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Spatially resolved penetration depth measurements and vortex manipulation in the ferromagnetic superconductor $\text{ErNi}_2\text{B}_2\text{C}$

Dirk Wulferding,^{1,2,*} Ilkyu Yang,^{1,2,*} Jinho Yang,^{1,2} Minkyung Lee,^{1,3} Hee Cheul Choi,^{1,3} Sergey L. Bud'ko,^{4,5} Paul C. Canfield,^{4,5} Han Woong Yeom,^{1,2} and Jeehoon Kim^{1,2,†}

¹*Center for Artificial Low Dimensional Electronic Systems,*

Institute for Basic Science, 77 Cheongam-Ro, Nam-Gu, Pohang 790-784, Korea

²*Department of Physics, Pohang University of Science and Technology, Pohang 790-784, Korea*

³*Department of Chemistry, Pohang University of Science and Technology, Pohang 790-784, Korea*

⁴*Ames Laboratory, U.S. Department of Energy, Ames, Iowa 50011, USA*

⁵*Department of Physics and Astronomy, Iowa State University, Ames, Iowa 50011, USA*

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We present a local probe study of the magnetic superconductor, $\text{ErNi}_2\text{B}_2\text{C}$, using magnetic force microscopy at sub-Kelvin temperatures. $\text{ErNi}_2\text{B}_2\text{C}$ is an ideal system to explore the effects of concomitant superconductivity and ferromagnetism. At 500 mK, far below the transition to a weakly ferromagnetic state, we directly observe a structured magnetic background on the micrometer scale. We determine spatially resolved absolute values of the magnetic penetration depth λ and study its temperature dependence as the system undergoes magnetic phase transitions from paramagnetic to antiferromagnetic, and to weak ferromagnetic, all within the superconducting regime. In addition, we estimate the absolute pinning force of Abrikosov vortices, which shows a position- and temperature dependence as well, and discuss the possibility of the purported spontaneous vortex formation.

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I. INTRODUCTION

The interplay between magnetism and superconductivity has caught the attention of many condensed matter scientists. Once thought to be mutually exclusive, several materials have since emerged in which a coexistence of magnetic order and superconductivity can be found.¹⁻³ This is contrasted, e.g., by high temperature cuprate superconductors; although a low temperature rare-earth-related magnetic ordering may occur within the superconducting phase,⁴ there is a clear separation between the Cu-based strong antiferromagnetic and the superconducting phases.⁵ Nevertheless, spin fluctuations in the Cu-O planes that arise from the melting of the antiferromagnetically ordered phase upon doping seem to support and mediate superconductivity.^{5,6}

The possibility of studying materials that exhibit magnetic order and superconductivity simultaneously could shed a new light on the importance of magnetic correlations for the pairing mechanism of Cooper pairs in unconventional superconductors. In particular, our insight into high temperature superconductivity could greatly benefit from a detailed study of the interplay among intrinsic magnetism, penetration depth λ , and coherence length ξ .

From an applied point of view, the pinning of Abrikosov vortices in type-II superconductors is a central issue, as increased pinning forces F_P can greatly enhance both critical currents J_c and critical magnetic fields H_{c2} .⁷ The presence of an intrinsic magnetic field (with $B_{int} < H_{c2}$) can have a strong effect on F_P and may thus present an alternative to artificially introduced pinning centers.

