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Ferroelectricity in corundum derivatives

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The search for new ferroelectric (FE) materials holds promise for broadening our understanding of FE mechanisms and extending the range of application of FE materials. Here we investigate a class of ABO_3 and $A_2BB'O_6$ materials that can be derived from the X_2O_3 corundum structure by mixing two or three ordered cations on the X site. Most such corundum derivatives have a polar structure, but it is unclear whether the polarization is reversible, which is a requirement for a FE material. In this paper, we propose a method to study the FE reversal path of materials in the corundum derivative family. We first categorize the corundum derivatives into four classes and show that only two of these allow for the possibility of FE reversal. We then calculate the energy profile and energy barrier of the FE reversal path using first-principles density functional methods with a structural constraint. Furthermore, we identify several empirical measures that can provide a rule of thumb for estimating the energy barriers. Finally, the conditions under which the magnetic ordering is compatible with ferroelectricity are determined. These results lead us to predict several potentially new FE materials.

I. INTRODUCTION

Ferroelectricity requires a material to have a spontaneous electric polarization that can be reversed by an external electric field.¹ The search for new ferroelectric (FE) materials holds promise for broadening our understanding of FE mechanisms and extending the range of application of FE materials. A switchable spontaneous polarization implies a hysteresis effect that can be used in memory devices.² FE materials also exhibit high and tunable electric permittivity, which can be used in capacitors to increase the capacitance and reduce the size of devices. In addition, FE materials are piezoelectric and pyroelectric, according to symmetry considerations. These combined properties make FE materials ideal for electric, mechanical and thermal sensors. Recently, research on multiferroics, in which FE and ferromagnetic orders coexist in the same material, has further extended the range of application of FE materials.³⁻⁹

The most intensively studied family of FE oxides is that of the perovskite oxides such as $BaTiO_3$.^{10,11} Perovskite oxides have the chemical formula ABO_3 with the A cation much larger than the B cation. The FE distortion is usually driven by B -site off-centering and typically requires an empty d shell on the B cation, which is not compatible with magnetism. Recently, rocksalt-ordered $A_2BB'O_6$ double perovskites (and more complex $AA'BB'O_6$ materials) have also attracted great interest.^{12,13}

The corundum derivatives ABO_3 and $A_2BB'O_6$ make up a family of oxides that can be derived from the corundum structure with cation ordering. Most corundum derivatives are polar and thus can potentially be new FE oxides.¹⁷⁻³² $LiNbO_3$ (LNO) is a well-known example of a FE corundum derivative.¹⁴⁻¹⁶ Despite the similar chemical formula, corundum derivatives are different from perovskites in many aspects. The high-symmetry parent structure is rhombohedral for corundum derivatives but cubic for perovskites. The polar-

ization reversal mechanisms are also distinct. In corundum derivatives, the polarization reversal is driven by the small A or B cations migrating between oxygen octahedra,^{15,16} so that d^0 configuration is not required. This is in contrast to the off-centering displacement of d^0 B cations in the oxygen octahedra in most perovskites. The huge number of potential combinations of A , B and B' cations in the corundum-derivative family opens the possibility to achieve not only ferroelectricity but also multiferroicity.^{18,19}

In this paper, we use first-principles density functional methods to systematically study the polar structure and the coherent FE reversal paths for a variety of corundum derivatives. First, the structures of corundum derivatives are introduced in Sec. II A. Then the structural criteria for corundum derivatives to be FE are discussed in Sec. II B. In Sec. II C, we propose a systematic method to analyze the coherent FE barrier and energy profile. Lastly, the new method is applied to several corundum derivatives, and empirical measures that can provide a rule of thumb for estimating the reversal barrier are summarized in Sec. III.

II. PRELIMINARY

A. Structure

The corundum derivatives ABO_3 and $A_2BB'O_6$ can be derived from the corundum structure X_2O_3 with cation ordering as shown in Fig. 1. In the 10-atom rhombohedral unit cell, the cations are spaced along the three-fold rotation axis and each one is surrounded by a distorted oxygen octahedron. Two thirds of the oxygen octahedra are filled with cations, while one third of them are cation-vacant.

