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Dissociation products and structures of solid H₂S at strong compression

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Hydrogen sulfides have recently received a great deal of interest due to the record high superconducting temperatures of up to 203 K observed on strong compression of dihydrogen sulfide ($\rm H_2S$). A joint theoretical and experimental study is presented in which decomposition products and structures of compressed $\rm H_2S$ are characterized, and their superconducting properties are calculated. In addition to the experimentally known $\rm H_2S$ and $\rm H_3S$ phases, our first-principles structure searches have identified several energetically competitive stoichiometries that have not been reported previously: $\rm H_2S_3$, $\rm H_3S_2$, $\rm HS_2$, and $\rm H_4S_3$. In particular, $\rm H_4S_3$ is predicted to be thermodynamically stable within a large pressure range of 25–113 GPa. High-pressure X-ray diffraction measurements confirm the presence of $\rm H_3S$ and $\rm H_4S_3$ through decomposition of $\rm H_2S$ that emerges at 27 GPa and coexists with residual $\rm H_2S$, at least up to the highest pressure studied in our experiments of 140 GPa. Electron-phonon coupling calculations show that $\rm H_4S_3$ has a small T_c of below 2 K, and that $\rm H_2S$ is mainly responsible for the observed superconductivity of samples prepared at low temperature (<100K).

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Superconductivity with a transition temperature T_c of up to 203 K was observed recently in solid H₂S at Megabar pressures, which is the highest record among all known superconductors [1]. Ashcroft suggested that metallic hydrogen would be a superconductor at high pressures with a T_c around room temperature [2], and subsequently predicted that hydrogen-rich metallic compounds might also be superconducting at high pressures [3]. Early theoretical studies focussed on high-pressure silicon and aluminum hydrides [4, 5], and a number of potential high-temperature superconductors have now been proposed in compressed hydrogen-rich compounds, with T_c s estimated in the range 40–250 K (e.g., GaH₃ [6, 7], SnH_4 [8], GeH_4 [9], NbH_4 [10], Si_2H_6 [11], $SiH_4(H_2)_2$ [12], CaH₆ [13], YH₃ [14], YH₄ and YH₆ [15]). Unfortunately, they have not been realized in practice, in part because of demanding experimental challenges. Very recent experimental studies have observed superconductivity in compressed phosphine (PH₃) with a T_c above 100 K [16].

The high pressure phase diagram of H_2S has been studied extensively. H_2S is a sister molecule of H_2O , and is the only known stable compound in the H-S system at ambient pressure. High-pressure diamond anvil cell experiments led to the discovery of a metallic phase at

about 96 GPa [17–28]. However, partial decomposition of H₂S and elemental sulfur was observed in Raman [27] and XRD studies [22] at room temperature above 27 GPa. H₂S had not been considered as a candidate for superconductivity because it was believed to dissociate into elemental sulfur and hydrogen under high pressures [29]. Recent first-principles structure searches predicted energetically stable metallic structures of H₂S above 110 GPa [30] and excluded dissociation into its elements. An estimated maximum T_c for metallic H₂S of 80 K at 160 GPa was predicted [30]. Motivated by this study, Drozdov et al. [1] performed high-pressure experiments on solid H₂S looking for superconductivity and found an astonishing T_c of 203 K at 155 GPa [1]. Interestingly, H_2S shows complex superconducting behavior at high pressures with the emergence of two different superconducting states. Samples prepared at low temperature (100 K) have a T_c of $\sim 30 \text{ K}$ at 110 GPa at the onset of superconductivity, which increases rapidly to a maximum value of 150 K at 200 GPa, while samples at room temperature or above show a maximum T_c of 203 K at 155 GPa.

Strobel *et al.* synthesized another H-S compound, H_3S , by compressing a mixture of H_2S and H_2 above 3.5 GPa [31]. The superconducting T_c of H_3S at 200 GPa was

recently predicted to be as high as 191–204 K [32], with H_3S in a cubic $Im\bar{3}m$ structure. The same $Im\bar{3}m$ structure was already predicted to occur for H₃O via the decomposition of water (H₂O) at terapascal pressures [33]. The agreement between experimental [1] and theoretical values of T_c [32] led to the proposal by Drozdov et al. that H₃S could be formed by decomposition of H₂S and might be responsible for the observed superconductivity at 203 K [1]. This proposal was supported by firstprinciples density-functional-theory (DFT) studies which suggested that it is thermodynamically favorable for H₂S to decompose into $H_3S + S$ [34–36] at pressures above 43 GPa [35]. However, there is a lack of experimental evidence to support the formation of H₃S, and the low T_c superconducting phase has not been fully explored. There is an urgent need to characterize the decomposition products of compressed H₂S in an effort to build an understanding of the complex superconducting behavior exhibited by the H-S system.

