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Temperature - Pressure phase diagram of the cubic Laves phase Au₂Pb

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The temperature (T) as a function of pressure (P) phase diagram is reported for the cubic Laves phase compound Au₂Pb, which was recently proposed to support linearly dispersing topological bands, together with conventional quadratic bands. At ambient pressure, Au₂Pb exhibits several structural phase transitions at $T_1 = 97$ K, $T_2 = 51$ K, and $T_3 = 40$ K with superconductivity below $T_c = 1.2$ K. Applied pressure results in a rich phase diagram where T_1 , T_2 , and T_3 evolve strongly with P and a **possible** new phase is stabilized for $P > 0.64$ GPa that also supports superconductivity below 1.1 K. These observations suggest that Au₂Pb is an ideal system in which to investigate the relationship between structural degrees of freedom, band topology, and resulting anomalous behaviors.

I. INTRODUCTION

The cubic Laves phase compounds M_2X can be considered as being relatives of the pyrochlore structure, where the tetrahedrally arranged M atoms are distributed inside a face centered cubic arrangement of X atoms.¹ Prior work has shown that this structure accommodates a multitude of binary chemical combinations,² making it a deep reservoir for electronic and magnetic states including superconductivity,³⁻⁵ electronic valence changes,^{6,7} itinerant electron magnetism,⁸ geometrically frustrated magnetism,⁹ and other effects. Recent work addressing Au₂Pb indicates that this family of materials is now expanded to include topologically protected electronic states. The calculated electronic band structure for Au₂Pb includes a crystallographically protected Dirac point at room temperature, in addition to other conventional bands at the Fermi energy (E_F).¹⁰ With decreasing temperature, Au₂Pb undergoes several structural phase transitions at $T_1 = 97$ K, $T_2 = 51$ K, and $T_3 = 40$ K. Below T_3 , Au₂Pb enters a primitive orthorhombic structure, where electronic structure calculations predict that the Dirac point is gapped but retains topological protection. Other band crossings at E_F are also present at low T , providing conduction electrons that produce metallic behavior and conventional BCS superconductivity ($T_c \approx 1.2$ K).

While the presence of conventional bands at E_F makes Au₂Pb distinct from simple three dimensional Dirac semimetals (at high T)¹¹ or topological insulators (at low T)¹², it is of interest because it offers the opportunity to study the relationship between conventional electrons and quasiparticles associated with linearly dispersing bands. This includes the question of how conventional BCS superconductivity might interact with gapped topological bands. It is also possible that the simultaneous presence of linearly dispersing and quadratic bands could result in unusual transport and thermodynamic properties. The complex structural evolution additionally allows for study of how a Dirac point is influenced

by changes in the crystal symmetry.

Hydrostatic pressure is a useful tool to systematically probe lattice structures and concomitant electronic states. For this reason, we undertook to study electrical transport under applied pressure $P < 1.8$ GPa in single crystals of Au₂Pb. Our measurements reveal an unusually rich $T-P$ phase diagram that includes several structural phases and superconducting regions. In particular, we find that while T_1 increases monotonically for pressures up to 1.83 GPa, T_2 and T_3 are initially suppressed and meet near $P_1 \approx 0.64$ GPa. For $P \geq P_1 \approx 0.64$ GPa, another **likely** phase boundary that **may be** structural in nature is seen at T_4 , which increases with P . Superconductivity is seen at low temperatures throughout the entire measured P range. This multitude of structural phases and the persistence of superconductivity will be useful for uncovering anomalous electronic behavior and disentangling topological behaviors from those that are due to material specific details. We additionally compare to the Laves phase analogue, Au₂Bi, which is a conventional metal that does not exhibit any structural phase transitions but does support superconductivity.

II. EXPERIMENTAL METHODS

Single crystals of Au₂Pb were grown using a molten Pb flux as described previously¹⁰. Elemental Au and Pb were mixed in the ratio 2:3 and sealed under vacuum in a quartz tube. The mixture was heated at a rate of 50 °C/hr to 600 °C, held at this temperature for 24hr, and slowly cooled at a rate of 3°C/hr to 300°C. The crystals were separated from the flux by centrifuging at this temperature. Single crystals of Au₂Bi were made using a similar approach, where the molar ratio was 3:7.

