic susceptibility, showing clearly the structural and magnetic phase transitions. (c) Temperature dependence of the magnetic susceptibility, showing clearly the structural and magnetic phase transitions. (c) Temperature dependence of the magnetic susceptibility, showing clearly the structural and magnetic phase transitions.

Figure 5(a) shows temperature dependence of the zero field cooled (ZFC) and field cooled (FC) magnetic susceptibility $\chi$. Figure 5(b) is temperature derivative of $\chi$, $d\chi/dT$. Figure 5(c) shows temperature dependence of the magnetic $(1, 0, 1)$ Bragg peak (green diamonds) and $(2, -2, 0)$ nuclear Bragg intensity (red squares). These results establish $T_N$ (green dashed line) and $T_s$ (red dashed...
increase of the (4 0 0) Bragg reflection signals the change of structural distortion near $T_s$.\(^{41}\)

Figure 6(a) shows temperature dependent resistivity $R$ and its temperature derivative $dR/dT$ for SrFe$_{1.97}$Ni$_{0.03}$As$_2$. The dip of the $dR/dT$ at $T = 175$ K indicates the coexisting structural and magnetic transition, different from the two features for the separated $T_N$ and $T_s$ in BaFe$_{1.97}$Ni$_{0.03}$As$_2$. Figure 6(b) is temperature dependence of the (4 0 0) nuclear Bragg peak intensity. The dramatic increase of the peak intensity also signals the structural transition. The observed intensity hysteresis is consistent with first order nature of the structural and magnetic phase transition.

Large single crystals were selected and cut into rectangular shapes along the orthorhombic [1, 0, 0] and [0, 1, 0] directions by a high-precision wire saw. The well-cut samples were placed inside a uniaxial pressure device in the [1, 1, 2] $\times$ [1, −1, 0] scattering plane, where both the (1, 0, 1) and (0, 1, 1) magnetic Bragg peaks can be reached\(^{41}\).

B. Neutron resonance spin echo measurements

Neutron spin echo (NSE) technique has been demonstrated to be an effective method to measure the slow dynamics (quasielastic scattering) with an extremely high energy resolution ($\sim 1 \mu$eV or even to $\sim 1$ neV)\(^{67}\). By combining triple axes spectrometer and neutron resonance spin echo (NRSE) technique, the TRISP spectrometer at the Forschungsneutronenquelle Heinz Maier-Leibnitz (MLZ) is capable of measuring the lifetime of excitations with an energy resolution $\Delta E \sim 1 \mu$eV in the range of about 1 $\sim$ 200 $\mu$eV\(^{68}\).

Compared with typical neutron scattering experiments where $S(Q, \omega)$ ($E = \hbar \omega$) is usually measured, neutron spin echo measures $I(Q, \tau_{NSE})$ or $P(Q, \tau_{NSE})$, where $P$ is the polarization of the scattered neutrons, which is the time Fourier transform of the $S(Q, \omega)$ and thus provides direct information of $S(Q, \omega)$ such as energy line-width (lifetime) and intensity\(^{48,69}\).

The basic principle of NSE can be understood in a simplified picture as shown in Figure 7(a). We assume neutrons polarized along the y direction with a velocity $v_1$ enter the first arm of NSE spectrometer with a constant
FIG. 8: (Color online) (a) Measurements of the neutron polarization in one period of $\phi$ for $\tau = 16.29$ ps and 39.25 ps. The solid lines are cosine fittings of the data using eq. (8). $P(\tau)$ for various temperatures. The solid lines are fittings by eq. (10). The brown dashed line shows a drawing of eq. (10) with $T = 5 \mu eV$ for comparison purpose. The corresponding Lorentzian $S(\omega)$ are shown as the solid green and brown lines in the inset.

magnetic field $B$ [Fig. 7(a)]. The precession angle in the first arm ($L_1$) is then $\phi_1 = \omega_L t = \gamma |B| L_1 / v_1$, where $\gamma = 2 \mu_N / h = 3.916$ kHz/Gauss is the magnetoratio of neutron, $L_1$ is the length of the first neutron guide arm, and $t$ is the time for neutron to travel through the first arm. After interactions with the sample, some neutrons are scattered into different energy with velocity $v_2$. In the second arm ($L_2$), the neutron spin will precess along the opposite direction, generating $-\phi_2 = -\omega_L L_2 / v_2$. Assuming $L_1 = L_2 = L$ and $v_2 = v_1 + \delta v$, $\delta v << v_1$, the net phase after passing through both field regions will be $\phi = \frac{\hbar}{m} \delta v$. Since neutron energy transfer is $\hbar \omega = \frac{1}{2} m (v_2^2 - v_1^2) \approx m v_1 \delta v$, the net phase can be written as

$$\phi = \left( \frac{\hbar \omega L}{mv_1^2} \right) \omega \equiv \omega T_{NSE}$$

where $T_{NSE}$ is defined as

$$T_{NSE} = \left( \frac{\hbar \omega L}{mv_1^2} \right) = 1.863 \times 10^{-16} B(\text{gauss})L(\text{cm}) \lambda^3(\text{Å})$$

Note $T_{NSE}$ is not a physical time but a quantity determined by specific parameters of the spectrometer, with the dimension of time.