Based on the combinations and arrangements of cations, the corundum derivatives can be classified into four types, which we denote as follows. An oxygen oc-

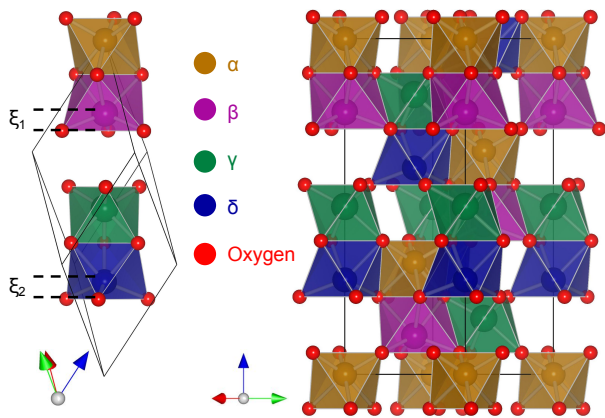


FIG. 1. Structure of corundum derivatives. The unit cell in the rhombohedral setting is shown at the left; an enlarged hexagonal-setting view is shown at right. The cations α , β , γ , and δ are all identical in the X_2O_3 corundum structure. For the LNO-type ABO_3 , $\beta = \delta = A$, $\alpha = \gamma = B$; for the ilmenite ABO_3 , $\beta = \gamma = A$, $\alpha = \delta = B$; for the ordered-LNO $A_2BB'O_6$, $\beta = \delta = A$, $\gamma = B$, $\alpha = B'$; for the ordered-ilmenite $A_2BB'O_6$, $\beta = \gamma = A$, $\delta = B$, $\alpha = B'$. At left, ξ_1 (or ξ_2) is the distance between β (or δ) and the oxygen plane that it penetrates during the polarization reversal.

tahedron with an A or B cation inside is written as “ A ” or “ B ”, and if an oxygen octahedron is cation-vacant, the octahedron is denoted by “ $-$ ”. This notation is then used to represent the column of six face-sharing oxygen octahedra in the unit cell for each of the four different types of corundum derivatives. Thus, the LNO-type ABO_3 is $AB-AB-$, the ilmenite ABO_3 is $AB-BA-$, the ordered-LNO $A_2BB'O_6$ is $AB-AB'-$, and the ordered-ilmenite $A_2BB'O_6$ is $AB-B'A-$. Other combinations, such as $AA-BB-$, are connected to the four existing types as explained in Sec. II B.

B. Coherent FE polarization reversal

Experimentally, the FE polarization reversal process is a complicated one that typically proceeds by nucleation and motion of domain walls, involving both intrinsic atomic motion and extrinsic pinning by defects. In this paper we have chosen to focus only on coherent FE domain reversal, in which every unit cell undergoes the polarization reversal simultaneously. This coherent reversal process is clearly highly oversimplified, but previous studies of perovskite oxides have shown that the coherent barrier provides a figure of merit that is often a useful indicator of the real barrier to polarization reversal. For example, the well-known FE perovskite $PbTiO_3$ has a coherent barrier around 0.2 eV per five-atom cell,¹⁰ so perovskite oxides with barriers lower than this may be considered likely to be FE.

The atomic origin of ferroelectricity in LNO is well-understood.^{15,16} In LNO, the polarization reversal is

TABLE I. Corundum-derived structures before and after polarization reversal.

	Before	After
LNO-type	$AB-AB-$	$-BA-BA$
Ilmenite	$AB-BA-$	$-BB-AA$
Ordered-LNO	$AB-AB'-$	$-BA-B'A$
Ordered ilmenite	$AB-B'A-$	$-BB'-AA$

driven by an infrared-active (IR-active) mode that is associated with the motion of Li cations along the rhombohedral axis. In the reversal process, each Li cation penetrates through an oxygen plane and migrates into an adjacent unoccupied oxygen octahedron. In our notation, the polarization reversal process interchanges Li with $-$, so that the polar structure changes from $LiNb-LiNb-$ to its inversion image $-NbLi-NbLi$.

For all types of polar corundum derivatives, we assume that the polarization reversal mechanism is similar to that of LNO, i.e., that the reversal process interchanges A or B with $-$. The structures before and after this process are listed in Table I. Under such an operation, the LNO-type structure is transformed into its own inversion-reversed image, which is a typical FE behavior. The same is true for the ordered-LNO structure. By contrast, the ilmenite-type $AB-BA-$ is transformed into $BB-AA-$, and the ordered-ilmenite $AB-B'A-$ into $BB'-AA-$. These structures are not inversion-equivalent to the starting structures. Moreover, they exhibit face-sharing A -containing octahedra, making them relatively unfavorable energetically. Additionally, both the ilmenite structure and its switched partner are centrosymmetric. For these reasons, we exclude the ilmenite and ordered-ilmenite structures from further consideration as FE candidates.

