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# Relaxation Dynamics in the frustrated Cr<sub>9</sub> antiferromagnetic ring probed by NMR

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We investigate the magnetic properties and the phonon-induced relaxation dynamics of the first regular Cr<sub>9</sub> antiferromagnetic (AF) ring, which represents a prototype frustrated AF ring. Geometrical frustration in Cr<sub>9</sub> yields an energy spectrum with twofold degenerate low-lying levels and a low-spin ground state. The electronic relaxation dynamics is probed by <sup>1</sup>H-NMR through the temperature dependence of the spin-lattice relaxation rate  $1/T_1$ . We develop a microscopic model that reproduces  $1/T_1(T)$  curves, taking also into account the wipeout effect. By interpreting these measurements we determine the spin-phonon coupling strength and we investigate the decay of the cluster magnetization due to the spin-phonon interaction. We find that at very low temperatures the relaxation is characterized by a single dominating Arrhenius-type relaxation process, whereas several relevant processes emerge at higher temperatures. In addition, we calculate the temperature and magnetic field dependence of level lifetimes.

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## I. INTRODUCTION

Molecular nanomagnets (MNM)s<sup>1</sup> are spin clusters whose magnetic interactions can be engineered at the synthetic level. Being among the first examples of real spin systems of finite size, they are at the forefront of research in condensed-matter physics and constitute test beds for fundamental concepts in quantum mechanics. Sophisticated experiments and targeted research activities have unveiled a variety of fundamental quantum phenomena<sup>2</sup> and of potential technological applications<sup>3</sup>. One of the most important goals is to reach a deep understanding of the relaxation dynamics of MNMs, because this aspect is of paramount importance in the design of new molecules acting as classical or quantum bits. One of the most important classes of MNMs is that of even-membered antiferromagnetic (AF) rings, where the metal ions form almost perfect regular polygons. These systems are characterized by a highly non-classical  $S = 0$  ground state ( $\mathbf{S}$  being the total spin of the molecule) and can display quantum tunneling of the Néel vector<sup>4,5</sup>, which is the AF counterpart of magnetization tunneling. These systems have been also exploited to investigate the nature of the elementary excitations in finite AF systems<sup>5,6</sup>. One of the most studied AF rings is Cr<sub>8</sub><sup>7</sup>, which is formed by eight AF-coupled Cr<sup>3+</sup> ions ( $s = 3/2$ )<sup>6-8</sup>. Heterometallic rings with a magnetic ground state can be obtained from homonuclear ring by chemical substitution of one or two magnetic centers. In particular, Cr<sub>7</sub>M rings (M = Zn, Cd, Mn, Ni) are derived from Cr<sub>8</sub> by substitution of one divalent cation M for a trivalent Cr ion<sup>9</sup>. Among them, Cr<sub>7</sub>Ni has been shown to be an excellent candidate to encode qubits<sup>2,10-13</sup>. In addition, magnetically-open AF

rings like Cr<sub>8</sub>Cd are reference systems to study the microscopic magnetic behaviour of finite AF chains<sup>14</sup>.

The attention is now focusing on the last missing members of the AF rings family: Closed rings with an odd number of magnetic ions. This kind of molecules is very important because they can be considered as model systems for frustration-induced properties. Indeed, if these rings have a regular geometry and half-integer local spins, they obey the definition of *degenerate frustration* given by O. Kahn<sup>15</sup>, displaying a degenerate pair of  $S = 1/2$  doublets as ground states. However, sizeable structural distortions in the geometry of these molecular polygons lead to the removal of frustration and thus of the degeneracy in the ground state, even if there are still competing AF interactions<sup>15</sup>. The simplest odd-numbered molecular AF rings are AF triangles like Cu<sub>3</sub><sup>16</sup>, whereas larger rings have been much more challenging to synthesize. The first example of AF ring with  $N = 9$  is Cr<sub>8</sub>Ni<sup>17,18</sup>, which however is not frustrated because the Ni<sup>2+</sup> ion breaks the nonagonal symmetry. Another interesting molecule is the {VO}<sub>7</sub><sup>19</sup> ring, which has been characterized only by low-temperature DC magnetization measurements. Recently, the first examples of Cr<sub>9</sub> rings have been synthesized and studied<sup>20-22</sup>, but none of them displays the characteristics of a degenerate-frustrated ring. Indeed, they all have at least one significant bond defect, leading to a sizeable removal of the degeneracy in the  $S = 1/2$  ground state or even to a ground state with  $S > 1/2$ .

In this paper we study the first regular Cr<sub>9</sub> AF ring (of formula C<sub>90</sub>H<sub>162</sub>Cr<sub>9</sub>F<sub>9</sub>O<sub>36</sub><sup>23</sup>), which represents a prototype of a practically degenerate-frustrated homometallic ring. In this compound all the Cr-Cr edges are bridged

in the same manner, by one fluoride and two pivalate ligands (see Fig.1) and susceptibility and low temperature magnetization measurements are very well reproduced by assuming a single exchange constant. Frustration in molecular nanomagnets yields energy spectra with degenerate levels and novel physical properties, which affect their relaxation dynamics<sup>24,25</sup>. While magnetic relaxation in even-membered AF rings like Fe<sub>6</sub> and Cr<sub>8</sub> has already been theoretically and experimentally investigated<sup>26,27</sup>, no equivalent experimental or theoretical studies exist on frustrated AF rings.

