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Superconductivity in metastable phases of phosphorus-hydride compounds under high pressure

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Hydrogen-rich compounds have been extensively studied both theoretically and experimentally in the quest for novel high-temperature superconductors. Reports on sulfur-hydride attaining metallicity under pressure and exhibiting superconductivity at temperatures as high as 200 K have spurred an intense search for room-temperature superconductors in hydride materials. Recently, compressed phosphine was reported to metallize at pressures above 45 GPa, reaching a superconducting transition temperature (T_C) of 100 K at 200 GPa. However, neither the exact composition nor the crystal structure of the superconducting phase have been conclusively determined. In this work the phase diagram of PH_n ($n = 1, 2, 3, 4, 5, 6$) was extensively explored by means of *ab initio* crystal structure predictions using the Minima Hopping Method (MHM). The results do not support the existence of thermodynamically stable PH_n compounds, which exhibit a tendency for elemental decomposition at high pressure even when vibrational contributions to the free energies are taken into account. Although the lowest energy phases of $\text{PH}_{1,2,3}$ display T_C 's comparable to experiments, it remains uncertain if the measured values of T_C can be fully attributed to a phase-pure compound of PH_n .

PACS numbers:

In December 2014, Drozdov *et al.* reported a superconducting critical temperature (T_C) of 203 K in an ultra-dense phase of sulfur-hydride (SH_3)¹, identified by *ab initio* crystal structure searches², breaking the record- T_C previously held by the cuprates. Subsequent experimental and theoretical studies have confirmed that superconductivity is of conventional nature and occurs in the predicted bcc phase^{1,3}, demonstrating the potential of *ab-initio* crystal structure search methods to identify new superconductors. Several studies have meanwhile appeared in literature, discussing different aspects underlying the exceptional T_C , such as the role of bonding, Coulomb screening, phonon anharmonicity, etc.^{4–11}.

High- T_C superconductivity based on a conventional electron-phonon (*ep*) coupling mechanism has been suggested by Ashcroft almost fifty years ago. He originally proposed that this could be achieved if hydrogen was sufficiently compressed, a prediction that has not yet been verified due to the required extreme pressures^{12–17}. More recently, he suggested that the chemical pre-compression of hydrogen in hydrogen-rich compounds could be an effective route to reach metallization and high- T_C superconductivity at experimentally accessible pressures¹⁸, stimulating an intense activity of *ab initio* searches and predictions for high- T_C superconducting hydrides^{2,19–31}. Until 2014, however, all high-pressure phases which have been synthesized experimentally exhibited rather low T_C ^{32–35}.

Eventually, the discovery of SH_3 showed that high- T_C in hydrogen-rich solids can indeed be achieved. Thus, all stable hydrogen-containing molecules which can be placed into the compressing chamber of a diamond anvil

cell are potential candidates for high- T_C superconductors, as long as they remain stable against decomposition, amorphization, and the possible formation of metal-hydrides during the measurement of T_C ^{32–35}.

In fact, less than one year after the discovery of superconductivity in SH_3 , Drozdov *et al.* have very recently reported high- T_C superconductivity in a second hydrogen-rich compound at extreme pressures: resistivity measurements on phosphine (PH_3) show that the samples, which are semiconducting at ambient pressure, metallize above 40 GPa and become superconducting at around 80 GPa, exhibiting a maximum T_C of 100 K at about 200 GPa³⁶. Neither the exact composition of the superconducting phase and its crystal structure, nor the mechanism responsible for the high- T_C have been conclusively determined at this point. Analogies with superconducting SH_3 , which was obtained from SH_2 precursor, suggest that the superconductivity in the P-H system is of conventional nature, but that the composition of the superconducting phase might be different from the original PH_3 stoichiometry.

To shed light on this matter we used *ab initio* techniques to map out the high-pressure phase diagram of the P-H binary system by exploring the compositional and configurational space of PH_n with a sophisticated structure prediction method, and estimated the superconducting properties of the most promising phases. We found that all high-pressure binary phases of P and H are metastable with respect to elemental decomposition in the pressure range 100–300 GPa. However, the critical temperatures of the three phases closest to the convex hull (PH , PH_2 and PH_3) reproduce to a good approx-

