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Reconciliation of local and long range tilt correlations in underdoped $La_{2-x}Ba_xCuO_4$ ($0 \le x \le 0.155$)

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A long standing puzzle regarding the disparity of local and long range CuO_6 octahedral tilt correlations in the underdoped regime of $La_{2-x}Ba_xCuO_4$ is addressed by utilizing complementary neutron powder diffraction and inelastic neutron scattering (INS) approaches. This system is of interest because of the strong depression of the bulk superconducting transition at x = 1/8 in association with charge and spin stripe order. The latter unidirectional order is tied to Cu-O bondlength anisotropy present in the so-called low-temperature tetragonal (LTT) phase. On warming, the lattice exhibits two sequential structural transitions, involving changes in the CuO_6 tilt pattern, first to the low-temperature orthorhombic (LTO) and then the high-temperature tetragonal (HTT) phase. Despite the changes in static order, inspection of the instantaneous local atomic structure suggests that the LTT-type tilts persist through the transitions. Analysis of the INS spectra for the x = 1/8 composition reveals the dynamic nature of the LTT-like tilt fluctuations within the LTO and HTT phases. Within the low-temperature phase, the Cu-O bond-length splitting inferred from lattice symmetry and fitted atomic position parameters reaches a maximum of 0.3% at x = 1/8, suggesting that electron-phonon coupling may contribute to optimizing the structure to stabilize stripe order. This splitting is much too small to be resolved in the pair distribution function, and in fact we do not resolve any enhancement of the instantaneous bond-length distribution in association with stripe order. This study exemplifies the importance of a systematic approach using complementary techniques when investigating systems exhibiting a large degree of complexity and subtle structural responses.

I. INTRODUCTION

Since the discovery of high-temperature superconductivity in $La_{2-x}Ba_xCuO_4$ [1], the connection between the lattice and electronic structures has been the subject of considerable attention [2, 3]. The further discovery [4] of the "1/8 anomaly"—a dramatic dip in the superconducting transition temperature T_c at the dopant concentration of x = 1/8—motivated careful powder diffraction studies of the structural phase diagram [5–8]. The latter revealed a low temperature transition (~ 60 K) to a crystal structure with inequivalent Cu-O bonds in orthogonal directions within the CuO_2 planes. It is this structural anisotropy, associated with a particular pattern of tilts of the CuO_6 octahedra, that pins charge stripes [9, 10]. While the charge stripes are compatible with superconducting correlations within the CuO_2 planes [11, 12], the 90° rotation of the structural anisotropy from one layer to the next leads to frustration of the interlayer Josephson coupling and the depression of the onset of bulk superconducting order [13, 14].

Given the strong response of the electronic properties to the crystal symmetry, it is of considerable interest to understand the nature of the structural transitions in $La_{2-x}Ba_xCuO_4$. Both powder [8, 15] and single-crystal [16–18] diffraction studies clearly demonstrate that the transition to the low-temperature structure, involving a change in tilt direction of the CuO₆ octahedra, is of first order. A surprisingly different perspective is given by a pair-distribution-function (PDF) analysis of neutron scattering measurements [19]. In the latter analysis, the local structure appears to be unaffected by warming through the transition, retaining the low-temperature tilt pattern to higher temperatures. That picture is supported by an x-ray absorption fine structure (XAFS) study [20]. Furthermore, the local tilts appear to remain in the high-temperature phase where the average tilts are zero [20–22]. The aim of the present paper is to resolve the apparent conflict between local and long-range measures of tilt correlations in La_{2-x}Ba_xCuO₄.

In terms of the symmetry of the average structure, the thermal sequence of structural transitions is well understood [23]. The high-temperature tetragonal (HTT) phase (space group I4/mmm) has the highest symmetry, with no octahedral tilts (see Table I and Fig. 1); here, the in-plane lattice parameters, $a_t = b_t$, correspond to the shortest Cu-Cu distance. On cooling, there is a second-order transition to the low-temperature orthorhombic (LTO) phase (space group Bmab), involving tilts of the CuO₆ octahedra about $[110]_t$ axes of the HTT phase; as nearest-neighbor octahedra must rotate in opposite directions, the unit cell volume increases by

TABLE I. Wyckoff positions for atomic sites in each of the structural phases, which are identified by acronym and space group. We distinguish between cases where orthogonal Cu-O(1) bonds are equivalent (OE) or inequivalent (OI); note that all O(1) sites are equivalent in OE phases, but that there are two inequivalent O(1) sites in the OI phases. Relative to the HTT phase, the other structures have a doubled unit cell volume.