AF rings are characterized by a relatively fast phonon-induced relaxation. Hence, the best technique to probe such dynamics is nuclear magnetic resonance (NMR)<sup>26,28</sup>. Therefore, we have investigated Cr<sub>9</sub> by <sup>1</sup>H-NMR, by measuring the temperature-dependence of the proton spin-lattice relaxation rate  $1/T_1(T)$  for different values of the applied magnetic field<sup>26,29</sup>. We have developed a theoretical model for Cr<sub>9</sub> including magnetoelastic couplings which allows us to reproduce  $1/T_1$  data, taking also into account the subtle wipeout effect<sup>30</sup>. The interpretation of these measurements has allowed us to estimate the coupling between electron spins and phonons, and to study the decay of the molecular magnetization. We find that Cr<sub>9</sub> is characterized by one dominating Arrhenius relaxation process only at low temperature, whereas several relaxation processes are important above  $T = 3$  K. We note in passing that in the ideal case all the corresponding relaxation rates are twofold degenerate, like low-lying energy levels. At last, the so-obtained model allows us to predict the temperature and magnetic field dependence of level lifetimes and to propose a challenging neutron scattering experiment to directly investigate how the frustration is ultimately removed and the resulting low-frequency quantum dynamics.

## II. THEORETICAL MODEL

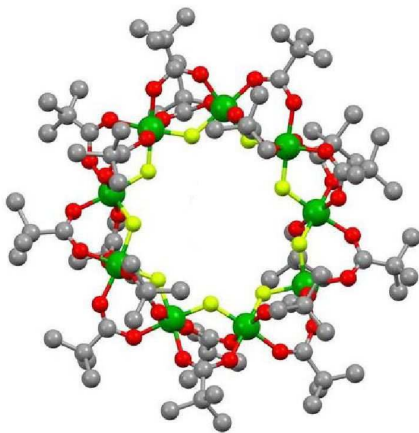


FIG. 1. Molecular structure of Cr<sub>9</sub> crystallised from acetone. Green, Cr; red, O; grey, C; yellow, F (hydrogen atoms not shown for clarity).

Cr<sub>9</sub> contains nine AF-coupled Cr<sup>3+</sup> ions ( $s = 3/2$ ). Previously studied Cr<sub>9</sub> molecules have had one significant bond defect, with only one pivalate and one fluoride on one Cr-Cr edge<sup>20,21</sup>, leading to a significantly weaker exchange interaction between those two Cr<sup>3+</sup> ions. The Cr<sub>9</sub> variant studied in this paper, with a formula Cr<sub>9</sub>F<sub>9</sub>{O<sub>2</sub>CC(CH<sub>3</sub>)<sub>2</sub>}<sub>18</sub><sup>23</sup> has identical bridging on each edge, with one fluoride and two pivalates present on each edge. The compound has been characterized by mass spectrometry and elemental analysis, and by X-ray diffraction studies. When recrystallized from toluene, crystals are obtained in high yield that form in the hexagonal crystal system. Diffraction studies reveal a nine-metal ring formed about a three-fold crystallographic axis; as the organic ligands cannot be arranged with three-fold symmetry, the remainder of the structure is highly disordered leading to poor diffraction. Recrystallisation of these Cr<sub>9</sub> crystals from acetone or n-propanol produces very small crystals in poor yield but which form in a monoclinic or orthorhombic crystal system respectively, which allows a full crystal structure to be obtained (shown in Fig.1 for crystals grown from acetone). In turn, if these crystals are recrystallized again from toluene we regain the hexagonal crystals. As Cr<sub>9</sub> is chemically identical in each crystal, we have carried out physical studies on the crystals formed in high yield from toluene. However to interpret the NMR spectroscopy we used the full structure obtained on Cr<sub>9</sub> crystallised from acetone to determine the H-atom positions.

Magnetic properties of this regular Cr<sub>9</sub> variant can be described by the following spin Hamiltonian :

$$\mathcal{H}_1 = J \sum_{i=1}^N \mathbf{s}_i \cdot \mathbf{s}_{i+1} + g\mu_B \mathbf{B} \cdot \sum_{i=1}^N \mathbf{s}_i \quad (1)$$

( $s_i = 3/2$  for Cr<sup>3+</sup> and  $N = 9$  is the number of magnetic ions in the molecule, with the usual cyclic boundary condition  $N + 1 = 1$ ). The first term represents the isotropic Heisenberg exchange interaction, with the same exchange parameter  $J$  for all the bonds, and the last one is the Zeeman coupling to an external magnetic field ( $g = 1.98$  for Cr<sup>3+</sup>). Anisotropy effects due to the introduction of a small zero-field splitting term in (1) are discussed in Section V.

We determine the exchange parameter  $J$  in (1) by susceptibility and low-temperature magnetization measurements (Fig.2). DC SQUID magnetometry on a powdered sample of Cr<sub>9</sub> has been performed on a MPMSXL-5 SQUID magnetometer, in the temperature range of 2 – 300 K and field range of 0 – 5 T. The monotonic decrease of  $\chi T$  indicates the presence of dominant AF interactions leading to a low-spin ground state (Fig.2). Low-temperature magnetization data saturate to  $1\mu_B$  per molecule (inset of Fig.2). This value of the magnetization per molecule points to a  $S = 1/2$  ground state at least up to 5 T, being  $g = 1.98$ . Fig. 2 shows that magnetic measurements can be well reproduced by the model Hamiltonian in Eq. (1) with a single AF exchange cou-

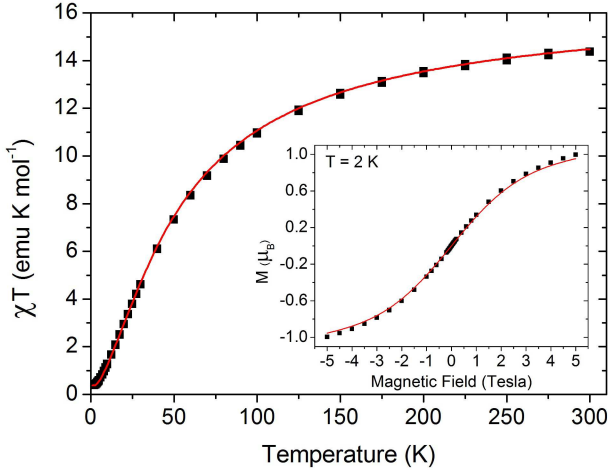


FIG. 2. Measured temperature dependence of  $\chi T$  of  $\text{Cr}_9$  (black circles) compared with theoretical calculations (solid line). Inset: Experimental (squares) and calculated (line)  $\text{Cr}_9$  magnetization per molecule at  $T = 2$  K as a function of the applied magnetic field. All the calculations are obtained with the Hamiltonian in Eq.(1) and  $J = 1.35$  meV and  $g = 1.98$ .

pling  $J = 1.35$  meV. Within this model, the  $\text{Cr}_9$  molecule has a perfect  $C_9$  symmetry and therefore geometrical frustration. Indeed, the lowest-energy multiplets in the spectrum (Fig.3-top panel) are twofold degenerate. In particular, the energy gap between the  $S = 1/2$  ground manifold and the first excited multiplets with  $S = 3/2$  is  $\Delta_{01} = 1.2$  meV. The calculated magnetic field dependence of the low-lying energy levels is displayed in Fig.3.

