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Structural investigation of the bilayer iridate $Sr_3Ir_2O_7$

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A complete structural solution of the bilayer iridate compound $Sr_3Ir_2O_7$ presently remains outstanding. Previously reported structures for this compound vary and all fail to explain weak structural violations observed in neutron scattering measurements as well as the presence of a net ferromagnetic moment in the basal plane. In this paper, we present single crystal neutron diffraction and rotational anisotropy second harmonic generation measurements unveiling a lower, monoclinic symmetry inherent to $Sr_3Ir_2O_7$. Combined with density functional theory, our measurements identify the correct structural space group as No. 15 (C2/c) and provide clarity regarding the local symmetry of Ir^{4+} cations within this spin-orbit Mott material.

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I. INTRODUCTION

The spin-orbit Mott (SOM) state as realized in the Ruddlesden-Popper (RP) strontium iridates $(Sr_{n+1}Ir_nO_{3n+1})$ remains of considerable interest due to the unique physics arising from the confluence of comparable strong spin-orbit coupling and electron-electron interactions in the presence of a strong cubic crystal field.¹⁻³ Subtleties in the lattice structures of these systems are of critical importance in determining both the spin-orbital content of the ground state wave function,³ the resulting magnetic ground state,⁴ and details within the electronic band structure.⁵ In particular, for the n = 2 member of the RP series (Sr₃Ir₂O₇) both density functional theory (DFT)⁶⁻⁸ and models of magnetic order⁹ and dynamics^{10,11} are sensitive to subtleties in the local crystal fields at Ir sites.

The structure of $Sr_3Ir_2O_7$ was originally reported as a distorted bilayer perovskite variant described by the tetragonal space group I4/mmm (No. 139) with unit cell dimensions a = 3.896 Å, c = 20.879 Å.¹² In initial studies, evidence of an in-plane rotation (along the unique tetragonal c axis) of the octahedral cages surrounding the Ir atoms was observed via x-ray scattering; however this was refined within a disordered I4/mmm model, where the phasing of the octahedral rotations from site to site is random. Other subsequent x-ray investigations have also observed incoherent rotations among the oxygen octahedra¹³—potentially arising from compositional disorder.

A separate x-ray study put forward an orthorhombic unit cell (a = 5.522 Å, b = 5.521 Å, c = 20.917Å) indexed with an improper Hermann-Mauguin symbol $Bbca^{14}$ (space group No. 68) and modeled using coherent intralayer counter-rotations of neighboring octahedra along the c-axis. Additional support for this orthorhombic model with coherent octahedral rotations was provided by a transmission electron microcopy (TEM) study of the reflection conditions observed in electron diffraction patterns.¹⁵ Here the reciprocal lattices of both *Bbcb*and *Acaa*-type structures, each an alternate setting of the *Ccce* space group (No. 68), were superimposed to match the observed patterns—demonstrating that this system is prone to twinning. This TEM-derived structural solution parallels that of the analogous ruthenate compound $Sr_3Ru_2O_7$,¹⁶ where all modes of octahedral rotation about their symmetry axes were considered as candidate structures.

Even when accounting for the coherent phasing of octahedral rotations, Ccce still fails to completely describe some subtle aspects of $Sr_3Ir_2O_7$'s lattice structure. Neutron diffraction measurements¹⁷ have observed peaks in the [H 0 L] zone (*Bbcb* setting) that violate the reflection condition H,L = 2n imposed by the space group.¹⁸ These weak violations were later confirmed to be of structural origin via a polarized neutron scattering study¹⁹ and are reminiscent of those observed within the n = 1system Sr_2IrO_4 (also via neutron diffraction).^{20,21} While in Sr_2IrO_4 two unique Ir environments were ultimately refined,^{22,23} the origin of the Bragg violations in $Sr_3Ir_2O_7$ and their implication for its lattice structure remains an open question.