The rare earth borocarbides $R\text{Ni}_2\text{B}_2\text{C}$ (with $R = \text{Dy}$, Ho , Er , and Tm) exhibit magnetism within the superconducting phase.¹ Conspicuously, their superconducting and magnetic transition temperatures are comparable, suggesting similar energy scales for magnetism and superconductivity.³ The observation of a pronounced isotope effect in these intermetallic compounds points towards conventional phonon mediated superconductivity.^{8,9} Of these borocarbides, $\text{ErNi}_2\text{B}_2\text{C}$ has a relatively high superconducting transition temperature of $T_c = 10.5$ K and develops antiferromagnetic order around $T_N = 6$ K.¹⁰ Remarkably, below $T_{WFM} = 2.3$ K a weak ferromagnetic phase can be detected with a net magnetic moment of $0.39\mu_B/\text{Er}$ and a resulting intrinsic magnetic field of about $B_{int} = 500 - 700$ G.^{11,12} Previous tunnel diode oscillator (TDO) experiments focusing on the magnetic penetration depth λ uncovered a pronounced temperature dependence with clear features at T_N and T_{WFM} , therefore indicating a strong impact of the magnetic properties on λ , as well as fingerprints of the formation of a spontaneous vortex lattice (i.e. induced by intrinsic magnetism) below T_{WFM} .¹³ At the same time, Bitter decoration experiments¹⁴ and scanning Hall probe measurements¹² revealed a microscopic variation of the intrinsic magnetic field emerging below T_N in the form of well-ordered, micrometer sized magnetic stripes, along which vortices tend to order. A spontaneous vortex phase in the weak ferromagnetic regime was not observed, though. However, the Bitter decoration experiments were conducted down to 1.9 K, which is only slightly below T_{WFM} , and the spatial resolution of scanning Hall probes is rather limited. In fact, until now no clear consensus on the issue of spontaneous vortex lat-

tice formation in $\text{ErNi}_2\text{B}_2\text{C}$ has been reached, partly due to its low ferromagnetic transition temperature. This open issue together with the microscopic variation of the magnetic field calls for a local probe investigation of $\text{ErNi}_2\text{B}_2\text{C}$ at sub-Kelvin temperatures.

Here we present a magnetic force microscopy (MFM) study on $\text{ErNi}_2\text{B}_2\text{C}$ at He-3 temperatures and with a high spatial resolution. We observe magnetic stripe-like features at $T = 500$ mK, that arise from twin domain boundaries. Their pronounced temperature behavior supports the spontaneous vortex formation scenario. Using the magnetic moment of the tip we estimate the pinning force of a single vortex. In addition, a spatially resolved determination of the penetration depth λ is presented for the first time, which reveals a close relation between λ and the microscopically varying intrinsic magnetism.

II. EXPERIMENTAL DETAILS

A single crystal of $\text{ErNi}_2\text{B}_2\text{C}$ was grown via Ni_2B flux growth technique.^{10,15} The sample's magnetic properties have been measured to determine T_c using an MPMS superconducting quantum interference device (Quantum Design, Inc.). The crystal orientation was determined by polarized Raman scattering experiments, using the orientation dependence of the B_{1g} phonon mode intensity.¹⁶ Prior to MFM measurements, the sample was mechanically polished to obtain a fresh surface within the ab plane with a roughness as small as 5 nm. MFM measurements were performed with a unique home-built He-3 MFM probe with a vector magnetic field capability ($2T - 2T - 9T$ along the x - y - z direction) and a temperature range of 320 mK – 300 K.¹⁷ All experiments were carried out with no magnetic fields applied and with a commercially available tip.¹⁸

III. EXPERIMENTAL RESULTS & DISCUSSION

We firstly discuss the origin of magnetic stripes and the local variation of the magnetic penetration depth, before moving on to the pinning force. Synchrotron x-ray scattering experiments on $\text{ErNi}_2\text{B}_2\text{C}$ revealed a structural tetragonal-to-orthorhombic distortion upon entering the antiferromagnetic phase at $T_N = 6$ K. This leads to the formation of twin domain boundaries below T_N along $[110]$ and $[1\bar{1}0]$,¹⁹ which are already inhabited by a ferromagnetic component aligned along the c axis.²⁰ In small applied magnetic fields (of the order of 10 G) vortices were found along the boundaries, thus forming stripes with roughly $5 \mu\text{m}$ spacing.²¹ The transition at T_{WFM} is driven by magneto-elastic coupling, which enhances Ruderman-Kittel-Kasuya-Yosida (RKKY) interactions among the Er $4f$ electrons, and thereby a long-range ordered weak ferromagnetism is induced in the bulk, as evidenced by inelastic neutron scattering ex-

