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### Pressure induced novel compounds in the Hf-O system from first-principles calculations

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#### Abstract

Using first-principles evolutionary simulations, we have systematically investigated phase stability in the Hf-O system at pressure up to 120 GPa. New compounds  $Hf_5O_2$ ,  $Hf_3O_2$ , HfO and  $HfO_3$ are discovered to be thermodynamically stable at certain pressure ranges. Two new high-pressure phases are found for  $Hf_2O$ : one with space group *Pnnm* and anti-CaCl<sub>2</sub>-type structure, another with space group  $I4_1/amd$ . *Pnnm*-HfO<sub>3</sub> shows interesting structure, simultaneously containing oxide  $O^{2-}$  and peroxide  $[O-O]^{2-}$  anions. Remarkably, it is  $P\bar{6}2m$ -HfO rather than OII-HfO<sub>2</sub> that exhibits the highest mechanical characteristics among Hf-O compounds. *Pnnm*-Hf<sub>2</sub>O, *Imm*2-Hf<sub>5</sub>O<sub>2</sub>,  $P\bar{3}1m$ -Hf<sub>2</sub>O and  $P\bar{4}m$ 2-Hf<sub>2</sub>O<sub>3</sub> phases also show superior mechanical properties, theoretically these phases become metastable phases to ambient pressure and their properties can be exploited.

#### INTRODUCTION

Hafnium oxide  $HfO_2$  has a wide range of technological applications. In electronics industry, hafnium oxide-based material is currently used as an excellent high-k gate dielectric[1] and oxygen-deficient hafnium oxide also received additional interest for resistive-switching memories[2]. As for other applications, even though the hardness of hafnia (HfO<sub>2</sub>) is not that high for it to be considered as a superhard material[3], it still attracts attention as a potential candidate for hard oxide-based materials[4]. Unlike carbides or nitrides, oxides are more stable in the oxygen atmosphere at high temperature, which is valuable for many applications, Many oxide ceramics, especially those involving transition metals, are promising for application as hard coatings, since metal d electrons and strong bonds define their remarkable mechanical properties (high hardness, good chemical resistance, high tensile strength, and good fracture toughness)[5]. As compared to most transition metal oxide ceramics, hafnium oxide ceramics exhibit enhanced mechanical properties (higher fracture toughness) and structural stability (low thermal conductivity). Here, we want to explore all possible stable compounds of Hf-O system at pressure up to 120 GPa.

Under ambient temperature, experiments[6, 7] indicated that pure Hf is stable in the  $\alpha$ -phase (hexagonal close-packed structure, space group:  $P6_3/mmc$ ) and transforms to  $\omega$ -phase (hexagonal structure, space group: P6/mmm) at 46-58 GPa and then to  $\beta$ -Hf (body centered cubic, space group:  $Im\bar{3}m$ ) at 71.1 GPa-78.4 GPa. Our GGA calculated results indicate the transition pressures:  $\alpha$ -phase  $\rightarrow \omega$ -phase at 49 GPa and  $\omega$ -phase  $\rightarrow \beta$ -Hf at 70 GPa, which are in accord with above experimental results. It has been suggested that the solubility of oxygen in the octahedral interstitial sites of  $\alpha$ -Hf (hcp-Hf) can be as high as 20 at.%[8], while solubility of oxygen in  $\beta$ -Hf (bcc-Hf) is only 3 at.%[9]. Several experimental[10, 11] and theoretical studies[12, 13] have investigated the interstitial oxygen in hcp-Hf. Now it is well established that three stoichiometric compositions Hf<sub>6</sub>O, Hf<sub>3</sub>O and Hf<sub>2</sub>O can be formed with increasing occupation of the octahedral-interstitial positions in hcp-Hf by oxygen atoms. Hf<sub>2</sub>O<sub>3</sub> was theoretically predicted to form upon increasing the concentration of oxygen vacancies in monoclinic HfO<sub>2</sub>[14].

The phase sequence of HfO<sub>2</sub> at ambient temperature with increasing pressure is: baddeleyite (monoclinic, space group:  $P2_1/c$ )  $\rightarrow$  orthorhombic I (orthorhombic, space group: Pbca, OI)  $\rightarrow$  orthorhombic II (orthorhombic, space group: Pnma, OII)[15–17]. Orthorhombic OII-HfO<sub>2</sub> with experimentally reported hardness between 6-13 GPa[18] has been speculated to be much harder than the low-pressure phases (baddeleyite and OI-HfO<sub>2</sub>) because of its comparatively high bulk modulus[5, 19].

In this study, we systematically investigate the structure and stability of Hf-O compounds up to a pressure of 120 GPa by the first-principles evolutionary algorithm USPEX. Several new stoichiometries in the Hf-O system have been predicted under high pressure. Furthermore, we verify the dynamical and mechanical stability of these new high-pressure phases at 0 GPa by calculating their phonons and elastic constants. To better understand the correlations between hardness and O content, we estimate the hardness of these phases at 0 GPa using Chen's hardness model[20]. Quenchable high-pressure phases often possess superior mechanically properties, and we indeed find novel hafnium oxides with unusual mechanical properties.