	$\begin{array}{c} \text{HTT} \\ I4/mmm \\ \text{OE} \end{array}$	LTO Bmab OE	LTLO Pccn OI	$\begin{array}{c} \text{LTT} \\ P4_2/ncm \\ \text{OI} \end{array}$
Cu	2(a): 0, 0, 0	4(a): 0, 0, 0	4(a): 0, 0, 0	4(d): 0, 0, 0
O(1)	$4(c): 0, \frac{1}{2}, 0$	8(e): $\frac{1}{4}$, $\frac{1}{4}$, z	4(c): $\frac{1}{4}$, $\frac{1}{4}$, z 4(c): $\frac{1}{4}$, $\frac{3}{4}$, z	4(e): $\frac{1}{4}$, $\frac{1}{4}$, z 4(e): $\frac{1}{4}$, $\frac{3}{4}$, 0
La, Ba, $O(2)$	4(e): 0, 0, z	8(f): 0, y , z	8(e): x, y, z	8(i): x, x, z



FIG. 1. (Color online) Structural details of $La_{2-x}Ba_xCuO_4$. La/Ba are shown as large green spheres, Cu as intermediate blue spheres, and O as small red spheres. (a) Basic structural motif is shown for I4/mmm (HTT) phase, featuring CuO₆ octahedral unit and La/BaO₉ cage. O(1) and O(2) denote planar and apical oxygen respectively. Panels (b)-(e) highlight various aspects of the average crystal structures as follows: CuO₆ octahedral tilt symmetry (top row), in-plane bond-length distribution within CuO₄ plaquette (middle row), and dispersion of La/Ba-O distances within the La/BaO₉ cage (bottom row). Equal interatomic distances are represented by the same color. HTT denotes high temperature tetragonal (I4/mmm), LTO is low temperature orthorhombic (Bmab), LTT is low temperature tetragonal ($P4_2/ncm$), and LTLO is low temperature less orthorhombic (Pccn). The underlying in-plane symmetry is OE in HTT and LTO models, and OI in LTT and LTLO models, as indicated.

a factor of two, with $a_o \approx b_o \approx \sqrt{2}a_t$. (This is the structure of $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ in the superconducting phase [24].) Further cooling leads to a second transition involving a change in the octahedral tilt axis towards the $[100]_t$ and $[010]_t$ directions. When the shift in the tilt axis is complete, the structure is the low-temperature tetragonal (LTT; space group $P4_2/ncm$), while a partial shift results in the low-temperature less-orthorhombic (LTLO; space group Pccn); in both cases, the unit cell size is the same as for LTO.

For charge ordering, the key distinction among these different phases is the degree of symmetry among the Cu-O bonds. The tilt pattern in the LTO phase leaves the Cu-O bonds in (approximately) orthogonal directions equivalent; we will denote such a symmetry as "orthogonal equivalent" (OE). In contrast, the tilt of an octahedron about a $[100]_t$ axis, as in the LTT phase, leaves two in-plane oxygens within the CuO₂ plane but shifts the orthogonal pair above and below the plane; together with slight distortions of the octahedra to satisfy the tetragonal lattice symmetry, this results in inequivalent O(1) sites (see Table I) and two different Cu-O bond lengths. We will label this case as "orthogonal inequivalent" (OI), and note that the LTLO phase also has an OI symmetry. The phase diagram for the relevant range of doping in La_{2-x}Ba_xCuO₄ is shown in Fig. 2(a).

The structural transformations have been analyzed in terms of a Landau-Ginzburg model, in which the degenerate octahedral tilts about $[110]_t$ and $[1\overline{10}]_t$ axes are taken as the order parameters [5, 23]. When only one



FIG. 2. (Color online) (a) Average structure (x, T) phase diagram of LBCO which has been replotted to highlight whether the structure is OE or OI. Open symbols and solid lines are from Hücker et al. [17], solid symbols are from the present study. Shaded are regions of interest for this study having average OE (HTT and LTO) and OI (LTLO/LTT) symmetries, as indicated. (b) Local structure phase diagram with phase designations based on the results presented in this study. Please see text for definitions of OE and OI.

order parameter is finite, one obtains the LTO phase; when both are finite and equal, the structure is LTT. This model allows an elegant analysis of the phase diagram, and predicted the possible occurrence of the LTLO phase as confirmed in a closely-related system [25]. It has also motivated detailed studies of the octahedral tilts in $La_{2-x}Sr_xCuO_4$ [26–28], $La_{1.65}Nd_{0.35}CuO_4$ [29], and $La_{2-x}Ba_xCuO_4$ [30, 31]; however, these studies have been done at points of reciprocal space that have a finite structure factor for both LTO and LTT-like tilts. Hence, while these measurements have been interpreted in terms of LTO-like (OE) tilts, they could not uniquely distinguish the fluctuations from LTT-like (OI) tilts.

Helpful guidance is provided by a calculation of the potential-energy surface as a functional of octahedral tilts performed with density functional theory for a rough model of $\text{La}_{2-x}\text{Ba}_x\text{CuO}_4$ with x = 0.10 [32]. The calculation finds that the lowest energy is given by LTT tilts, with local minima corresponding to LTO tilts higher in energy by about 15 meV. It was proposed that the LTO phase might be stabilized with increasing temperature due to the entropy associated with low-energy octahedral tilt fluctuations [32]. This proposal gained support from a Monte Carlo study of the temperature dependence of a model including both the mean-field potential energy and interactions between neighboring octahedra [33]. The latter calculation yielded evidence for strong local LTT-like tilt amplitudes throughout the LTO phase.

In this paper, we present neutron total scattering measurements on polycrystalline samples of $La_{2-x}Ba_xCuO_4$ with x = 0.095, 0.125, and 0.155 obtained as a function of temperature. We analyze these data sets both by Rietveld refinement and by the pair distribution function analysis technique. The two approaches yield complementary evidence for dynamical LTT-like tilts within the LTO phase, as well as local tilt fluctuations in the HTT phase. We directly confirm the LTT-like tilt fluctuations in the LTO phase through inelastic neutron scattering measurements on a single crystal of $La_{2-x}Ba_xCuO_4$ with x = 0.125.