C. Energy profile calculations

For the LNO-type and the ordered-LNO FE candidates, we firstly analyze the symmetry of the reversal path. The ground state symmetry is $R3c$ for the LNO-type materials, and $R3$ for the ordered-LNO ones, but the symmetry of the reversal path is not straightforward. In this paper, we assume that the three-fold rotation is always preserved, so that the symmetry of the path can only be $R3c$ or $R3$ for the LNO-type case, and $R3$ for the ordered-LNO case. If the structure acquires an inversion center at the midpoint of the path when the polarization is zero ($R\bar{3}c$ or $R\bar{3}$ for the two cases respectively), the energy profile would be symmetric. If the inversion symmetry at the midpoint is broken, as for example by magnetic ordering, the energy profile would be asymmetric.

Based on the symmetry of the reversal path, we adopt different methods to calculate the energy profile of the

FE reversal. In the case when the inversion symmetry is present at the midpoint structure, the polarization reversal can be analyzed in terms of an unstable IR-active phonon mode at the high-symmetry midpoint. In general, even if the midpoint is not in a high-symmetry reference structure, the motion of the small A cations is responsible for the polarization reversal. As illustrated in Fig. 1, we define ξ_1 (ξ_2) to be the distance between the first (second) A cation and the oxygen plane that it penetrates as this A cation moves along its path. Then $\xi_1 + \xi_2$ is adopted as a “reaction coordinate” to describe the reversal. Finally, we use either the unstable IR-active mode at the midpoint (for the high-symmetry case) or $\xi_1 + \xi_2$ (otherwise) as a structural constraint, and relax all other internal structural degrees of freedom while stepping through a sequence of values of this constraint. This gives us the energy profile along the path, from which the energy barrier is obtained by inspection.

D. First-principles methods

Our calculations are performed with plane-wave density functional theory (DFT) implemented in VASP.³³ The exchange-correlation functional that we use is PBEsol, a revised Perdew-Burke-Ernzerhof generalized-gradient approximation that improves equilibrium properties of densely-packed solids.³⁴ The ionic core environment is simulated by projector augmented-wave (PAW) pseudopotentials.³⁵ For transition metal elements Mn and Fe, we use a Hubbard $U = 4.2$ eV on the $3d$ orbitals.^{28,36} For the Os $5d$ orbital, we use a Hubbard $U = 1.4$ eV.³¹ The magnetic moments are collinear and spin-orbit coupling is neglected. The cutoff energy for all calculations is 550 eV. The energy error threshold varied slightly in different calculations, but an accuracy between 1.0×10^{-5} and 1.0×10^{-7} eV is achieved in all calculations. The forces are reduced below 0.001 eV/Angstrom for calculations of structural relaxation. A $6 \times 6 \times 6$ Monkhorst-Pack k -mesh is used in the calculations. Linear-response methods are used to calculate the Γ -point force-constant matrices. The spontaneous polarization is calculated using the Berry phase formalism.³⁷

III. RESULTS AND DISCUSSION

In this paper, we apply the method of calculating the energy profile described in Sec. II C to fully analyze the coherent FE reversal path of the LNO-type corundum derivatives LiNbO_3 ,¹⁴ LiTaO_3 ,¹⁴ ZnSnO_3 ,²⁰ FeTiO_3 ,^{18,19} and MnTiO_3 ,¹⁸ and the ordered-LNO corundum derivatives $\text{Li}_2\text{ZrTeO}_6$,²⁵ $\text{Li}_2\text{HfTeO}_6$,²⁵ Mn_2FeWO_6 ,³⁰ Mn_3WO_6 ,³² and $\text{Zn}_2\text{FeOsO}_6$.³¹

TABLE II. Oxidation states of the LNO-type ABO_3 and the ordered-LNO $A_2BB'O_6$ corundum derivatives. The oxidation state of O ion is -2 in all materials.

LNO-type	A	B	Ordered LNO	A	B	B'
LiNbO_3	+1	+5	$\text{Li}_2\text{ZrTeO}_6$	+1	+4	+6
LiTaO_3	+1	+5	$\text{Li}_2\text{HfTeO}_6$	+1	+4	+6
ZnSnO_3	+2	+4	Mn_2FeWO_6	+2	+2	+6
FeTiO_3	+2	+4	Mn_3WO_6	+2	+2	+6
MnTiO_3	+2	+4	$\text{Zn}_2\text{FeOsO}_6$	+2	+3	+5

A. Ground state structure and magnetic order

The properties of FE materials are sensitive to atomic displacements and strain, so it is essential to start our calculation with accurate structural parameters. The lattice constants and Wyckoff positions obtained from our calculations are summarized in the Supplement, with experimental results provided for reference. Our structural parameters are very close to the experimental results. The oxidation states, obtained by rounding the integrated charge around each cation, are also displayed in Table II and are in good agreement with experimental observations.