Irreversible relaxation dynamics in MNMs is caused by the interaction of electronic spins with phonons, behaving like a heat bath. With the formalism of master equations we can describe the time evolution of the molecular observables and the decoherence phenomena induced by electron spin-phonon interactions<sup>26</sup>. Since NMR measurements typically probe only the quasi-elastic spectral contribution to the electronic spin dynamics<sup>26,31</sup>, we focus on the time evolution of the population  $p_s(t)$  of each eigenstate  $|s\rangle$  of (1), given by the master equations:

$$\dot{p}_s = \sum_t W_{st} p_t. \quad (2)$$

$W_{st}$  is an element of the rate matrix  $\mathbb{W}$ , i.e. the probability per unit time that a transition between the eigenstates  $|t\rangle$  and  $|s\rangle$  is induced by the interaction with the phonon heat bath. Here we assume that each magnetic ion experiences a spherically symmetric magneto-elastic coupling with the surrounding atoms. Thus we can write the transition rates as<sup>32</sup>:

$$W_{st} = \gamma^2 \pi^2 \Delta_{st}^3 n_{ph}(\Delta_{st}) \times \sum_{i,j=1}^N \sum_{q_1, q_2=x,y,z} \langle s | O_{q_1, q_2}(\mathbf{s}_i) | t \rangle \langle s | O_{q_1, q_2}(\mathbf{s}_j) | t \rangle^* \quad (3)$$

where  $n_{ph}(x) = (e^{\hbar x/k_B T} - 1)^{-1}$ ,  $\Delta_{st} = (E_s - E_t)/\hbar$

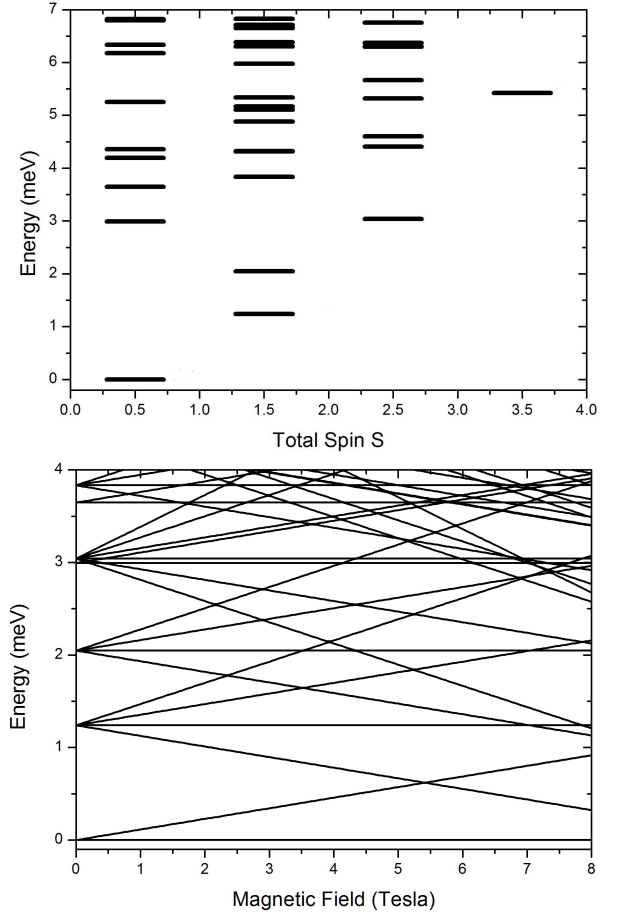


FIG. 3. Top-panel: Spectrum of (1) for  $J = 1.35$  meV and  $B = 0$ . Energy levels are arranged into multiplets of given total spin  $S$  with degeneracy  $2S + 1$ . The lowest total-spin multiplets are degenerate because of frustration. Bottom-panel: Magnetic field dependence of the lowest lying energy levels of  $\text{Cr}_9$ . The ground state energy is set to zero for each value of  $B$ .

and  $O_{q_1, q_2}(\mathbf{s}_i) = (s_i^{q_1} s_i^{q_2} + s_i^{q_2} s_i^{q_1})/2$  are the quadrupolar operators. The coupling strength  $\gamma$  is the only free parameter<sup>33</sup> and it can be determined from NMR experimental data<sup>25,28</sup>.

The study of dynamical correlation functions of the fluctuations of molecular observables  $\mathcal{S}_{\mathcal{P}, \mathcal{Q}}(t) = \langle (\mathcal{P}(t) - \mathcal{P}_{eq})(\mathcal{Q}(t) - \mathcal{Q}_{eq}) \rangle$  allow us to understand the relaxation dynamics of MNMs, where  $\mathcal{P}$  and  $\mathcal{Q}$  are molecular observables defined by spin operators acting on the electronic spins of the system (e.g. magnetization  $\mathcal{M} = \sum_i s_i$ ). In our theoretical framework, the Fourier transform of the correlation function is expressed as a sum of Lorentzians<sup>26</sup>:

$$\mathcal{S}_{\mathcal{P}, \mathcal{Q}}(\omega) = \sum_{i=1}^n A(\lambda_i, T, B) \frac{\lambda_i(T, B)}{\lambda_i(T, B)^2 + \omega^2} \quad (4)$$

( $n$  is the dimension of the Hilbert space). The relaxation rates  $\lambda_i$  are the eigenvalues of  $-\mathbb{W}$  and they are the in-

verse of the characteristic relaxation times  $\tau_{rel}^{(i)} = 1/\lambda_i$ . The weights  $A(\lambda_i, T, B)$  of each rate  $\lambda_i$  are calculated by equations (2) and (3), as explained in Ref.26 and 34.

