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Binod K. Rai, Iain W. H. Oswald, Julia Y. Chan, and E. Morosan Phys. Rev. B **93**, 035101 — Published 4 January 2016 DOI: 10.1103/PhysRevB.93.035101

Intermediate valence to heavy fermion through a quantum phase transition in $Yb_3(Rh_{1-x}T_x)_4Ge_{13}$ (T = Co, Ir) single crystals

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(Dated: December 9, 2015)

Single crystals of Yb₃(Rh_{1-x}T_x)₄Ge₁₃ (T = Co, Ir) have been grown using the self-flux method. Powder X-ray diffraction data on these compounds are consistent with the cubic structure with space group $Pm\bar{3}n$. Intermediate valence behavior is observed in Yb₃(Rh_{1-x}T_x)₄Ge₁₃ upon T = Co doping, while T = Ir doping drives the system into a heavy fermion state. Antiferromagnetic order is observed in the Ir-doped samples Yb₃(Rh_{1-x}T_x)₄Ge₁₃ for $0.5 < x \le 1$ with T_N = 0.96 K for Yb₃Ir₄Ge₁₃. With decreasing x, the magnetic order is suppressed towards a quantum critical point around $x_c = 0.5$, accompanied by non-Fermi liquid behavior evidenced by logarithmic divergence of the specific heat and linear temperature dependence of the resistivity. The Fermi liquid behavior is recovered with the application of large magnetic fields.

PACS numbers: 75.30.Mb, 71.10.Hf

I. INTRODUCTION

Valence instabilities have often been observed in rare earth compounds with nearly full or empty 4f shells. Therefore, compounds with Ce or Yb can be tuned with extrinsic parameters such as pressure, magnetic field, or doping, resulting in a variety of states such as heavy fermion (HF),^{1–3} superconductivity,⁴ intermediate valence,⁵ and mixed valence^{6,7}. While existing literature often uses intermediate and mixed valence terminology interchangeably, these actually refer to two distinct behaviors: temperature-dependent or temperature-independent mixtures of both magnetic and non-magnetic rare earth ions. In this paper the focus is on the temperature-dependent scenario, denoted as intermediate valence. Intermediate valence compounds can be tuned to a HF state with the application of pressure or doping, which effectively shifts the 4f energy level relative to the conduction band.⁸⁻¹¹ In turn, the magnetic order in some HF systems can be suppressed towards a quantum critical point (QCP), often accompanied by non-Fermi liquid (NFL) behavior.^{12–18}

Compounds with the stoichiometry $A_3T_4M_{13}$ (3-4-13) (A is a rare earth or alkaline earth, T is a transition metal and M is a group 14 element) exhibit diverse properties such as magnetism and superconductivity,¹⁹⁻²² structural phase transitions²³ and intermediate valence behavior.^{24,25} A few Ce based 3-4-13 compounds are reported as paramagnetic (PM) HFs (Ce₃Co₄Sn₁₃^{26,27} and Ce₃Rh₄Sn₁₃²⁸) or magnetically ordered HFs (Ce₃Pt₄In₁₃²⁹ and Ce₃Ir₄Sn₁₃^{30,31}). However, no Yb based 3-4-13 PM or magnetically ordered HFs are known to date. Polycrystalline Yb₃T₄Ge₁₃ (T = Ir, Rh) compounds have been reported to order antiferromagnetically around T_N = 2.3 K,^{32,33} a temperature very close to that of the magnetic order in Yb₂O₃. In this study on single crystals of Yb₃(Rh_{1-x}T_x)₄Ge₁₃, we present evidence that the x = 1, T = Ir compound is an antiferromagnetic HF with T_N = 0.96 K, while the x = 0 analogue shows intermediate valence behavior. Furthermore, the intermediate valence was found to persist with T = Co doping up to x = 1, while T = Ir doping changes the system from intermediate valence to heavy fermion around x = 0.25. Additionally, the magnetic order in Yb₃(Rh_{1-x}Ir_x)₄Ge₁₃ is suppressed towards a QCP around a critical Ir composition $x_c = 0.5$, accompanied by NFL behavior at H = 0. Since no 2.3 K transition was observed in single crystals of Yb₃(Rh_{1-x}T_x)₄Ge₁₃ (T = Co, Ir) without prolonged air exposure, it is possible that the earlier reported polycrystalline samples displayed the Yb₂O₃ transition caused by surface oxidation in air.