The on-site magnetic moments are investigated for FeTiO_3 , MnTiO_3 , Mn_2FeWO_6 , Mn_3WO_6 and $\text{Zn}_2\text{FeOsO}_6$ by integrating the spin density inside the PAW sphere. Our DFT+ U calculation predict that the magnetic moment is about $3.7 \mu_B$ on each Fe^{2+} , $4.6 \mu_B$ on each Mn^{2+} , and $4.2 \mu_B$ on Fe^{3+} . These results are in agreement with the d^6 state of Fe^{2+} and the d^5 configuration of Fe^{3+} and Mn^{2+} . The magnetic moment on Os^{5+} is $2.1 \mu_B$ from our calculation, which is consistent with the high-spin d^3 state after taking into account the screening of the Os moment arising from the hybridization between Os $5d$ and O $2p$ orbitals.

The energy of different magnetic orderings is also studied. In our calculation, we only consider magnetic structures that preserve the periodicity of the rhombohedral unit cell. Our results suggest that the ground-state magnetic ordering is anti-ferromagnetic (AFM) for FeTiO_3 and MnTiO_3 and ferrimagnetic (FiM) for $\text{Zn}_2\text{FeOsO}_6$. To investigate the magnetic structures of Mn_2FeWO_6 and Mn_3WO_6 , four different types of unit cell are considered in the calculation. We adopt a notation like “ udu ” to describe the possible spin structure on the three cations excepting W. Here “ u ” is spin-up, “ d ” is spin-down, and the spins are given on cations A_1 , A_2 and B in that order, where A_1 and A_2 are face-sharing with B' and B cations respectively. (Note that A_1 , A_2 and B correspond to cations β , δ and γ respectively in Fig. 1.) The four possible states (not counting those that are trivially related by a global spin reversal) are uuu , uud , udu , and udd . The energy of each fully-relaxed magnetic structure is listed in the Supplement. Of those, the most stable state for both Mn_2FeWO_6 and Mn_3WO_6 is udu . However, for

TABLE III. The energy and the unstable phonon modes at the midpoint structure of LiNbO_3 , LiTaO_3 , ZnSnO_3 , FeTiO_3 and MnTiO_3 with symmetry $\text{R}\bar{3}\text{c}$ and $\text{R}\bar{3}$. The energy of the ground-state structure is set to be zero as reference and the unit is meV per unit cell. The imaginary frequency of the unstable phonon is given in units of cm^{-1} .

	Energy		Unstable modes		
	$\text{R}\bar{3}\text{c}$	$\text{R}\bar{3}$	$\text{R}\bar{3}\text{c}$	$\text{R}\bar{3}$	$\text{R}\bar{3}$
			A_{2u}	A_{2g}	A_u
LiNbO_3	303	259	$216i$	$123i$	$158i$
LiTaO_3	163	129	$178i$	$116i$	$1i$
ZnSnO_3	255	241	$93i$	$30i$	$47i$
FeTiO_3	1014	735	$195i$	$75i$	—
MnTiO_3	550	468	$177i$	$73i$	$114i$

Mn_3WO_6 , the energy difference between the uud and udu states is tiny, so we considered the polarization reversal for both magnetic states.

B. Symmetry of the reversal path

For the LNO-type materials, the simplest possible reversal path would be one in which the two A cations move synchronously, so that $\xi_1 = \xi_2$ everywhere along the path. In this case the symmetry along the path is $\text{R}\bar{3}\text{c}$, except at the midpoint where there is an inversion center and the symmetry becomes $\text{R}\bar{3}\text{c}$. Another possibility is that the cations move sequentially, one after the other, so that $\xi_1 \neq \xi_2$ for at least part of the path. In this case the symmetry is $\text{R}\bar{3}$ except at the $\text{R}\bar{3}$ midpoint. In order to find out which scenario occurs, we calculate the energy of the midpoint structures with symmetry $\text{R}\bar{3}\text{c}$ and $\text{R}\bar{3}$ respectively; the results are shown in Table III. For all LNO-type materials that we have studied, the $\text{R}\bar{3}$ midpoint structure is energetically favored, which implies that the reversal occurs via the lower-symmetry $\text{R}\bar{3} \rightarrow \text{R}\bar{3} \rightarrow \text{R}\bar{3}\text{c}$ scenario, at least in the central portion of the path. This striking result demonstrates that the midpoint of the FE reversal path in the LNO-type FE materials is *not* identified with the high-temperature paraelectric structure,^{15,16} but instead has lower symmetry.