periments.²² In our MFM data [see Fig. 1(a)] a structured magnetic background can be clearly seen in the form of bright stripes with a separation of $\approx 7.5 \mu\text{m}$ at $T = 500$ mK, i.e. deep within both the superconducting and the weak ferromagnetic phase. The stripes run from the lower right corner to the upper left corner [highlighted by dashed lines in Fig. 1(a)] and at 45° from the crystallographic a and b axes. We therefore ascribe the stripes to regions of increased ferromagnetism. Their orientation along the $[110]$ or $[1\bar{1}0]$ direction suggests a coincidence with twin domain boundaries.^{19,21} Indeed, magnetic stripes of the same orientation and comparable spacing have been observed in Bitter decoration experiments for $T < T_N$ and attributed to twin boundaries.^{14,20} However, the magnetic stripes in our experiment evidence a considerably different temperature behavior, as discussed further below.

In order to probe the influence of the varying internal magnetic field on the superconductivity in the sample, we performed local measurements of λ across two stripes along the blue arrow in Fig. 1(a). The determination of λ can be done by slowly bringing the tip to the surface at a fixed sample position and measuring the Meissner force gradient acting upon the magnetic tip. By comparing the Meissner force curves to those of a well-known standard sample (a Nb film), one can obtain the absolute values of λ .²³ In Fig. 1(b) we plot two Meissner force curves measured at the beginning (dashed black) and at the end (solid green) of the arrow. A clear shift is observed, indicating a spatial variation in λ . In the inset of Fig. 1(b) several absolute λ values at different positions (open squares) are plotted. These values, measured under the same conditions, vary by more than 20% within a few micrometers, while following closely the changes in the intrinsic ferromagnetism due to the stripe formation.²⁴ This is to be expected, as the magnetic penetration depth will be enhanced in the presence of an increased intrinsic magnetic field. In fact, we can reinterpret our MFM images in the superconducting state as maps of changes in λ .

The temperature dependence of λ [see Fig. 1(c)] can be well-described by a BCS-type behavior, i.e. $\lambda(T) = \frac{\lambda(0)}{\sqrt{1-(T/T_c)^2}}$, where $\lambda(0)$ is the penetration depth at $T = 0$ K. The fit yields $\lambda(0) \approx 190$ nm and $T_c \approx 9.1$ K. Our directly obtained penetration depth $\lambda(0)$ is larger than those previously reported from bulk probe experiments,^{10,25} while T_c is slightly below the reported value of 10.5 K. Aside from the different experimental approaches, it is known that the T_c of as-grown samples is lower than that of annealed samples.²⁶ Indeed, bulk magnetization measurements of our as-grown sample yield a T_c of 9.9 K [see red line in Fig. 1(c)]. Another important consideration is a possible deviation of $\text{ErNi}_2\text{B}_2\text{C}$ from the BCS behavior. In fact, a pronounced non-BCS-type behavior is apparent below T_c in the highly resolved temperature dependence of the TDO study,¹³ which is related to the different magnetic phases within the superconduct-