The polarization along $y$ direction of the scattered neutrons can be analyzed and detected [Fig. 7(a)]. The average polarization $< \sigma_y >$ for neutrons with energy transfer $\hbar \omega$ is

$$< \sigma_y > = < \cos \phi > = \int d \omega S(\mathbf{Q}, \omega) \cos \omega T_{NSE}.$$ 

Thus $< \sigma_y >$ is the cosine Fourier transform of $S(\mathbf{Q}, \omega)$ for $\omega$ and has been shown equal to the intermediate scattering function $I(\mathbf{Q}, \tau)$. Therefore, the $T_{NSE}$ dependent polarization $P(\tau)$, that is, $I(\mathbf{Q}, \tau)$, provide direct information about $S(\mathbf{Q}, \omega)$.48

In the NRSE, the precession fields and spin flippers are replaced by four short bootstrap rf spin flipper coils $\text{C1-C4 in Fig. 7(b)}$, which can improve the energy resolution by a factor of 4 compared with the NSE with the same $B$ and $L$. The neutrons only precess in bootstrap while keep their spin directions in $L_1$ and $L_2$. $L_2$ can be tuned by translating the flipper $C4$, by which the intensity with respect to the position of $C4$, $I(x_{c4})$, can be measured. For a fixed $\tau$, the measured intensity can be described as

$$I(x_{c4}) = \frac{I_0}{2} \left[ 1 + P \cos \left( \frac{2 \pi}{\Delta x_{c4}} (x_{c4} - x_{c4,0}) \right) \right],$$

where $P$ is the polarization, $I_0$ is the averaged intensity of the scattered beam, $\Delta x_{c4}$ is the period of the intensity modulation, and $x_{c4,0}$ is the reference position of $C4$.

The measurements of the $P(\tau)$ for BaFe$_{1.97}$Ni$_{0.03}$As$_2$ under $P \approx 15$ MPa are summarized in Figure 8. Figure 8(a) shows the intensity modulations for $\tau = 16.29$ ps and 39.25 ps of $Q=(1, 0, 1)$ at $T = 102$ K. The polarizations are obtained through fitting the data by eq. (8). The fitted $P(\tau)$ for different temperatures are plotted in Figure 8(b). Assuming the possible broadening in energy of the magnetic reflections is caused by some slow dynamics (quasielastic scattering), the corresponding $S(\omega)$ can be described by a simple Lorentzian:

$$S(\omega) = \frac{1}{\pi} \frac{\Gamma}{(\omega - \omega_0)^2 + \Gamma^2},$$

where $\Gamma (\Gamma \geq 0)$ (Half Width at Half Maximum) is the line-width of the quasielastic scattering ($\omega_0 = 0$). Followed by eq. (9), the $P(\tau)$ should be fitted by the Fourier transform of eq. (9):

$$P(\tau) = P_0 \exp \left( -\frac{\Gamma \tau}{\hbar} \right),$$

All the $P(\tau)$ in our measurements can be well described by this exponential decay, as shown in Figure 8(b). The fitted energy line-widths $\Gamma$ are less than 1 $\mu eV$, meaning the signal are resolution limited at the measured temperatures. The comparison between $S(\omega)$ for resolution limited ($\Gamma \leq 1$ $\mu eV$) and $\Gamma = 5 \mu eV$ is shown in the inset of Figure 8(b), as a reference. The temperature dependence of $\Gamma$ is shown in Figure 2(b) of the main text, which must have values greater than zero. The large error bars for the values of $\Gamma$ near $T_N$ are due to experimental uncertainties of $P(\tau)$ in Fig. 8(b).
FIG. 9: (Color online) Measurement of the $\Delta \phi_{\text{tot}}$ between $T = 113$ K and $T = 118.6$ K, by which the relative change of $d$ spacing can be tracked.