The energy differences between $\text{R}\bar{3}\text{c}$ and $\text{R}\bar{3}$ structures can be explained by comparing their unstable phonons, for which the frequencies are listed in Table III. At $\text{R}\bar{3}\text{c}$ symmetry, all the LNO-type candidates have *two* unstable modes along the rhombohedral axis direction, namely one A_{2u} and one A_{2g} mode. The A_{2u} mode is IR-active, and it describes the synchronous movement of A cations. The non-polar A_{2g} mode, however, is related to the out-of-phase movement of the two A cations. Comparing the unstable modes in the $\text{R}\bar{3}\text{c}$ and $\text{R}\bar{3}$ structures, we find that the unstable non-polar mode is absent in the $\text{R}\bar{3}$ structure. Therefore, the unstable A_{2g} mode is responsible for the energy reduction in going from the $\text{R}\bar{3}\text{c}$ to

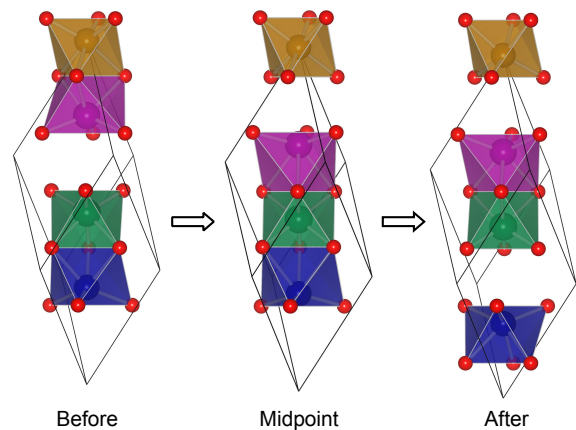


FIG. 2. Structural evolution along the polarization reversal path of the LNO-type and the ordered-LNO corundum derivatives. “Before” and “After” are the initial and final structures on the reversal path with symmetry $\text{R}\bar{3}\text{c}$ for the LNO-type and $\text{R}\bar{3}$ for the ordered-LNO corundum derivatives; “Midpoint” denotes the structure halfway between these and exhibits $\text{R}\bar{3}$ structural symmetry in both cases.

the $\text{R}\bar{3}$ structure. In addition, we find an unstable E_u mode in LiNbO_3 and FeTiO_3 for both the $\text{R}\bar{3}\text{c}$ and $\text{R}\bar{3}$ structures. As the three-fold rotational symmetry is preserved in our calculation, the E_u modes are not allowed to relax and further lower the energy.

For the ordered-LNO materials, since the two A cations are not related by any symmetry even in the ground state, the two A cations move sequentially so that $\xi_1 \neq \xi_2$. Therefore, the reversal path adopts the $\text{R}\bar{3}$ symmetry, except at the $\text{R}\bar{3}$ midpoint. The only exception in our calculations is the case of the udu magnetic state in Mn_2FeWO_6 and Mn_3WO_6 , where the magnetic moments break inversion symmetry so that the midpoint structure slightly deviates from $\text{R}\bar{3}$ to $\text{R}\bar{3}\text{c}$. Leaving aside this small distortion, the midpoint structures of the LNO-type and the ordered-LNO paths have the same structural symmetry, even though the ordered-LNO compounds have lower symmetry in their ground state.

The sequence of movements of the A cations along the FE reversal path is illustrated in Fig 2, and described quantitatively using our computed results for LiNbO_3 and Mn_2FeWO_6 as paradigmatic examples in Fig. 3. The “Before” and “After” structures in Fig. 2 correspond to the points at the top right and bottom left corners of Fig. 3 respectively. For the LNO-type case, the ideal $\text{R}\bar{3}\text{c}$ “Midpoint” structure would correspond to the origin on the plot, but the reversal path does not pass through this point because of an unstable A_{2g} mode along the $\xi_1 = -\xi_2$ direction. The “bubble” in the center confirms the significant effect of the unstable A_{2g} mode. Our “Midpoint” in Fig. 2 is thus displaced from the origin along the line $\xi_1 = -\xi_2$. There is a spontaneous breaking of symmetry at the point where the structure departs from the $\xi_1 = \xi_2$ diagonal; at this point the system “randomly” makes a choice between two equivalent paths, marked by filled