Here we present a joint theoretical and experimental study of compressed $\rm H_2S$ which clarifies the possible decomposition products and their structures. First-principles DFT structure searches were used to predict several new stoichiometries ($\rm H_2S_3$, $\rm H_3S_2$, $\rm HS_2$, and $\rm H_4S_3$) and a new structure in $\rm H_3S$ not reported previously. High pressure X-ray diffraction (XRD) experiments demonstrate that above 27 GPa, $\rm H_2S$ partially decomposes into $\rm S + \rm H_3S + \rm H_4S_3$. $\rm H_4S_3$ emerges as the major component at around 66 GPa and coexists with a small fraction of $\rm H_3S$ and residual $\rm H_2S$, at least up to the highest pressure studied experimentally of 140 GPa.

Extensive structure searches over 44 H-S stoichiometries at 25, 50, 100 and 150 GPa were performed using the CALYPSO [37, 38] and AIRSS [4, 39] methods, which have been successfully used to investigate structures of materials at high pressures [4, 13, 40–46]. The underlying structural relaxations were performed using the Vienna ab initio simulation package (VASP) [47] for CALYPSO and the CASTEP plane-wave code [48] for AIRSS. Electron-phonon coupling (EPC) calculations were performed with density functional perturbation theory using the Quantum-ESPRESSO package [49]. XRD data were collected at the 15U1 beamline at the Shanghai Synchrotron Radiation Facility (SSRF) with a monochromatic beam of wavelength 0.6199 Å. The diffraction patterns were integrated with the FIT2D computer code [50] and fitted by Rietveld profile matching using the GSAS+EXPGUI programs [51, 52]. More information about the calculations and experiments is provided in the Supplemental Material [53].

Figure 1 shows convex hull diagrams at 25, 50, 100 and 150 GPa which summarize the results of the structure searches. The effects of including quantum zero-point vibrational motion are significant and they tend to increase with pressure. Our results suggest that up to six H-S compounds lie on the convex hull at some pressures and

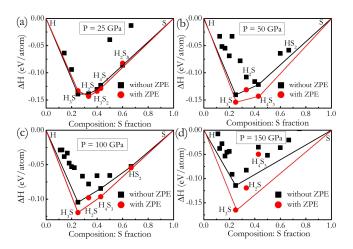


FIG. 1: (Color online) Results from structure searching at 25 (a), 50 (b), 100 (c) and 150 GPa (d). Convex hulls are shown as continuous lines, with (red) and without (black) the inclusion of zero point vibrational enthalpy (ZPE).

are therefore thermodynamically stable. Besides the experimentally known H₂S and H₃S compounds, we predict four additional stable compounds: H₄S₃, H₃S₂ H₂S₃ and HS₂. Note that H₂S is predicted to be stable only below 25 GPa, while H₃S is predicted to appear at all pressures considered. Enthalpy calculations show that H₃S becomes energetically more stable than H₂S+1/2H₂ at around 6 GPa (Supplemental Material, Fig. S1 [53]). The newly predicted H₃S₂ and H₂S₃ phases have very narrow pressure ranges of stability and are unstable above 34 and 25 GPa, respectively (Supplemental Material, Fig. S3 [53]). We have therefore omitted further discussion of these two compounds. HS₂ is predicted to be energetically stable between 64 and 116 GPa on the basis of static-lattice enthalpy calculations. The stable pressure range was revised to be between 75 and 87 GPa when the zero-point vibrational enthalpy was included (Supplemental Material, Fig. S9 [53]). The corresponding crystallographic parameters and phonon dispersion curves are provided in the Supplemental Material [53].