#### COMPUTATIONAL METHODOLOGY

Searching the stable high-pressure structures in Hf-O system was done using firstprinciples evolutionary algorithm (EA) as implemented in the USPEX code 21–23 combined with ab initio structure relaxations using density functional theory (DFT) with the PBE-GGA functional[24], as implemented in the VASP package[25]. In our work, variablecomposition structure searches [23] for the Hf-O system with up to 32 atoms in the unit cell were performed at 0 GPa, 10 GPa, 20 GPa, 30 GPa, 40 GPa, 50 GPa, 60 GPa, 70 GPa, 80 GPa, 90 GPa, 100 GPa, 110 GPa and 120 GPa. The initial generation of structures was produced randomly using space group symmetry, each subsequent generation was obtained by variation operators including heredity (40%), lattice mutation (20%), random (20%)and transmutation (20%). The electron-ion interaction was described by the projectoraugmented wave (PAW) pseudopotentials[26], with  $5p^66s^25d^4$  and  $2s^22p^4$  shells treated as valence for Hf and O, respectively. The generalized gradient approximation (GGA) in the Perdew-Burke-Ernzerhof form<sup>[24]</sup> was utilized for describing exchange-correlation effects. The plane-wave energy cutoff was chosen as 600 eV and  $\Gamma$ -centered uniform k-meshes with resolution  $2\pi \times 0.06$  Å<sup>-1</sup> were used to sample the Brillouin zone, resulting in excellent convergence. Phonon dispersions were calculated using the finite-displacement method with the Phonopy code[27].



FIG. 1: Convex hull diagrams for the Hf-O system at (a) 0 GPa, (b) 20 GPa, (c) 30 GPa, (d) 40 GPa, (e) 60 GPa, and (f) 110 GPa, respectively. Solid squares and solid line arrows denote stable phases while open squares and dash line arrows represent the compounds for comparison.

#### **RESULTS AND DISCUSSIONS**

Crystal structure prediction for the Hf-O system

Thermodynamic convexhull, which defines stable compounds, is based on the free enthalpies (at T = 0 K, enthalpies) of the compounds and pure elements in their stable forms. The high-pressure convex hull and pressure-composition phase diagram of the Hf-O system are depicted in Fig. 1 and Fig. 2, respectively. See the supplementary material Fig. S1 for detail convexhull information of Hf-O compounds at a certain pressure. Besides the three well-known phases of HfO<sub>2</sub> and three suboxides ( $R\bar{3}$ -Hf<sub>6</sub>O,  $R\bar{3}c$ -Hf<sub>3</sub>O and  $P\bar{3}1m$ -Hf<sub>2</sub>O), our structure searches found hitherto unknown compounds with new stoichiometries, including



FIG. 2: Pressure-composition phase diagram of the Hf-O system.

 $Hf_5O_2$ ,  $Hf_3O_2$ , HfO and  $HfO_3$ . Note that two new high-pressure phases of  $Hf_2O$  (denoted as Pnnm- $Hf_2O$  and  $I4_1/amd$ - $Hf_2O$ ) were also found by our searches. Recent work[28] indicated that  $Hf_{12}O_5$  is a stable compound at low temperature, disproportionate above 220 K, therefore it is not expected to be observed experimentally. Our work indicates that  $Hf_{12}O_5$  is actually stable only in the pressure range from 8 GPa to 37 GPa. The related thermodynamic stability, dynamical stability, mechanical stability, phase status at 0 GPa and calculated stable pressure ranges for Hf-O compounds are listed in I.

Our calculation confirms that  $Hf_2O_3$  proposed by Xue[14] can exist as a metastable phase (it is dynamically and mechanically stable at 0 GPa), and shows that it should be a stable phase in the pressure range 20-23 GPa. The predicted transition from monoclinic-HfO<sub>2</sub> to OI-HfO<sub>2</sub> occurs at 10 GPa, which is coincides with experimental observations[15]. The transition from OI-HfO<sub>2</sub> to OII-HfO<sub>2</sub> occurs at 18 GPa, which is lower than the experimental result 30-37 GPa[3, 15] but in good agreement with other theoretical estimates of 17 GPa[3]. Furthermore, our calculated result shows that OII-HfO<sub>2</sub> is stable up to at least 120 GPa, which agrees with previous experimental work[3]. According to our predictions, only

TABLE I: Thermodynamic stability (TS), dynamical stability (DS), mechanical stability (MS), phase status (PS) at 0 GPa and calculated pressure ranges of stability for Hf-O compounds. Thermodynamic stability means that this structure is located on the convex hull at 0 GPa; dynamical stability means that no imaginary frequency exits in the whole Brillouin zone in the phonon dispersion crurves at 0 GPa; mechanical stability means that the elastic constants matrix is positive definite at 0 GPa.  $\sqrt{}$  = thermodynamic or dynamical or mechanical stability;  $\times$  = thermodynamic or dynamical or mechanical instability.