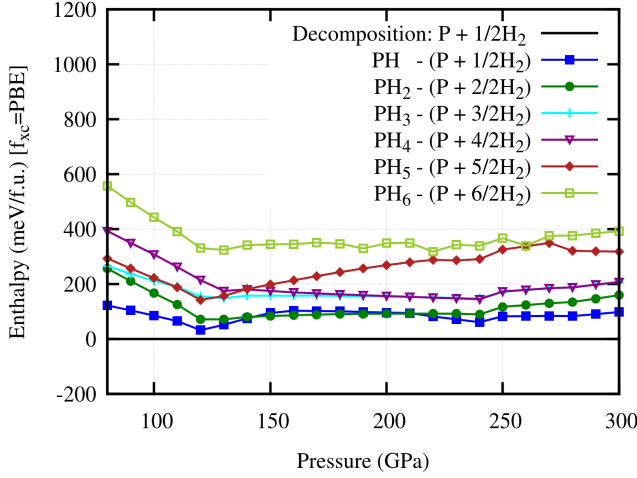


Figure 1. (Color online) Calculated enthalpies for PH_n ($n = 1, 2, 3, 4, 5, 6$) for the low-lying structures found in this work. Values are given with respect to the elemental decomposition ($\text{P} + 1/2\text{H}_2$). The reference structures for hydrogen are $\text{P6}_3\text{m}$ (0-120 GPa) and $\text{C2}/c$ (120-300 GPa) from Ref.³⁷. The reference phases for phosphorus are: $\text{Pm}\bar{3}\text{m}$ (0-10 GPa), R3m (20-110 GPa), P6mm (120-240 GPa), $\text{Im}\bar{3}\text{m}$ (250-270 GPa) and $\text{I}\bar{4}3d$ (280-300 GPa). The change in slope at around 120 GPa is due to the phase transition in elemental hydrogen.

imation the experimental T_C values. Possible ways to reconcile our results with experiments are discussed at the end of this manuscript.

To sample the enthalpy landscape we employed the Minima Hopping method (MHM)^{38,39}, which has been successfully used for global geometry optimization⁴⁰ in a large variety of applications^{41–43}, including superconducting materials at high pressure^{6,31}. The enthalpies as a function of pressure for the ground state structures⁴⁴ at each composition are shown in Fig. 1 with respect to elemental decomposition. The ground state structures were determined by the MHM at 100, 150, 200 and 300 GPa, and further relaxed at intermediate pressures to obtain a smooth phase diagram. An additional search was carried out at zero pressure. The various phases of pure H and P for the convex hull construction were obtained from a structural search, and for hydrogen they coincide with the ones reported by Needs *et al.*³⁷: $\text{P6}_3\text{m}$ (0-120 GPa) and $\text{C2}/c$ (120-300 GPa). The complex phase diagram of elemental phosphorus^{45,46}, with at least six structural transition between 0 and 300 GPa, is closely reproduced by our calculations - see supplemental Material. At zero pressure, molecular phosphine (PH_3), as well as the crystalline phases of PH, PH_2 and PH_3 identified by our MHM runs, are all stable with respect to elemental decomposition (see supplemental materials). Moreover, we found two compositions (PH and PH_3) forming the convex hull with enthalpies of formation between -50 and -60 meV/atom. In the crystalline phases, the molecules retain their geometry and are held together by van-der-Waals interactions; these molecular crystals are

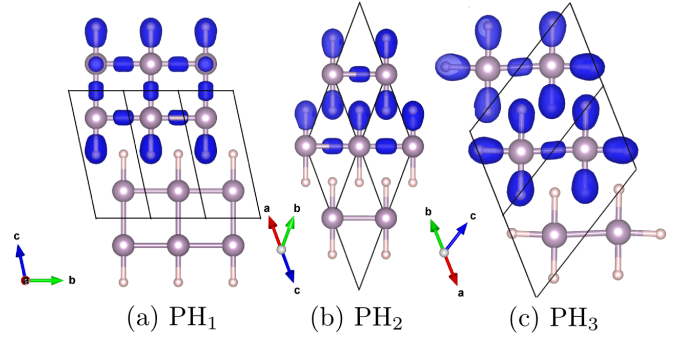


Figure 2. (Color online) Low-lying enthalpy structures found for different compositions under pressure at 120 GPa. The large and small spheres denote the P and H atoms, respectively. The ELF at a fixed value of 0.8 is shown in the upper part of each structure.

semiconducting with gaps of 0.9 (PH), 2.1 (PH_2) and 3.7 eV (PH_3 , respectively). Given the complexity of the phase diagram of elemental phosphorus, it is likely that binary phases considered here will undergo several phase transitions between ambient pressure and 100 GPa, but analyzing these transitions is well beyond the scope of this work. Assuming that the PH_3 zero-pressure structure is representative at higher pressures, we estimate a metallization pressure of ~ 35 GPa, which is in accordance with experiments - see supplemental materials for details.