For H_3S , besides the P1, Cccm, R3m and Im $\bar{3}m$ structures of earlier studies [32], our searches predict a monoclinic C2/c structure (4 f.u/cell) that was not reported earlier. The C2/c structure consists of weakly bonded H_2S and H_2 molecules (Supplemental Material, Fig. S1b [53]), and is calculated to be more stable at pressures of 2–112 GPa than the Cccm structure proposed previously [32] (Supplemental Material, Fig. S1a [53]). Static-lattice enthalpy calculations give a zero-temperature phase sequence for H_3S of P1 \rightarrow C2/c (2 GPa) \rightarrow R3m (112 GPa) \rightarrow Im $\bar{3}m$ (180 GPa).

 $\rm H_4S_3$ adopts an orthorhombic $\rm P2_12_12_1$ (4 f.u./cell) structure that consists of weakly bonded HS and $\rm H_2S$ molecules at 25 GPa (Fig. 2a). The H-S bond lengths

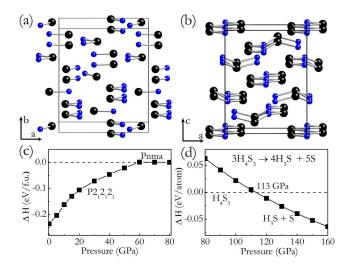


FIG. 2: (Color online) Energetically favorable structures of H_4S_3 with space groups $P2_12_12_1$ (a) and Pnma (b). Small and large spheres represent H and S atoms, respectively. (c) Calculated enthalpy curves of the $P2_12_12_1$ structure with respect to the Pnma structure for H_4S_3 as a function of pressure. (d) Decomposition enthalpy curves of H_4S_3 into (H_3S+S) as a function of pressure.

within the HS and $\rm H_2S$ molecules are 1.354 Å and 1.387-1.391 Å, respectively, which are significantly shorter than the H-S separation of 1.913-1.932 Å between molecules. With increasing pressure, the neighboring molecules bond with each other forming planar H-S-H-S zigzag chains and puckered H-S-H-S chains, respectively. $\rm P2_12_12_1$ transforms to a Pnma structure at 60 GPa (Fig. 2c). The convex hull data suggests two synthesis routes for $\rm H_4S_3$: (i) decomposition of $\rm 8H_2S \rightarrow S + 4H_3S + H_4S_3$ above 25 GPa; (ii) reaction of $\rm 4H_3S + 5S \rightarrow 3H_4S_3$ in the pressure range of 25–113 GPa. Theoretically, it is found that $\rm H_4S_3$ decomposes into $\rm H_3S + S$ above 113 GPa (Fig. 1d and Fig. 2d).

The H₂S samples were initially compressed to 10 GPa at low temperature (77 K) and then warmed to room temperature. Powder XRD patterns were then collected on increasing pressure from 10 to 140 GPa at room temperature, as shown in Fig. 3a. The XRD patterns collected at pressures up to 46 GPa are in excellent agreement with previous data [18–22], and the successive transitions of phase $I' \to \text{phase IV} \to \text{phase V}$ are well reproduced. The XRD data at 10 GPa correspond to phase I'. Phase IV with additional peaks at around 12° and 15° (shown by arrows in Fig. 3a) was observed at 16 GPa. The diffraction peaks of phase IV weaken at pressures above 27 GPa, and a new diffraction profile observed at 46 GPa is responsible for phase V. The XRD data show that the IV \rightarrow V transition begins above 27 GPa, in excellent agreement with previous results [19, 22].

Previous high-pressure Raman [27] and XRD [22] stud-

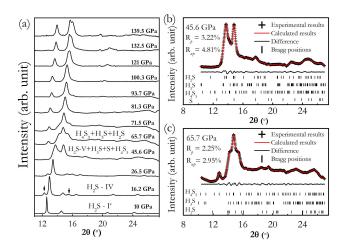


FIG. 3: (Color online) (a) XRD patterns of H₂S collected at various pressures at room temperature with an incident wavelength of 0.6199 Å. [(b) and (c)] Rietveld refinements of XRD profiles at 45.6 GPa based on the compositions Pc-H₂S, I4₁/acd-S, C2/c-H₃S and P2₁2₁2₁-H₄S₃ with phase fractions of 1147:85:31:1, and at 65.7 GPa based on compositions of Pnma-H₄S₃, C2/c-H₃S and Pc-H₂S with phase fractions of 5:3.4:1, respectively. The cross symbols and red solid lines represent observed and fitted patterns, respectively. The solid lines at the bottom are the difference between the observed and fitted patterns. Vertical bars under the pattern represent the calculated positions of reflections arising from the compositions.