Single crystals of Au₂Pb and Au₂Bi were structurally characterized at room temperature by single crystal x-ray diffraction using an Oxford-Diffraction Xcalibur2 CCD system with graphite monochromated Mo $K\alpha$ radiation. Data was collected using ω scans with 1° frame

widths to a resolution of 0.5 Å, equivalent to $2\theta = 90^\circ$. The data collection, indexing, and absorption correction were performed using the Agilent CrysAlisPro software¹³. Subsequent structure refinement was performed by using CRYSTALS¹⁴. A crystallographic information file (CIF) for Au₂Pb has been deposited with ICSD (CSD No. 430187)¹⁵. For subsequent measurements, single crystals were selected and aligned using a four-axis Enraf Nonius CAD-4 Single Crystal X-Ray Diffractometer. The obtained orientation matrix allowed for an unambiguous determination of the crystalline axes to within a degree.

Specimens were prepared for electrical resistivity ρ measurements by attaching Pt wires using a home built micro-spot welder. Samples of Au₂Pb were loaded into a piston-cylinder pressure cell. The pressure P was determined by measuring the superconducting transition of 6N polycrystalline Pb. Daphne 7474 oil was used as the pressure-transmitting medium^{16,17}. The electrical resistivity ρ was measured with currents applied along the [100] direction (at room temperature) for temperatures $1.8 \text{ K} < T < 300 \text{ K}$ and $P \leq 1.8 \text{ GPa}$ using a Quantum Design Physical Property Measurement System and an SR830 lock-in amplifier with a Keithley 6221 as the current source. Additional resistivity measurements under applied pressure were performed at the National High Magnetic Field Laboratory, Tallahassee, for temperatures between $500 \text{ mK} < T < 2 \text{ K}$ using a standard He-3 cryostat. Electrical resistivity and heat capacity measurements were performed at ambient pressure on an aligned single crystal of Au₂Bi using the He-3 option in a Quantum Design Physical Properties Measurement System for temperatures $400 \text{ mK} < T < 20 \text{ K}$.

III. RESULTS

Our measurements verify that Au₂Pb and Au₂Bi crystallize in the space group $Fd\bar{3}m$ (#227) where Au₂Pb has unit cell parameter $a = 7.9141(2) \text{ \AA}$ (Fig. 1(a)); the structural parameters resulting from the x-ray refinement for Au₂Pb are summarized in Table I. Au₂Pb and Au₂Bi are cubic Laves phases with a pyrochlore lattice,¹ where the gold is in the 16c position at (0, 0, 0) and lead/bismuth are in the 8b position at (3/8, 3/8, 3/8) (Table II). The single crystal x-ray diffraction for Au₂Pb displayed a site vacancy defect on the Pb-site, yielding a formal stoichiometry of Au₂Pb_{0.95}. For simplicity, the compound will be referred to as Au₂Pb throughout the rest of the manuscript.

The gold atoms form a network of corner-shared tetrahedra connected along the $\langle 111 \rangle$ -directions, with a Au–Au distance of 2.798 Å. The gold network in turn forms voids in which the lead atoms reside as trigonal chains along $\langle 110 \rangle$, with a Pb–Pb distance of 3.427 Å. Au is 12-fold coordinated, surrounded by six Au-atoms and six Pb-atoms (Fig. 1(b)), forming an icosahedron. Pb is 16-fold coordinated with twelve Au-atoms and four

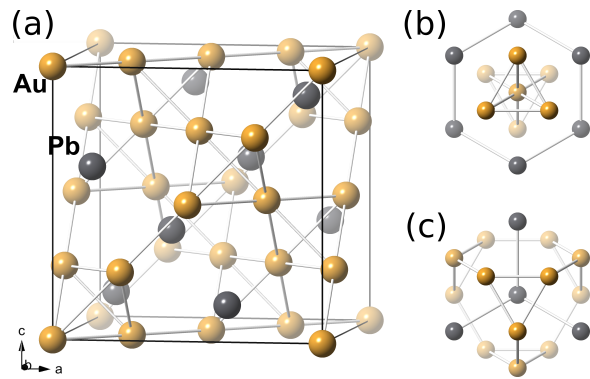


FIG. 1. Crystal structure of Au₂Pb, showing (a) the unit cell, (b) local coordination of Au along [111], and (c) local coordination of Pb along [111].