In the following, we will focus on high pressures (80-200 GPa), which are relevant for superconductivity. The formation enthalpies of all the identified structures are positive and in a range of 30-200 meV/f.u. for hydrides with low hydrogen contents (PH, PH_2 and PH_3), and larger for higher H content up to PH_6 .

The ground state structures at 120 GPa of pressure for PH ($\text{I4}/mmm$), PH_2 ($\text{I4}/mmm$) and PH_3 ($\text{C2}/m$) are shown in Fig. 2. The bond lengths are ~ 1.4 Å for the P-H bonds and ~ 2.1 Å for the P-P bonds in all three structures. Figure 2 clearly shows the dominating tendency of P atoms to form polymers with hydrogen saturating the dangling bonds, resulting in 1D chains or 2D layers. This picture is confirmed when looking at the iso-surfaces of the electron localization function (ELF), clearly showing that electrons are localized to form P-P and P-H bonds. No or only weak interactions are observed between the polymeric chains, which is in strong contrast to other hydrogen-rich materials that are stable against decomposition and exhibit a 3D network of strongly interacting host atoms and hydrogen^{31,47}. With increasing hydrogen content the dimensionality of the polymers decreases from layers and sheets (PH, PH_2) to chains (PH_3 , PH_4), until over-saturation is reached and H_2 molecules precipitate, intercalating the P-H polymers in PH_5 and PH_6 .

Fig. 1 shows that, although none of the binary phases are thermodynamically stable, some lie very close to the convex hull at around 120 GPa. Therefore, an in-depth

investigation was conducted to assess whether effects going beyond those included in our MHM searches could stabilize any of these phases in the range between 100 and 150 GPa.

A detailed analysis of the phase stability at 120 GPa is shown in Fig. 3. We first investigated how the use of different exchange-correlation functionals influences the stability of the various compounds. PBE values are shown as black triangles in Fig. 3. In the local density approximation (not shown) we obtain fairly similar phase stabilities. We also report results obtained by means of the more demanding Heyd-Scuseria-Ernzerhof (HSE) hybrid functional^{48–51}. Although hybrids are considered to give better results than semilocal functionals for structural and electronic properties in semiconductors⁴⁹ and intermetallic alloys⁵², they have not been systematically validated for metallic systems, where severe anomalies in the lattice stability and electronic properties have been recently reported⁵³. The HSE results, plotted as green squares in Fig. 3, show nevertheless a similar trend as obtained with PBE and LDA. HSE predicts slightly higher formation enthalpies than PBE for PH, PH₂, PH₃ and PH₆, and lower values for PH₄ and PH₅. Finally, the semi-empirical DFT-D2 method of Grimme⁵⁴, which takes into account van-der-Waals interactions, consistently predicted a lower stability of the binary phases compared to PBE. The positive formation enthalpies predicted by all four exchange-correlation functionals strongly suggest that none of the binary PH_n phases are in fact thermodynamically stable.

Next, we investigated the influence of vibrational entropy and zero-point energy (ZPE) on the phase stability. Phonon calculations were carried out with the frozen phonon approach as implemented in the PHONOPY package⁵⁵ with sufficiently large super-cells. The ZPE and free energy within the harmonic approximation at temperatures of 100, 200, 300 and 400 K are shown as colored gradients in Fig. 3. There is a clear distinction in the vibrational effect on the stability for PH_n-phases with high and low hydrogen content: PH, PH₂ and PH₃ increase in stability, whereas PH₄ and PH₅ decrease. This behavior can be attributed to the existence of H₂ molecules in the crystal lattice of the hydrogen-rich phases which induce high-energy vibrational modes responsible for an increased ZPE.