The rest of the paper is organized as follows: In Sec. II we describe the experimental and analysis methods, and the choice of reciprocal lattice used to index the reflections. In Sec. III we present three subsections dedicated to our results on average crystal structure, local structure, and octahedral tilt dynamics. In Sec. IV we discuss the various properties as a function of the nominal Ba content and temperature, compare our results with the literature, and in Sec. V finish with a short summary.

II. EXPERIMENTAL

Finely pulverized samples of $La_{2-x}Ba_xCuO_4$, with Bacontent in the $0.095 \le x \le 0.155$ range, as well as an undoped La₂CuO₄ polycrystalline reference, were grown using standard solid state protocols; these were used for the total scattering atomic PDF experiments. Neutron timeof-flight measurements were carried out on the NPDF instrument at Los Alamos Neutron Scattering Center at Los Alamos National Laboratory. Powders (15 grams each) were loaded under helium atmosphere into standard extruded vanadium containers and sealed. Temperature dependent measurements in the 15 K $\leq T \leq$ 550 K range were performed using a closed cycle cryo-furnace sample environment for 2 hours at each temperature on each sample, yielding good statistics and a favorable signal to noise ratio at high momentum transfers. Raw data were normalized and various experimental corrections performed following standard protocols [34]. High resolution experimental PDFs were obtained from the Sine Fourier transform of the measured total scattering structure functions, F(Q), over a broad range of momentum transfers, Q ($Q_{\text{max}} = 28 \text{ Å}^{-1}$). Data reduction to obtain the PDFs, G(r), was carried out using the program PDFGETN [35]. The average structure was assessed through Rietveld refinements [36] to the raw diffraction data using GSAS [37] operated under EXPGUI [38], utilizing I4/mmm (HTT), Bmab (LTO), P4₂/ncm (LTT), and Pccn (LTLO) models from the literature [17]. Structural refinement of PDF data was carried out using PDF-FIT2 operated under PDFGUI [39] using the same models.

The single crystal of $La_{2-x}Ba_xCuO_4$ with x = 0.125was grown using the traveling-solvent floating zone method and has been characterized previously, as described elsewhere [17]. The crystal, of size $\phi \sim 8 \text{ mm} \times 20 \text{ mm}$, was studied by inelastic neutron scattering using the HYSPEC instrument (beam line 14B) at the Spallation Neutron Source, Oak Ridge National Laboratory [40]. For the experiment on HYSPEC, the crystal was mounted in a Displex closed-cycle cryostat. With the *c* axis vertical, scattering wave vectors $\mathbf{Q} = (H, K, 0)$ are in the horizontal scattering plane. A fixed incident energy of 27 meV and a chopper frequency of 300 Hz were used for all data shown here, and the graphite-crystal array in the incident beam was put in the flat mode (no vertical focusing) to improve the resolution along Q_z . For a typical measurement, the position-sensitive detector tank was placed at a particular mean scattering angle, and then measurements were collected for a series of sample orientations, involving rotations about the vertical axis in steps of 0.2°. From such a set of scans, a four-dimensional data set was created and analyzed with the MANTID [41] and DAVE [42] software packages. Slices of data corresponding to particular planes in energy and wave-vector space can then be plotted from the larger data set. Wave vectors will be expressed in units of $(2\pi/a, 2\pi/b, 2\pi/c)$ with a = b = 5.355 Å and c = 13.2 Å, corresponding to the LTT phase.

The measurements of the soft phonon that tilts along the Cu-O bonds were performed in the vicinity of the (330) position, which corresponds to a superlattice peak in the LTT but not the LTO phase. To sample the fluctuations associated with the tilts of the LTO phase, it was necessary to tilt the sample so as to put (032) in the scattering plane. We then looked at the behavior along (H, 3, 2).

III. RESULTS

A. Average crystal structure

Typical Rietveld fits are shown in Fig. 3 for reference. The resulting temperature evolution of the in-plane lattice parameters is shown in Fig. 4, where the vertical dashed lines indicate the temperatures of the structural phase transitions. These are in good agreement with published work [17], as indicated in the phase diagram shown in Fig. 2.

Figure 5 shows the evolution of the Rietveld refined average in-plane Cu-O distances. Undoped La_2CuO_4 is in the LTO phase down to the lowest temperature and has a single Cu-O planar-bond length (solid black circles in all panels of Fig. 5), highlighting the OE nature of the LTO tilts. The biggest effect on doping is a significant shortening of the average Cu-O bond-length, highlighted by the red arrows in Fig. 5. This is due to the decrease in electronic charge in the Cu-O bonds, which are stabilized because charge is removed from anti-bonding states. At low temperature, where the doped samples enter the LTT/LTLO phase [17], Rietveld analysis reveals two distinct Cu-O bond-lengths consistent with the OI tilts.