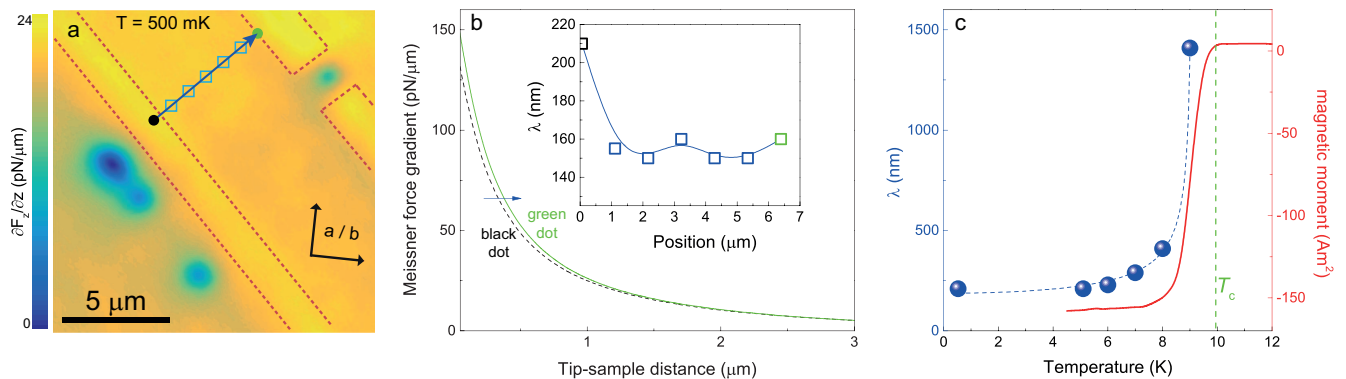


FIG. 1. (Color online) (a) A $15 \mu\text{m} \times 15 \mu\text{m}$ MFM image obtained at $T = 500 \text{ mK}$ and 300 nm tip-sample distance. The blue arrow marks a line of $6.5 \mu\text{m}$ length along which spatially resolved λ measurements were performed. The dashed lines outline the magnetic stripes. (b) Meissner force curves obtained at the beginning [i.e. black dot in (a)] and at the end of the arrow [i.e. green dot in (a)]. The inset shows local λ values along the blue arrow in (a). (c) Temperature dependence of λ obtained at a single position (blue spheres) and the magnetic moment measured at $H = 30 \text{ Oe}$ (solid red line). The dashed blue line is a fit according to the BCS theory.

ing regime. Since our temperature dependence is more coarse, a deviation from the BCS behavior could be obscured.

In addition to the magnetic stripes, we clearly see four separate vortices in Fig. 1(a). They are aligned antiparallel to the magnetic stripes, as indicated by the MFM contrast. Furthermore, they remain above T_{WFM} and even above T_N (as discussed below). Therefore, they exist independently of any intrinsic magnetic property. We ascribe these features to vortices induced by a weak external stray field. As this stray field is present regardless of the temperature (i.e. already above T_c , in contrast to the weak intrinsic ferromagnetism), its flux lines will be trapped inside $\text{ErNi}_2\text{B}_2\text{C}$ upon cooling through T_c . The observation of $n = 4$ vortices on a scan area of $A = 15 \times 15 \mu\text{m}^2$ could already be accounted for by $H_{stray} = \frac{n \cdot \Phi_0}{A} \approx 0.37 \text{ Oe}$, considering that each vortex corresponds to a flux quantum of Φ_0 . Although this estimation is somewhat rough due to our limited scan area, we expect that the stray field does not exceed 1 Oe , and is therefore below the accuracy of our vector magnet with a resolution of 1 Oe .

In order to study the depinning of vortices in $\text{ErNi}_2\text{B}_2\text{C}$, we manipulate the separate, stray field induced vortices via the tip-sample interaction. In Figs. 2(a) and 2(b) two $15 \mu\text{m} \times 15 \mu\text{m}$ MFM images are shown at $T = 1.5 \text{ K}$ and lift heights (LH) of 200 nm and 300 nm . The scan area corresponds to the one in Fig. 1(a). While at $LH = 200 \text{ nm}$ a manipulation of the lower vortices along the twin boundary is observed, an increase to $LH = 300 \text{ nm}$ leads to an image of static vortices. For all images the fast scan direction is horizontal, while the slow scan direction is vertical, from the bottom to the top. Note that the direction of the manipulated vortex motion always follows the bright stripe. We recall that the magnetic flux direction within the twin boundary is anti-parallel to that of the stray field vortices, as

evidenced by the opposing contrast that correspond to opposing magnetic forces acting on the tip. It is therefore energetically unfavorable for a separate vortex to move into the stripe. On the other hand, the upper right vortex caught between two domain boundaries can move neither up nor down and hence experiences a much stronger pinning. To estimate the pinning force of vortices as a function of temperature, we consider the magnetic force between tip and vortex, given by $F_{lv} = \frac{m\Phi_0}{2\pi} \cdot \frac{1}{[z+\lambda(T)]^2}$.²⁷ Here, $m = (3.7 \pm 0.2) \text{ nAm}$ is the magnetic moment per unit length of the tip, $\Phi_0 = h/2e$ is the magnetic flux quantum of a single vortex and z is the distance between tip and sample surface around which the vortex manipulation sets in. m has been estimated via monopole-monopole approximation.²⁷ Considering that at $T = 1.5 \text{ K}$ the onset of the vortex manipulation is at a tip-sample distance of $200 \text{ nm} - 300 \text{ nm}$, we can get a rough estimation of the pinning force F_P for vortices in the range of $5 - 8 \text{ pN}$.