For PH, formation energy is less than 5 meV/atom at 0 K, whereas for PH₂ and PH₃ it is about 7 meV/atom and 30 meV/atom, respectively. Comparing the free energies at finite temperatures reveals that all phases are destabilized by vibrational entropy by a few meV, pushing them away from the convex hull with increasing temperature. Since anharmonic effects become increasingly important at higher temperatures we recomputed the free energy for PH, PH₂ and PH₃ within the quasi-harmonic approximation, taking into account the thermal lattice expansion. These calculations, however, showed only minor effects on the stabilities and the distance from the convex hull of all three binary phases slightly increased

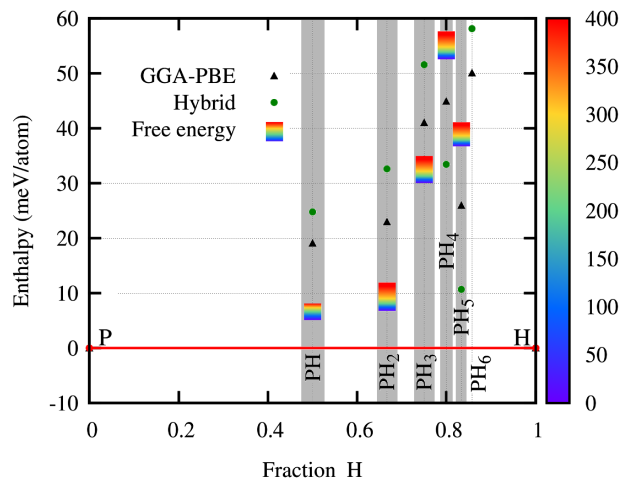


Figure 3. (Color online) Predicted formation enthalpies of PH_n with respect to decomposition into P and H at 120 GPa. The solid red line denotes the convex hull of stability. Black triangles show PBE and green squares hybrid functional values (HSE06). The color-gradient scale indicate the free-energy within the harmonic approximation at temperatures up to 400 K (colorbar in Kelvin on the right) as computed on top of PBE energies.

by a few meV per atom.

Having ruled out that any of the standard corrections to the electronic enthalpy can stabilize our phases in the experimentally relevant regime, we are left with the question of which phase and chemical composition was experimentally observed by Drozdov *et al.* We can rule out that the superconductivity observed is due to some residual elemental phase, as hydrogen is not metallic at these pressures and elemental phosphorus displays much lower critical temperatures⁵⁶, not higher than a few Kelvin.

On the other hand, our phonon calculations show that the ground states at fixed compositions of PH₁, PH₂ and PH₃ are all dynamically stable, i.e. with no imaginary modes in the whole Brillouin zone. Therefore, one of these metastable phases might have been synthesized through a non-equilibrium process or possibly through anisotropic stress in the anvil cell, as the order of magnitude of the relevant energy barriers in these cases could be in the range of few tens of meV. In fact, the compositions closest to the hull are PH and PH₂, indicating a possible decomposition of the original phosphine molecules (PH₃) under pressure into PH and PH₂, similarly to what is observed in sulfur-hydrides where the initial, molecular SH₂ decomposes under pressure to form SH₃.

To assess whether any of these three metastable phases could be a reasonable candidate for superconductivity, we calculated the Eliashberg spectral functions for the electron-phonon (*ep*) interaction:

$$\alpha^2 F(\omega) = \frac{1}{N_{EF}} \sum_{\mathbf{k}\mathbf{q},\nu} |g_{\mathbf{k},\mathbf{k}+\mathbf{q},\nu}|^2 \delta(\epsilon_{\mathbf{k}}) \delta(\epsilon_{\mathbf{k}+\mathbf{q}}) \delta(\omega - \omega_{\mathbf{q},\nu}), \quad (1)$$

where N_{E_F} is the DOS at the Fermi level, $\omega_{\mathbf{q},\nu}$ is the phonon frequency of mode ν at wavevector \mathbf{q} and $|g_{\mathbf{k},\mathbf{k}+\mathbf{q},\nu}|$ is the electron-phonon matrix element between two electronic states with momenta \mathbf{k} and $\mathbf{k} + \mathbf{q}$ at the Fermi level.

From the Eliashberg function we also obtained the electron-phonon coupling constant λ and the logarithmic average phonon frequency ω_{\log} ^{57,58} (which, in the McMillan-Allen-Dynes parametrization for T_C , sets the energy scale for the phononic pairing). In order to avoid using the empirical μ^* parameter and bias the theoretical predictions towards the experiments, we compute the critical temperatures within density functional theory for superconductors (SCDFT), which uses as input the Eliashberg function in an isotropic approximation, while the residual Coulomb forces in the Cooper pairing are included within the static random phase approximation^{59–62}, as used in Ref. 6 and 63.