In this paper, we utilize single crystal neutron scattering and rotational anisotropy second harmonic generation (RA-SHG) measurements to resolve the structure of $Sr_3Ir_2O_7$. The point group for the lattice is constrained via RA-SHG measurements to be either 4/m or 2/m or one of even lower symmetry, which when combined with single crystal neutron data identifies the monoclinic space group C2/c as the correct structural symmetry. Density functional theory calculations were used to guide the space group search and identify the most energetically fa-



FIG. 1: Radial **Q** scan at T = 315 K through the (1, 0, 3) reflection demonstrating a violation of the general reflection condition $H_{,L} = 2n$ for the orthorhombic *Bbcb* space group. Data reproduced from Ref. [17]

vored mode of lattice distortion. In addition to in-plane rotations, oxygen octahedra in this new lower symmetry can tilt off-axis, suggesting that the anomalous, weak inplane ferromagnetism of $Sr_3Ir_2O_7$ originates from these tilts combined with strong spin-lattice coupling. Using probes sensitive to both oxygen sites as well as point group symmetry, our measurements ultimately provide a foundation for understanding the further structural distortions observed in this system during metallization via pressure²⁴ and electron substitution.²⁵

II. EXPERIMENTAL AND COMPUTATIONAL DETAILS

The method for growing the $Sr_3Ir_2O_7$ single crystals used in our study is reported elsewhere.²⁵ Neutron scattering measurements were conducted by measuring a small single crystal (mass 5.6 mg, dimensions 1.25 mm × 1.13 mm × 0.1 mm) in the time-of-flight single crystal Laue diffractometer TOPAZ at Oak Ridge National Laboratory. Sample orientations were optimized with the CRYSTALPLAN software²⁶ for an estimated coverage of 99.8% of equivalent reflections for the nominal orthorhombic cell for this system. Reduction of the raw data including Lorentz corrections, absorption, time-offlight spectrum, and detector efficiency corrections were carried out with ANVRED3.²⁷ The raw peaks were integrated using a 3-D ellipsoidal routine,²⁸ and the reduced dataset was refined using SHELXL.²⁹

To guide the search for the correct space group, density functional theory was employed to compare several potential solutions. Of the resulting relaxed structural geometries, those that did not display the correct antiferromagnetic ordering of the Ir 5d moments in the sim-



FIG. 2: Refined lattice structure of $Sr_3Ir_2O_7$. Red atoms denote oxygen sites, blue atoms within octahedra denote iridium sites, and green atoms denote strontium sites. (a) The in-plane oxygen octahedral rotations as viewed along the *a*-axis. (b) Out-of plane oxygen octahedral tilt mode, viewed along the *b*-axis. c) Off-axis view of the chemical unit cell. Atom positions are those of the T = 300 K refinement to the C2/c space group.

ulated structures could be discarded. Structures which remained served as initial conditions for refinement to the neutron diffraction dataset. The calculations were performed using the projector augmented-wave method³⁰ in the Vienna Ab initio Simulation Package (VASP).^{31,32} The PBE functional³³ was used with a screened on-site Coulomb repulsion parameter U of 2 eV on the Ir d orbitals, and spin-orbit coupling (SOC) taken into account. Taken together, the +U interaction and SOC open up a Mott-Hubbard gap within the Ir 5d band. Since the material is layered, Van der Waals interactions are accounted for via Becke-Johnson damping,³⁴ as implemented in VASP. For the 48-atom unit cell, a planewave cutoff of 500 eV and $4 \times 4 \times 1$ Γ -centered k-point mesh were used.

Determining the point group of $Sr_3Ir_2O_7$ was accomplished through the use of RA-SHG techniques. These data were acquired using the rotating scattering plane based technique described in Ref. [35] from cleaved surfaces of $Sr_3Ir_2O_7$ with the long cell axis parallel to the surface normal. Incident light was provided by a Ti:sapph regenerative amplifier (800 nm center wavelength, 60 fs pulse duration, 10 kHz repetition rate) and focused to a spot size less than 100 μ m on the crystal with

a fluence less than 1 mJ/cm^2 . The linear polarization of the incident (in) and reflected (out) light was selected to be either in (P) or out of (S) the scattering plane. The orientation of the two in-plane crystallographic axes were determined independently by x-ray Laue diffraction.