ies have claimed that decomposition of H₂S occurs at room temperature above 27 GPa. Indeed, we found that H₂S partially decomposes in phase V. Unfortunately, we have not found it possible to resolve the decomposition products and their crystal structures from our current XRD data. Therefore we use the predicted structures and convex hull data to help in analysing the experimental data. At 50 GPa, our calculations suggest an energetically allowed dissociation path of $8H_2S \rightarrow S + 4H_3S +$ H₄S₃ (Fig. 1b). The XRD profile at 46 GPa was therefore fitted to a mixture of $H_2S + S + H_3S + H_4S_3$ by performing Rietveld refinements using the most energetically stable structures. Remarkably, we found that the XRD profile can be well indexed by a mixture of Pcstructured H₂S, I4₁/acd-structured S, C2/c-structured H₃S and P2₁2₁2₁-structured H₄S₃, with phase fractions (ratios of numbers of unit cells) of 1147:85:31:1, as shown in Fig. 3b. The existence of a large proportion of H₂S demonstrates the partial decomposition. We also attempted other Rietveld refinements fitting the XRD patterns to pure H_2S , $H_2S + S + H_3S$ or $S + 4H_3S + H_4S_3$, but all of these fits gave poorer results (Supplemental Material, Fig. S11 [53]). The calculated decomposition pressure (30 GPa) for $8H_2S \rightarrow S + 4H_3S + H_4S_3$ (Supplemental Material, Fig. S17 [53]) is in excellent agreement with the value of 27 GPa observed in experiment [22].

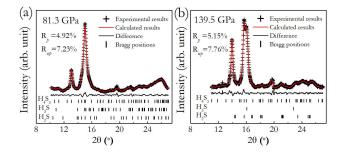


FIG. 4: (Color online) Rietveld refinements of XRD profiles at 81.3 GPa based on Pnma-H₄S₃ + C2/c-H₃S + Pmc2₁-H₂S with phase fractions of 43:6:1 (a) and at 139.5 GPa based on Pnma-H₄S₃ + R3m-H₃S + P-1-H₂S with phase fractions of 56:7:1 (c).

With increasing pressure, more H₂S decomposes and its contribution to the XRD signal is reduced. The XRD pattern collected at 66 GPa shows entirely different features to that at 46 GPa. Rietveld refinement shows that a mixture of Pnma-structured H₄S₃, C2/c-structured H₃S, and Pc-structured H₂S with phase fractions 5:3.4:1 gives the best fit to the experimental data (Fig. 3c). The disappearance of elemental S and the reduction in the ratio of H₃S are understandable since a reaction of 4H₃S + 5S \rightarrow 3H₄S₃ takes place as inferred from our convex hull calculations (Fig. 1b and 1c). The two shoulders on the main peak at 15° originate primarily from H₃S and H₂S. These shoulders weaken when the pressure is increased to 82 GPa and the XRD pattern can then be well indexed by Pnma-structured H₄S₃, C2/c-structured H₃S and Pmc2₁-structured H₂S with a major contribution (86%) from H_4S_3 (Fig. 4a). We also tried to refine the XRD profile at 82 GPa with the inclusion of HS_2 , which is calculated to be stable in between 75 and 87 GPa. However, the inclusion of HS₂ results in a poorer fit with higher R_p and R_{wp} values (Supplemental Material, Fig. S13(a) [53]), which excludes HS₂ as a decomposition product. Our results demonstrate that H₄S₃ coexists with H₃S and H₂S at least up to 140 GPa, the highest pressure studied experimentally (Fig. 4b). At this pressure, a refinement based on Pnma-structured H₄S₃ and C2/c-structured H₃S leads to poorer fits with higher R_p and R_{wp} values (Supplemental Material, Fig. S14 [53]), which supports the existence of residual H_2S (about 1.6%).

 ${\rm H_4S_3}$ is predicted to become metallic at 102 GPa (Supplemental Material, Fig. S18 [53]). However, the calculated electron-phonon-coupling parameter ($\lambda=0.42$) is very small at 140 GPa due to the low density of states at the Fermi level of 0.09 eV⁻¹/atom. As a result, the T_c estimated from the Allen and Dynes modified McMillan equation [54] with μ^* of 0.16–0.13 is only 0.75–2.1 K at 140 GPa.