Compound	Space group	TS	DS	MS	$\mathbf{PS}$	Stable pressure	range (GPa)
						This work	Al-Khatatbeh <i>et al</i> [3]
Hf <sub>6</sub> O	$R\bar{3}$	$\checkmark$	$\checkmark$	$\checkmark$	stable	0-43.9	
$\mathrm{Hf}_{3}\mathrm{O}$	$R\bar{3}c$	×	$\checkmark$	$\checkmark$	metastable	3.3-31.3	
$\mathrm{Hf}_5\mathrm{O}_2$	Imm2	×	$\checkmark$	$\checkmark$	metastable	41-83.3	
$\mathrm{Hf}_{12}\mathrm{O}_5$	$R\bar{3}$	×	$\checkmark$		metastable	7.7-42.8	
$\mathrm{Hf}_{2}\mathrm{O}$	$P\bar{3}1m$	×	$\checkmark$	$\checkmark$	metastable	7.2-57.7	
$\mathrm{Hf}_{2}\mathrm{O}$	Pnnm	×	$\checkmark$	$\checkmark$	metastable	57.7-105	
$\mathrm{Hf}_{2}\mathrm{O}$	$I4_1/amd$	×	×	$\checkmark$	unstable	105-120	
$\mathrm{Hf}_{3}\mathrm{O}_{2}$	C2/m	×	$\checkmark$		metastable	81.1-120	
HfO	$P\bar{6}2m$	×	$\checkmark$	$\checkmark$	metastable	16-120	
$\mathrm{Hf}_{2}\mathrm{O}_{3}$	$P\bar{4}m2$	×	$\checkmark$	$\checkmark$	metastable	19.5-22.5	
$\mathrm{HfO}_{2}$	$P2_{1}/c$		$\checkmark$	$\checkmark$	stable	0-10	0-9.1
$\mathrm{HfO}_{2}$	Pbca	×	$\checkmark$	$\checkmark$	metastable	10-17.9	9.1-16.8
$\mathrm{HfO}_{2}$	Pnma	×	$\checkmark$		metastable	17.9-120	16.8-
$HfO_3$	Pnnm	×	×	$\checkmark$	unstable	110-120	

baddeleyite-type  $HfO_2$  and  $R\bar{3}$ - $Hf_6O$  are stable at 0 GPa, in contrast with the Zr-O system (Zr<sub>6</sub>O, Zr<sub>3</sub>O, Zr<sub>2</sub>O, ZrO and ZrO<sub>2</sub> are stable at 0 GPa)[29].

In order to study the ordering of interstitial oxygen atoms in hcp-HfO<sub>x</sub>, Hirabayashi et al.[10] used electron, neutron and X-ray diffraction to analyze single crystals containing 13.4 at % O and 15.8 at % O and found two types of interstitial superstructures: HfO<sub> $\frac{1}{6}$ </sub> and HfO<sub> $\frac{1}{6}$ </sub> below 600 K. The space group of HfO<sub> $\frac{1}{6}$ </sub> reported by Hirabayashi[10] is  $R\bar{3}$ , which is



FIG. 3: (Color online) Equation of state of  $Hf_2O$ . Our calculations were fit to a third-order Birch-Murnaghan equation of state to find  $B_0$  and  $B'_0$ .

identical to our findings. The space group of  $\text{HfO}_{\frac{1}{6}+}$  is  $P\bar{3}1c$  in Hirabayashi' experiment[10]. At 0 K and 0 GPa, our results produce three energetically competitive phases for Hf<sub>3</sub>O and their ordering by energy is  $R\bar{3}c$ -Hf<sub>3</sub>O (-10.075 eV/atom)  $< P\bar{3}1c$ -Hf<sub>3</sub>O (-10.072 eV/atom)  $< P6_322$ -Hf<sub>3</sub>O (-10.069 eV/atom). Therefore, one can note that  $P\bar{3}1c$ -Hf<sub>3</sub>O ( $P\bar{3}1c$ -Zr<sub>3</sub>O type), exhibits very close but higher energy than  $R\bar{3}c$ -Hf<sub>3</sub>O at 0 GPa and 0 K. In order to consider the effects of temperature, quasi-harmonic free-energy of  $R\bar{3}c$ -Hf<sub>3</sub>O and  $P\bar{3}1c$ -Hf<sub>3</sub>O were calculated using the Phonopy code[27]. The results indicate that free energy of  $P\bar{3}1c$ -Hf<sub>3</sub>O decreases faster than that of  $R\bar{3}c$ -Hf<sub>3</sub>O with temperature, enabling  $P\bar{3}1c$ -Hf<sub>3</sub>O to become more stable than  $R\bar{3}c$ -Hf<sub>3</sub>O at 1000 K, thus explaining experimental result.

Hf<sub>2</sub>O undergoes a trigonal-to-orthorhombic I phase transition 58 GPa and orthorhombic I-to-orthorhombic II transition at 105 GPa. The crystal structure of the new high-pressure phase Pnnm-Hf<sub>2</sub>O is anti-CaCl<sub>2</sub>-type. The Birch-Murnaghan equation of state[30] was used to fit the compressional behavior of the predicted Hf<sub>2</sub>O phases (Fig. 3). The third-order Birch-Murnaghan EOS is given as1. Most materials have  $3 \leq B'_0 \leq 6[31, 32]$ . The  $B'_0$  of  $P\bar{3}1m$ -Hf<sub>2</sub>O, Pnnm-Hf<sub>2</sub>O and  $I4_1/amd$ -Hf<sub>2</sub>O is 4.0, 3.8 and 3.4, respectively.



