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Field-Induced Quadrupolar Quantum Criticality in PrV$_2$Al$_{20}$

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PrV$_2$Al$_{20}$ is a heavy fermion superconductor based on the cubic $\Gamma_3$ doublet that exhibits non-magnetic quadrupolar ordering below $\sim$ 0.6 K. Our magnetotransport study on PrV$_2$Al$_{20}$ reveals field-induced quadrupolar quantum criticality at $\mu_0H_c \sim 11$ T applied along the [111] direction. Near the critical field $\mu_0H_c$ required to suppress the quadrupolar state, we find a marked enhancement of the resistivity $\rho(H,T)$, a divergent quasiparticle effective mass and concomitant non-Fermi liquid (NFL) behavior (i.e. $\rho(T) \propto T^n$ with $n \leq 0.5$). We also observe the Shubnikov-de Haas effect above $\mu_0H_c$, indicating effective mass enhancement or $m^*/m_0 \sim 10$. This reveals the competition between the nonmagnetic Kondo effect and the intersite quadrupolar coupling which leads to pronounced NFL behavior in an extensive region of $T$ and $\mu_0H$ emerging from the quantum critical point.

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Quantum criticality in correlated electron systems has attracted significant attention because of the formation of novel quantum phases such as exotic superconductivity in the vicinity of a quantum critical point (QCP). Moreover, the breakdown of the standard Fermi-liquid behavior has been seen almost routinely nearby a magnetic QCP in a variety of strongly correlated electron systems, ranging from cuprates, iron pnictides and heavy fermion intermetallics. Whether another type of instability such as orbital ordering and its associated orbital fluctuations may drive novel types of metallic state and unconventional superconductivity has been an active area of research. Experimentally, however, quantum criticality due solely to an orbital origin was never observed in metallic systems.

For the study of quantum criticality, 4f-electron systems are well suited. These systems provide various archetypical examples due to the availability of high-purity single crystals and the relatively low characteristic energy scales which are highly tunable by disorder-free control parameters such as magnetic field or pressure. To date, among heavy-fermion intermetallics, most of the study on QC was performed on compounds containing either Ce (4f$^1$) or Yb (4f$^{13}$) (see, for example, Refs. 9–13) ions whose crystalline-electric-field (CEF) ground-state is composed of Kramers doublets and therefore is magnetic.

In transition metal systems, the coupling between spins and orbitals is unavoidable and produces various interesting spin-orbital ordered and disordered states. In contrast, an f-electron system may provide a nonmagnetic CEF ground-state doublet, where orbitals are the only active degree of freedom. In effect, some Pr (4f$^2$)-based cubic compounds are found to host the $\Gamma_3$ non-Kramers ground-state doublet, which has no magnetic moment but carries an electric quadrupole moment. In these systems, due to strong intra-atomic spin-orbit coupling, the total angular momentum $J$ represents the magnetic and orbital states, and in particular, the electric quadrupole moment corresponds to the orbital degree of freedom. A number of cubic 4f$^2$ $\Gamma_3$ systems were studied and various interesting electric phenomena were experimentally reported including a ferro and antiferro quadrupolar ordering depending on the type of the RKKY-type interaction. As a competing effect, a nonmagnetic form of the Kondo effect is proposed that quenches the quadrupole moments. Thus, the tuning of these competing effects may lead to quadrupolar QC.

In fact, quadrupolar quantum criticality was suggested by recent experiments on the new cubic $\Gamma_3$ systems PrT$_2$Al$_{20}$, where $T$ corresponds to a transition metal such as Ti and V. In these systems, the hybridization between the f-moments and the conduction (c-) electrons is found to be not only strong but tunable. The strong c-f hybridization is evident from a number of observations, including the Kondo-effect in the resistivity (i.e. $\rho(T) \propto -\ln T$), a Kondo-resonance peak observed near the Fermi-energy, and a large hyperfine constant in the NMR measurements. The tunability of the hybridization strength in PrT$_2$Al$_{20}$ is demonstrated by both chemical and physical pressure measurements: the substitution of Ti by V enhances the Kondo-effect and induces an anomalous metallic behavior due to the hybridization. PrT$_2$Al$_{20}$ exhibits a ferro-quadrupole ordering at $T_Q = 2$ K with a subsequent superconducting (SC) transition at $T_c = 0.2$ K. While the SC effective mass of PrT$_2$Al$_{20}$ is moderately enhanced under ambient pressure, i.e. $m^*/m_0 \sim 16$ ($m_0$ is the free electron mass), the application of pressure increases $T_c$ up to 1 K and $m^*/m_0$ up to 110 at $P \sim 8$ GPa, while suppressing $T_Q$. This indicates that the pressure-induced heavy-fermion superconductivity emerges in the vicinity of a putative quadrupolar QCP.