II. METHODS

Single crystals of Yb₃(Rh_{1-x}T_x)₄Ge₁₃ (T = Co, Ir) were prepared using a self-flux method as discussed elsewhere.³⁴ Powder x-ray diffraction patterns were collected at T = 300 K in a Rigaku D/Max X-ray diffractometer using Cu K α radiation. Rietveld analysis was performed using the GSAS software package.³⁵ DC magnetic susceptibility was measured in a Quantum Design (QD) Magnetic Properties Measurement System (MPMS) with a iHelium ³He option, with the magnetic field H || a. Heat capacity data were collected in a QD Physical Properties Measurement System (PPMS) with a ³He insert using an adiabatic thermal relaxation method. The temperature-dependent AC resistivity of bar-shaped crystals was measured in the QD PPMS, with the current $i \parallel a, i = 1$ mA, f = 17.77 Hz.

III. RESULTS AND ANALYSIS

Rietveld analysis on powder X-ray diffraction pattern of Yb₃(Rh_{1-x}T_x)₄Ge₁₃ (T = Co, Ir) confirms the cubic structure with space group $Pm\bar{3}n$.³⁴ Fig. 1a displays an example of a powder diffraction pattern for x = 0, with a



FIG. 1: (a) Room temperature measured (symbols) and calculated (observed) powder X-ray diffraction pattern for Yb₃Rh₄Ge₁₃, together with the calculated peak positions (blue vertical lines). Aminute amount of Ge flux is marked with an asterisk. (b) Experimental (full) and estimated (open) lattice parameters for Yb₃(Rh_{1-x}T_x)₄Ge₁₃ as a function of x (full triangles). The open triangles correspond to the lattice parameters for the trivalent Yb compounds estimated from the lanthanide contraction extrapolation between the R = Tm and Lu R₃T₄Ge₁₃ compounds.

asterisks marking minute amount of Ge flux. Fig. 1b (full symbols) shows the variation in the experimental lattice parameter a as function of x, with x increasing to the left (right) for dopant T = Co (Ir). With Co doping, a small lattice contraction is observed in $Yb_3(Rh_{1-x}Co_x)_4Ge_{13}$, resulting from the fact that relatively bigger Rh atoms $(r_{Rh} = 0.66 \text{ Å})$ are replaced by smaller Co atoms $(r_{Co} =$ (0.58 Å).³⁶ A much smaller change in *a* is registered for Ir doping in Yb₃(Rh_{1-x}Ir_x)₄Ge₁₃ given that Ir ionic radius $(r_{Ir} = 0.68 \text{ Å})$ is very close to that of Rh. However, a comparison of the measured lattice parameters (full symbols) with the expected values (open symbols) for the Yb^{3+} compounds is very informative. The open symbols correspond to lattice parameter values calculated using the expected Lanthanide contraction³⁶ across the $R_3T_4Ge_{13}$ series with R = Tm, Yb, Lu (T = Co, Rh, Ir). For each T, the reported a values for $\mathbf{R} = \mathbf{Tm}$ and $Lu^{34,37}$ were used to determine the expected parameter for the R = Yb trivalent analogue. For example, for the Yb₃Ir₄Ge₁₃ sample, the expected value was linearly interpolated from the lattice parameters of $Tm_3Ir_4Ge_{13}^{37}$ and Lu₃Ir₄Ge₁₃³⁴. From Fig. 1b, it is readily apparent that Yb is likely in a trivalent state in the T = Ir compounds, while the deviation from the expected lattice parameter for R^{3+} in the T = Co and Rh compounds implies that the Yb ion is in a mixed (less then trivalent) or intermediate (temperature-dependent) valence state. This is indeed consistent with magnetization and transport data presented below.