It is noteworthy that the difference in the in-plane Cu-O bondlengths of doped samples at base temperature is quite small—0.005(1) Å at most at 20 K, as indicated by the blue double arrows in Fig. 5(a)-(c). This may be compared to the distortions of ~0.25 Å observed in the ground state of LaMnO₃ due to the cooperative Jahn-Teller effect [43, 44], which are nearly two orders of magnitude larger. Nonetheless, because they are long-range ordered and can be observed crystallographically, such a small difference in the average bond-lengths can be reliably measured, giving us a direct indication of the bro-



FIG. 3. (Color online) Rietveld fits of the average structure models to LBCO data at 15 K. Closed blue symbols represent the data, solid red lines are the models, and solid green lines are the differences (offset for clarity). Vertical ticks mark reflections. (a) x = 0 using *Bmab* model, (b) x = 0.095 using *Pccn* model, (c) x = 0.125 using $P4_2/ncm$ model, and (d) x = 0.155 using *Pccn* model.

ken symmetry between orthogonal Cu-O bonds. Notably, despite the average tilt angles decreasing monotonically with increasing doping we see that the bond length mismatch (the difference between the x and y bond lengths) increases from x = 0.095 to x = 0.125 before decreasing again at x = 0.15, suggesting a stronger electronic stabilization of the orthogonal inequivalency around 1/8 doping.

The first-order character of the low-temperature transition has a signature in the temperature dependence of the orthorhombic strain, shown in the insets to Fig. 4 (b)-(d). On cooling through the LTO phase, the strain grows with decreasing temperature. This growth slows as the low-temperature transition is approached so that at ~ 30 K above the low-T transition the average orthorhombicity even decreases, followed by a sharp drop at the transition. The small decrease in strain on approaching the transition is consistent with the presence of a 2-phase coexistence region, as identified in past studies [8, 17, 18, 45].



FIG. 4. Temperature evolution of in-plane lattice parameters of $La_{2-x}Ba_xCuO_4$ obtained from Rietveld refinements for: x = 0 (a), x = 0.095 (b), x = 0.125 (c), and x = 0.155(d). HTT parameters are given in F4/mmm setting. Vertical dashed lines indicate crystallographic phase transitions as specified in the text. Insets to (b)-(d) display temperature evolution of the lattice orthorhombicity ($\eta = 2(a-b)/(a+b)$) for doped samples, with their maxima marked by vertical arrows. Vertical dashed lines indicate low temperature structural phase transitions. Sloping dashed straight lines are guides to the eye emphasizing anomalous trends seen in highlighted regions and discussed in the main text.



FIG. 5. (Color online) Temperature evolution of the average in-plane Cu-O bondlengths (solid blue circles) in $La_{2-x}Ba_xCuO_4$ obtained from Rietveld refinements: x = 0.095 (a), x = 0.125 (b), and x = 0.155 (c). In all three panels: solid black symbols show in-plane Cu-O bond for x=0 sample as a reference. Horizontal dashed lines are guide to the eye, vertical dashed lines mark crystallographic phase transitions. Vertical double arrows highlight the magnitude of changes discussed in the main text.

If the LTO-HTT transition were purely displacive, then we would expect the atomic displacements associated with the octahedral tilts of the LTO phase to decrease continuously to zero on approaching the transition from below. Figure 6 demonstrates that this is not the case: the longer La-O2 bonds (O2 = apical oxygen)



FIG. 6. (Color online) Temperature evolution of the average La-O(2) interatomic distances for (a) x = 0.095, (b) x = 0.125, and (c) x = 0.155 composition. Bond multiplicity is indicated by a number where applicable. Short La-O(2) bond that connects two LaO₂ planes is shown in separate panels. Vertical dashed lines indicate structural phase transitions.

are split into three distances in the LTO phase, and this splitting abruptly drops to zero at the transition to the HTT phase. The residual, disordered displacements in the HTT phase are apparent in the jump in the mean square atomic displacements, shown in Fig. 7. Nevertheless, given the clear evidence that the transition is second order [16, 17], the apparent jump in the bond lengths must be an artifact of the Rietveld refinement. The La-O2 bond length is affected most strongly by displacements of the apical oxygens, associated with octahedral tilts, which are anisotropic. Note that in the fitting, we have assumed isotropic mean square atomic displacements, $U_j = \langle u_j^2 \rangle$ where u_j is the displacement of an atom at site j and the average is over all equivalent sites in the sample. If there are disordered tilts present in the LTO phase, then the fitting process may result in unrealistic O2 displacements to compensate for the associated impact on Bragg peak intensities. It follows that anisotropic local displacements of the apical oxygens, such as occur in tilt fluctuations, might be modeled by finite average displacements, even when the true *average* static displacement is essentially zero (just below the transition).

If the disordered tilts change continuously across the transition, then we should expect to see an anomalous jump in U_{iso} for O2 on entering the HTT phase. Figure 7 shows that this, indeed, is the case. In fact, there is also a jump at the low-temperature transition, indicating that there are anisotropic fluctuations present in the LTO phase that cannot be compensated by adjusting the symmetry-allowed atomic displacements. The lower red curve corresponds to a Debye-model fit [46] to the O2 U_{iso} of La₂CuO₄ (gray circles). This involves two parameters, the Debye temperature θ_D , and an offset factor U_0 [47, 48]; the behavior for La₂CuO₄ is well described by the parameter values θ_D of 500(2) K and U_0 of 0.0023(2) Å². In the other Figure panels, in each case the upper red curve is obtained by adding a dopingdependent offset to match the experimental values at the lowest temperature, but keeping the Debye temperature