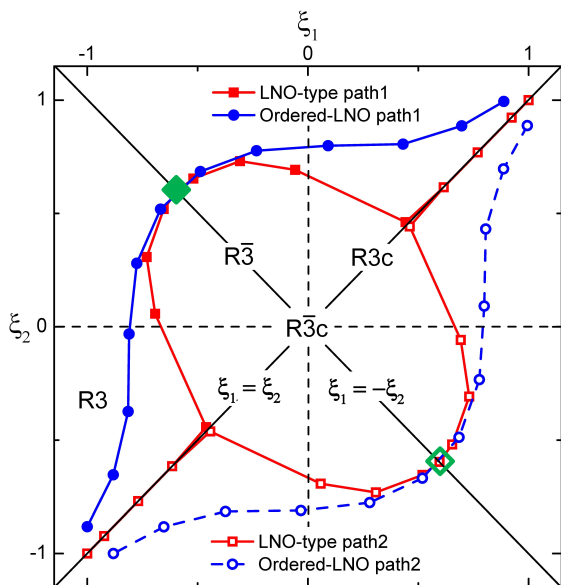


FIG. 3. Movements of A cations in LNO-type (red, here LiNbO_3) and ordered-LNO (blue, here Mn_2FeWO_6) corundum derivatives along the polarization reversal path. ξ_1 and ξ_2 are the distances from A atoms to the oxygen planes that are penetrated during the polarization reversal, here rescaled to a range between -1 and 1 . The symmetry at an arbitrary (ξ_1, ξ_2) point is $R3$; on the $\xi_1 = \xi_2$ and $\xi_1 = -\xi_2$ diagonals it is raised to $R3c$ and $R\bar{3}$ respectively; and at the origin ($\xi_1 = \xi_2 = 0$) it reaches $R\bar{3}c$. Green diamonds denote the midpoint structure in the parameter space. In the LNO-type case “path1” and “path2” (filled and open red square symbols) are equivalent and equally probable, while the ordered-LNO system deterministically follows “path1” (full blue line), which becomes “path2” (dashed blue) under a relabeling $\xi_1 \leftrightarrow \xi_2$.

and open red symbols in Fig. 3.

For the ordered-LNO materials the two A cations are inequivalent, and one of them is already closer to the oxygen plane in the ground state. Let this be the one labeled by ξ_1 . It is energetically favorable for this particular A cation to migrate first in the reversal path, which causes either the B or B' cation to be sandwiched between two A cations in the “Midpoint” structure as illustrated in Fig. 2. The system thus deterministically follows the path indicated by the full blue line in Fig. 3, with the configuration always staying on one side of the $\xi_1 = \xi_2$ diagonal. If we would reverse the convention on the definition of ξ_1 and ξ_2 , the system would be described by the dashed blue path in Fig. 3.

C. Polarization reversal barrier

Using the methods described in Secs. IIC and IID, we compute the relaxed structures and energies for a sequence of constrained values of our “reaction coordinate” $\xi = \xi_1 + \xi_2$ for each material of interest. A selection of results for the energy along the path are presented in Fig. 4,

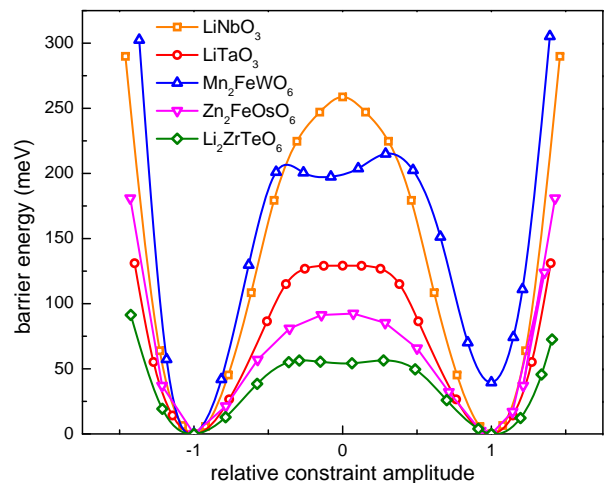


FIG. 4. The polarization reversal energy profile for LiNbO_3 , LiTaO_3 , Mn_2FeWO_6 , $\text{Zn}_2\text{FeOsO}_6$, and $\text{Li}_2\text{ZrTeO}_6$.

and quantitative results for the energy barrier E_{barrier} and the spontaneous polarization P_S in the ground-state structure are reported in Table IV. For Mn_3WO_6 and Mn_2FeWO_6 with udu magnetic ordering, the FE reversal changes the magnetic state to duu , so that the energy profile is no longer symmetric and the two minima become inequivalent. For these two compounds, the value of the energy barrier in Table IV is that of the highest barrier along the transformation path.