TABLE I: Parameters for $Yb_3(Rh_{1-x}T_x)_4Ge_{13}$ (T = Co) from ICF model fits.

x	E_{ex}/k_B (K)	T_{sf} (K)	$\chi(0) \ (\ \mathrm{emu}/\mathrm{mol}_{Yb})$	θ (K)	C'
0.00	810(11)	208(7)	0.00011(3)	28(2)	0.037(4)
0.25	780(11)	180(9)	0.00036(6)	47(5)	0.098(1)
0.50	740(9)	155(7)	0.00045(1)	52(4)	0.13(1)
0.75	671(1)	122(1)	0.00060(1)	110(1)	0.28(1)
1.00	621(1)	94(1)	0.00030(1)	262(1)	0.74(1)



FIG. 2: Temperature-dependent magnetic susceptibility M/H for H = 0.1 T of Yb₃(Rh_{1-x}Co_x)₄Ge₁₃ together with ICF model fit (dashed lines).

The temperature-dependent magnetic susceptibility for Yb₃(Rh_{1-x}Co_x)₄Ge₁₃, shown in Fig. 2a, reveals a broad maximum above ~ 150 K, a typical feature of intermediate valence systems. According to the interconfiguration-fluctuation (ICF) model,³⁸ the rare earth Yb can fluctuate between the non-magnetic 4f¹⁴ (J = 0 and $\mu_{eff} = 0$) and magnetic 4f¹³ (J = 7/2 and $\mu_{eff} = 4.54 \ \mu_B$) ground states. The ICF magnetic susceptibility is of the form^{38–40}

$$\chi(T) = \chi(0) + \frac{C'}{T+\theta} + \frac{8N_A(4.54\mu_B)^2}{3k_BT(1+\frac{T_{sf}}{T})[8+e^{\frac{E_{ex}}{k_BT(1+\frac{T_{sf}}{T})}}]}$$

where C' and θ are the Curie-Weiss constant and Weiss temperature associated with the small fraction of Yb^3+



FIG. 3: (a) Temperature-dependent magnetic susceptibility M/H of Yb₃(Rh_{1-x}Ir_x)₄Ge₁₃ for H = 0.1 T. Inset: low temperature M/H showing the antiferromagnetic ordering temperature T_N marked by vertical arrows. (b) Inverse magnetic susceptibility H/M vs. T for Yb₃(Rh_{1-x}Ir_x)₄Ge₁₃ at H = 0.1 T, with an example of a Curie-Weiss fit (dotted line).

ions, E_{ex} is the energy gap between the magnetic and non-magnetic configurations, and T_{sf} is the spin fluctuation temperature related to the rate of valence fluctuation between 2+ and 3+ states. The fit values for C', θ , E_{ex} and T_{sf} are shown Table I. Both E_{ex} and T_{sf} decrease while C' increases with increasing Co concentration in $Yb_3(Rh_{1-x}Co_x)_4Ge_{13}$, consistent with departure from the intermediate valence state with increasing x. This was already suggested by the difference between the experimental (full) and calculated (open) lattice parameters for the trivalent Yb compounds seen in Fig. 1b. Bv contrast. Ir doping rapidly drives $Yb_3(Rh_{1-x}Ir_x)_4Ge_{13}$ towards the trivalent, local moment Yb limit: even for x = 0.25, the broad maximum caused by intermediate valence disappears as shown in Fig. 3a, and instead the magnetic susceptibility has a Curie-Weiss temperature dependence. The effective moment values μ_{eff} and Weiss temperatures θ determined from the Curie-Weiss fits of the inverse susceptibility (Fig. 3b) are listed in the Table II. As x approaches 1 in $Yb_3(Rh_{1-x}Ir_x)_4Ge_{13}$, the effective moment increases