FIG. 7. (Color online) Temperature evolution of atomic displacement parameter (ADP) of apical oxygen (solid blue symbols) in $La_{2-x}Ba_xCuO_4$ for: x = 0.095 (a), x = 0.125 (b), and x = 0.155 (c). Vertical dashed lines indicate transitions between crystallographic phases as labeled and specified in the text. In all panels ADP data for x = 0 sample are presented by solid gray symbols, with solid red line representing a fit of the Debye model, as discussed in the text. Debye model for ADPs of doped samples has the same Debye temperature as for x = 0, but different offset such as to provide a good fit to ADP in the low temperature phases. Anomalous jumps in ADP discussed in the main text are indicated by double arrows. Insets focus on low temperature transitions.

the same as that obtained for the undoped end-member. The offset grows with Ba concentration, which is consistent with the disorder in O2 positions induced by Ba substitution for La [20]. It appears to capture the underlying trend in each case, with the excess disorder associated with the jumps gradually becoming indistinguishable from the thermal effects with increasing temperature. This is in agreement with earlier observations in $La_{2-x}Ba_xCuO_4$ and $La_{2-x}Sr_xCuO_4$ of persisting local tilt fluctuations across these macroscopic phase transitions [49–52]. Similar anomalies have been seen in other systems, where they are typically ascribed either to the inadequacy of the structural model used, or sometimes more specifically to the presence of nanoscale structural features, such as broken symmetry states, that do not propagate over long length-scales [47, 48, 53, 54].

B. Local structure

Using the same neutron scattering data, we have characterized the local structure of La_{2-x}Ba_xCuO₄ by the PDF approach. Figure 8 shows PDF fits over intermediate *r*-ranges at 15 K using the average structure models, establishing the overall data quality and displaying that good fits can be obtained on this length scale. Here, we have taken account of the correlated motion of short interatomic bonds [55–57] by defining the mean-square relative displacement σ_{ij}^2 of atoms at positions *i* and *j*,



FIG. 8. (Color online) PDF fits of the average structure models to LBCO data at 15 K. Closed blue symbols represent the data, solid red lines are the models, and solid green lines are the differences (offset for clarity). (a) x = 0 using *Bmab* model, (b) x = 0.095 using *Pccn* model, (c) x = 0.125 using *P42/ncm* model, and (d) x = 0.155 using *Pccn* model.

separated by distance r_{ij} , as

$$\sigma_{ij}^2 = (\langle u_i^2 \rangle + \langle u_j^2 \rangle) [1 - (r_0/r_{ij})], \qquad (1)$$

where the parameter r_0 is fixed at 1.6 Å for all PDF calculations in this paper.

To explore the origin of enhanced mean-square displacements in the Rietiveld refinements shown in Fig. 7, we focus on the very local structure. We first evaluate the expected effects on the PDF of the symmetry change across the low-temperature transition in the case where the local and average structures agreed. Fig. 9(b)-(d) shows a comparison of PDFs simulated using parameters from the Rietveld refinements at base temperature (blue profile, OI model) and at the temperature of maximum orthorhombic strain (red profile, OE model), bracketing the low temperature transition in the doped samples. The changes expected in the PDF across the transition are clearly observable in the respective difference curves, with the strongest features just below 3 Å (marked by arrows), corresponding to La–O2 bonds.

The actual measured PDFs at the same temperatures



FIG. 9. (Color online) PDF comparison of the average and local structure behavior in $La_{2-x}Ba_xCuO_4$. Top row: simulated PDFs calculated using parameters from fully converged Rietveld refinements reflecting average structure behavior. Low-T profiles are shown in blue, higher-T profiles are shown in red. (a) 15 K vs 50 K LTO structure PDFs for x = 0; (b) 15 K LTLO vs 60 K LTO PDFs for x = 0.095; (c) 15 K LTT vs 80 K LTO PDFs for x = 0.125; (d) 15 K LTLO vs 70 K LTO PDFs for x = 0.155. Bottom row: comparison of the raw experimental PDF data for the same respective temperatures as considered in (a)-(d): lower temperature data shown in blue, higher temperature data shown in red. Difference curves (high-T minus low-T PDF) are offset for clarity. Shaded areas represent span of the difference curves observed for x=0 composition. Changes observed in the average structure (marked by filled arrows) are not observed in the local structure (empty arrows), as experimental PDFs do not change across the OE/OI phase transitions in doped $La_{2-x}Ba_{x}CuO_{4}$ samples.

are shown in Fig. 9(f)-(h). The difference curves show nothing above the noise level, indicating the absence of change in the local structure across the transition, in contrast to the predictions from the average structure. In fact, the temperature difference is similar to that observed in pure La₂CuO₄, Fig. 9(e), where there is no change in the average structure. These results are consistent with earlier work [49].