Evidence for strong hybridization in PrV$_2$Al$_{20}$ is fur-
ther provided by the recent discovery of heavy-fermion superconductivity at $T_c = 50$ mK with a large specific heat jump $\Delta C/T \sim 0.3$ J/mol K$^2$ below $T_Q = 0.6 - 0.7$ K under ambient pressure$^{26}$. The effective mass of the quasiparticles participating into the superconducting condensate is found to be as large as $140 m_0$, which is one order of magnitude larger than that of its Ti analog$^{24}$. This result indicates that Pr$_2$Al$_2$O$_{19}$ should be located in the vicinity of a QCP associated only with multipole moments.

To realize such quantum criticality due to multipole moments, the magnetic field is another useful control parameter that couples quadratically with quadrupole moments, thus more weakly than with magnetic moments. The high-field phase diagram of Pr$_2$Al$_2$O$_{19}$ was investigated through specific-heat measurements under fields up to 9 T applied along all three main crystallographic orientations. Overall, the low-field phase boundaries for the [100], [110] and [111] directions are very similar to one another and nearly independent of $\mu_0 H$, as often observed in various quadrupolar ordered systems$^{20,23}$. Moreover, high field magnetization measurements revealed a field-induced first-order transition at $\mu_0 H \sim 11$ T for $H_\parallel[100]$ which is most likely due to the switching of the quadrupole order parameter in the $\Gamma_3$ ground doublet$^{29}$.

Here, we report the discovery of field-tuned quantum criticality based solely on the quadrupolar (orbital) degrees of freedom at ambient pressure in Pr$_2$Al$_2$O$_{19}$. We studied, through magneto-transport measurements, the magnetic phase diagram of Pr$_2$Al$_2$O$_{19}$ for $H_\parallel[111]$. We found unusual non-Fermi liquid behavior, i.e. $\rho = \rho_0 + AT^n$ with $n \leq 0.5$, a divergent quasiparticle effective mass and a large enhancement in the residual resistivity $\rho_0$ around the magnetic field-induced quantum-phase transition at the critical-field $\mu_0 H_c \sim 11$ T, where the quadrupolar transition temperature is suppressed to absolute zero. In addition, our observation of quantum oscillations reveal a heavy mass state with $m^*/m_0 > 10$ in the paraquadrupolar state beyond $\mu_0 H_c$, indicating non-magnetic Kondo effect competing with the quadrupolar coupling as the origin of the pronounced quantum criticality observed over an extensive region of $T$ and $\mu_0 H$. The experimental condition is described in detail in the supplemental material$^{20}$.

The temperature dependence of the resistivity $\rho(T)$ in both the low field ($\mu_0 H \leq 8$ T) and the high field ($\mu_0 H \geq 9.5$ T) regions, is presented in Figs. 1(a) and 1(b), respectively. Both the magnetic field and the electric currents were applied along the [111] direction. When the field is lower than 10 T, one observes a sudden decrease in $\rho(T)$ upon cooling due to the quadrupolar phase-transition. Correspondingly, a peak is observed in the $T$ derivative of the resistivity at a low temperature $T_Q$ which systematically changes with field, as shown in Fig. 1(c). On the other hand, the resistivity under fields surpassing 11 T shows such a smooth temperature dependence that the anomaly associated with the quadrupolar ordering no longer exists. Thus, a quantum phase transition between the low-field quadrupolar and high-field paraquadrupolar phases should be located at $\mu_0 H_c \sim 11$ T. Such a field-induced suppression of a quadrupolar phase was predicted for the Pr$_2$Al$_2$O$_{19}$ system using a mean-field theory based on a localized picture$^{31}$. Previous magnetization measurements$^{29}$ for fields aligned along [111]-direction did not detect evidence for an ordered state in contrast to what is observed for fields aligned along the [100]-direction. This is consistent with our results.