FIG. 4: M(H) isotherms at T = 1.8 K for Yb₃(Rh_{1-x}T_x)₄Ge₁₃ with (a) T = Co and (b) T = Ir. (c) The Yb₃(Rh_{1-x}T_x)₄Ge₁₃ magnetic moment at H = 7 T and T = 1.8 K as a function of x

towards the theoretical value for trivalent Yb μ_{eff} = 4.54 μ_B /Yb). A cusp in the magnetic susceptibility (inset of Fig. 3a) for the x = 0.75 and 1.00 samples signals antiferromagnetic order below T = 0.57 K (x = 0.75) and T = 0.96 K (x = 1.00).

A comparison of the field-dependent magnetization isotherms for the Co and Ir doped Yb₃Rh₄Ge₁₃ reinforces the observations from the temperature-dependent magnetic susceptibility: for Yb₃(Rh_{1-x}Co_x)₄Ge₁₃, the M(H) at T = 1.8 K (Fig. 4a) remains very small and linear. At low temperature (T = 1.8 K), the Ir-doped

TABLE II: Parameters for $Yb_3(Rh_{1-x}T_x)_4Ge_{13}$ (T = Ir) from Curie-Weiss fits.

х	$\mu_{eff} \ (\mu_B/Yb)$	θ (K)
0.25	3.7	101
0.50	3.6	49
0.75	3.8	24
1.00	4.2	17

samples (Fig. 4b) display increasing M(H) values with increasing x. However, the maximum at the highest measured field $\mu[7T; 1.8K]$ is still substantively lower than the saturated Yb³⁺ moment $\mu_{sat} = 4 \ \mu_B$. The $\mu[7T; 1.8K]$ values for all Yb₃Rh₄Ge₁₃ doped samples are summarized in Fig. 4c, illustrating the transition from intermediate valence behavior to a magnetic state around x = 0.25 in Yb₃(Rh_{1-x}Ir_x)₄Ge₁₃.

The specific heat data reveal that this magnetic state corresponds to heavy fermion behavior in the Ir-doped $Yb_3Rh_4Ge_{13}$. The electronic specific heat coefficient $\gamma = C_p/T|_{T=0}$ for Yb₃(Rh_{1-x}Co_x)₄Ge₁₃ (Fig. 5) ranges from 35 to 55 mJ/mol_{Yb} K^2 , consistent with other intermediate valence compounds.^{39,41,42} On the other hand, the Ir-doped series shows large electron mass renormalization (Fig. 6), with $\gamma > 1.2$ J/mol K² for x = 0.50. Upon approaching this composition from the x = 1 limit, the magnetic order at $T_N = 0.96$ K in Yb₃Ir₄Ge₁₃ is suppressed below 0.35 K, indicative of a QCP around x =0.5. At the critical composition, the H = 0 specific heat scaled by temperature C_p/T (Fig. 6a) displays logarithmic divergence ranging over nearly a decade in temperature (dotted line). This is a signature of non-Fermi liquid behavior often observed in the quantum critical regime of HF compounds.^{12,42–45} The application of the magnetic field restores the Fermi liquid behavior for H > 3T (Fig. 6b-d) for samples with low Ir content (x = 0.25, 0.5 and x = 0.75). However, for the highest Ir content (Fig. 6e), the peak at T_N moves up in temperature and broadens with increasing magnetic fields. Such behavior is often observed in HF compounds,^{44,46,47} and it is attributed to the magnetic entropy increase with increasing field, caused by the modification of local moment intersite interactions.^{46,47}



FIG. 5: H = 0 Yb₃(Rh_{1-x}Co_x)₄Ge₁₃ specific heat scaled by temperature C_p/T .