Pb-atoms surrounding it (Fig. 1(c)), forming a 16-vertex Frank-Kasper polyhedron¹.

The ambient pressure electrical resistivities for Au₂Pb and Au₂Bi are shown in Fig. 2. The residual resistivity ratios $RRR = \rho_{300\text{K}}/\rho_0$ for Au₂Pb and Au₂Bi are 9 and 20, respectively. For Au₂Pb, the structural transitions at $T_2 = 51 \text{ K}$ and $T_3 = 40 \text{ K}$ are easily observed and superconductivity appears below $T_c = 1.2 \text{ K}$ (Fig. 2b), as previously reported.¹⁰ In comparison, Au₂Bi shows typical

TABLE I. Selected single crystal x-ray diffraction data, along with collection and refinement parameters. (Lattice parameters are for Au₂Pb_{0.951(11)})

Compound	Au ₂ Pb
Composition	Au ₂ Pb _{0.951(11)}
Formula weight	590.90 g/mol
Space group	$Fd\bar{3}m$ (#227)
Unit cell parameter	$a = 7.9141(2) \text{ \AA}$
Volume	$495.69(1) \text{ \AA}^3$
Z	8
Data collection range	$4.46^\circ \leq \theta \leq 45.93^\circ$
Reflections collected	6344
Independent reflections	130
Parameters refined	6
R_1, wR_2	0.0431, 0.0687
Goodness-of-fit on F^2	0.9942

TABLE II. Atomic coordinates and equivalent thermal displacement parameters, along with interatomic distances.

Atom	Site	Occ.	x	y	z	$U_{\text{eq}} (\text{\AA}^2)$
Au	16c	1	0	0	0	0.0320(5)
Pb	8b	0.951(11)	3/8	3/8	3/8	0.0191(5)

Bond	Distance (Å)
Au–Au	2.798(1)
Pb–Pb	3.427(1)
Au–Pb	3.281(1)

metallic behavior with no evidence for structural phase transitions, suggesting that it is useful as a conventional metallic Laves phase analogue to Au_2Pb . We additionally find that Au_2Bi exhibits superconductivity near 1.7 K (Fig. 2b), as previously reported.¹⁸ Heat capacity measurements (Fig. 2c) show that the Au_2Bi superconductivity occurs in the bulk, where the ratio $\Delta C/\gamma T_c = 1.9$, is comparable to what is seen for Au_2Pb .¹⁰ This value is larger than what is expected for a BCS superconductor ($\Delta C/\gamma T_c = 1.43$), but is smaller than that of elemental lead.¹⁹ A fit to the data using the expression $C/T = \gamma + \beta T^2$ gives an electronic coefficient $\gamma = 2.3$ mJ/mol-K² and a Debye temperature $\Theta_D = 153$ K ($\beta = 1.6$ mJ/mol-K⁴). For Au_2Pb , we find $\gamma = 1.9$ mJ/mol-K² and $\Theta_D = 133$ K, as previously reported.¹⁰