Under a field of 11 T the resistivity displays a sub-linear dependence on $T$, which contrasts markedly with the Fermi liquid behavior, i.e. $\rho \propto T^2$, shown in the inset of Fig. 1(b). In contrast, for fields beyond 15 T the resistivity displays a super-linear or $T^2$-dependence.
at the lowest temperatures as seen in Fig. 1 (b). A detailed analysis of the field and temperature dependence of \( \rho \) will be described below. Figure 1(d) displays the field dependence of the magnetoresistivity for \( T < 1 \) K. \( \rho(H) \) exhibits a sharp peak at \( \mu_0 H_c \sim 11 \) T. In addition, below 10 T it displays a marked drop as the temperature is reduced below \( T = 0.6 \) K, due to the transition towards quadrupolar ordered state. If this peak resulted solely from thermal critical fluctuations associated with a finite temperature transition between the quadrupolar phase to the paraquadrupolar state, this peak would be expected to shift to lower fields with increasing \( T \) and eventually reach zero field near \( T_Q \sim 0.6 \) K. However in \( \text{PrV}_2\text{Al}_{20} \), a pronounced peak is still observed at nearly the same field \( \sim 11 \) T at \( T \sim 1 \) K >> \( T_Q \), indicating the development of quantum critical scattering at \( \sim \mu_0 H_c \) and at much higher \( T \)'s than \( T_Q \). In addition to the main peak at \( \sim 11 \) T, a small peak was observed below 2 T in the quadrupolar ordered state below 0.6 K. This may be associated with the change in the order parameters such as the lifting of the degeneracy between the \( O^0_6 \) and \( O^2_2 \) states.

To clearly illustrate the field-induced enhancement of the resistivity above \( T_Q \), Fig. 2(a) shows a contour plot of \( \rho \) as a function of both \( T \) and \( H \parallel [111] \). The change in color between blue and green at \( \sim 0.5 \) K found below 10 T follows the quadrupolar transition temperature \( T_Q \) (squares) determined by the temperature scans discussed above. This line of \( T_Q \) connects smoothly with the line depicting the peak position (circle) in the field dependence of the resistivity \( \rho(H) \). These results indicate that the peak in the magnetoresistance at low temperatures corresponds to the quadrupolar phase boundary (solid line in Fig. 2(a)), which reaches the quantum critical point at \( \mu_0 H_c \sim 11 \) T.

Remarkably, the peak observed in \( \rho(H) \) around 11 T survives up to \( \sim 1 \) K > \( T_Q \) as discussed above, and this pronounced peak in \( \rho(T, H) \) (red region in Fig. 2(a)), which is observed in the paraquadrupolar regime cannot be explained within a simple localized f-moment scenario. Figure 2 (b) shows \( \rho(T) \) as a function of \( T^{1/2} \) at \( \mu_0 H = 11 \) T near the quantum-critical field. \( \rho(T) \) under \( \mu_0 H = 11 \) and 11.5 T shows a concave curvature, indicating that the exponent \( n \) in \( \rho(T) = \rho_0 + A T^n \) is even smaller than 0.5. On the contrary, above 15 T, \( \rho(T) \) exhibits a convex curvature indicating the emergence of Fermi liquid behavior at the lowest \( T \)'s, as shown in Fig. 1 (b). The characteristic temperature \( T_{FL} \) below which \( \rho(T) \) displays FL-behavior or \( \rho(T) = \rho_0 + A T^2 \) increases with field (Fig. 2 (a)). Figure 2 (c) indicates the field dependence of \( A^{-1/2} \) obtained from \( \rho(T) \) above 15 T. Accordingly, upon approaching the quantum-critical field, the corresponding \( A \) values diverge, exceeding \( \sim 5 \, \mu\Omega\text{cm}/K^2 \). It can be fit to \( \sqrt{A} = \sqrt{A_0}/(\mu_0 H - \mu_0 H_A^A) \) with \( \sqrt{A_0} = 8.92 \, (\mu\Omega\text{cm}/K^2)^{1/2} \), and \( \mu_0 H_A^A = 10.5 \) T (Fig. 2(c)). Significantly, \( \mu_0 H_A^A \) is found to be consistent with the critical field \( \sim 11 \) T determined by the peak in \( \rho(H) \). According to the Kadowaki-Woods relation, the critical enhancement in \( A^{1/2} \) indicates the divergence of the effective mass upon approaching the QCP.

The sharp magnetoresistance peak at \( \mu_0 H_c \sim 11 \) T, which is observed even above \( T_Q \), indicates a significant role for hybridization effects in the quantum criticality. In effect, at a pressure-induced quantum critical point, the enhancement in the residual resistivity has been reported and attributed to quantum critical fluctuations. In Pr-based compounds with a \( \Gamma_3 \) ground doublet, such an enhancement in \( \rho_0 \) was also observed under zero field, especially above \( \sim 7 \) GPa in \( \text{PrTl}_2\text{Al}_{20} \), which is accompanied by the suppression of the quadrupole-order. \( T_c \) as well as the effective mass \( m^* \) also increase considerably above \( \sim 7 \) GPa, while \( T_Q \) starts to decrease, suggesting...
the proximity to a putative quantum critical point\textsuperscript{25}. In Pr\textsubscript{2}Al\textsubscript{20}, the similarly dramatic enhancement in both $\rho_0$ and in $m^*$ $\sim A^{1/2}$ under magnetic field, coupled to the anomalous $T$-dependence of the resistivity at the critical field $\mu_0 H_c \approx 11$ T, provides firm experimental evidence for field-induced quantum criticality based on the strong hybridization between the conduction electrons and the nonmagnetic quadrupolar / orbital degrees of freedom in the $\Gamma_3$ ground doublet. As discussed above, the resistivity follows $\rho = \rho_0 + AT^n$, with $n \leq 0.5$ at $\mu_0 H_c$, in sharp contrast to $n = 1$ and $1.5$, which are usually observed around a QCP in Ce/Yb based heavy-fermion compounds with a ground Kramers doublet\textsuperscript{9–13}.