Further confirmation of this comes from explicit short range PDF modeling that was carried out using both OE-type and OI-type models fit to the data at base temperature and at the maximum orthorhombicity temperature in the doped samples. These fits are shown in Fig. 10. While the OE-type model readily explains the La₂CuO₄ data at both base and intermediate temperature, Fig. 10(a) and (e), it gives an unsatisfactory fit to the region of the La–O2 bonds in the doped samples. Such a discrepancy at base temperature (Fig. 10(b)-(d)) is expected, since the underlying atomic structure there is OI. At the temperature of maximum orthorhombic strain, the discrepancy with the OE fits remains, as shown in Fig. 10(f)-(h), whereas OI fits do much better,



FIG. 10. (Color online) OE versus OI PDF models for the local structure (solid gray lines). Data are shown as open gray symbols, difference curves (solid red lines) are offset for clarity. (a)-(d) 15 K data vs LTO model (OE symmetry) explains x = 0 data well (as it should), fails for x = 0.095, 0.125, and 0.155 (as it should). The largest discrepancies are marked by arrows. (e) LTO for x=0 sample at 50 K, (f)-(h) data at T of maximum orthorhombicity (60 K, 80 K, and 70 K for x = 0.095, 0.125, and 0.155 respectively) vs LTO model (fails at same places as at 15 K); (i)-(k) same as (f)-(h) but with LTLO/LTT models (OI symmetry)—underlying data correspond to OI symmetry. Inset: La/Ba-O(2) distances (shaded area) contribute principally to the misfits marked by arrows in (b)-(d) and (f)-(h).

as indicated in Fig. 10(i)-(k).

We saw previously that $U_{iso}(O(2))$ provides a distinctive measure of the tilt disorder that cannot be simulated by the symmetry-allowed structural parameters in the Rietveld refinements. We now consider the behavior of $U_{iso}(O(2))$ obtained from fits to the PDF data (for the range 15 < r < 40 Å), as shown in Fig. 11(a)–(c). At each temperature, separate fits have been performed with the LTT (LTLO), LTO, and HTT models. At all temperatures, we find that the *R*-factor, measuring the quality of fit, is always smallest for LTT (LTLO), followed by LTO, and then HTT. As one can see, $U_{iso}(O(2))$ from the LTT (LTLO) fit shows a monotonic increase with temperature, with no anomalies at the transition temperatures. The LTO fit is consistent with LTT at high temperature, but is larger in the LTO and LTT phases. The results for HTT are considerably larger at all temperatures.

As a measure of the distinctly OI tilts, we define the parameter δ as

$$\delta = \Delta U_{iso} / \langle x_{\mathcal{O}(2)} \rangle^2, \qquad (2)$$

where ΔU_{iso} is the difference in parameter values obtained from the LTO and LTT (LTLO) fits, normalized to



FIG. 11. (Color online) Semi-quantitative exploration of the OI-ness of LBCO via assessment of *T*-dependence of apical oxygen isotropic atomic displacement parameter (ADP) as obtained by fitting different structural models (as indicated by arrows in (a)-(c)) to the PDF data over 4 nm *r*-range. (a) x = 0.095, (b) x = 0.125, and (c) x = 0.155. Difference between the observed ADPs using LTO and LTLO/LTT models from panels (a)-(c) are displayed in (d)-(f) for x = 0.095, x = 0.125, and x = 0.155, respectively, normalized by the square of the average transverse displacement of apical oxygen. See text for details.

the square of the average transverse displacement of the O(2) site in the LTT phase at low temperature, $\langle x_{O(2)} \rangle^2$. The temperature dependence of δ is plotted in Fig. 11(d)–(f) for the doped samples. For x = 0.125, we find evidence for substantial OI tilts throughout the LTO phase, with a reduced magnitude for x = 0.095 and 0.155. On entering the HTT phase, we have already seen evidence that tilt disorder is present; however, the fact that $\delta \approx 0$ suggests that there is little preference between OI and OE tilts at high temperature. It is consistent with the idea that, in the HTT phase, the Cu-O(2) bond precesses rather smoothly around the z axis as discussed before [5, 32, 58].

We now address the length-scale of the local OI tilts. This can be obtained qualitatively from a direct comparison of the experimental PDF data at 15 K and 100 K (well above the phase coexistence region) for all samples studied. This is shown in Fig. 12(a)-(d). Panel (a) shows the result for La₂CuO₄; only small differences are seen in the PDFs beyond the expected uncertainties (e.g., indicated by the green arrow), and these provide a measure of the signal we should expect due to thermal effects within the same phase. From Fig. 12(b)–(d), it is clear that in



FIG. 12. (Color online) Comparison of LBCO PDF data at 15 K (closed blue symbols) and at 100 K (solid red line) with difference curve (solid green line) offset for clarity. Horizontal gray dashed lines mark experimental uncertainty on 2σ level. Light-red solid line represents a 0.5 Å running average of the absolute value of the difference curve, multiplied by 2 and offset for clarity. (a) x = 0, (b) x = 0.095, (c) x = 0.125, and (d) x = 0.155. Difference in data for x = 0 sample displays the change expected from canonical thermal evolution effects without symmetry changes. Differences in the data for all three doped samples display similar level of change as x = 0sample up to ~ 9 Å with first substantial changes seen on longer length-scale. Low r assessment: green arrows mark changes seen in the data for all the samples, while the red arrows mark significant changes seen only in the doped samples. presumably associated with the change in average symmetry. Empty arrows around 3 Å mark places where changes are expected from the average structure, but not observed locally, as shown in Fig. 9 and discussed in the text. Local structure across the global OI to OE phase transition is preserved on sub-nanometer length-scale.

the doped samples there are additional signals in the difference curve, starting near a distance of 9 Å, that are reproducible from sample to sample and especially evident in the running average of the difference curve (red curve). This suggests that the OI tilt correlations within the LTO phase have a correlation length that is < 9 Å.