FIG. 10: (Color online) Larmor diffraction measurements of $P(\tau)$ for BaFe$_{1-x}$Ni$_x$O$_3$As$_2$. (a) Comparison of $P(\phi_{\text{tot}})$ at $Q = (4, 0, 0)$ between $T = 4$ K and 121 K with $P \approx 10$ MPa. (b) $P(\phi_{\text{tot}})$ for the (4, 0, 0) and (0, 4, 0) reflections measured at $T = 102.4$ K with $P \approx 10$ MPa. The inset shows the Gaussian distribution of the $d$ spacing. (c) Temperature dependence of the $P(\phi_{\text{tot}})$ for the (4, 0, 0) peak at $P = 0$. $P(\phi_{\text{tot}})$ for the two $d$ spacings shows clear modulation which can be fitted by eq. (14) (solid curves) due to the twinning caused by the tetragonal-to-orthorhombic structural transition.

C. Larmor diffraction measurements

We now turn to the neutron Larmor diffraction measurements. Larmor diffraction is a neutron Larmor precession technique capable of measuring lattice spacing expansion and spread with a resolution better than $10^{-5}$ in term of $\Delta d/d$. It is sensitive to minor change of lattice spacing $d$ but insensitive to sample mosaicity and not much affected by slight misalignment. The total precession phase $\phi_{\text{tot}}$ dependent polarizations $P(\phi_{\text{tot}})$ can be used to determine the $d$ spread and the splitting between multiple $d$ spacings with small differences, such as the peak splitting caused by the tetragonal-to-orthorhombic structural transitions in iron pnictides.

Figure 7(b) is a schematic of Larmor diffraction. The spin flippers are tuned to be parallel with the diffracting planes and the neutron precession directions in $L_1$ and $L_2$ are the same. Assuming $L_1 = L_2 = L$, the total neutron precession phase is $\phi_{\text{tot}} = 2\omega_L L/v$. From the Bragg law $|Q| = |G| = 2k_\|\sin \theta_B$, $|G| = 2\pi/d$, and the neutron velocity $v = \hbar k_\|/m$, the total Larmor phase $\phi_{\text{tot}}$ can be written as

$$\phi_{\text{tot}} = \frac{2\omega_L L m \sin \theta_B}{\pi \hbar} d. \quad (11)$$

Consequently, the variation of the Larmor phase is proportional to the change of the $d$ spacing (caused by external or thermal effect), that is

$$\Delta \phi_{\text{tot}} = \phi_{\text{tot}} \frac{\Delta d}{d}. \quad (12)$$

For $d$ change induced thermal expansion, the evolution of
$P(\phi_{\text{tot}})$ at different temperatures and the relative change of the $\phi_{\text{tot}}$ ($\Delta \phi_{\text{tot}}$) can be obtained by fitting the intensity modulations $I(\phi_{\text{tot},0} + \Delta \phi)$ using eq. (8), where the modulations are measured by scanning $x_{c}$ near $x_{c,0}$ [Fig. 7(b) and Fig. 9]. The $\Delta \phi_{\text{tot}}$ between different temperatures (or pressures/Qs) can be used to determine the evolution of the lattice spacings. To facilitate data analysis, $\Delta \phi_{\text{tot}}$ between two neighbouring conditions should be kept within $2\pi$. Figure 9 is an example of lattice thermal expansion at $Q = (4, 0, 0)$ of BaFe$_{1.97}$Ni$_{0.03}$As$_2$. The difference in $x_{c}$ ($\delta L$) between $T = 113$ K and 118.6 K, $\delta L$, can be converted to lattice expansions according to eq. (11, 12). In present measurements, 1 mm is equivalent to $\sim 1 \times 10^{-5}$ in $\Delta d/d$, with resolution $\sim 1 \times 10^{-5}$. Note lattice expansion measurements is only valid for single $d$ spacing at one $Q$. Systems showing coexisting multiple $d$ spacings around the same $Q$ with small differences between them cannot be measured by this method.

Besides the lattice expansion measurements, the $P(\phi_{\text{tot}}) = \langle \cos \Delta \phi(\phi_{\text{tot}}) \rangle$ in a wide range of $\phi_{\text{tot}}$ has been demonstrated to be the Fourier transform of the lattice spacing distribution $[f(\Delta d/d)]^{47,70}$. For a single-Gaussian distribution of $d$ with FWHM=$\varepsilon_{FW}$, the $P(\phi_{\text{tot}})$ can be derived as

$$P(\phi_{\text{tot}}) = P_0 \exp\left(-\frac{\phi_{\text{tot}}^2 \varepsilon_{FW}^2}{16 \ln 2}\right),$$