### III. NMR AS A PROBE OF RELAXATION DYNAMICS

Phonon-induced relaxation dynamics in AF rings is characterized by fast relaxation times  $\tau_{rel}^{(i)}$ , which can be probed by the proton spin-lattice relaxation rate  $1/T_1$ , measured by NMR. In fact, thermal fluctuations of the electronic spins generate fluctuations in the local hyperfine fields at the nuclear sites, causing relaxation of the nuclear spins.  $^1\text{H}$  pulsed NMR experiments are performed on powdered samples of  $\text{Cr}_9$  by means of a HyRe-Spect NMR spectrometer<sup>35</sup>, at several applied magnetic fields and in the temperature range 2 – 100 K. The  $^1\text{H}$  nuclear spin-lattice relaxation rate  $1/T_1$  is determined by monitoring the recovery of the longitudinal nuclear magnetization after the full irradiation of the nuclear absorption line, using a comb of radiofrequency pulses followed by a  $\pi/2 - \pi/2$  solid-echo sequence.

The theoretical model of Section II allows one to interpret also  $^1\text{H}$ -NMR experiments. By the same density matrix formalism used for the electron spin-phonon coupling, we can describe an ensemble of protons in an external static magnetic field, coupled to the perturbative fluctuating field produced by electronic spins. We follow the theory of relaxation processes of Redfield (for further details see Refs.25, 36, and 37) and we calculate the spin-lattice  $\frac{1}{T_1}$  and the spin-spin  $\frac{1}{T_2}$  relaxation rates taking as inputs the positions of the magnetic ions and protons in the molecule:

$$\frac{1}{T_1} = \sum_{\substack{i,j=1,N \\ p,p'=x,y,z}} C_{i,j}^{p,p'} \left[ \mathcal{S}_{s_i^p, s_j^{p'}}(\omega_L) + \mathcal{S}_{s_i^p, s_j^{p'}}(-\omega_L) \right], \quad (5)$$

$$\frac{1}{T_2} = \frac{1}{2T_1} + \sum_{\substack{i,j=1,N \\ p,p'=x,y,z}} K_{i,j}^{p,p'} \left[ \mathcal{S}_{s_i^p, s_j^{p'}}(0) \right], \quad (6)$$

where the  $C_{i,j}^{p,p'}$  and  $K_{i,j}^{p,p'}$  are geometric coefficients of the hyperfine dipolar interaction between magnetic ions and protons<sup>28</sup>.

Since  $\text{Cr}_9$  is a homometallic regular ring,  $\frac{1}{T_1}$  measurements can be used to directly probe the relaxation of the cluster magnetization<sup>26</sup>. Indeed, for each eigenstate  $|t\rangle$   $\langle t|s_i^p|t\rangle = \langle t|s_j^p|t\rangle = \frac{1}{N}\langle t|S_p|t\rangle$ , where  $S_p = \sum_i s_i^p$  is the  $p$  component of the *total* spin operator. Then 5 and 6 become

$$\frac{1}{T_1} = \sum_{p,p'=x,y,z} G_{p,p'} \left[ \mathcal{S}_{S_p, S_{p'}}(\omega_L) + \mathcal{S}_{S_p, S_{p'}}(-\omega_L) \right], \quad (7)$$

$$\frac{1}{T_2} = \frac{1}{2T_1} + \sum_{p,p'=x,y,z} J_{p,p'} \left[ \mathcal{S}_{S_p, S_{p'}}(0) \right], \quad (8)$$

where the  $G_{p,p'}$  and  $J_{p,p'}$  are geometrical coefficients depending only on the positions of the spins and of the probed nuclei<sup>38</sup>.