To further verify the NFL regime in $Yb_3(Rh_{1-x}T_x)_4Ge_{13}$, the electrical resistivity was measured and is shown in Figs. 7 and 8. Consistent with the specific heat data, as well as with other intermediate



FIG. 6: (a) Yb₃(Rh_{1-x}Ir_x)₄Ge₁₃ C_p/T vs. T for H = 0. C_p/T vs. T in applied magnetic field H for (b) x = 0.25, (c) x = 0.50, (d) x = 0.75 and (e) x = 1.0.

valence systems, 39,41,42 the H = 0 electrical resistivity of the Co-doped series (Fig. 7a) shows no anomaly and a weak metallic temperature dependence. The $Yb_3(Rh_{1-x}Co_x)_4Ge_{13}$ samples $(0 \le x \le 1)$ display Fermi liquid behavior, marked by the quadratic temperature dependence of the resistivity (Fig. 7b-f) at low temperatures. Conversely, in the Ir doping the FL signatures are clouded by the emergent Kondo behavior common to HFs, 4,12,29,48 reflected in the local maxima that develop in $\rho(T)$ starting at x = 0.25 (symbols, Fig. 8a-d). This local maximum becomes more pronounced with increasing x, as the overall resistivity values increase, and the metallic behavior is replaced by a semiconducting-like temperature dependence in $Yb_3Ir_4Ge_{13}$ (Fig. 8d). To examine whether the semiconducting behavior of $Yb_3Ir_4Ge_{13}$ is due to disorder as is the case in the 3-4-13 germanides,³⁴ room temperature single crystal X-ray diffraction measurements were performed for the three parent compounds $Yb_3T_4Ge_{13}$ (T = Co, Rh and Ir). While Yb₃Rh₄Ge₁₃ and Yb₃Co₄Ge₁₃, showing poor metallic resistivity (Fig. 7a), have ADP ratios 3.98 and 3.54, respectively, $Yb_3Ir_4Ge_{13}$ crystals have large ADP ratio = 4.88, a value well within the range of other reported semiconducting 3-4-13



FIG. 7: (a) H = 0 temperature-dependent electrical resistivity of Yb₃(Rh_{1-x}Co_x)₄Ge₁₃. (b-f) H = 0, $\rho(T)$ vs T² (symbols) together with the $\rho(T) = \rho_o + AT^2$ fits (dashed lines).

germanides.³⁴ This suggests that disorder is at play in Yb₃Ir₄Ge₁₃, and indeed the high temperature resistivity (symbols, Fig. 8d) can be fit to an activated resistivity $\rho(T) = \rho_0 e^{-E_g/k_B T}$ (solid line, Fig. 8d). The linear fit (dashed line) of the semi-log plot $\ln \rho \ vs. 1/T$ (bottom inset, Fig.8d) yields a small gap value $E_g/k_B \approx 120$ K. However, clear deviations from the semiconducting behavior occur at low temperatures (below ~ 100 K). Together with the large $C_p/T \approx 1$ J/mol K², the low temperature deviation from the exponential resistivity suggest that the transport properties of Yb₃Ir₄Ge₁₃ are likely a convolution of large ADP and Kondo behavior.

The magnetic order in Yb₃Ir₄Ge₁₃ is marked by a sharp increase in the $H = 0 \rho(T)$, which corresponds to a minimum in the resistivity derivative $d\rho(T)/dT$ at $T_N = 0.96$ K (triangles, Fig. 8e). Not surprisingly, this transition temperature is consistent with the value determined from the magnetization derivative $d(MT)/dT^{49}$ and C_p/T as illustrated for x = 1 in Fig. 8e (pentagons and circles respectively). At lower compositions ($x \leq$ 0.5), a resistivity drop occurs around T = 1 K (not shown) in the Ir-doped series (x = 0.25 and 0.5), of asof-yet unknown origin. The drop in the resistivity at lower temperature was less than 9 %. While a supercon-