where the FWHM represents the magnitude of the $d$ spread. It is usually expressed in term of $\Delta d/d$. The data shown in the Figure 3 of the main text are temperature dependence of the FWHM (lattice spacing spread). All of our $P(\phi_{\text{tot}})$ for single $d$ spacing are well described by this model, resulting in a Gaussian distribution of the $d$ values. Figure 10 shows the $P(\phi_{\text{tot}})$ of BaFe$_{1.97}$Ni$_{0.03}$As$_2$ under $P \approx 10$ MPa and their fittings by eqs. (13),(14). A clear difference between $T = 4$ K and $T = 121$ K in Figure 10(a) indicates different FWHM of the $d$ spread. Figure 10(b) compares $P(\phi_{\text{tot}})$ for the $(4,0,0)$ and $(0,4,0)$ reflections at $T = 102.4$ K. The corresponding FWHMs of the $d$ distributions are also shown as an inset. Their differences suggest that the $d$ spread along the pressure-applied orientation is much larger.

Figure 10(c) shows temperature dependence of $P(\phi_{\text{tot}})$ for an un-pressured BaFe$_{1.97}$Ni$_{0.03}$As$_2$ sample. Its evolution at high temperature ($T > 109$ K) indicates the broadening of the $d$ spread. Below 109 K, clear modulations are seen in $P(\phi_{\text{tot}})$. This is caused by the peak splitting of the orthorhombic $(4,0,0)$ and $(0,4,0)$ reflections in a twinned sample. For systems showing two or more coexisting $d$ spacings around some $Q$, their $d$ spacing distribution functions are superposition of multiple Gaussian distributions. In this case, the interference between different $d$ spacings will appear and can be used to identify the specific values and spread of the involved $d$ spacings.

For the peak splitting (two $d$ spacings) in BaFe$_{1.97}$Ni$_{0.03}$As$_2$, interference between scattered neutrons from $d_1$ and $d_2$ gives rise to the modulating polarization

$$P(\phi_{\text{tot}}) = A \sqrt{a^2 + (1-a)^2 + 2a(1-a)\cos(\phi_{\text{tot}} \Delta \varepsilon)},$$

where

$$A = P_0 \exp\left(-\frac{\phi_{\text{tot}}^2 \varepsilon_{FW}^2}{16 \ln 2}\right),$$

here we assume both $d$ spacings have the same $\varepsilon_{FW}$. $a$ and $(1-a)$ denote the populations of the $d_1$ and $d_2$.

$$\Delta \varepsilon = \frac{d_1 - d_2}{(d_1 + d_2)/2},$$

is the lattice distortion. The definition of $\Delta \varepsilon$ is similar with the orthorhombic lattice distortion $\delta = (a-b)/(a+b)$ in iron pnictides, with $\Delta \varepsilon = 2\delta^5$. The $P(\phi_{\text{tot}})$ at $T = 107.5$ K and 105.2 K in Figure 10(c) are well described by eq. (14). The fitted lattice distortions and $d$ spreads are shown in Figure 3 and 4 of the main text. The resolution in determining $\Delta \varepsilon$ here depends on the range of $\phi_{\text{tot}}$ and the $d$ spread of the sample since the dips of the polarization is critical for fitting $\Delta \varepsilon$. The resolution of $\Delta \varepsilon$ for two $d$ spacings is $7 \times 10^{-4}$ in the present work. Thus the possible distortions at temperatures slightly lower than $T_s = 114$ K [such as the 109.5 K data shown in Figure 10(c)] in BaFe$_{1.97}$Ni$_{0.03}$As$_2$ cannot be distinguished from the broadening of the $d$ spread.
Figure 11 are $P(\phi_{tot})$ for temperatures across the structural transition of the BaFe$_2$As$_2$ sample. $P(\phi_{tot})$ in Figure 11(a) is a beating pattern caused by interference between two $d$ spacings below $T_s$, similar with that shown in Figure 10(c). The corresponding $d$ spacing distributions are shown in Figure 11(e). The orthorhombic distortions can be determined as $\delta = (d_2 - d_1)/(d_2 + d_1)$. Upon warming the sample to $T = 137$ K, a temperature slightly lower than $T_s$, a more complicated pattern [Fig. 11(b)] indicates the coexistence of four $d$ spacings [Fig. 11(f)]. This is consistent with the coexisting orthorhombic antiferromagnetic ($\delta_1$) and orthorhombic paramagnetic ($\delta_2$) phases revealed by high resolution X-ray diffraction measurements. The four-$d$ spacing model of $P(\tau)$ can be derived analytically (not shown here) and fit the data very well. Figure 11(c) and (g) are results for $T \sim T_s$, where the $\delta_2$ is indistinguishable and only one broad $d$ spread can be fitted. Here, the orthorhombic antiferromagnetic phase ($\delta_1$) is about to disappear, suggesting this temperature is near $T_s$. For temperature higher than $T_s$ in Figure 11(d) and (h), only one $d$ spacing is observed, indicating the system enters into the paramagnetic tetragonal phase. In Figure 11(a,b), the magnitude of the lattice distortions determines the beating periods (overall line shape) and the relative populations of different $d$ spacings control whether the polarization can reach zero at dips. In the present study, the overall line shapes of all $P(\tau)$ are well fitted by specific multiple $(2 - 4) d$ spacing models [green curves in Figure 11(a)-(d)], indicating that the lattice distortions are well determined.