### IV. NMR RESULTS

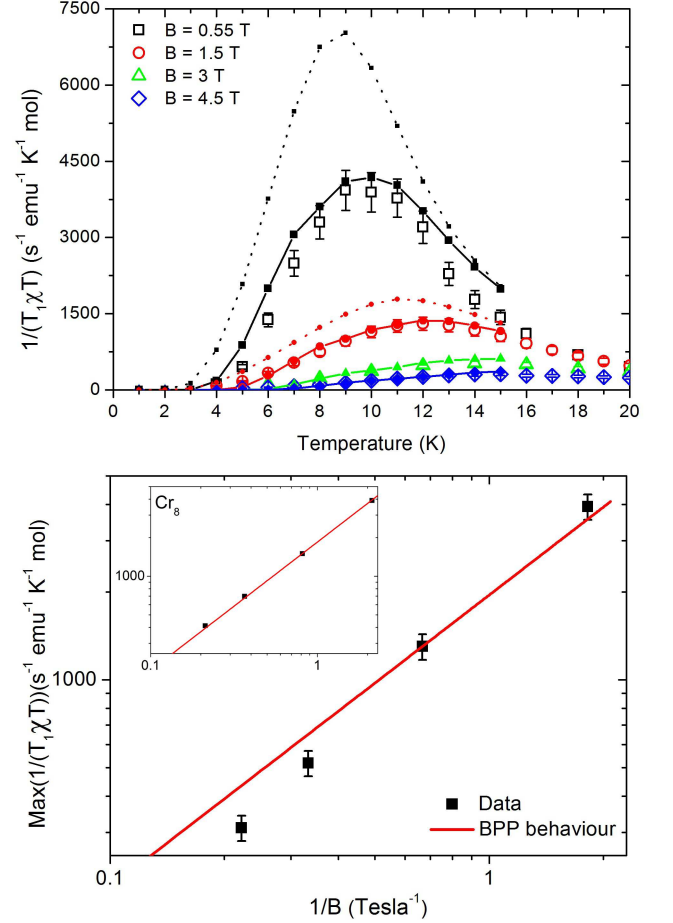


FIG. 4. Top panel:  $^1\text{H}$  NMR  $(1/T_1)/(\chi T)$  data on  $\text{Cr}_9$  powders as a function of temperature at four different applied magnetic fields (scatter) and calculations exploiting equation (5) and taking into account the wipeout effect (line&scatter). Dashed-line&scatter for  $B = 0.5$  T and  $B = 1.5$  T represent calculations of  $(1/T_1)/(\chi T)$  with no wipeout effect. Bottom panel: Experimental height of the peaks of  $(1/T_1)/(\chi T)$  of  $\text{Cr}_9$  for the four different values of the inverse magnetic field (scatter), compared with the BPP behaviour, determined by taking as a reference the data at  $B = 1.5$  T (solid line). Inset: Experimental peaks of  $(1/T_1)/(\chi T)$  for  $\text{Cr}_8$ <sup>31</sup>, compared with the BPP behaviour, determined by taking as a reference the data at  $B = 1.23$  T.

The temperature-dependence of the spin-lattice relaxation rate  $1/T_1$  is shown in Fig.4, normalized to  $\chi T$ , which is proportional to the size of equilibrium fluctuations.  $(1/T_1)/(\chi T)$  displays a peak at 10 K when  $B = 0.55$  T, which lowers and moves to higher tem-



peratures by increasing the field. The bottom panel of Fig.4 shows that Cr<sub>9</sub> deviates from the Bloembergen Purcell Pound (BPP) behavior, i.e., the height of the peaks in  $(1/T_1)/(\chi T)$  for different values of  $B$  does not scale exactly as  $1/B$ . The BPP behavior has been observed in the even-numbered homometallic ring Cr<sub>8</sub> (see inset of Fig.4) and other nanomagnets<sup>26,31</sup>, whose dynamics is characterized by a single dominating relaxation rate  $\lambda_0$ . Hence, this suggests the presence of more than one relevant relaxation frequency in the temperature range where  $(1/T_1)/(\chi T)$  displays a peak, even if Cr<sub>9</sub> is homometallic. The origin of the peak in the temperature-dependence of  $(1/T_1)/(\chi T)$  can be understood by using (4) to rewrite the Fourier transforms of the correlation functions at the Larmor frequency  $\mathcal{S}_{S_p, S_p}(\pm\omega_L)$  of Eq.(7). As mentioned above, in the case of homometallic AF rings only a single lorentzian dominates the sum in Eq.(4)<sup>26,31</sup> and  $(1/T_1)/(\chi T)$  displays a peak at the temperature at which the relaxation rate of this lorentzian matches  $\omega_L$ . If the relaxation dynamics is not mono-lorentzian but the different relevant rates are close to one another when they approach  $\omega_L$ , we have again a single-peak in the  $(1/T_1)/(\chi T)$ <sup>25,28</sup>. Thus, Cr<sub>9</sub> NMR data point to this second situation.

Experimental data are interpreted within the theoretical framework illustrated in II and III. By fitting the position of the peak in temperature, it is possible to determine the spin-phonon coupling strength  $\gamma$ . The presence of a peak at 10 K in the  $(1/T_1)/(\chi T)$  curve of Cr<sub>9</sub> with  $B = 0.55$  T yields  $\gamma = 4 \times 10^{-4}$  THz<sup>-1</sup>. With the same  $\gamma$  it is possible to reproduce the position and height of the peaks of  $(1/T_1)/(\chi T)$  also for the other values of  $B$  (1.5, 3 and 4.5 T). Thus, we obtain a good overall quantitative agreement between data and calculations (Fig. 4), in spite of the complexity of the NMR technique applied to this kind of systems. Furthermore, the value of  $\gamma$  found for Cr<sub>9</sub> is similar to that of other related AF ring like Cr<sub>7</sub>Ni and Cr<sub>8</sub> ( $\gamma = 2.8 \times 10^{-4}$  THz<sup>-1</sup>)<sup>28</sup>. Since measurements have been made on powders, to reproduce the experimental data we average over all the possible orientations of the applied magnetic field. To reduce the computational effort in the diagonalization of the rate matrix  $\mathbb{W}$ , it is necessary to truncate the molecule Hilbert space. The reduction to the subspace spanned by the total-spin manifolds up to 150 K allows us to reproduce the temperature dependence of  $(1/T_1)/(\chi T)$  in the most interesting region, i.e. where it displays a peak, up to  $T = 15$  K. Anyway this truncation leads to a slight overestimate of the calculated  $(1/T_1)/(\chi T)$  with respect to the corresponding experimental values for  $T > 12$  K<sup>39</sup>.

<sup>1</sup>H NMR measurements are often affected by the so-called wipeout effect. It consists of a signal loss in the NMR signal intensity, due to the enhancement of the transverse relaxation rates  $1/T_2$  of the protons over the limit fixed by the experimental setup (around  $67 - 100$  (ms)<sup>-1</sup> in our experimental conditions, corresponding to  $T_2 \sim 10 - 15$   $\mu$ s)<sup>30</sup>. Thus, to calculate the spin-lattice relaxation rate of Cr<sub>9</sub> we take into account also the wipeout effect. For

each hydrogen we calculate  $1/T_1$  and  $1/T_2$  as a function of the temperature, the orientation and the modulus of the applied magnetic field with (7) and (8). Then we retain only the hydrogen nuclei whose transverse relaxation rate is lower than the above-mentioned threshold. In order to obtain the  $(1/T_1)/(\chi T)$  curves of Cr<sub>9</sub> in Fig.4, we set  $1/T_2^{thresh} = 81.7$  (ms)<sup>-1</sup>, corresponding to  $T_2^{thresh} = 12.2$   $\mu$ s. This approach has already been applied to reproduce the wipeout effect in the Fe<sub>7</sub> cluster, yielding very good results<sup>25</sup>. Furthermore, the comparison between experimental data and calculations of  $(1/T_1)/(\chi T)$  performed retaining all the protons in the molecule (dashed line&scatter in Fig.4-top panel) shows the extent of the signal loss due to the wipeout effect, which is, as expected, stronger at low fields. Thus, we can conclude that the wipeout effect is a crucial ingredient in the interpretation of <sup>1</sup>H NMR experimental data.