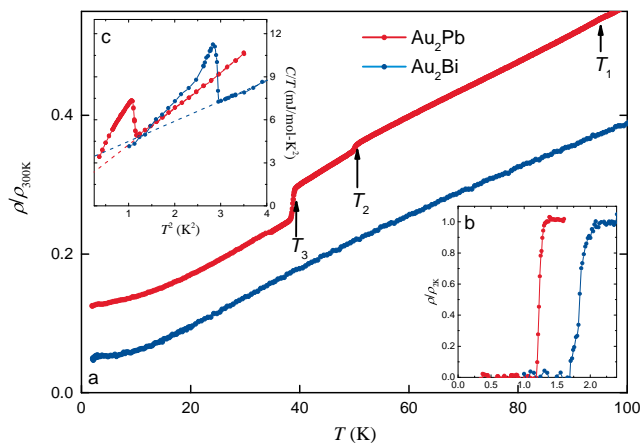


FIG. 2. (a) Cooling curves of the room temperature normalized electrical resistivity $\rho/\rho_{300\text{K}}$ versus temperature T for Au_2Pb and Au_2Bi , where the structural transitions T_1 , T_2 , and T_3 in Au_2Pb are indicated by arrows. (b) Zoom of the normalized resistivity $\rho/\rho_{2\text{K}}$ for $T \leq 2.2$ K, where superconductivity appears as sharp drops to zero resistivity. (c) Heat capacity divided by temperature C/T vs. T^2 for Au_2Pb and Au_2Bi , where the superconducting transitions appear as sharp lambda-type transitions. The dotted lines are fits to the data as described in the text.

The electrical resistivity as a function of temperature under several values of hydrostatic pressure is shown in Fig. 3. Metallic behavior is seen for all pressures with a room temperature resistivity of $35.9 \mu\Omega\text{cm}$ for $P = 0$ which decreases to $33.0 \mu\Omega\text{cm}$ for $P = 1.83$ GPa. We find residual resistivity ratios $RRR = \rho_{295\text{K}}/\rho_0$ in the range 8.1-9.2, slightly increasing with increasing P . The previously reported transition at T_1 appears as a weak reduction in ρ , which becomes more pronounced and increases with increasing P at a rate of 19 K/GPa (Fig. 3b), indicating that this phase transition would occur at room temperature near $P \approx 9$ GPa. T_2 and T_3 appear as sharp reductions in the resistivity, consistent with an earlier report of structural phase transitions at these temperatures under ambient pressure (Fig. 3a,d,e).¹⁰ The features at T_2 and T_3 decrease linearly at rates of 21.5 K/GPa and

1.8 K/GPa, respectively, and finally intersect near $P_1 \approx 0.64$ GPa (determined by extrapolation). For pressures larger than 0.64 GPa, another phase transition appears as a sharp reduction in the resistivity at T_4 , which produces a more pronounced decrease in resistivity than T_2 and T_3 combined. Unlike T_2 and T_3 , T_4 increases linearly at a rate of 12.6 K/GPa, reaching 52 K at $P = 1.83$ GPa (Fig. 3d). All of the observed phase transitions show hysteresis under P (summarized in Fig 5). At low temperature and zero pressure, bulk superconductivity is observed below $T_c = 1.2$ K. Superconductivity persists at 1 GPa, with a slightly reduced transition temperature $T_c = 1.1$ K (Fig. 3e).

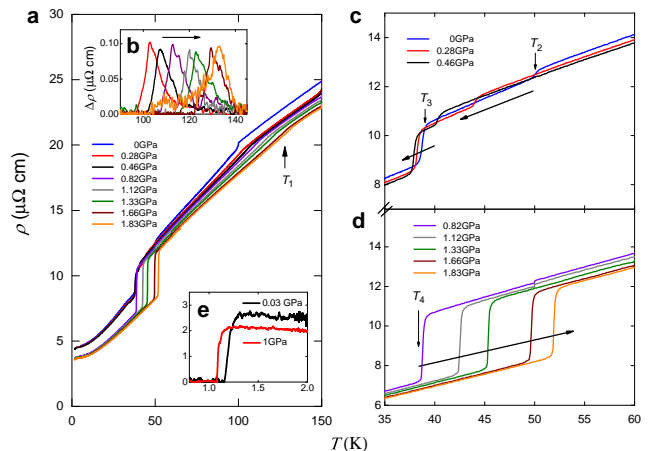


FIG. 3. (a) Cooling curves of the electrical resistivity ρ versus temperature T at pressures $0 \text{ GPa} \leq P \leq 1.83 \text{ GPa}$ for Au_2Pb . Note that the sharp kink for $P = 0$ near $T = 100$ K is an artefact due to a change in the T sweep rate in this data set only. **Smaller kinks are also seen in panel d near 50 K for the same reason.** (b) Zoom of $\rho(T)$ at several P near the anomaly T_1 , after background subtraction. The arrow is a guide to the eye showing the transition temperatures and their evolution. (c) Zoom of $\rho(T)$ for $P \leq 0.46$ GPa at temperatures near the sharp anomalies at T_2 and T_3 . (d) Zoom of $\rho(T)$ for $P \geq 0.82$ GPa at temperatures near the sharp anomaly at T_4 . (e) $\rho(T)$ for $P = 0.03$ and 1 GPa showing superconductivity at low T . The superconducting temperature evolves from $T_c = 1.2$ K at 0.03 GPa to $T_c = 1.1$ K at 1 GPa.