The orthorhombic lattice distortions for BaFe$_2$As$_2$ and SrFe$_{1.97}$Ni$_{0.03}$As$_2$ obtained from Larmor diffraction measurements of $P(\phi_{tot})$ are shown in Figure 12. These results are consistent with previous results measured by X-ray diffraction. The error bars in Figures 3 and 4 of the main text are fitting errors of the raw data at different temperatures according to formulas discussed above.

**D. $d$ spread anisotropy between $a$ and $b$**

Another interesting discovery is the doping dependent $d$ spread anisotropy under uniaxial pressure. The samples shown in Figure 13 exhibit similar temperature dependence of the $d$ spread between (4, 0, 0) and (0, 4, 0), suggesting that the difference of $d$ spread between $a$ and $b$ is trivial. However, we note that the FWHM of (0, 4, 0), along the uniaxial pressure direction, is much larger than $a$ in underdoped samples [Fig. 13(a)-13(c)]. This may be attributed to an inhomogeneous distribution of the pressure induced strain field. However, we find very small differences in $d$ spread between (4, 0, 0) and (0, 4, 0) in the overdoped BaFe$_{1.88}$Ni$_{0.12}$As$_2$ [Fig. 13(d)], suggesting the $d$ spread anisotropy between $a$ and $b$ is non-trivial and may be associated with antiferromagnetic/structural instability or even nematic susceptibility in overdoped samples.

**E. The lattice distortions and Young’s modulus**

The Young’s modulus $Y$ along the $b$-axis ($\sim C_{00}$) can be estimated by $Y = P/\delta$, where $\delta$ is pressure induced lattice distortion. At $\sim 250$K, the $Y$ for BaFe$_2$As$_2$, BaFe$_{1.97}$Ni$_{0.03}$As$_2$ and BaFe$_{1.88}$Ni$_{0.12}$As$_2$ estimated from our neutron Larmor diffraction experiments are $\sim 50$ GPa, $\sim 50$ GPa and $\sim 100$ GPa, respectively. Compared with the shear modulus $C_{00}$ obtained by ultrasound spectroscopy, the estimated $Y$ for $x = 0$ and $x = 0.03$ are $\sim 30\%$ larger. These differences are mainly caused by the errors in our estimation of the applied pressure $P$ through measuring compressed spring distances and estimated spring constant. However, they will not affect temperature dependence of the pressure-induced FWHM of $\Delta d/d$ and its comparison with other iron pnict-
tides, thus will not alter the conclusions of our experiments.

\[ F = F_0 + T_0 f[\varphi, \delta] + T_0 \tilde{f}[M, \varphi], \]

where

\[ f[\varphi, \delta] = \frac{a}{T_0} T - T_0 \varphi^2 + \frac{B}{4T_0} \varphi^4 + \frac{C_{66,0}}{2T_0} \delta^2 - \frac{\lambda}{T_0} \delta \varphi - \frac{P \delta}{T_0} \]

Here we chose to normalize the free energy by the Curie-Weiss temperature \( T_0 \) associated with the quadratic \( \varphi^2 \) term (if \( T_0 \) is negative, it is replaced by \( |T_0| \)). Treating the electronic nematic order parameter \( \varphi \) as a dimensionless variable, this has an advantage that all the coefficients in the free energy are dimensionless (here we choose, without loss of generality, \( a = B = 1 \)). The remaining Landau expansion parameters can be fixed from the experiment. Indeed, it is convenient to express the external uniaxial stress \( P \) in terms of the dimensionless stress variable \( \sigma = P/C_{66,0} \). Then, the last three terms in Eq. (18) can be written as follows:

\[ \frac{\lambda}{|T_0|} \left[ \left( \frac{C_{66,0}}{\lambda} \right) \left( \frac{\delta^2}{2} - \delta \sigma \right) - \delta \varphi \right] \]

Minimizing the free energy with respect to \( \delta \), we find

\[ \delta = \frac{\lambda}{C_{66,0}} \varphi + \sigma. \]