III. NEUTRON DIFFRACTION RESULTS

We first examine the refined results from single crystal diffraction data collected from $Sr_3Ir_2O_7$. Diffraction data were collected and patterns refined both at 100 K and 300 K. As a starting procedure for refinement, the undistorted tetragonal parent I_4/mmm structure was transformed into candidate lower-symmetry space groups^{36–39} corresponding to pure rotations about axes of high symmetry.¹⁶ Distortions of the octahedra were introduced using the relaxed structures from DFT calculations as initial positions. These structures were then refined to the single crystal neutron diffraction data at T = 300 K to evaluate which set of octahedral rotations most faithfully reproduced the observed pattern. Neutron scattering as a probe is particularly well-suited to this task as, compared to synchrotron radiation, it is more sensitive to the oxygen comprising the octahedra. Similar to Sr₃Ir₂O₇'s ruthenate analog, all tetragonal subgroups rendered poor fits and the two best models which emerged were refined within space groups No. 68 (Ccce) and No. 15 (C2/c).

The former group *Ccce* is consistent with the previously reported structure,^{14,15} and represents the coordinated rotation of in-plane octahedra with the rotational sense about the long (here, b) axis for intralayer neighboring cages being opposite. However this structure fails to account for the weak Bragg violations (> 10^3 times weaker than primary peaks) known to exist in this system as illustrated in Fig. 1 where one such forbidden reflection at $\mathbf{Q} = (1, 0, 3)$ is reproduced. This implies that there is a further distortion of the lattice into a lower symmetry than those previously reported. Alternatively, the C^2/c monoclinic group, related to Ccce by the transformation matrix $-b+\frac{1}{4}$, $a+\frac{1}{4}$, c, can account for these violations and represents a combination of the previous in-plane octahedral rotation with an additional octahedral tilt mode,¹⁶ as seen projected separately in panels (a) and (b) of Fig. 2. Taken blindly however, the R1 values resulting from refinement of the time-of-flight data alone were comparable for each candidate group, mandating further constraints to determine the correct solution.

IV. ROTATIONAL ANISOTROPY SECOND HARMONIC GENERATION RESULTS

To further distinguish between the two possible solutions, rotational anisotropy second harmonic generation measurements were taken. RA-SHG is a technique capable of directly determining the crystallographic point group symmetry of a material. In these experiments, light of frequency ω is obliquely incident on the surface of a crystal and the intensity of light reflected at 2ω is measured as a function of the angle (ϕ) between the scattering plane and some in-plane crystalline axis.³⁵ By performing these measurements using different combinations of incident and outgoing light polarization, the entire nonlinear optical susceptibility tensor can be determined, which embeds all the point group symmetries of the material. This technique has recently been used to help identify subtle structural distortions in Sr₂IrO₄^{22,40} that lower the point group symmetry from 4/mmm to 4/m.