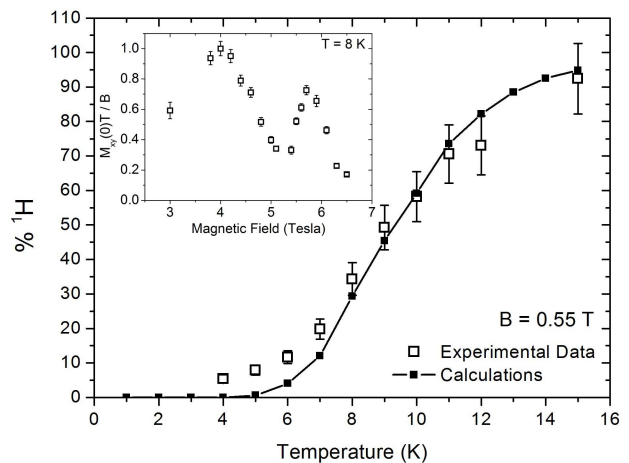


FIG. 5. Fraction of protons probed by NMR (black) deduced by the initial transverse nuclear magnetization at  $B = 0.55$  T and  $B = 1.5$  T (see Section III) compared with fraction of protons taken into account in our calculations (red&blue) determined as described in Section IV. Inset: Renormalized transverse nuclear magnetization  $M_{xy}^H(0)T/B$  as a function of the applied magnetic field  $B$  at  $T = 8$  K. Data have been also renormalized so that the maximum value of the magnetization in the explored magnetic fields range is set to 1.

As a test, we have also measured the transverse nuclear magnetization  $M_{xy}^H(0)$ , obtained by the extrapolation at zero time of the transverse nuclear magnetization  $M_{xy}^H(t)$  recovery curve. The quantity  $M_{xy}^H(0)T$ , where  $T$  is the temperature, is proportional to the number of protons resonating at the irradiation frequency. Transverse nuclear magnetization measurements as a function of temperature have been performed at  $B = 0.55$  T since wipeout is generally stronger at small fields (see also Fig.4-top panel).  $M_{xy}^H(0)T$ , and thus the number of probed protons, decreases by lowering the temperature due to the wipeout effect<sup>30</sup>. In Fig. 5 we compare the number of protons in Cr<sub>9</sub> probed by NMR measurements with the number of <sup>1</sup>H nuclei included in our calculations by the

method described above. The graph shows that with our calculations it is possible to reproduce the wipeout effect, confirming the reliability of our model.

The bottom panel of Fig.3 shows that we predict a level crossing between the first and the second excited levels of  $\text{Cr}_9$  at about 5.4 T. At the level crossings there is a strong increase of both  $1/T_1$  and  $1/T_2$  due to inelastic contributions to the relaxation dynamics, thus we expect a strong wipeout effect<sup>40</sup>. We have therefore measured  $M_{xy}^H(0)T$  as a function of the applied magnetic field at  $T = 8$  K, in order to populate the lowest excited levels involved in the crossing. Experimental data are shown in the inset of Fig.5. As expected, the transverse nuclear magnetization displays a minimum between 5 and 5.5 T, indicating a strong wipeout effect and confirming the level crossing field.

## V. RELAXATION DYNAMICS

From the analysis of the NMR data we have determined the unique free parameter in Eq. 3, the electron spin-phonon coupling strength  $\gamma$ . Thus, we can investigate the relaxation dynamics of the  $\text{Cr}_9$  cluster by studying the spectrum of fluctuations of the cluster magnetization  $M$  with equation (4) ( $\mathcal{P} = \mathcal{Q} = M = \sum_i s_i$ ). Figure 6 report the calculated weight  $A(T, B; \lambda_i)$  of the characteristic relaxation rates  $\lambda_i$  of the autocorrelation of  $M$  (see equation (4)), as a function of the inverse temperature. It is worth to stress that  $\gamma$  merely fixes the relaxation timescale (a variation of  $\gamma$  only produces rigid vertical shifts in Fig.6). Between 2 K and 20 K the relaxation rates  $\lambda_i(T)$  are roughly in the range between  $10^{-8}$  -  $10^{-3}$  THz. Figure 6 shows that the decay of magnetization in  $\text{Cr}_9$  is characterized by a single time only for very low temperatures, even for small applied fields. Indeed, above  $T \simeq 3$  K several relevant relaxation rates emerge. In particular, in the temperature range  $10 \lesssim T \lesssim 15$  K, where the relaxation rates intersect the proton Larmor frequencies  $\omega_L$  (see the red lines in Figs.6), there are several rates with an appreciable weights, but close to one another. This explains why a single peak in the  $(1/T_1)/(\chi T)(T)$  is observed in spite of the multi-time relaxation dynamics. Only below  $T \simeq 3$  K there is a single relaxation process, whose  $T$ -dependence follows the Arrhenius law.