The values of T_C are shown in Fig. 4 and are compared to the experimental values reported by Drozdov *et al.*³⁶. In the two right panels of the same figure we show λ and ω_{\log} for the three phases as a function of pressure⁶⁴.

Our calculated behavior of T_C with respect to pressure shows a fair agreement with experiments for all three structures (PH, PH₂ and PH₃); The best agreement is found for PH₂, which has a T_C of 40 K at 100 GPa that increases under pressure and reaches a maximum value of 78 K at 220 GPa. The PH system shows the best agreement in the rate at which T_C grows with pressure in the 120-260 GPa window ($dT_C/dP \simeq 0.4(K/GPa)$), while showing a high pressure shift of about 20 GPa with respect to the experimental data.

The similar superconducting behavior of the three compounds results from the compensation of different behaviors of λ and ω_{\log} , shown in the right panels of the same figure. These reflect different features of the three Eliashberg functions, shown in Fig. 5, together with that of SH₃ for reference. The PH_{1,2,3} spectra have an overall similar shape, *i.e.* they are roughly proportional to the phonon density of states, dominated by P modes at low frequencies (< 80 meV), and hydrogen modes at high frequencies.

A gap separates the hydrogen bond-bending vibrations from the rest of the spectrum; this part moves to higher energies with increasing hydrogen content, but has very little influence on T_C due to the high frequencies involved. The spectrum of SH₃ is more compact, extending up to 200 meV, having peaks of the $\alpha^2F(\omega)$ higher, this result in a large λ ($\simeq 1.9$).

As more and more theoretical predictions of new superconducting hydrides are available, there is an increasing effort towards a systematic understanding of the factors leading to high- T_C ^{47,65}. It is becoming clear that the original idea of Ashcroft¹⁸, that the heavier atoms merely exert chemical pressure on the hydrogen lattice, is oversimplified, and other factors, such as the formation of strong atomic bonds between H and the heavier elements, play a crucial role. A good indicator of the

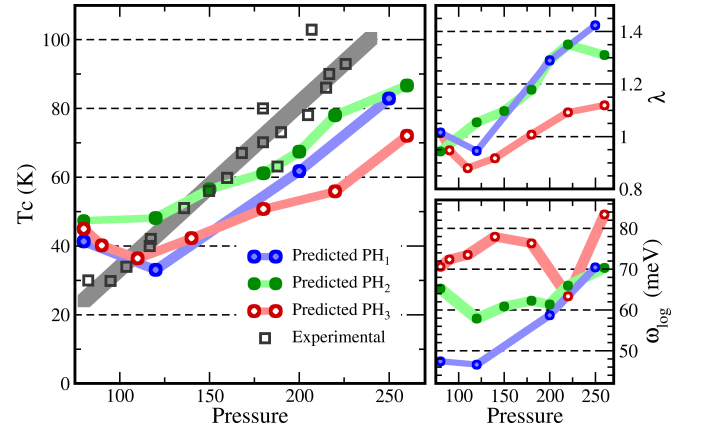


Figure 4. (Color online) Left: SCDFT calculated critical temperatures T_C for PH (blue), PH₂ (green) and PH₃ (red) as a function of pressure. Experimental T_C by resistivity measurements from Drozdov *et al.*³⁶ are shown in black squares. Overall a good agreement is found between the experimental values and those for PH, PH₂ and PH₃. Although the PH₂ composition shows significantly better agreement. Right: trend in pressure of the (BCS-like) electron phonon coupling coefficient λ (top panel) and of the phononic characteristic frequency ω_{\log} (bottom panel) as a function of pressure.

tendency of a material to follow one or another behavior is the electronegativity of the heavy atom. Atoms which are less electronegative than H tend to form solids which contain H₂ units with large characteristic vibration frequencies, but relatively weak matrix elements (electron-phonon coupling). More electronegative atoms, on the other hand, tend to form polar-covalent bonds, which couple strongly to phonons^{9,47}.

Phosphorus, with an electronegativity equal to that of hydrogen, lies on the border between the two regions and for the three hydrides considered in this study the electronic structure indicates a strong P-H hybridization in the whole energy range (see supplemental material). The values of the electronic density of state (DOS) at the Fermi level – N_{E_F} – are comparable (0.31 – 0.38 *st/eV f.u.*), and sensibly lower than those in SH₃ (0.54). The ratio $\eta = \lambda/N_{E_F}$, which can give an indication of the “stiffness” of the underlying lattice, ranges from 3 in PH₃ to 3.8 in PH, and is 3.6 in SH₃.