Fig. 3 shows RA-SHG patterns from Sr₃Ir₂O₇ acquired under all four linear polarization geometries at room temperature (> T_N). The bottom row shows best fits to calculations based on the three crystallographic point groups that have been proposed for $Sr_3Ir_2O_7$: tetragonal 4/mmm (I_4/mmm) ,¹² orthorhombic mmm (Bbcb),^{14,15} and orthorhombic 2mm $(Bb2_1m)$.¹⁹ For the non-centrosymmetric 2mm point group, we assume the dominant contribution to SHG to be of bulk electricdipole origin. For the centrosymmetric 4/mmm and mmm point groups on the other hand, bulk electricdipole SHG is forbidden, and we instead assume the dominant contribution to be of bulk electric-quadrupole origin, consistent with the case for $\mathrm{Sr}_2\mathrm{IrO}_4$.^{22,40} It is clear from Figs. 3 (e)–(h) that none of these three proposed point groups can describe the RA-SHG data. On the other hand, by assuming bulk-electric quadrupole induced SHG from a centrosymmetric 4/m point group, we obtain excellent agreement with the data as shown in Figs. 3 (a)–(d) (We note that bulk magnetic dipole induced SHG from a 4/m point group does not qualitatively match the data). Any sub-group of 4/m (such as 2/m) fits the data equally well since it naturally contains all elements of the 4/m electric-quadrupole susceptibility tensor. Taken together with the diffraction data presented in Section III, these results suggest that $Sr_3Ir_2O_7$ crystallizes in a 2/m point group but is very close to being 4/m.

V. STRUCTURAL MODEL OF Sr₃Ir₂O₇

With the RA-SHG analysis unambiguously ruling out the orthorhombic point group mmm associated with *Ccce*, we exclude space group No. 68 as a possible solution and focus exclusively on No. 15 (C2/c). Tables I and II list the complete refinement results obtained at T = 300 K and T = 100 K respectively. The relative atomic positions reported correspond to the standard setting of space group C2/c (No. 15) wherein the unique axis (associated with the single oblique angle β) is b, and the long axis is now a. Atomic displacement factors were also refined with all U_{ij} matrices passing a check for posi-



FIG. 3: RA-SHG patterns (open circles) from $Sr_3Ir_2O_7$ acquired under (a) S_{in} - P_{out} , (b) P_{in} - P_{out} , (c) S_{in} - S_{out} and (d) P_{in} - S_{out} polarization geometries at T = 295 K. The intensities of all patterns are normalized against the PP trace. Red lines overlaid on the data are best fits to bulk electric quadrupole induced RA-SHG calculated using either of the centrosymmetric 4/m or 2/m point groups. The bottom row (e)–(h) shows the corresponding best fits to bulk electric-quadrupole induced RA-SHG from the centrosymmetric 4/mmm (green) and mmm (blue) point groups as well as to bulk electric-dipole induced RA-SHG from the non-centrosymmetric 2mm point group (orange). Responses that are absent in the plots are forbidden by symmetry.

tive definiteness. Each atomic site within the cell refined to be fully occupied within error. Associated unit cell parameters can be found in Table III.

To converge, fits require refining the structure as a twin and obtain final R1 values of 5.7% (300 K) and 5.9% (100 K). Our choice of twin law is informed by the 'accidental' pseudosymmetry of the unit cell. Previously, the unit cell parameters comprising the basal plane (b and c for C2/c) have been consistently reported as identical to within experimental precision and no measurable obliquity of the cell has been reported. As no tetragonal space groups produce a satisfactory solution the conditions $b \approx c, \beta \approx$ 90° instead represent an effective tetragonal metric of the system. The twin law which permits the refinement to converge is a symmetry operator of the tetragonal point group 4/mmm: a two-fold rotation about the [011] direction (basal plane diagonal). In real space, for a small deviation from the condition $\beta = 90^{\circ}$, this is tantamount to an altering of the rotational phasing of the octahedra (along the long axis) at the twin boundary. The twin scale factor was refined to 0.497, very near the ideal 'perfect twin' value of 0.5. We note that because the twin law is not a symmetry operator of the point group of the individual's lattice (2/m), this is classified as twinning by pseudo-merohedry.⁴¹