Plots of the resistivity at constant temperature under varying pressure $\rho(P)$ are shown in Fig. 4. For $T > 51$ K, $\rho(P)$ is nearly constant for $P < 1.8$ GPa. For $T \leq 51$ K, there is a large reduction of ρ which first appears at large P and T and moves to lower P with decreasing T . For $38 \text{ K} < T < 51$ K, there is a second transition at lower pressures that evolves with temperature. For $T < 38$ K, there is a single transition pressure that remains nearly constant at $P_1 \approx 0.64$ GPa with decreasing T . We infer that these features are associated with the **proposed** low temperature structural phase transitions seen in $\rho(T)$.

These results are collected in Fig. 5 to build the $T - P$ phase diagram. The solid circles are the $\rho(T)$ cool down curves (Fig. 3), the hollow circles are from the $\rho(T)$ of

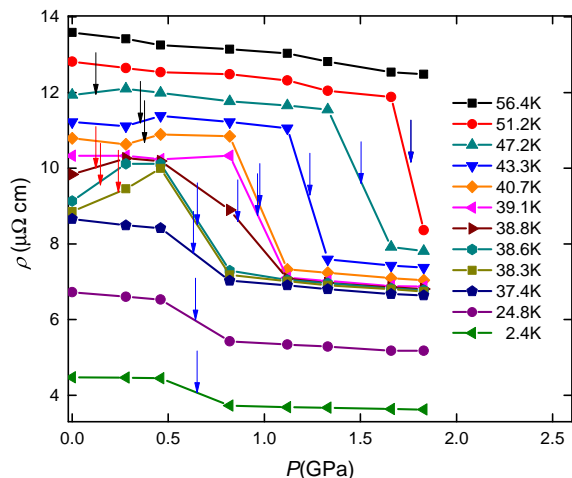


FIG. 4. Electrical resistivity ρ versus pressure P at several temperatures T . The arrows indicate the phase transitions. Several structural transitions appear as sharp kinks in $\rho(P)$ as described in the text. The black arrows indicate T_2 , the red arrows indicate T_3 , and the blue arrows indicate T_4 .

warm up curves and the triangles are from $\rho(P)$ (Fig. 4). While the precise location of the phase boundaries in the phase diagram need additional measurements to establish the extent of the phase fields (particularly where T_2 and T_3 intersect), there appear to be five distinct regions including the previously described Dirac semimetal phase which extends from room temperature to $T = 97$ K for $P = 0$ and several other low T phases labeled 1-4. Region 1 spans the entire pressure range. Region 2 is a small wedge separating 1 and 3. Regions 3 and 4 are the low T /low P and low T /high P phases which are separated by the nearly vertical phase boundary at $P_1 \approx 0.64$ GPa. We further find that superconductivity is present in both regions 3 and 4, where the transition temperature is slightly suppressed by ≈ 0.1 K in region 4.

IV. DISCUSSION

The past several years have witnessed intense interest in materials that support novel electronic states arising from unusual band structures. Examples include materials with topologically protected linearly dispersing bands such as Dirac semimetals (Na_3Bi ²⁰ and Cd_3As_2 ²¹), Weyl semimetals (Nb,Ta(P,As)),²² and topological insulators ($\text{Bi}_2(\text{Se,Te})_3$),¹² as well as other unusual metallic phenomena such as the axial anomaly (PdCoO_2 ²³). While these materials exhibit remarkable behavior, they are often limited in terms of opportunities to test microscopic models by transforming their thermodynamic ground state: e.g., using probes such as applied pressure. As demonstrated in this study, Au_2Pb and potentially the alloy $\text{Au}_2\text{Pb}_{1-x}\text{Bi}_x$ provide the unusual examples where the evolution of topological behavior under