FIG. 8: (a-d) $H \leq 0.5$ (full) and 9 T (open) temperaturedependent electrical resistivity for Yb₃(Rh_{1-x}Ir_x)₄Ge₁₃. Insets: low temperature resistivity range. Solid line in (d) represents the high temperature fit to an activated resistivity $\rho(T) = \rho_0 e^{-E_g/k_B T}$, with E_g determined from the linear fit of ln ρ vs 1/T (dashed line, bottom inset) $E_g/k_B = 120$ K. (e) The ordering temperature T_N (vertical dashed line) for Yb₃Ir₄Ge₁₃ determined from peaks in C_p/T (H = 0, pentagons, left axis), d(MT)/dT (H = 0.1 T, circles, right axis), and a minimum in the resistivity derivative (H = 0, triangles, very left axis).

ducting transition just above 0.4 K cannot be ruled out, no corresponding signatures were visible in the low field susceptibility data (H = 5 Oe, not shown) or zero field specific heat data (Fig. 6), both measured down to 0.4 K. A small magnetic field (H = 0.5 T) suppresses the drop in resistivity, and the resulting H = 0.5 T low temperature $\rho(T)$ becomes linear (Fig. 9a). This behavior is indicative of NFL behavior previously suggested by the specific heat data. The FL behavior in the low Ir-doped samples (x = 0.25 and 0.5) is recovered for H = 9 T (Fig. 9b).



FIG. 9: (a) $\rho(T)$ vs. T and (b) $\rho(T)$ vs T² (symbols), together with linear fits (dotted lines).



FIG. 10: T-x phase diagram of $Yb_3(Rh_{1-x}T_x)_4Ge_{13}$.

IV. CONCLUSIONS

The newly grown single crystals of $Yb_3(Rh_{1-x}T_x)_4Ge_{13}$ (T = Co, Ir) are found to adopt a cubic crystal structure with space group $Pm\bar{3}n$. The ICF magnetic susceptibility behavior, small electronic specific heat coefficient values γ , and the quadratic temperature dependence of the resistivity at low temper-

atures show that the Co-doped samples are intermediate valence systems. By contrast, the γ values are at least one order of magnitude larger (> 560 mJ/mol_{Yb} K^2 at T = 0.4 K) for $x \ge 0.25$ in Yb₃(Rh_{1-x} Ir_x)₄Ge₁₃, indicating a cross-over towards heavy fermion behavior with Ir doping. This scenario is supported by other measurements in these crystals, showing Curie-Weiss magnetic susceptibility and Kondo-type local maxima in the $\rho(T)$ data. Antiferomagnetic order at $T_N = 0.96$ K (marked by the vertical line in Fig. 8e) in $Yb_3Ir_4Ge_{13}$ is confirmed by d(MT)/dT, C_p/T , and $d\rho(T)/dT$. This represents the first known magnetically ordered Yb-based HF in the family of 3-4-13 compounds. The magnetically ordered state is suppressed down to temperatures below 0.35 K by $x_c = 0.5$, as shown in the T x phase diagram in Fig. 10. The logarithmic behavior of the specific heat data and the linear resistivity below x_c = 0.5 are indicative of a quantum critical point around this composition, accompanied by NFL behavior at H =0. The FL behavior on the HF side of the phase diagram is recovered with application of large magnetic fields (Figs. 6b-d and 9).

To investigate the possibility of a spin pseudogap similar to what was recently revealed by nuclear magnetic resonance (NMR) in YbPtGe₂,^{39,50} NMR measurements on Yb₃(Rh_{1-x}Co_x)₄Ge₁₃ are currently underway. Pressure may be used to drive the ICF compounds Yb₃(Rh_{1-x}Co_x)₄Ge₁₃ towards the local moment limit, as a shrinking unit cell may be conducive to a non-magnetic (large) Yb²⁺-to-magnetic (small) Yb³⁺ transition. In turn, the magnetic state in Yb₃(Rh_{1-x}Co_x)₄Ge₁₃ under pressure may be tuned towards a QCP, and this is the subject of an on-going study.

V. ACKNOWLEDGEMENTS

This work was supported by the Gordon and Betty Moore Foundation EPiQS initiative through grant GBMF4417 and the Welch Foundation.

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