A representative oxygen octahedral cage surrounding each Ir site is depicted in Fig. 4. The full refinement reveals only a slight tetragonal distortion in the apical direction (\hat{a} , for the standard setting used here), with a distortion parameter of only $\Delta_d = \frac{1}{6} \sum_{n=1,6} \left[(d_n - d)/d \right]^2 =$ 1.10×10^{-4} where d is the average of the octahedral bond lengths. In comparing this new model at 300 K with previous reports, two distinguishing attributes should be highlighted: first, the in-plane rotation angle of 11.5° closely matches previous measurements.¹⁴ Next, in contrast to *Ccce*, the out-of-plane tilt (now permitted) refines to a value of 0.23°. At 100 K, the in-plane rotation angle increases to 11.8° and the tilt to 0.33°. Represen-

Atom	Wyckoff Site	х	у	Z	U ₁₁
Ir	8f	0.59755(4)	0.7495(5)	0.7500(4)	0.00670
Sr(1)	4e	0.500000	0.2489(11)	0.750000	0.01010
Sr(2)	8f	0.68747(7)	0.7507(9)	0.2494(5)	0.00930
O(1)	4e	0.500000	0.7480(14)	0.750000	0.00460
O(2)	8f	0.69414(8)	0.7487(9)	0.7496(7)	0.00400
O(3)	8f	0.09674(14)	0.4499(9)	0.4490(5)	0.01450
O(4)	8f	0.09610(14)	0.9488(9)	0.5507(5)	0.01650
Atom	U ₂₂	U ₃₃	U ₁₂	U ₁₃	U ₂₃
Ir	0.00800	0.00210	-0.00030	-0.00170	-0.00040
Sr(1)	0.00700	0.01200	0.00000	-0.00100	0.00000
Sr(2)	0.01200	0.01100	0.00190	-0.00190	-0.00170
O(1)	0.02100	0.02200	0.00000	-0.00230	0.00000
O(2)	0.00700	0.02100	0.00130	-0.00180	-0.00050
O(3)	0.01120	0.00700	-0.00010	-0.00040	0.00290
O(4)	0.01040	0.00840	0.00060	-0.00100	-0.00270

TABLE I: Results of refinement of T = 300 K neutron diffraction data to the C2/c model. Wyckoff site labels, relative atomic coordinates and anisotropic displacement factor matrices U_{ij} are included. R1 = 0.057

TABLE II: Results of refinement of T = 100 K neutron diffraction data to the C2/c model. Wyckoff site labels, relative atomic coordinates and anisotropic displacement factor matrices U_{ij} are included. R1 = 0.059

Atom	Wyckoff Site	Х	у	Z	U ₁₁
Ir	8f	0.59754(4)	0.7502(11)	0.7504(2)	0.00720
Sr(1)	$4\mathrm{e}$	0.500000	0.2490(2)	0.750000	0.00890
Sr(2)	8f	0.68756(7)	0.7491(16)	0.2505(4)	0.01070
O(1)	$4\mathrm{e}$	0.500000	0.7481(16)	0.750000	0.00700
O(2)	8f	0.69432(8)	0.7490(10)	0.7502(5)	0.00510
O(3)	8f	0.09592(14)	0.4460(9)	0.4465(5)	0.01130
O(4)	8f	0.09688(16)	0.9476(10)	0.5525(7)	0.01140
Atom	U ₂₂	U ₃₃	U ₁₂	U ₁₃	U ₂₃
Ir	0.00930	0.00240	0.00140	0.00060	-0.00060
Sr(1)	0.00300	0.00800	0.00000	0.00310	0.00000
Sr(2)	0.00300	0.01100	0.00000	0.00610	-0.00260
O(1)	0.00400	0.01900	0.00000	0.00800	0.00000
O(2)	0.00700	0.01000	0.00100	0.00180	0.00320
O(3)	0.00620	0.00390	0.00020	-0.00080	-0.00040
O(4)	0.01160	0.00790	0.00000	-0.00060	-0.00460

TABLE III: Lattice Parameters for $Sr_3Ir_2O_7$ at measured temperatures. Space group C2/c, Z = 4.