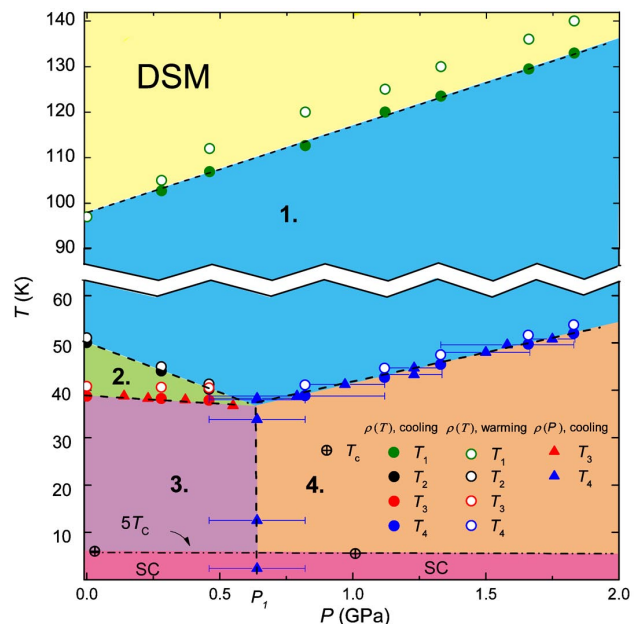


FIG. 5. The temperature-pressure $T - P$ phase diagram for Au_2Pb . The filled/hollowed circles are from the cooling/warming curves of $\rho(T)$ (Fig. 3) and the triangles are from the $\rho(P)$ at various T (Fig. 4). The ambient pressure phase transitions $T_1 (= 97\text{K})$ for both cooling and warming curves are from ref. [10].

the influence of intrinsic structural phase transitions can be systematically explored. In order to do this, it will first be important to determine the structures and electronic characteristics of regions 1, 2, and 4 and to carry out accompanying band structure calculations.

The presence of superconductivity in both the low and high pressure regions for Au_2Pb presents additional opportunities. Prior work suggests that the ambient pressure superconductivity in Au_2Pb occurs in the bulk and can be described as being due to weak coupling electron-phonon interactions in the BCS framework. It is appealing to attribute this superconductivity to the quadratically dispersing bands that are predicted to cross E_F along the $\Gamma - K$ line: i.e., the “conventional bands”.¹⁰ If this is the right picture, then Au_2Pb is a model system in which to investigate what happens in a material that hosts both conventional superconductivity and gapped linearly dispersing bands. Prior work suggests that such a material might support Majorana fermions,²⁴ although this has yet to be substantiated. Comparison to Au_2Bi will help to independently determine whether behavior seen in Au_2Pb is uniquely associated with topological bands.

Our pressure study further amplifies the novelty of this situation by showing that there **likely** is a distinct high pressure phase which also supports superconductivity. It will be of interest to determine whether the high pressure phase includes topological bands and whether they are

significantly different from those at ambient pressure. In the case that the high pressure bands are all conventional, this would give the opportunity to definitively separate what superconducting behaviors are uniquely associated with the presence of topological bands. In particular, further studies of the magnetoresistance and magnetization will be of use to search for unusual power law behaviors and to index quantum oscillation Landau levels, which would unambiguously characterize topological behavior.

V. CONCLUSION

We have presented the $T - P$ phase diagram for the cubic Laves phase compound Au_2Pb , which supports several structural phases and superconductivity over a broad range of pressures. At ambient pressure, we compare it to the conventional metallic Laves phase analogue Au_2Bi . Our observations have important implications for understanding the interplay between conventional and linearly dispersing bands, particularly with respect to possible anomalous transport behavior and the relationship with

superconductivity. Owing to its structural tunability, both with temperature and pressure, it will be possible to systematically explore these effects under different conditions. Such information is needed to separate what features should be attributed to topological behavior and which are merely due to specific details of this material.

VI. ACKNOWLEDGEMENTS

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