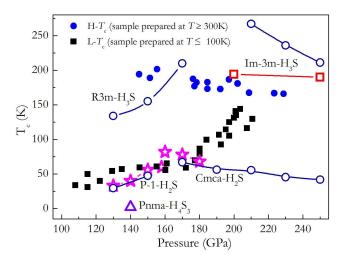


FIG. 5: (Color online) Superconducting transition temperatures (T_c) calculated for various H-S compounds and experimental values for compressed H₂S [1]. Solid squares and circles show experimental data from Fig. 1(b) and Fig. 2 (b) of Ref. 1, respectively, where different runs are represented by the same symbols. The open stars, squares and circles show calculated data from Ref. 30, Ref. 36 and Ref. 55, respectively. Open triangles denote calculated T_c for Pnma-H₄S₃ in the present study. Note that the T_c values (open squares) for Im $\bar{3}$ m-H₃S taken from Ref. 36 include anharmonic effects, while all other estimated T_c s are calculated within the harmonic approximation.

In Fig. 5, we compare the calculated T_c values for H₄S₃, H₂S and H₃S to experimental data measured in compressed H_2S [1], where T_c obtained for samples prepared at low and high temperatures are denoted by L- T_c and H- T_c , respectively. On the one hand, the observed L- T_c [1] at pressures below 160 GPa can only be quantitatively reproduced by H₂S, while the nature of the rapidly increasing L- T_c above 160 GPa remains unclear because the calculated T_c values of H_3S , H_4S_3 , and H_2S are too high, too low, and tending to decrease, respectively. On the other hand, although the values of T_c for Im3m structured H₃S calculated within the harmonic approximation are much higher than the observed H- T_c [55], the inclusion of anharmonic effects reproduces the $H-T_c$ data above 180 GPa quite well [36]. However, at low pressures around 150 GPa, T_c values [55] estimated for R3m-H₃S within the harmonic approximation are \sim 45 K lower than the observed H- T_c . Meanwhile, the predicted T_c for R3m-H₃S increases with pressure, in stark contrast to the experimental observation of a decrease in $H-T_c$. Further study is required to understand the steep T_c increase of L- T_c above 160 GPa and the high H- T_c at around 150 GPa.

We find that kinetics plays an important role in determining the experimentally observed H-S structures. Theory suggests that H_2S and H_4S_3 decompose above 30

and 113 GPa (Supplemental Material Fig. S17 and Fig. 2d), respectively. However, H_2S and H_4S_3 are observed to persist up to at least 140 GPa. Large kinetic barriers must therefore play a major role in suppressing decomposition at high pressures, as has been found in other materials [56–59].

In summary, first-principles structure searching calculations have been used to predict four new stable H-S compounds with stoichiometries H₃S₂, H₂S₃, HS₂ and H_4S_3 and a new C2/c structure of H_3S , enriching the phase diagram of H-S systems at high pressures. The formation of H₄S₃ and H₃S was confirmed by XRD experiments to occur through decomposition of compressed H_2S above 27 GPa resulting in the products $S + H_3S +$ H_4S_3 . H_4S_3 becomes a major component at around 66 GPa and is stable up to at least 140 GPa, with a small fraction of H₃S and residual H₂S. We have also examined potential superconductivity of metallic H₄S₃ via explicit calculations of electron-phonon coupling parameters and the superconducting T_c . Our work suggests that kinetically protected H₂S in samples prepared at low temperature is responsible for the observed superconductivity below 160 GPa.

After the submission of this work we became aware of an unpublished experimental study [60] by Einaga et al. supporting the formation of H₃S upon dissociation of H₂S, in agreement with our experimental results. However, their results suggested that H₃S is the major component with some unidentified phases. We attribute this discrepancy to the different experimental protocols used in the two experiments: in our experiments samples were compressed at ambient temperature above 10 GPa, whereas in Ref. 60 a temperature of 220 K was used. The unidentified minor phase in the data of Einaga et al. might be attributed to the H₄S₃ compound predicted here. It is possible that the use of different experimental protocols could give rise to similar dissociation products with different phase fractions, depending on the exact path followed.

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