We find that the cations that are sandwiched in the midpoint structures of ordered-LNO candidates are Zr for $\text{Li}_2\text{ZrTeO}_6$, Hf for $\text{Li}_2\text{HfTeO}_6$, W for Mn_2FeWO_6 and Mn_3WO_6 , and Os for $\text{Zn}_2\text{FeOsO}_6$. These results are consistent with the analysis of ξ_1 and ξ_2 in the ground state, as mentioned in Sec. III B. We find that the energy difference between the B and B' sandwiched midpoint structures can be attributed mainly to the Madelung energy, as shown in the Supplement. Among the computed energy barriers, those for ZnSnO_3 , $\text{Li}_2\text{ZrTeO}_6$, $\text{Li}_2\text{HfTeO}_6$, Mn_2FeWO_6 , Mn_3WO_6 , and $\text{Zn}_2\text{FeOsO}_6$ are lower than or comparable to those of the established FE materials LiNbO_3 and LiTaO_3 .

We have analyzed our calculations in an attempt to

TABLE IV. Coherent polarization reversal barrier E_{barrier} (meV) per unit cell and spontaneous polarization P_S ($\mu\text{C}/\text{cm}^2$) for FE candidates.

LNO-type	E_{barrier}	P_S	Ordered-LNO	E_{barrier}	P_S
LiNbO_3	259	82	$\text{Li}_2\text{ZrTeO}_6$	57	33
LiTaO_3	129	57	$\text{Li}_2\text{HfTeO}_6$	61	32
ZnSnO_3	241	57	Mn_2FeWO_6	215	63
FeTiO_3	763	105	udu Mn_3WO_6	240	69
MnTiO_3	468	94	udu Mn_3WO_6	272	70
			$\text{Zn}_2\text{FeOsO}_6$	92	52

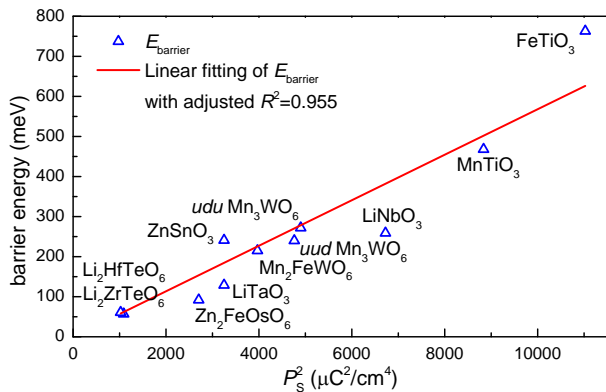


FIG. 5. Empirical proportionality between the coherent FE energy barrier and P_S^2 . The red curve is the fitting polynomial $E_{\text{barrier}} = (\mu/2)P_S^2$, with $\mu/2 = 0.057 \text{ meVcm}^4/\mu\text{C}^2$.

extract empirical rules of thumb that may help point in the direction of more new materials with low reversal barriers. Firstly, we have considered how the energy barriers are correlated with the spontaneous polarizations. In a FE material the energy E is often approximated as a double well of the form $E(P) = E_0 - \mu P^2 + \nu P^4$ with positive μ and ν . Minimizing $E(P)$ within this model gives the spontaneous polarization as $P_S^2 = \mu/2\nu$ and the energy barrier $E_{\text{barrier}} = E(0) - E(P_S) = \mu^2/4\nu$, which can also be written as $E_{\text{barrier}} = (\mu/2)P_S^2$. Thus, as long as μ can be taken as approximately constant, E_{barrier} is proportional to P_S^2 . Interestingly, we find that our computed coherent barrier energies E_{barrier} roughly follow this trend with $\mu/2 = 0.057 \text{ meVcm}^4/\mu\text{C}^2$ as shown in Fig. 5. Therefore we suggest that FE corundum derivatives are more likely to be discovered in materials having a relatively low spontaneous polarization.