We have analyzed the dominant relaxation processes by inspecting the eigenvectors and the matrix elements of  $\mathbb{W}$ . In fact, the former give information about the starting and the final states of the processes and the latter are the transition probabilities. In small fields (Fig. 6) the dominant relaxation rates for  $T \lesssim 3$  K involve levels of the two degenerate  $S = 1/2$  ground doublets and of the second excited  $S = 3/2$  multiplets with  $E = 23.7$  K (see Fig. 7, blue arrow). They correspond to an Orbach process<sup>41</sup> following the Arrhenius law with an energy barrier  $\Delta/k_B \approx 24$  K, which is the dominant one up to  $T \cong 7$  K. At about  $T = 3$  K there is a second rate whose weight

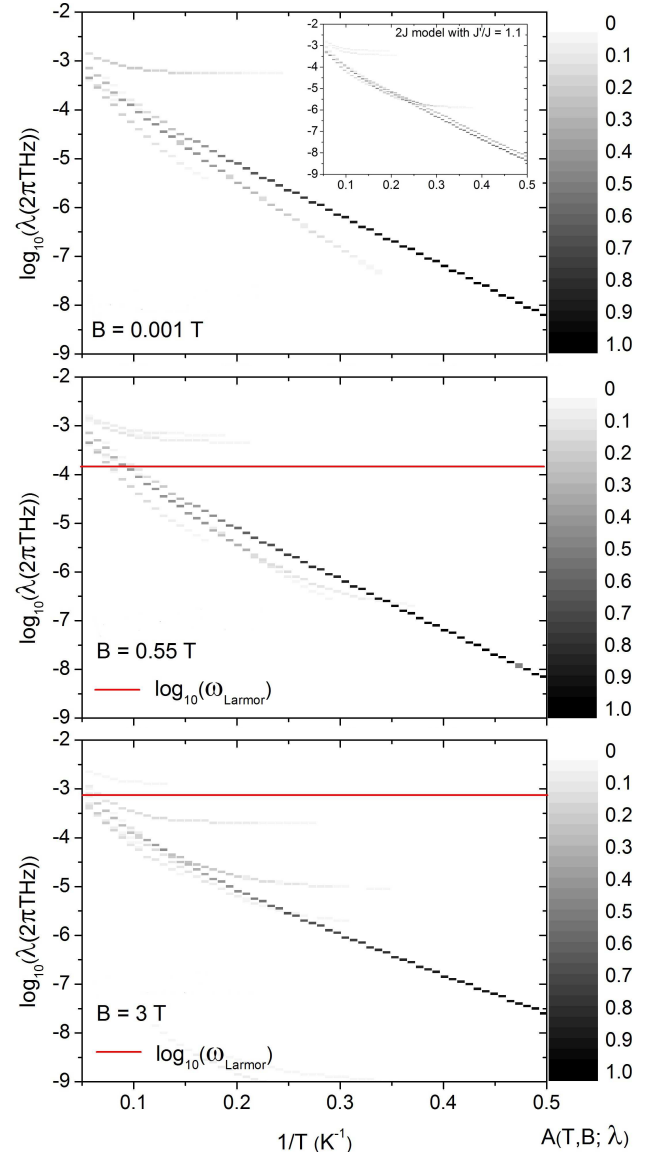


FIG. 6. Intensity plot showing the calculated weights  $A(T, B; \lambda_i)$  of the magnetization autocorrelation versus  $1/T$  (x axis) for  $B=0.001$  T,  $B = 0.55$  T and  $B = 3$  T respectively. The y axis is  $\log_{10}(\lambda_i)$  (in  $2\pi\text{THz}$ ). The plot maps  $A(T, B; \lambda_i)/\chi T$ , i.e. for each value of  $T$  the spectra have been normalized by  $\chi T$ , which is proportional to the size of equilibrium fluctuations. When the rates  $\lambda_i$  with significant weight intersect  $\omega_L$  (red line),  $1/T_1$  displays a peak (see Fig. 4). Inset: Intensity plot of the calculated weights  $A(T, B; \lambda_i)$  versus  $1/T$  for  $B=0.001$  T obtained with a 2J model Hamiltonian with  $J'/J = 1.1$ .

becomes relevant in the relaxation dynamics, corresponding to a process from the two degenerate first excited multiplets with  $S = 3/2$  and  $E = 14.4$  K towards higher excited levels with  $S = 1/2$  and  $S = 5/2$ . At higher temperatures ( $T > 7$  K, close to the  $1/T_1$  peak temperature), these processes become the dominant ones (red arrows in Fig. 7). The presence of an applied magnetic field (see

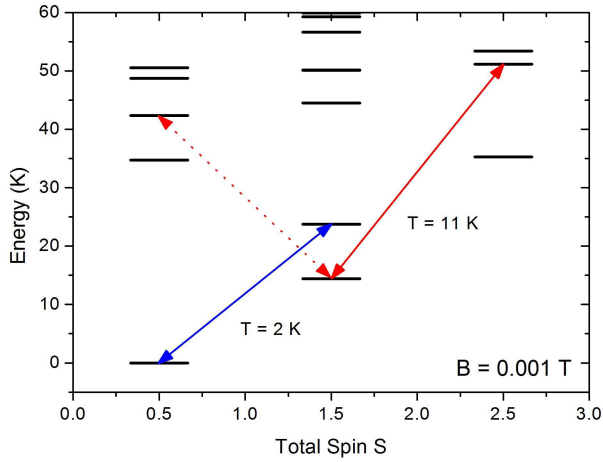


FIG. 7. Relaxation paths corresponding to the dominant relaxation rates  $\lambda_i$  of  $\text{Cr}_9$  with  $B \rightarrow 0$  in the low-temperature regime ( $T = 3.6$  K, blue arrows) and with  $T = 11.2$  K (red arrows).

Figs. 6) leads to a faster relaxation, especially at low  $T$ . Anyway, the dynamics still have a multiple-times character above 3 K and the relevant relaxation paths always involve the same total-spin multiplets, even if split by the Zeeman interaction.