In practice, PH_{1,2,3} and SH₃ have a quite similar bonding and lattice stiffness to each other: what makes the latter exhibit a yet unmatched record T_C , is the extremely high value of its N_{E_F} , due to the presence of the van-Hove singularity close to the Fermi level^{10,11}. As the Fermi level of PH₂ and PH₃ falls in a shallow minimum of the density of states (see supplemental material), the same effect could be used to increase their T_C , by doping a small fraction of S or Si impurities into the samples.

In conclusion, the phase stability and superconducting properties of the recently reported PH₃ compound under pressure have been investigated with *ab initio* calculations. Our extensive structural searches show that

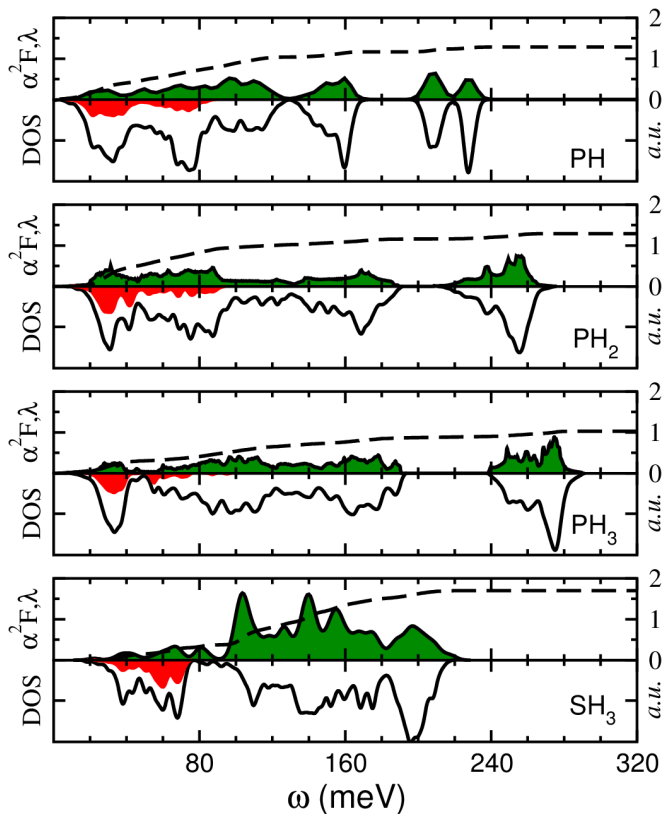


Figure 5. (Color online) Eliashberg spectral function and frequency-dependent ep coupling parameters $\lambda(\omega)$ – top panels – and phonon density of states (DOS) for the three PH_n compounds considered in the present study and SH_3 at 200 GPa. The shaded area (red) in the DOS panels is the P/S partial phonon DOS.

the hydrogen-rich phosphorus phases are thermodynamically unstable in the high-pressure regime of the phase diagram. Although including vibrational zero-point effects in our calculations improves the stability of PH, PH_2 and PH_3 , they remain metastable. Nevertheless, in view of their small distance from the convex hull, any of these structures may have been synthesized through non-equilibrium effects, or by anharmonic effects, as discussed in^{5,66}. Several of them were predicted to be good phonon-mediated superconductors and could thus in principle account for the measured high- T_C in experiments. In our opinion, the phase/composition that yields the best

agreement with experiments are PH and PH_2 , which are both close to the convex hull (< 7 meV/atom) and would show a pressure dependence in T_C similar to the experimental measurements. While experimentally it is still unclear if the observed high- T_C can be fully attributed to a phase of a binary phosphorus-hydride, and further experiments are called for to validate both our predictions and the results reported by Drozdov *et al.*³⁶. Finally, our calculations give a strong indication that the observed critical temperatures are those to be expected for the low energy, low-H content phases of P-H systems.

Note: While writing the present manuscript, we became aware of two works which report structural searches of phosphorus-hydrides, employing evolutionary algorithms^{67,68}. Both studies agree with our conclusions that none of the predicted phases is thermodynamically stable in the pressure range of 100-200 GPa. Shamp *et al.*⁶⁷ also suggest an $I4/mmm$ PH_2 structure as a possible candidate for the high- T_C phase. They also report a *polymeric* PH_2 structure which is more stable at low pressures. Based on our calculations, however, the *polymeric* structures for PH_2 show higher enthalpies than the $I4/mmm$ structure.

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