When increasing the temperature from 1.5 to 4.5 K and thereby moving from the weak ferromagnetic phase into the antiferromagnetic phase, the magnetic stripes vanish while the twin boundaries remain [see Figs. 2(c) – 2(f)]. Hence, the background in the MFM images appears to be homogeneous. In contrast, stray field induced vortices remain as expected. In this intermediate temperature regime the pinning force is strongly reduced compared to the weak ferromagnetic phase. This is in good accordance with previous magnetization and transport experiments, where a threefold decrease in the relative F_P was reported when heating the sample up through T_{WFM} [see solid blue line in Fig. 2(g)].²⁸ Still, the direction of vortex manipulation remains along the twin boundaries, which continue to carry a reduced ferromagnetic component along the c axis and anti-parallel to the vortex flux. This agrees well with the previous Bitter decoration experiment, where field-induced vortex stripes occur

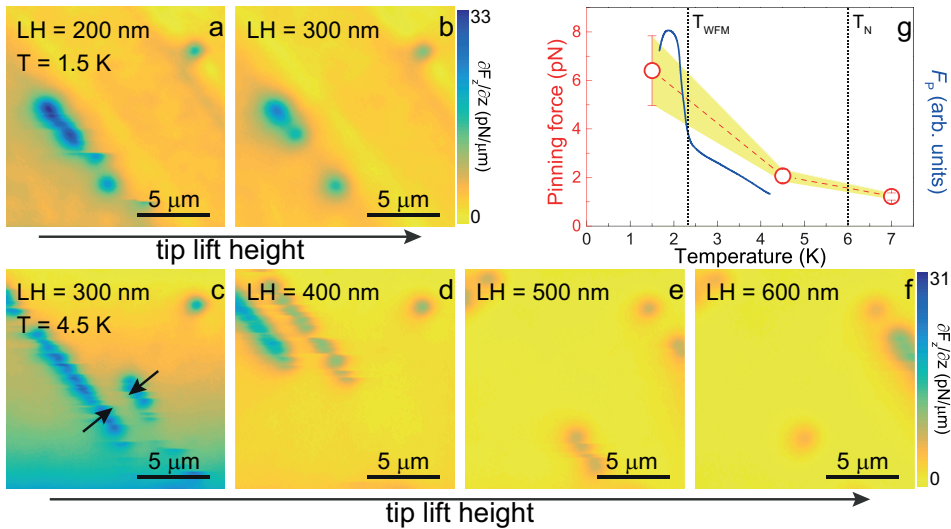


FIG. 2. (Color online) (a) and (b): MFM images taken at $T = 1.5$ K with 200 nm and 300 nm tip lift height (LH). (c) – (f): MFM images taken at $T = 4.5$ K with 300 nm, 400 nm, 500 nm, and 600 nm tip lift height. (g) The pinning force of the vortices obtained from MFM measurements as a function of temperature (red circles) compared to the pinning force estimated from measurements of the critical current I_c (solid blue line).²⁸

along $[110]$ and $[\bar{1}\bar{1}0]$.¹⁴ Their work reports parallel vortex stripes with $1 - 2 \mu\text{m}$ spacing, which is also confirmed by our observations of parallel vortex lines aligned on both sides of the twin boundaries [see arrows in Fig. 2(c)]. We manage to manipulate the vortex position at 4.5 K up to a tip-sample distance of 500 nm. Only at $LH \geq 600$ nm, a static vortex image is obtained, leading to a pinning force of 2.0 – 2.5 pN.