The PDF analysis presented here is based on total scattering data that do not discriminate between the elas-



FIG. 13. (Color online) (a) Diagram of the (H, K, 0) plane of reciprocal space indicating fundamental Bragg peaks (filled circles) and LTT superlattice peaks (open circles), with dotdashed (dashed) line indicating the orientation of the data slice in (b) [(d)]. (b) Map of scattering intensity for E vs. $\mathbf{Q} = (3 + \xi, 3 - \xi, 0)$. (c) Intensity (integrated over $2 \le E \le$ 4 meV) vs. $\mathbf{Q} = (3, 3, L)$. (d) Intensity map for E vs. $\mathbf{Q} =$ $(3 + \zeta, 3 + \zeta, 0)$. All measurements are at T = 180 K, in the LTO phase.

tic and inelastic scattering channels, and hence the PDF does not distinguish whether the underlying short-range features are static or dynamic. This is in contrast to the Rietveld analysis, which is sensitive only to the time-averaged information in the Bragg peaks; the inelastic information is largely in the tails of the Bragg peaks. To test the static or dynamic character, we turn next to inelastic neutron scattering on a single crystal, focusing on $La_{2-x}Ba_xCuO_4$ with x = 0.125.

C. Octahedral tilt dynamics

The inelastic scattering about the (330) reciprocal point of our $La_{2-x}Ba_xCuO_4$ with x = 0.125 is shown in Fig. 13. The cuts in reciprocal space that were taken are shown schematically in Fig. 13(a). Figures 13(b) and (d) show the dispersion of excitations along the transverse and longitudinal directions, respectively, within the LTO phase at T = 180 K. In both cases, one can see a soft phonon with intensity that can be resolved between 2 and 10 meV. In the transverse direction, these excitations connect to the transverse acoustic modes dispersing from the neighboring (240) and (420) fundamental Bragg points. Another perspective is given by the constant energy slices shown in Fig. 14 for several different energies, where we compare with results at 60 K, slightly above the low-temperature transition. For dispersion in the longitudinal direction, the intensity becomes quite weak



FIG. 14. (Color online) Constant-energy slices, with signal integrated over ± 1 meV, through the soft-phonon scattering around (330). (a,d) E = 10 meV; (b,e) E = 7 meV; (c,f) E = 3 meV. Data obtained at T = 60 K for (a–c) and 180 K for (d–f).

as one moves away from the (330) point. Figure 13(c) shows that the excitations, integrated between 2 and 4 meV, have a finite width along Q_z , demonstrating that the LTT tilt fluctuations have 3D character.

The temperature dependence of the scattering near (330) is presented in Fig. 15. There is a clear superlattice reflection at (330) in the LTT phase at 50 K. Warming to 60 K, just across the transition to the LTO phase, very weak elastic scattering is still detectable; however, this is completely gone at 120 K. In contrast, soft phonon fluctuations (integrated over 2 to 5 meV) centered at (330) are clearly seen in the LTO phase and even in the HTT, at 250 K. At 50 K, the intensity from the soft fluctuations has all condensed into the elastic superlattice peak. (There must be acoustic phonons dispersing out of the superlattice peak, but these are too weak for us to detect.) The temperature dependences of both the elastic and inelastic signals are summarized in Fig. 15(a).

The correlation length for the LTT-like tilts within the LTO phase can be estimated from the Q-width of the soft-phonon scattering. (Here, for simplicity, we ignore resolution corrections.) Taking the inverse of the half-width-at-half-maximum for the fitted peaks in Fig. 15(e-h), we find an effective correlation length of ~ 5 Å in the LTO phase, decreasing to about half of that in the HTT phase. This is consistent with estimate of < 9 Å



FIG. 15. (Color online) Single crystal results at the (330) LTT superlattice position for x = 0.125. (a) Summary of the temperature dependence of the elastic (red circles) and inelastic (blue triangles) integrated intensities obtained from the following panels; vertical dashed lines denote phase boundaries, while dashed lines through data points are guides to the eye. (b)-(d) Elastic channel (integrated over ± 1.5 meV) measured along the longitudinal direction at 120, 60, and 50 K, respectively. Solid lines are Gaussian-peak fits, used to determine the integrated intensity; weak, *T*-independent peaks are diffraction from the aluminum sample holder. (e)-(i) Inelastic signal from the soft-phonon fluctuations (2-5 meV integration) measured at 250, 180, 120, 60, and 50 K, respectively. Lines are Gaussian-peak fits.

obtained from the PDF analysis.

For comparison, Fig. 16 (a) and (b) show the dispersion of tilt fluctuations in the transverse direction about the (032) position (an LTO superlattice peak) in the LTO and HTT phases, respectively. The intensity is much stronger than at (330) because of a much larger structure factor. There is substantial intensity from soft tilt fluctuations, and even quasielastic scattering, at 250 K in the HTT phase, as seen previously [30]. In the LTO phase at 180 K, much of the low-energy weight is due to the residual soft mode that condenses at the LTT transition. We note that scattering at (032) is allowed in both the LTO and LTT phases; it follows that one cannot uniquely distinguish between OE and OI soft tilt fluctuations at



FIG. 16. (Color online) (a,b) Intensity map as a function of energy vs. $\mathbf{Q} = (H, 3, 2)$, showing the transverse dispersion of tilt modes about the (032) superlattice peak position of the LTO phase, obtained at T = 180 and 250 K, respectively. (c,d) Intensity, integrated over a window of ± 1 meV along the transverse direction, for E = 0 (blue squares), 2.5 (red triangle), and 5 meV (green circles), at T = 180 and 250 K, respectively.

this \vec{Q} -point, in contrast to fluctuations at (330).