	T = 300 K	T = 100 K
a	20.935(4) Å	20.917(3) Å
b	5.5185(13) Å	5.5080(10) Å
c	5.5099(9) Å	5.4995(7) Å
β	$90.045(18)^{\circ}$	$90.069(15)^{\circ}$
V	636.6(2) Å ³	633.60(17) Å ³

tative projections of both features, alongside the full unit cell, are seen in Fig. 2. The presence of a tilt angle representing only a $\sim 0.3\%$ deviation from the orthorhombic model with a nearly identical in-plane rotation at these temperatures is consistent with the fact that, by merit of diffraction data refinement alone (excluding weak viola-

tions), C2/c and Ccce describe the single crystal diffraction data equally well.

VI. DISCUSSION

As a separate metric aiding in the differentiation among possible space groups for $\text{Sr}_3\text{Ir}_2\text{O}_7$, density functional theory calculations were employed. Atom positions in the two models for C2/c and Ccce were allowed to relax, subject to symmetry constraints, and the total energies of the resulting configurations were compared. The energy associated with the monoclinic group C2/cwas calculated to be 26 meV lower than that of Ccce, supporting the notion that the activation of the octahedral tilt mode permits a slight reduction of the overall energetics.



FIG. 4: Refined T = 300 K geometry of the IrO₆ octahedra in Sr₃Ir₂O₇ showing relevant bond lengths and their uncertainties. Oxygen atoms are depicted in red, with the central iridium atom in blue.

Based on the combination of neutron diffraction, RA-SHG data, and DFT analysis, the C2/c model is a more complete structural solution as it also resolves previous anomalies in reported neutron diffraction data. General reflection conditions for space group No. 15 (in the standard C2/c setting) impose the condition H+L = 2n;¹⁸ now the weak 'violations' of the orthorhombic solution observed previously¹⁹ are allowed reflections in C2/c. Structure factors corresponding to these reflections, calculated from the refined atomic positions in the monoclinic cell reported here, predict relative intensities of the order matching those observed in earlier triple-axis neutron studies.^{17,19}

The C2/c model also offers a microscopic explanation of the anomalous presence of a net ferromagnetic moment in the basal plane of Sr₃Ir₂O₇ as seen in prior bulk susceptibility measurements.^{14,25} The solution of the magnetic structure depicts antiferromagnetically ordered moments aligned out-of-plane, along the \hat{a} -direction;^{13,17,42} however neutron scattering would be unable to resolve small (< 1°) projections of the moment away from this axis. Assuming a mechanism of spin-locking to octahedral orientation⁴ similar to that observed in Sr₂IrO₄,^{23,43} the ordered moment in the C2/c setting would project a small component into the *b*-*c* plane below $T_N = 280$ K, resulting in a net ferromagnetic moment. To quantify this, the tilt angle observed at 100 K in conjunction with the reported ordered moment size of 0.36 $\mu_B/\text{Ir}^{17,25}$ would imply an in-plane ferromagnetic moment of $\approx 1 \times 10^{-3} \mu_B/\text{Ir}$, in relatively good agreement with *b*-*c* plane magnetization data previously reported in this system.^{14,44}

VII. CONCLUSIONS

The measurements outlined here provide a comprehensive, multi-probe study arriving at the structural solution of the bilayer iridate system $Sr_3Ir_2O_7$. The assignment of the monoclinic space group C^{2}/c (No. 15) readily accounts for previously reported rotations of the inplane octahedra while at the same time enabling a subtle octahedral tilt mode distortion not resolved in previous studies of this system. This tilt breaks the nominal orthorhombic symmetry, lowering the point group from mmm to 2/m as seen in the RA-SHG data, and permits scattering at previously observed Bragg violations of *Ccce*. Including this further distortion in the structural model is supported by DFT calculations, which demonstrate that such a tilt represents a lowering of the overall lattice energy. Our data provide the needed foundation for understanding how the lattice distorts and its subsequent role as this spin-orbit Mott system is driven toward the metallic state via doping or pressure.

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