FIG. 4: (Color online) Average bond lengths in Hf-O compounds at 0 GPa.

$$P(V) = \frac{3B_0}{2} \left[ \left( \frac{V}{V_0} \right)^{-\frac{7}{3}} - \left( \frac{V}{V_0} \right)^{-\frac{5}{3}} \right] \left\{ 1 + \frac{3}{4} (B'_0 - 4) \left[ \left( \frac{V}{V_0} \right)^{-\frac{2}{3}} - 1 \right] \right\}$$
(1)

#### Structures of the Hf-O compounds

Table II lists the detailed crystallographic data of Imm2- Hf<sub>5</sub>O<sub>2</sub>, Pnnm- Hf<sub>2</sub>O,  $I4_1/amd$ -Hf<sub>2</sub>O, C2/m-Hf<sub>3</sub>O<sub>2</sub>,  $P\bar{6}2m$ -HfO, C2/m-Hf<sub>2</sub>O<sub>3</sub> and Pnnm-HfO<sub>3</sub> compounds at 0 GPa. The mechanical stabilities of all the Hf-O compounds have been checked by the mechanical stability restrictions[33] at 0 GPa, see the supplementary for the criteria of mechanical stability. Except the three well-known structures: baddeleyite-HfO<sub>2</sub>, orthorhombic I-HfO<sub>2</sub>, II-HfO<sub>2</sub>, the dynamical stabilities of all the other phases are checked by calculating phonon dispersion (see supplementary material Fig. S2 for detail). Except for Pnnm-HfO<sub>3</sub> and  $I4_1/amd$ -Hf<sub>2</sub>O, no imaginary phonon frequencies are found in the whole Brillouin zone at both ambient and high pressure, which means that they are dynamically stable and probably quenchable to ambient pressure. In contrast, HfO<sub>3</sub> and  $I4_1/amd$ -Hf<sub>2</sub>O are stable only at high pressure, but at 0 GPa shows total dynamical instability and most likely decomposes. The special electronic structure of HfO<sub>3</sub> will be discussed below. The weighted average lengths of Hf-Hf and Hf-O bonds in Hf-O compounds are plotted in Fig. 4.

Compound Space group Enthalpy of formation Lattice constants Wyckoff positions х у  $\mathbf{Z}$ (Å) (eV/atom) $Hf_5O_2$ Imm2-1.52a = 14.455Hf 4c  $0.711 \ 0.50 \ 0.566$ b = 3.141Hf 2b $0.00 \quad 0.50 \quad 0.098$ Hf 4c  $0.097 \ 0.00 \ 0.594$ c = 5.082O 4c $0.645 \ 0.00 \ 0.818$  $Hf_2O$ Pnnm -1.76a = 5.092Hf 4g  $0.263 \ 0.341 \ 0.50$ O 2c $0.00 \quad 0.50 \quad 0.00$ b = 5.723c = 3.175 $Hf_2O$  $I4_1/amd$ -1.67a = 4.554Hf 8e  $1.00 \quad 0.50 \quad 0.50$ c = 8.920O 4b $1.00 \ 1.00 \ 0.50$  $Hf_3O_2$ C2/m-2.04a = 11.967Hf 4i 0.625 0.50 0.007b = 3.131Hf 4i  $0.465 \ 0.00 \ 0.346$  $0.286 \ 0.00 \ 0.676$ c = 11.198Hf 4i  $\beta=99.67^\circ$ O 4i 0.378 0.50 0.607O 4i $0.787 \ 0.00 \ 0.192$ HfO  $P\bar{6}2m$  $0.00 \quad 0.00 \quad 0.50$ -2.60 $a{=}5.230$  ${
m Hf}$  1b  $c{=}3.187$ Hf 2c $0.667 \ 0.333 \ 0.00$ O 3g  $0.00 \ 0.592 \ 0.50$  $P\bar{4}m2$  $Hf_2O_3$ -3.11a = 3.137Hf 2g  $0.00 \quad 0.50 \quad 0.744$  $0.00 \quad 0.50 \quad 0.135$ c = 5.638O 2gO 1c  $0.50 \quad 0.50 \quad 0.50$ -2.22  $HfO_3$ Pnnm a = 6.027Hf 4g  $0.801 \ 0.693 \ 0.00$ b = 6.172O 4g  $0.067 \ 0.399 \ 0.50$ c = 3.958O 4g  $0.340 \ 0.141 \ 0.50$  $0.50 \ \ 0.50 \ \ 0.312$ O 4e

TABLE II: Structural parameters of Imm2-Hf<sub>5</sub>O<sub>2</sub>, Pnnm-Hf<sub>2</sub>O, C2/m-Hf<sub>3</sub>O<sub>2</sub>,  $P\bar{6}2m$ -HfO, C2/m-Hf<sub>2</sub>O<sub>3</sub> and Pnnm-HfO<sub>3</sub> at 0 GPa.



FIG. 5: (Color online) Octahedral voids in hcp hafnium.