Moving from the magnetically ordered ($T < T_N$) into the paramagnetic superconducting regime ($T > T_N$), we study the vortex dynamics as a function of temperature at a constant LH of 700 nm (see Fig. 3). It is important to note that the vortex configuration changes strongly around $T_N = 6$ K [see Figs. 3(a) and 3(b)]. A detailed investigation of the critical current revealed a dynamic domain formation and annihilation in a narrow temperature regime around T_N , which leads to a considerable increase in antiferromagnetic antiphase domain boundaries on which vortices strongly get pinned.²⁹ These domain dynamics are evidenced by our observation of vortex rearrangements at $T = 6$ K. Above T_N , the structure relaxes from orthorhombic to tetragonal, leading to a disappearance of the twin boundaries, and hence to a random distribution of vortices. This is contrasted by the Bitter decoration study,¹⁴ where a clear hexagonal vortex lattice forms for $T > T_N$ in an applied field of 25 Oe. Since our stray field is too weak to induce a considerable vortex density, local impurities may dominate the vortex arrangement instead. The increasing thermal energy of the vortices allows a manipulation with a LH of 700 nm at 7 K and higher, as it leads roughly to a twofold reduction in the pinning force compared to $T = 4.5$ K. We estimate a pinning force at 7 K of around 1.0 – 1.5 pN. The temperature dependence of the pinning force F_P is plotted in Fig. 2(g). It mirrors the critical current behavior, which is closely related to F_P ,²⁹ as both exhibit roughly a twofold decrease between 4.5 and 7 K. Moreover, our F_P data is consistent with the observation of a finite J_c at $T > T_N$ in Ref. [29], which was previously

conjectured to vanish above the Néel temperature.³⁰ At 7 and 8 K in the absence of twin boundaries, there is no more preferred vortex manipulation direction. Instead, vortices are being dragged equally to the left and right while a general upwards trend in motion is observed, thus following the slow scan direction. Eventually, thermally enhanced vortex dynamics overcome the pinning potential and $\text{ErNi}_2\text{B}_2\text{C}$ transits into a vortex liquid phase between 8 K and 9 K, i.e. close to T_c .

Our MFM images also allow us to comment on the issue of the coexistence mechanism in $\text{ErNi}_2\text{B}_2\text{C}$. It is believed that magnetism and superconductivity can coexist under two possible scenarios: (i) a spontaneous formation of vortices^{31,32} or (ii) a variation of magnetic moments on a length scale smaller than the penetration depth λ .^{31,33} We clearly detect a modulation of the magnetic background over several micrometers. However, additional small-scale magnetic variations are not observed in our MFM images down to our resolution limit of 20 nm. Hence we do not find direct evidence for scenario (ii) from our data, although we cannot exclude possible magnetic variations on a smaller length scale than the instrumental limit. In addition, a phase separation between purely ferromagnetic and superconducting regions is not evident as the magnetic stripes still exhibit a Meissner force. On the other hand, scenario (i) is possible if the condition $H_{c1} < B_{int} < H_{c2}$ is fulfilled.³⁴ For $\text{ErNi}_2\text{B}_2\text{C}$, the critical fields H_{c1} and H_{c2} are around 500 Oe and 12 kOe (below T_{WFM}), respectively.¹¹ As $B_{int} = 500 - 700$ G,^{11,12} we have a system at hand in which the spontaneous formation of vortices could very well be realized at $T < T_{WFM}$. We can estimate the number of vortices n expected to appear in the presence of the intrinsic magnetic field. For a $15 \times 15 \mu\text{m}^2$ image as shown in Fig. 1(a) our estimation yields $n = \frac{B_{int} \cdot A}{\Phi_0} \approx 7600$ vortices. It is tempting to reinterpret the magnetic stripes below T_{WFM} as regions of ultra-high vortex density, where single vortices cannot be resolved separately anymore. Considering that the twin boundaries carry a ferromagnetic