From the minimization with respect to \( \varphi \), it is easy to obtain

\[ \frac{d\varphi}{d\delta} = \frac{\lambda}{a(T - T_0) + 3B\delta^2} \]

and now the shear modulus \( C_{66} \equiv dP/d\delta = d^2F/d\delta^2 \) becomes

\[ C_{66} = C_{66,0} - \lambda \frac{d\varphi}{d\delta} = C_{66,0} - \frac{\lambda^2}{a(T - T_0) + 3B\delta^2}. \]

in other words the elastic modulus gets renormalized from its bare value \( C_{66,0} \) by virtue of the elastic-nematic coupling \( \lambda \). Equivalently, it follows from the above equation that the inverse nematic susceptibility \( \chi^{-1}_\varphi = d^2F/d\varphi^2 \mid_{\varphi \to 0} \) also gets renormalized from its bare value \( \chi^{\prime \prime}_\varphi = a(T - T_0) \):

\[ \chi^{-1}_\varphi = \chi^{\prime \prime}_\varphi - \frac{\lambda^2}{C_{66,0}} = a(T - T_s)^{CW}, \]

where \( T^{CW} = T_0 + \frac{\lambda^2}{C_{66,0}} \) is the renormalized Curie-Weiss temperature. One can now cast Eq. (22) above the transition temperature \( T_s = T_s^{CW} \) into the form

\[ \frac{d\delta}{dP} = \frac{1}{C_{66}} = \frac{1}{C_{66,0}} \frac{T - T_0}{T - T^{CW}}, \]

which is Eq. (3) in the main text. We now use this Eq. (24) to fit the data for the pressure-induced distortion \( \delta(P) - \delta(0) \approx P(d\delta/dP) \) [Fig. 1(c) in the main text], extracting the values of \( T_0 \) and \( T_s^{CW} \) which we quote in Table I for BaF\(_2\)As\(_2\) and SrFe\(_{1.97}\)Ni\(_{0.03}\)As\(_2\).

We now turn to the question of the strength of the elasto-nematic coupling constant \( \lambda \). The unknown dimensionless parameter \( r = C_{66,0}/\lambda \), can be fixed from the ratio \( \varphi/\delta \) in zero external stress (\( \sigma = 0 \)). Substituting the typical value of \( \delta \sim 3 \times 10^{-4} \) in SrFe\(_{1.97}\)Ni\(_{0.03}\)As\(_2\) and BaFe\(_{1.97}\)Ni\(_{0.03}\)As\(_2\) and choosing the value of the nematic order parameter \( \varphi = 1 \) deep inside the nematic phase for convenience, we find \( r \sim 300 \). As for the value of \( \lambda = \varphi/|T_0| \), it can also be fixed from the experiment since \( \lambda \) enters in Eq. (23) to renormalize the Curie-Weiss temperature. Therefore, one obtains \( \lambda = a(T_s^{CW} - T_0)/r \). Plugging in the values of \( T_s^{CW} \) and \( T_0 \) from our fittings of the lattice distortions (Table I), we obtain \( \lambda \approx 80 \) for SrFe\(_{1.97}\)Ni\(_{0.03}\)As\(_2\) and \( \lambda \approx 490 \) for BaFe\(_2\)As\(_2\), in other words the effective electron-lattice coupling is about \( \sim 6 \) times weaker in SrFe\(_{1.97}\)Ni\(_{0.03}\)As\(_2\) compared to the BaFe\(_2\)As\(_2\) compounds. For BaFe\(_{1.97}\)Ni\(_{0.03}\)As\(_2\), the quality of our data was insufficient to accurately determine the bare Curie-Weiss temperature \( T_0 \) (we were only able to determine \( T_s^{CW} = 88.5 \pm 1.0 \) K). However, from the estimated \( T_s^{CW} - T_0 \approx 50 \) K by the elastic measurements, we can deduce the approximate value of the coupling constant \( \lambda \approx 390 \), similar in magnitude to undoped BaFe\(_2\)As\(_2\).

<table>
<thead>
<tr>
<th>Sample</th>
<th>( T_s^{CW}(K) )</th>
<th>( T_0(K) )</th>
<th>( T_s^{CW} - T_0(K) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>BaFe(_2)As(_2)</td>
<td>134.9 ± 0.3</td>
<td>51.3 ± 8.7</td>
<td>83.5 ± 8.7</td>
</tr>
<tr>
<td>SrFe(<em>{1.97})Ni(</em>{0.03})As(_2)</td>
<td>170.9 ± 1</td>
<td>135.7 ± 6</td>
<td>35.2 ± 6.1</td>
</tr>
</tbody>
</table>