Furthermore, we have investigated the correlation between the spontaneous polarizations and the geometric properties of the crystals. Our results suggest that for each FE candidate, the polarization P along the reversal path is almost linearly related to the reaction coordinate ξ . Expecting $P(\xi)$ to be an odd function, we add a small cubic part and fit it as $P(\xi) = m\xi + n\xi^3$. The parameters m and n are different in each material, and they are determined by several factors that are not included in the reaction coordinate ξ , such as the displacements of the B cations and the valence states of the A cations. Despite these differences between materials, we find that the spontaneous polarizations P_S of corundum derivatives are correlated with the reaction coordinate ξ_S in the spontaneously polarized ground state, as shown in Fig. 6. This time a roughly linear fit will clearly not work. Again we try fitting $P_S(\xi_S)$ to an odd third-order polynomial, and find that $P_S = m\xi_S + n\xi_S^3$ gives a reasonable fit with $m = 13.3 \times 10^8 \mu\text{C}/\text{cm}^3$ and $n = 19.0 \times 10^{24} \mu\text{C}/\text{cm}^5$ as shown in the figure. As the distance between A cations and oxygen planes can be experimentally determined, this empirical rule can provide a rough estimation of the spontaneous polarization.

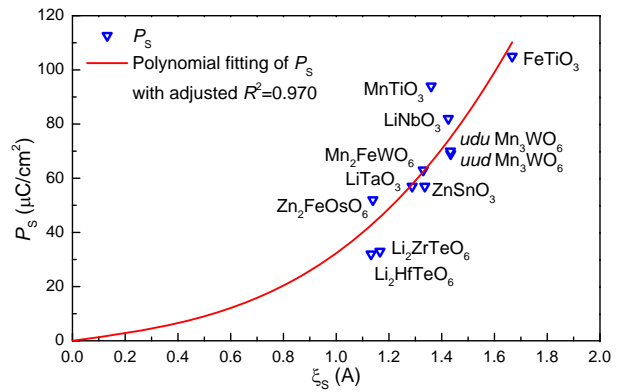


FIG. 6. Empirical correlation between the spontaneous polarization and the reaction coordinate ξ in the ground state. The red curve is the fitting polynomial $P_S = m\xi_S + n\xi_S^3$ with $m = 13.3 \times 10^8 \mu\text{C}/\text{cm}^3$ and $n = 19.0 \times 10^{24} \mu\text{C}/\text{cm}^5$.

D. Insulating vs. conducting

Our density-of-states calculations (not shown) indicate that FeTiO_3 and Mn_2FeWO_6 become conducting for cation configurations close to the central portion of the reversal path. A detailed analysis of the occupied d orbitals along the path reveals the reason for this metal-insulator transition. In the local octahedral environment of the ground state, the d orbitals are split into triply degenerated t_{2g} and doubly degenerated e_g orbitals. Under the threefold rotational symmetry, the t_{2g} orbitals are further split into a_{1g} and doubly degenerate e'_g irreps. The a_{1g} state has orbital character d_{z^2} with charge lobes directed along the rhombohedral axis, and since these lie closer to the neighboring cations, the energy of the a_{1g} state is lowered. Therefore, the ground-state arrangement of d orbitals in order of increasing energy is a_{1g} followed by e'_g and then e_g . In FeTiO_3 and Mn_2FeWO_6 , Fe is in the 2+ valence state and has a d^6 configuration. In the ground state, five electrons fully occupy one spin channel and the remaining one occupies the a_{1g} orbital in the minority spin channel. However, during the polarization reversal process, the Fe^{2+} ion temporarily moves away from its neighboring cations, and as a result, the a_{1g} orbital is no longer energetically favored. Instead, the minority electron occupies the doubly degenerate e'_g orbitals, leading to a metallic state. Since a metallic state along the polarization reversal path could short out the applied bias, it may be that the switching of polarization is not possible in such cases. We propose that d^3 , d^5 , and d^8 orbital configurations should be much more likely to avoid this conducting problem, and are therefore more suitable targets in the search for ferroelectrically switchable magnetic corundum derivatives.

IV. SUMMARY

In this paper, we have proposed a method to study the coherent FE reversal path of the corundum derivative family. By analyzing the structures, we have shown that only the LNO-type and the ordered-LNO corundum derivatives can be FE in the usual sense. We have calculated the energy profiles of the reversal paths using first-principles density-functional methods. Our calculations reveal that the symmetry of the FE barrier structure is lower than that of the paraelectric phase. According to our calculations, ZnSnO_3 , $\text{Li}_2\text{ZrTeO}_6$, $\text{Li}_2\text{HfTeO}_6$, Mn_3WO_6 , and $\text{Zn}_2\text{FeOsO}_6$ are predicted to be possible new FE materials. We have found empirically that the

energy barrier is roughly proportional to the the square of the spontaneous polarization, and that the spontaneous polarization is strongly correlated with the reaction coordinate ξ in the ground state. Finally, we have also argued that magnetic corundum derivatives are unlikely to be suitable for FE switching unless the magnetic ion is d^3 , d^5 or d^8 , since metallic configurations otherwise tend to appear along the FE reversal path.

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