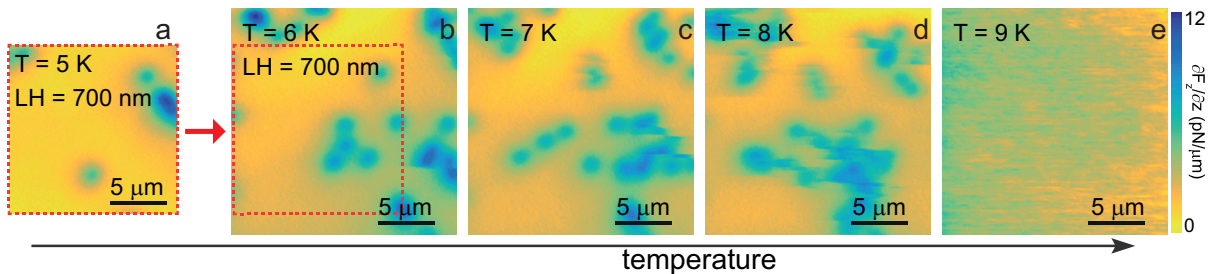


FIG. 3. (Color online) (a) A $15 \mu\text{m} \times 15 \mu\text{m}$ MFM image obtained at $T = 5 \text{ K}$, (b) – (e) $20 \mu\text{m} \times 20 \mu\text{m}$ MFM images taken at $T = 6 \text{ K}$, 7 K , 8 K , and 9 K . The lift height for all images was constant at 700 nm .

component aligned along the c axis,²⁰ and that the flux lines of the vortices induced by the weak intrinsic ferromagnetism run along the c axis as well, an accumulation of vortices in the vicinity of the twin boundaries could be energetically favorable. In this case the locally probed λ values in the striped region [see black / green dot, Fig. 1(a)] do not reflect the true penetration depth, as each force gradient curve has a contribution of both the Meissner force from the superconducting region as well as the magnetic force from the flux quanta. In a previous Bitter decoration study vortex stripes pinned along the $[100]$ direction have been observed at temperatures slightly below T_{WFM} and in applied magnetic fields of $15 - 20 \text{ Oe}$, which rearrange into a hexagonal vortex lattice above T_{WFM} .²¹ They were interpreted as a pinning of external field-induced vortices along ferromagnetic domains, that vanish above T_{WFM} [see Figs. 2(b) and 2(c)]. A spontaneous flux lattice, on the other hand, was not observed. In our experiments, carried out in negligible external magnetic fields, the stripes vanish completely above T_{WFM} . This is in stark contrast to several previous Bitter decoration experiments^{14,20,21} and further support for our scenario of the *spontaneous* vortex formation induced by the weak intrinsic ferromagnetic field. Note that also a slight rearrangement of stray field induced vortices can be found upon crossing T_{WFM} , which could result from an interaction with departing spontaneous vortices. In order to unambiguously prove the existence of spontaneous vortex stripes in $\text{ErNi}_2\text{B}_2\text{C}$, however, further experiments with a higher resolution or within a lower vortex density region (e.g., by applying an opposing magnetic field) are required in a narrow temperature regime around the weak ferromagnetic transition.

IV. SUMMARY

In summary, we have presented an MFM study of the magnetic superconductor $\text{ErNi}_2\text{B}_2\text{C}$ down to sub-Kelvin

temperatures. We introduced a straightforward method for locally determining the vortex pinning force F_P , as well as demonstrated for the first time a spatially resolved measurement of the penetration depth λ . Our measurements yield $\lambda(0) \approx 190 \text{ nm}$. Below T_{WFM} λ varies locally by more than 20% on a micrometer scale, while following closely changes in the intrinsic magnetic field. The pinning force of stray field induced vortices shows a strong temperature dependence that is related to the existence of various magnetic phases. We estimate the pinning forces to be around $1 - 8 \text{ pN}$, depending on the temperature. At the same time we find that F_P varies locally, and easy vortex manipulation directions exist in the magnetic phases, but are absent above T_N . Finally, a micrometer scale magnetic background detected at $T = 500 \text{ mK}$ that coincides with the twin domain boundaries and vanishes above T_{WFM} supports the scenario of spontaneous vortex stripe formation in $\text{ErNi}_2\text{B}_2\text{C}$.

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* Contributed equally to this work

† Corresponding author: jeehoon@postech.ac.kr

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