Structurally, hafnium oxides can be divided into four groups: suboxides with oxygen interstitials in hcp-Hf (Hf<sub>6</sub>O, Hf<sub>3</sub>O, Hf<sub>12</sub>O<sub>5</sub> and  $P\bar{3}1m$ -Hf<sub>2</sub>O); other suboxides (Hf<sub>5</sub>O<sub>2</sub>, *Pnnm*-Hf<sub>2</sub>O,  $I4_1/amd$ -Hf<sub>2</sub>O and HfO); normal oxides (Hf<sub>2</sub>O<sub>3</sub>, HfO<sub>2</sub>) and oxide peroxide (HfO<sub>3</sub>). The octahedral sites of hcp hafnium metal are depicted in Fig.5. Oxygen atoms prefer to occupy these octahedral sites and form ordered structures  $R\bar{3}$ -Hf<sub>6</sub>O,  $R\bar{3}c$ -Hf<sub>3</sub>O,  $R\bar{3}$ -Hf<sub>12</sub>O<sub>5</sub> and  $P\bar{3}1m$ -Hf<sub>2</sub>O, as shown in Fig. 6 (a) (b) (c) and (d), where Hf atom sites are omitted. The polyhedral representation of these structures is shown in Fig. 5 (e) (f) (g) and (h). Anti-CaCl<sub>2</sub>-type (*Pnnm*) structure of Hf<sub>2</sub>O can also be represented as an hcp-sublattice (distorted) of Hf atoms, where half of octahedral voids are occupied by O atoms. The structure of Hf<sub>3</sub>O<sub>2</sub> can be considered to be defective because each layer lacks some Hf atoms to form a Hf-graphene layer. These vacancies are responsible for low values of the mechanical properties of Hf<sub>3</sub>O<sub>2</sub>.



FIG. 6: (Color online) Oxygen sublattice representation (arrangement of oxygen atoms in the octahedral interstitial sites) and polyhedral representation of (a)&(b)  $R\bar{3}$ -Hf<sub>12</sub>O<sub>5</sub> (c)&(d)  $P\bar{3}1m$ -Hf<sub>2</sub>O (e)&(f)  $R\bar{3}$ -Hf<sub>6</sub>O (g)&(h)  $R\bar{3}c$ -Hf<sub>3</sub>O. Oxygen-centered octahedra and oxygen vacancies are shown in red and pink polyhedra, respectively. Oxygen sublattice representations (b, d, f, h) show only oxygen atoms (filled circles) and vacancies (open circles).

Similar with ZrO, the structure of HfO contains Hf-graphene layers stacked on top of each other (Zr-Zr distances within the layer are 3.01 Å, and between the layers 3.18 Å), as illustrated in Fig. 7(b), as well as additional Hf and O atoms. The structure can be represented as  $\omega$ -phase of Hf, intercalated with oxygen atoms. This structure, therefore, is built by a 3D-framework of short and strong Hf-O bonds, reinforced by rather strong Hf-Hf bonds. The former lead to high hardness, the latter improve toughness.  $P\bar{4}m2$ -Hf<sub>2</sub>O<sub>3</sub>, which was firstly proposed by Xue[14], has 8-fold and 6-fold coordination of Hf atoms, as shown in Fig 7.

Pnnm-HfO<sub>3</sub> becomes stable at pressures above to 110 GPa. This high-pressure phase originally derives from oxygen atom dissolving in both octahedral and tetrahedral voids of



FIG. 7: (Color online) Crystal structures of (a) Imm2-Hf<sub>5</sub>O<sub>2</sub> (b)  $P\bar{6}2m$ -HfO (c)  $P\bar{4}m2$ -Hf<sub>2</sub>O<sub>3</sub> and (d)  $P\bar{4}m2$ -Hf<sub>2</sub>O<sub>3</sub> (e)  $I4_1/amd$ -Hf<sub>2</sub>O. O-centered octahedra and O-centered tetrahedra are shown in red and blue polyhedra, respectively. Large spheres-Hf atoms; small spheres-O atoms.



FIG. 8: (Color online) Crystal structure of (a) *Pnnm*-HfO<sub>3</sub> (b) *Pnnm*-Hf<sub>2</sub>O; (c) *Pnnm*-HfO<sub>3</sub> (d) *Pnnm*-Hf<sub>2</sub>O.

a heavily distorted hcp-Hf, as shown in Fig 8(a). However, due to short distances between tetrahedral voids in the hcp structures, some O atoms form pairs and as a result  $HfO_3$  simultaneously contains oxide  $O^{2-}$  and peroxide  $[O-O]^{2-}$  anions, and can be described as "oxide peroxide". The O-O bond length in  $HfO_3$  is 1.44 Åat 110 GPa, which is a little smaller than the O-O bond length in peroxide  $[O-O]^{2-}$  ion with 1.47 Å[34] at ambient conditions. It

seems that peroxides and oxide peroxides (e.g.  $Al_4O_7$  and  $AlO_2$ ) become stabilized in many systems under pressure[35].