By comparing the relaxation dynamics of  $\text{Cr}_9$  with that of the even-membered parent compound  $\text{Cr}_8$ <sup>26</sup>, we find that both clusters are characterized by one dominating Arrhenius process at low temperatures, but in  $\text{Cr}_9$  additional relaxation processes emerge at significantly lower temperatures than in  $\text{Cr}_8$ . In addition, within the present model the relevant relaxation rates  $\lambda_i(T)$  in  $\text{Cr}_9$  are twofold-degenerate, reflecting the symmetry of Eqs. 1 and 3. These degeneracies are in fact a peculiar characteristic of highly symmetrical frustrated MNMs. For instance, the relaxation dynamics of the frustrated  $\text{Ni}_7$  cluster displays a band of almost degenerate and equally weighted frequencies<sup>24</sup>. These degeneracies can be lifted by reducing the symmetry of the  $\text{Cr}_9$  molecule. For instance, by assuming that one Cr-Cr bond is different from the others and thus introducing a different exchange coupling  $J' = 1.1J$  for this bond, the cluster is still characterized by competing AF interactions, but the degeneracy of the energy levels is removed. In this case the relaxation dynamics is dominated by two distinct rates even at low temperature (see Inset of Fig.6), showing the typical behavior of a cluster with competing AF interactions. For instance, in the  $\text{Fe}_7$  double-pyramid cluster, which is characterized by many competing AF interactions, we indeed found a multiple-time scale relaxation dynamics at low temperatures<sup>25</sup>. A lifting of these degeneracies would also result from a less symmetric form of the magneto-elastic coupling. Such a coupling would also lead to sizeable transition probabilities between the ground manifold and the lowest-energy  $S = 3/2$  multiplet, resulting in faster relaxation at very low temperatures. Yet, there

is no indication in the present data of a less symmetric model than the one assumed.

The degeneracy between the two  $S = 1/2$  ground

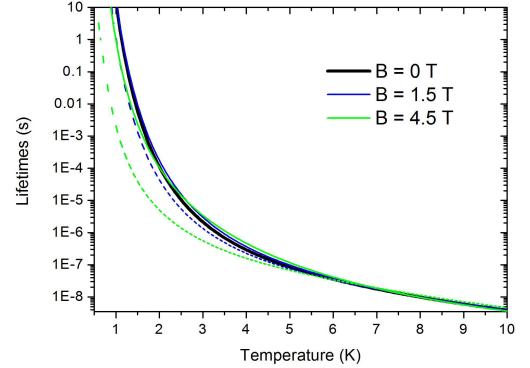


FIG. 8. Calculated temperature-dependence of the lifetime of the levels of the two  $S = 1/2$  ground doublets for several values of the applied magnetic field. Continuous and dashed lines correspond to  $|S = 1/2, M = -1/2\rangle$  and  $|S = 1/2, M = 1/2\rangle$ , respectively.

multiplets and the corresponding perfect frustration is expected to be slightly broken at low temperature because of the Jahn-Teller theorem. A very interesting experiment would be to exploit high-resolution four-dimensional inelastic neutron scattering<sup>42</sup> to study the low-energy peak corresponding to the transition between the two nearly degenerate  $S = 1/2$  multiplets. Indeed, the dependence of the intensity of this peak over the momentum transfer vector would yield direct information on how the frustration is removed and on the associated low-frequency quantum dynamics. The spin dynamics associated with this low-energy peak will be damped on a time-scale depending on the average of the lifetimes of the involved levels. Hence, we use the here-determined model of the magnetic relaxation of  $\text{Cr}_9$  to calculate the effect of spin-phonon interaction on the lifetimes of the lowest-energy levels<sup>26</sup>. Figure 8 reports the calculated temperature-dependence of the lifetime of the ground  $S = 1/2$  manifold for several values of the magnetic field. At low temperature the lifetime is very long, making the previously mentioned experiment very promising if large high-quality crystals become available. It is worth to add that direct transitions between the two  $S = 1/2$  doublets should not strongly limit the lifetimes, because of the small phonon density associated with a very small energy gap. In addition, Figure 8 shows that level lifetimes can be also controlled by applying an external magnetic field.

We have also studied the effects of anisotropy on the relaxation properties of  $\text{Cr}_9$ , by adding a small axial zero-field splitting term to the spin Hamiltonian in (1)<sup>43,44</sup>. We choose a typical value for the zero-field splitting parameter  $d_{Cr} = -0.03$  meV, as the one found in  $\text{Cr}_8$ <sup>6-8,42</sup>. The energy levels remain twofold-degenerate and thus we still find a pair of degenerate  $S = 1/2$  doublets as ground



state. We have found that the effect of anisotropy on relaxation is negligible<sup>45</sup>. In particular, the  $1/T_1$  curves calculated with anisotropy are very similar to those in the lack of anisotropy, provided the wipeout threshold is reduced from  $T_2^{thresh} = 12.2 \mu$  to  $T_2^{thresh} = 11.7 \mu$ , still within the dead-time interval fixed by the experimental setup. Thus, NMR data can be equally well reproduced with or without the anisotropy term. We have also verified that this term does not affect the relaxation dynamics, as we found find the same temperature- and field-dependence of the characteristic relaxation rates, which are still twofold degenerate.

## VI. CONCLUSIONS

We have investigated the magnetic properties and relaxation dynamics of the first regular  $\text{Cr}_9$  AF ring, which represents a prototype of practically degenerate-frustrated homometallic ring of half-integer spins. The energy spectrum of this kind of systems is characterized by a two-fold degeneracy of the low-energy total-spin multiplets. The relaxation of  $\text{Cr}_9$  has been investigated by measuring the temperature and magnetic field dependence of the spin-lattice relaxation rate  $1/T_1$  of  $^1\text{H}$  nuclei. The experimental results have been interpreted by a microscopic model including magnetoelastic couplings and

taking into account the wipeout effect. This model has allowed us to reproduce satisfactorily the experimental results and to study the phonon-induced decay of molecular magnetization. While magnetic relaxation of bipartite rings is well known, this is the first investigation of an odd-membered AF ring.

We have found that in  $\text{Cr}_9$  the relaxation dynamics is characterized by a single Arrhenius time only at very low temperatures, whereas above 3 K several relevant relaxation rates emerge. In addition, the model predicts the temperature and magnetic field dependence of level lifetimes, which are important for the feasibility of a neutron scattering experiment to directly probe the quantum dynamics resulting from the expected ultimate removal of frustration.

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