We now turn our attention to the magneto-nematic coupling. On symmetry grounds, nematic order parameter must couple to \( M^2 \) (since magnetization breaks time-reversal symmetry, \( \varphi \) does not). This can be shown explicitly by considering the magnetization \( M_{A,B} \) on the two sublattices composed of the next-nearest neighbor...
sites of the square lattice, in which case the nematic order parameter couples linearly to the product \((\mathbf{M}_A \cdot \mathbf{M}_B)\) [25,28,36,71]. Note that this conclusion holds independently of whether the microscopic origin of nematicity is purely magnetic [25,28,71] or orbital [31,33,36,72,73]. The magnetic phase transition itself may be intrinsically second-order, as in \(\text{BaFe}_{2-x} \text{T}_x \text{As}_2\) compounds, or first order, as in \(\text{SrFe}_{1.97} \text{Ni}_{0.03} \text{As}_2\), \(\text{Ba}_{1-x} \text{(K,Na)}_x \text{Fe}_2 \text{As}_2\), and \(\text{Ca}_{1-x} \text{La}_x \text{Fe}_2 \text{As}_2\). Below we consider both possibilities:

\[
\tilde{\mathcal{f}}_1[M, \varphi] = \frac{\mu}{2}(T - T_{N, 0})M^2 - \frac{\mu}{4}M^4 + \frac{\mu}{6}M^6 - \mu \varphi M^2
\]

\[
\tilde{\mathcal{f}}_2[M, \varphi] = \frac{\mu}{2}(T - T_{N, 0})M^2 + \frac{\mu}{4}M^4 - \mu \varphi M^2
\]

Since we are after the qualitative consequences of the magneto-nematic coupling, the precise values of the Landau coefficients are not essential (we take \(u = v = w = 1\) and \(\mu = 0.1\) for concreteness).

![FIG. 14: (Color online) Change in the lattice distortion as a function of temperature, calculated from the Landau theory assuming either 1st order (Eq. 25) or 2nd order (Eq. 26) magnetic phase transition coupled to the nematic order parameter \(\varphi\). The blue dashed curve is shifted to the left by \(\Delta T = 0.2T_0\) for clarity. These results should be compared to the neutron data in Fig. 1c in the main text.](image)

Having introduced the Landau formalism above, we now study the effect of the applied external stress \(P\) on the behavior of the lattice distortion. The calculated temperature dependence of \(\delta(P) - \delta(0)\) is shown in figure 14 for the realistic strain \(P = 20\) MPa and is shown to depend crucially on the nature of the magnetic phase transition. Indeed, the only difference between the two curves is the sign in front of the quartic \(M^4\) terms in Eqs. (25) and (26), while all the other Landau expansion parameters are kept the same (the two curves are offset horizontally for clarity). Note that for small \(P\), \(\delta(P) - \delta(0) \approx (d\delta/dP)P\) is proportional to the nematic susceptibility, which is expected to diverge at \(T_{CW}\) according to Eq. (24). Both curves in Fig. 14 exhibit an enhanced nematic susceptibility on approaching \(T_{CW}^{*}\), as expected. The main difference is the shape of the curve on approaching the transition, which has a distinct asymmetric “lambda” shape in the case of the second-order magnetic transition, and resembles closely the experimentally measured \(\delta(P) - \delta(0)\) for \(\text{BaFe}_{1.97} \text{Ni}_{0.03} \text{As}_2\) in Fig. 1c (see main text). By contrast, the Néel transition is first order in \(\text{SrFe}_{1.97} \text{Ni}_{0.03} \text{As}_2\), and the experimental behavior in Fig. 1(c) is close to the calculated sharp increase seen in our model (solid line in Fig. 14). Therefore, the Landau free energy results corroborate our conclusion that the nature of the magnetic transition is crucial to the observed temperature dependence of the lattice distortion.

We note in passing that for sufficiently strong coupling constant \(\mu\), the magnetic transition becomes weakly first-order even if the intrinsic free energy has positive \(M^4\) term in Eq. (26). This is likely the explanation for the observed change of the nature of the magnetic transition from weakly first order in \(\text{BaFe}_2 \text{As}_2\) to second order upon Co doping [5,7,8]. However for the values of the coupling constants in Fig. 14, this effect is imperceptible and the main difference between the two curves is due to the different intrinsic nature of the magnetic phase transition depending on the sign of the quartic term in Eqs. (25) and (26). We have verified that for the significantly larger values of the coupling constant \((\mu > 0.4\) in Eq. 26), it is indeed possible to obtain the shape similar to the dashed line in Fig. 14 because the magnetic transition becomes effectively first order. In either case, our conclusions remain intact.