#### Mechanical properties of Hf-O compounds

Previous studies [15, 19, 36] suggested that dense high-pressure phase OII-HfO<sub>2</sub> is quenchable to ambient conditions and has a high bulk modulus, and might be superhard (H > 40 GPa). However recent study [3] reported that the hardness of OII-HfO<sub>2</sub> is well below 40 GPa and therefore this phase is not superhard. Interestingly, our systematic results not only confirm known hardness of HfO<sub>2</sub> polymorphs: H(OII) < H(MI) < H(OI), but also suggest that HfO has the highest hardness among all hafnium oxides, see Fig. 10(f). In addition, *Pnnm*-Hf<sub>2</sub>O and *Imm*2-Hf<sub>5</sub>O<sub>2</sub> also exhibit higher hardness than other Hf-O compounds, as shown in Tab III. The hardness of HfO compounds does not monotonically change with O content, but a maximum at HfO.

The calculated modulus B, shear modulus G, Young's modulus E, Poisson's ratio v, and hardness of all stable Hf–O compounds are depicted in TableII and Fig.10 (for comparison, the elastic data of the high-pressure phase  $I4_1/amd$ -Hf<sub>2</sub>O and Pnnm-HfO<sub>3</sub> are reported at 0 GPa although they are unstable at 0 GPa.) The determination of the bulk modulus Band shear modulus G of polycrystalline aggregates from individual elastic constants,  $c_{ij}$ , can be established from the continuum theories based on Reuss[37] and Voigt[38] approaches that effective isotropic elastic constants are obtained by averaging the anisotropic elastic constants over all possible orientations of the grains in a polycrystal.  $B_R$ ,  $B_V$  and  $G_R$ ,  $G_V$  are respectively the bulk modulus and shear modulus from the Reuss and Voigt approximations (See equations from the supplementary material). Hill[39] proved that the Voigt and Reuss moduli are upper and lower bounds, and the actual elastic moduli for polycrystals can be approximated by the arithmetic mean of these two extremes. We have therefore utilized the Voigt-Reuss-Hill (VRH) approximation and expressed as follows:

$$B_{VRH} = \frac{1}{2} \left( B_V + B_R \right) \tag{2}$$

$$G_{VRH} = \frac{1}{2} \left( G_V + G_R \right) \tag{3}$$

Using the calculated values for B and Young's modulus E and Possion's ratio can be further calculated using the following relationships:

$$E = \frac{9BG}{3B+G} \tag{4}$$

$$\nu = \frac{3B - 2G}{2(3B + G))} \tag{5}$$

From Fig.9 we can conclude that the high O content in the crystal does not guarantee high hardness of Hf-O compounds and the structure plays an important role in determining mechanical properties as we discussed above. The Vickers hardness was calculated according to Chen's model[20]. The corresponding expression is given as follows:

$$H_v = 2(k^2 G)^{0.585} - 3 \tag{6}$$

where  $H_v$ , G and B are the hardness (GPa), shear modulus (GPa) and bulk modulus (GPa), respectively. The parameter k is the Pugh's modulus ratio, namely, k = G/B.

Anisotropic elasticity of single crystals has a great effect on the elastic behavior of polycrystals and can exert its influence on the anisotropic plastic deformation and crack behavior. Most materials are elastically anisotropic, and their Young's modulus will be an aisotropic property. It is useful in practice to show the directional variation of Young's modulus by three-dimensional diagrams, where deviations from sphericity directly reflect the degree and direction of anisotropy. We calculated the elastic anisotropy of five special phases:  $P\bar{6}2m$ -HfO, Pnnm-Hf<sub>2</sub>O, Imm2-Hf<sub>5</sub>O<sub>2</sub>,  $P\bar{3}1m$ -Hf<sub>2</sub>O and  $P\bar{4}m2$ -Hf<sub>2</sub>O<sub>3</sub>. As shown in Fig. 10, it is readily evident that  $P\bar{6}2m$ -HfO, Imm2-Hf<sub>5</sub>O<sub>2</sub>,  $P\bar{3}1m$ -Hf<sub>2</sub>O and  $P\bar{4}m2$ -Hf<sub>2</sub>O<sub>3</sub> exhibit a moderate amount of anisotropy of Young's modulus, particularly Imm2-Hf<sub>5</sub>O<sub>2</sub>,  $P\bar{3}1m$ -Hf<sub>2</sub>O while Pnnm-Hf<sub>2</sub>O tends to be considerably less anisotropic. The directional dependence of the Young's modulus for hexagonal, orthorhombic, trigonal and tetragonal crystals can be calculated according to the elastic compliance constants[33] (See the supplementary material for detail).



FIG. 9: (Color online) Compositional dependence of the computed mechanical properties of Hf-O compounds. The blue open circle represents Pnnm-Hf<sub>2</sub>O; purple open diamond represents  $I4_1/amd$ -Hf<sub>2</sub>O; red open triangle represents OI-HfO<sub>2</sub>; green open square represents OII-HfO<sub>2</sub>.



FIG. 10: (Color online) Orientational dependence of Young's moduli (in GPa) of (a) P62m-HfO
(b) Pnnm-Hf<sub>2</sub>O (c) Imm2-Hf<sub>5</sub>O<sub>2</sub> (d) P31m-Hf<sub>2</sub>O and (e) P4m2-Hf<sub>2</sub>O<sub>3</sub>.