Finally, the high-quality of our single crystals allows us to observe the Shubnikov-de Haas (SdH) effect above the critical field. Figure 3(a) illustrates a representative trace of the oscillatory signal superimposed into $\rho(H)$ (after subtraction of a polynomial fit) at $T = 70$ mK as a function of inverse field $1/\mu_0 H$, under fields aligned at an angle $\theta = 75^\circ$ away from the [111] direction and beyond the critical value required to suppress the quadrupolar state. The corresponding fast Fourier-transform spectra is shown in Fig. 3 (b) for two values of $T$, respectively at 60 mK (dark blue trace) and 220 mK (clear blue trace). One observes two main small frequencies $F_1 \sim 190$ T and $F_2 \sim 290$ T. The FFT spectra for $H$ at an angle $\theta = 75^\circ$, at $T = 70$ mK (dark orange trace) and 410 mK (brown trace) respectively, revealing a higher frequency $F_3 \sim 2$ kT.

An important piece of information is provided by the inset in Fig. 3 (b) which displays the amplitude of the FFT peaks as a function of $T$: solid lines are fits to the Lifshitz-Kosevich thermal damping term, i.e. $X/\sinh X$ with $X = 4\pi^3 k_B m^* T/eH$ (where $k_B$ is the Boltzmann constant, and $e$ is the electron charge) from which we extract the effective mass $m^*$ for each $F$. The resulting mass values are $m_1^* = (5.7 \pm 1.2) m_0$, $m_2^* = (6.8 \pm 1.2) m_0$ and $m_3^* = (10.6 \pm 1.2) m_0$, which are still moderately heavy, indicating the presence of the nonmagnetic Kondo effect based on the $c - f$ hybridization. This indicates that the nonmagnetic Kondo effect has a much higher energy scale than the CEF gap at the critical field\textsuperscript{30}. Thus, the quantum-critical behavior unveiled here cannot be ascribed to an $f$-electron localization transition involving the suppression of the Kondo-effect at low fields. The charge carriers are so heavy as $m^* \approx 140 m_0$ at zero-field, and still display moderately heavy masses at high fields. dHvA measurements were performed also in the isostructural compound Pr\textsubscript{2}Ti\textsubscript{2}Al\textsubscript{20} which displays ferro-quadrupole ordering below $2$ K\textsuperscript{32}. The effective masses extracted for the various Fermi surface sheets range between 0.52 and 0.82 $m^*/m_0$. These values are considerably smaller than the masses, ranging from 5.7 to 10 $m^*/m_0$, observed in Pr\textsubscript{2}V\textsubscript{2}Al\textsubscript{20}. This difference in effective masses is qualitatively consistent with much heavier masses for Pr\textsubscript{2}V\textsubscript{2}Al\textsubscript{20}, or $\sim 140 m_0$, versus $\sim 16 m_0$ for Pr\textsubscript{2}Ti\textsubscript{2}Al\textsubscript{20} as estimated from their superconducting transition under zero field. In contrast with the divergence found in the $A$ coefficient as $\mu_0 H \rightarrow \mu_0 H_c$, we could not detect any evolution of the cyclotron masses upon approaching the QCP thus indicating that other, probably undetected, Fermi surface sheets are involved in the QC phenomenology displayed by Pr\textsubscript{2}V\textsubscript{2}Al\textsubscript{20}, and that the detected cyclotronic orbits remain oblivious to the quantum fluctuations associated with orbital degrees of freedom. The observation of the SdH signal paves the path to further clarifying its electronic structure and to understanding the strong screening effects leading to the quadrupolar quantum criticality involving the prominent non-Fermi liquid behavior observed in Pr\textsubscript{2}V\textsubscript{2}Al\textsubscript{20}.

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30. See Supplemental Material, which includes Refs. [33, 34, 35] at [URL will be inserted by publisher] for the experimental method and the analysis of the CEF under magnetic field.