G. Interpretation of the resistivity anisotropy

The resistivity anisotropy \(\Delta \rho = (\rho_a - \rho_b)/\rho_b\) has been widely used as a proxy for the electronic nematic order parameter in the iron pnictides [12,20]. However in some compounds, in particular in \(\text{SrFe}_{1.97} \text{Ni}_{0.03} \text{As}_2\), the resistivity anisotropy is vanishingly small immediately above \(T_N\) [see Fig. 1(b) in the main text], whereas it is much larger in \(\text{BaFe}_2 \text{As}_2\). This is puzzling because the lattice distortion is comparable in both cases [Fig. 1(c)] and, according to Eq. (20), one expects the lattice distortion \(\delta\) to be proportional to the nematic order parameter.

To shed more light on this apparent inconsistency, we have plotted in Figure 15 the temperature dependence of the nematic order parameter \(\varphi\) under the uniaxial stress \(P = 20\) MPa. The two curves correspond to the first- and second-order nature of the magnetic transition, respectively, and the Landau parameters were kept the same in both cases (except for the sign of the quartic term in Eq. 25 and 26). Above the transition temperature, \(T > T_s\), the values of \(\varphi\) are predictably small, but importantly, they are identical in the two cases. In fact, the main difference lies in the temperature dependence immediately below \(T_s\). From Fig. 15, it would appear that in this regime, the nematic order parameter should be smaller for the second-order phase transition, however this is diametrically opposite from the comparison between \(\text{BaFe}_{1.97} \text{Ni}_{0.03} \text{As}_2\) and \(\text{SrFe}_2 \text{As}_2\) in Fig. 1(b) (see main text), where the magnetic tran-
transition in BaFe$_{1.97}$Ni$_{0.03}$As$_2$ is second order, yet resistivity anisotropy is much larger. This qualitative observation can be made sharper by considering Eq. (20), where the coupling constant $\lambda$ is estimated from experiment to be a factor of $\sim$ 5 larger in BaFe$_{1.97}$Ni$_{0.03}$As$_2$ and BaFe$_2$As$_2$ compared to SrFe$_{1.97}$Ni$_{0.03}$As$_2$, whereas the elastic modulus $C_{66,0} \approx$ 50 GPa is similar in all three materials. Then, BaFe$_2$As$_2$ is expected to have at least a factor of 5 larger lattice distortion compared to SrFe$_{1.97}$Ni$_{0.03}$As$_2$, assuming that $\varphi$ is the same in both materials. If one now equates the resistivity anisotropy with the nematic order parameter $\varphi$, as has commonly been done in the literature, then one is forced to conclude that $\varphi$ must be about 4 times larger in BaFe$_2$As$_2$ due to the larger resistivity anisotropy [see Fig. 1(b)]. Taken together, one would expect the lattice distortion $\delta$ to be a factor of $\sim$ 20 larger in BaFe$_2$As$_2$ and in BaFe$_{1.97}$Ni$_{0.03}$As$_2$ compared to SrFe$_{1.97}$Ni$_{0.03}$As$_2$ (factor of 4 due to larger resistivity anisotropy, times factor of 5 due to larger $\lambda$). And yet this clearly contradicts the experimental evidence in Fig. 1(c), according to which the lattice distortion is almost the same in all three materials.

One possible way out of this dilemma is that the Landau theory may not be applicable to describe the nematicity in the pnictides. However, given the excellent semi-quantitative agreement that Landau theory provides for the lattice distortion (Fig. 14 above) and its well documented success describing the elastic shear modulus measurements, such a conclusion is perhaps not well justified. Rather, a much more plausible conclusion is that resistivity anisotropy is a poor substitute for the nematic order parameter. While it is plausible that the two quantities are proportional to each other, as follows from the nematic susceptibility measurements, the coefficient of proportionality need not be constant and can have a strong temperature dependence (and likely material dependence), as suggested recently by Tanatar et al. in the recent study on FeSe. This material displays a non-monotonic temperature dependence of the resistivity anisotropy with a peak below $T_s$, qualitatively similar to FeSe. Further theoretical and experimental studies are necessary to elucidate the precise relationship of the resistivity anisotropy and the nematic order parameter in the iron pnictides and chalcogenides. Direct microscopic measurements of the nematic order parameter, for instance using the angle-resolved photoemission spectroscopy (ARPES) to probe the orbital splitting, combined with the uniaxial pressure measurements, would be desirable.

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FIG. 15: (Color online) Calculated temperature dependence of the nematic order parameter $\varphi$ coupled to either first or second order magnetic phase transition. Note that in both cases, the bare $\varphi^4$ term is positive, however the nematic transition is rendered first order (solid curve) when coupled to the first order magnetic order parameter in Eq. (25).

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