Compound		Space group	P	$B_H$	$G_H$	E	G/B	v	$H_v$
Hf <sub>6</sub> O	This work	$R\bar{3}$	0	129.2	72.8	183.8	0.56	0.26	9.55
${\rm Hf_{3}O}$	This work	$R\bar{3}c$	0	150.3	78.8	201.3	0.52	0.28	9.1
$\mathrm{Hf}_{5}\mathrm{O}_{2}$	This work	Imm2	0	150.0	95.3	235.9	0.64	0.24	13.9
$\mathrm{Hf}_{12}\mathrm{O}_5$	This work	$R\bar{3}$	0	163.3	94.5	237.7	0.58	0.26	12.1
$\mathrm{Hf}_{2}\mathrm{O}$	This work	$P\bar{3}1m$	0	175.2	103.1	258.6	0.59	0.25	13.2
$\mathrm{Hf}_{2}\mathrm{O}$	This work	Pnnm	0	173.0	110.3	272.9	0.64	0.23	15.5
$\mathrm{Hf}_{2}\mathrm{O}$	This work	$I4_1/amd$	0	159.1	65.1	171.9	0.41	0.32	5.1
$\mathrm{Hf}_{3}\mathrm{O}_{2}$	This work	C2/m	0	154.2	75.9	195.6	0.49	0.29	8.0
HfO	This work	$P\bar{6}2m$	0	210.7	128.1	319.5	0.61	0.25	16.1
$\mathrm{Hf}_{2}\mathrm{O}_{3}$	This work	$P\bar{4}m2$	0	243.9	127.1	324.8	0.52	0.28	12.9
$\mathrm{HfO}_{2}$	This work	$P2_1/c$	0	203.6	99.2	256.1	0.49	0.29	9.7
	Experiment[40]		0						9.9
$\mathrm{HfO}_{2}$	This work	Pbca	0	225.9	115.8	296.6	0.51	0.28	11.7
$\mathrm{HfO}_{2}$	This work	Pnma	0	226.3	93.8	247.3	0.41	0.31	7.2
	Experiment[41]		0						6-13
$\mathrm{HfO}_{3}$	This work	Pnnm	0	171.1	73.6	193.0	0.43	0.31	6.2

TABLE III: Calculated bulk modulus B, shear modulus G, Young's modulus E, Poisson's ratio vand hardness of Hf-O compounds, compared with literature data for HfO<sub>2</sub> at 0 GPa. All properties are in GPa (except dimensionless G/B and v).

#### Electronic structure of Hf-O compounds

Band structures of Hf-O compounds at 0 GPa (including phases stable at both zero and high pressure) are listed in supplementary Fig. S3. Band structures of  $P\bar{6}2m$ -HfO and  $P\bar{4}m2$ -Hf<sub>2</sub>O<sub>3</sub> at 0 GPa are depicted in Fig. 11.  $P\bar{4}m2$ -Hf<sub>2</sub>O<sub>3</sub> shows the semimetallic character based on both DFT band structure and hybrid functional HSE06 band structure. Interestingly, the chemical behavior of Zr and Hf are similar,  $P\bar{6}2m$ -ZrO has been confirmed to be a semimetal according to the band structures from both DFT and HSE06 calculations[29], therefore the band structure of  $P\bar{6}2m$ -HfO calculated by HSE06 is supposed to be similar. However the more accurate approach HSE06 result turns out that  $P\bar{6}2m$ -HfO



FIG. 11: (Color online) Band structures of  $P\bar{6}2m$ -HfO and  $P\bar{4}m2$ -Hf<sub>2</sub>O<sub>3</sub> at 0 GPa. The Fermi energy is set to zero. Hybrid-functional is believed to give the same level of accuracy as more rigorous GW quasi particle calculations. The black lines represent the band structure calculated by DFT-GGA method and open circle lines denote the band structure calculated by hybrid functional HSE06 method.

has the tiny band gap 0.112 eV between the conduction band and valence band while DFT-GGA band structure shows that very few states at the Fermi level and  $P\bar{6}2m$ -HfO should be a semimetal. Given HSE06 is more accurate than DFT method, we therefore teat  $P\bar{6}2m$ -HfO as a semiconductor instead of a semimetal according to its calculated HSE06 band structure.

Total and partial densities of states (DOS) calculated by DFT are presented in Fig. 13.  $R\bar{3}$ -Hf<sub>6</sub>O,  $R\bar{3}c$ -Hf<sub>3</sub>O, Imm2-Hf<sub>5</sub>O<sub>2</sub>,  $R\bar{3}$ -Hf<sub>12</sub>O<sub>5</sub>,  $P\bar{3}1m$ -Hf<sub>2</sub>O, Pnnm-Hf<sub>2</sub>O,  $I4_1/amd$ -Hf<sub>2</sub>O and C2/m-Hf<sub>3</sub>O<sub>2</sub> are predicted to be metallic with a sizable density of states at the Fermi level and the interactions between the Hf-d orbitals are responsible for their metallicity. The



FIG. 12: (Color online) ELF isosurface (ELF = 0.62) for HfO<sub>3</sub>. Blue and red atoms represent oxide  $O^{2-}$  and peroxide  $[O-O]^{2-}$  ions, respectively.



FIG. 13: (Color online) The normalized (per electron) total (TDOS) and partial densities of states (PDOS) of hafnium oxides at 0 GPa. The Fermi energy is set to zero.

DFT band gaps of  $P_{1/c}$ -HfO<sub>2</sub>, *Pbca*-HfO<sub>2</sub>, *Pnma*-HfO<sub>2</sub> and *Pnnm*-HfO<sub>3</sub> are 4.01 eV, 4.18 eV, 3.36 eV and 1.92 eV, respectively, and the highest occupied states are all derived mainly from O-p orbitals, as shown in Fig. 13(j, k, l and m). Therefore, according to their electronic character, Hf-O compounds can be divided into three types: metallic, including  $R\bar{3}$ -Hf<sub>6</sub>O,  $R\bar{3}c$ -Hf<sub>3</sub>O, *Imm*<sub>2</sub>-Hf<sub>5</sub>O<sub>2</sub>,  $R\bar{3}$ -Hf<sub>12</sub>O<sub>5</sub>,  $P\bar{3}1m$ -Hf<sub>2</sub>O, *Pnnm*-Hf<sub>2</sub>O,  $I4_1/amd$ -Hf<sub>2</sub>O and C2/m-Hf<sub>3</sub>O<sub>2</sub>; semimetallic, including  $P\bar{4}m$ 2-Hf<sub>2</sub>O<sub>3</sub>; insulating or semiconducting, including  $P\bar{6}2m$ -HfO,  $P2_1/c$ -HfO<sub>2</sub>, *Pbca*-HfO<sub>2</sub>, *Pnma*-HfO<sub>2</sub> and *Pnnm*-HfO<sub>3</sub>. Electron localization function (ELF) clearly reveals special featrure of HfO<sub>3</sub>, the coexistence of oxide O<sup>2-</sup> and peroxide [O-O]<sup>2-</sup> anions (Fig. 12). The peroxide is responsible for gap states, which significantly reduce the electronic band gap of HfO<sub>2</sub> (Fig. 13 (m)). To obtain further insight, we applied the Atoms in Molecules (AIM) theory developed by Bader [42]. Bader charges are +2.5 for Hf, -0.68 for peroxide anion and -1.16 for oxide anion in HfO<sub>3</sub> at 110 GPa, which shows a significantly ionic character of bonding. Valence electrons localize on O atoms in other Hf-O compounds (see ELF plots for other Hf-O compounds in the supplementary materials Fig. S4.).

#### CONCLUSIONS

We have systematically predicted stable compounds and crystal structures in the Hf-O system at pressures up to 120 GPa using ab initio evolutionary algorithm USPEX. Several new stable compounds, including Imm2-Hf<sub>5</sub>O<sub>2</sub>, C2/m-Hf<sub>3</sub>O<sub>2</sub>,  $P\bar{6}2m$ -HfO and Pnnm-HfO<sub>3</sub> are found for the first time. Pnnm-Hf<sub>2</sub>O and  $I4_1/amd$ -Hf<sub>2</sub>O, which are the new high-pressure phases of Hf<sub>2</sub>O, are also discovered. HfO<sub>3</sub> shows interesting structure, simultaneously containing oxide O<sup>2-</sup> and peroxide [O-O]<sup>2-</sup> anions. Our results demonstrate that Hf<sub>3</sub>O<sub>2</sub> is more ductile than other Hf-O compounds, and the hardest compound is HfO instead of OII-HfO<sub>2</sub>. The superior mechanical properties of  $P\bar{6}2m$ -HfO, such as bulk modulus B, shear modulus G, Young's modulus E and hardness  $H_v$ , can be attributed to the peculiar combination of strong Hf-O and Hf-Hf bonds. Pnnm-Hf<sub>2</sub>O, Imm2-Hf<sub>5</sub>O<sub>2</sub>,  $P\bar{3}1m$ -Hf<sub>2</sub>O and  $P\bar{4}m2$ -Hf<sub>2</sub>O<sub>3</sub> also show excellent mechanical properties. Clearly, high O content is not a key factor affecting the mechanical properties of Hf-O compounds. Suboxides: Hf<sub>6</sub>O, Hf<sub>3</sub>O, Hf<sub>12</sub>O<sub>5</sub> and  $P\bar{3}1m$ -Hf<sub>2</sub>O based on hcp-Hf sublattice provide easy pathways for absorbing or desorbing oxygen. The recognition of the common structural features between  $P\bar{6}2m$ -HfO

and  $\omega$ -Hf gives further insight into the physical properties and suggests that HfO can be made as a hard semimetallic coating on  $\omega$ -Hf substrate. *Pnnm*-Hf<sub>2</sub>O, *Imm*2-Hf<sub>5</sub>O<sub>2</sub>, *P* $\bar{3}1m$ -Hf<sub>2</sub>O and  $P\bar{4}m$ 2-Hf<sub>2</sub>O<sub>3</sub> phases in particular can be quenched to ambient pressure and can be candidates for applications requiring mechanically strong materials.

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