IV. DISCUSSION

The distribution of Cu-O(1) nearest-neighbor bond lengths has been the subject of some controversy over the years, and so deserves some discussion. Our Rietveld analysis finds a maximum bond length splitting of just 0.005 Å in the LTT phase of $La_{2-x}Ba_xCuO_4$ with x = 0.125, consistent with earlier diffraction work on $La_{2-x}Ba_xCuO_4$ [7]. To appreciate how small this splitting is, we compare various measures of the bond-length distribution in Fig. 17(a). The peak obtained from the PDF analysis is a simple gaussian that shows a very slight broadening with doping. The width of the PDF peak is significantly smaller than that obtained from the Rietveld analysis, as the former is sensitive to the correlated motion of nearest neighbors, whereas diffraction intensities only have information on the independent fluctuations of the distinct atomic sites. The PDF peak also broadens slightly with increasing temperature as shown in Fig. 17(b). The mean-squared relative displacement, σ^2 . obtained as a function of temperature for the x = 0.125sample is shown in Fig. 17(c). The solid line corresponds to the Einstein model [59],

$$\sigma^2 = \frac{\hbar}{2\mu\omega_{\rm E}} \coth\left(\frac{\hbar\omega_{\rm E}}{2k_{\rm B}T}\right),\tag{3}$$



FIG. 17. (Color online) (a) Normalized radial distribution function R(r) for Cu-O(1) bonds comparing results from different analyses. Green lines show the gaussian peaks obtained from PDF analysis for La_{2-x}Ba_xCuO₄ with x = 0 (solid) and x = 0.125 (dashed). The effective profile for the latter sample from the Rietveld refinement (red dashed line) is not sensitive to correlated motion. The blue solid line indicates the model for La_{2-x}Sr_xCuO₄ with x = 0.15 and T = 15 K from the XAFS study by Bianconi *et al.* [61] (b) Pair distribution function for La_{2-x}Ba_xCuO₄ with x = 0.125 at 10 K (blue) and 100 K (red). (c) Results for Cu-O(1) σ^2 for x = 0.125from PDF (blue filled circles) and the EXAFS analysis (red open circles) of Lanzara *et al.* [62]. The solid line corresponds to an Einstein-model calculation, as described in the text.

where μ is the reduced mass, and we have set $\hbar\omega_{\rm E} =$ 70 meV, the zone-boundary energy of the Cu-O bondstretching phonon [60]. The calculation indicates that the zero-point fluctuations of the Cu-O bond, corresponding to a bond-length spread of 0.05 Å, is an order of magnitude greater than the bond-length splitting in the LTT phase.

Besides the bond-length splitting, one might anticipate an enhanced bond-length disorder in association with the ordering of charge stripes. Such enhanced disorder has been detected in the case of nickelates, such as $La_{1.67}Sr_{0.33}NiO_4$ [63]. In the closely related $La_2NiO_{4.125}$, model fits to superlattice intensities indicated displacements of in-plane O atoms on the order of ± 0.02 Å [64]. In contrast, a similar analysis of displacements in the cuprate $La_{1.48}Nd_{0.4}Sr_{0.12}CuO_4$ indicates displacements of order ± 0.004 Å [65], which would be quite difficult to detect in the PDF analysis.

The Cu-O pair distribution can also be probed with the x-ray absorption fine structure (XAFS) technique. In a polarized Cu K-edge XAFS studies, Bianconi



FIG. 18. (Color online) Doping dependence of various system parameters of $La_{2-x}Ba_xCuO_4$. (a) Orthorhombicity at 100 K (dark blue solid symbols) from Rietveld. (b) Average planar Cu-O bond distance (solid black symbols) at 100 K temperature. (c) Average CuO₆ tilt angle extracted from apical oxygen (light red solid circles) and planar oxygen (dark red solid squares) positions at maximum orthorhombicity. (d) Orthorhombicity at 10 K after Hücker et al. [17] (light blue solid symbols). (e) Planar Cu-O bondlength anisotropy at 15 K (olive solid symbols). (f) In-plane correlation lengths ξ of charge ordering parallel (solid blue circles) and perpendicular (open blue circles) to the stripe direction at base temperature [17].

and coworkers [61, 66] have reported a splitting of the Cu-O bond distribution by 0.08 Å below 100 K in $La_{1.85}Sr_{0.15}CuO_4$. Their low-temperature distribution is reproduced in Fig. 17(a). The large splitting in this model appears to be inconsistent with our PDF data, which would detect a splitting of this magnitude. In a study of La_{1.875}Ba_{0.125}CuO₄ [62], a corresponding anomalous increase of σ^2 by 0.001 Å² on cooling below 60 K was reported; those data are indicated by open circles in Fig. 17(c). The magnitudes of σ^2 from the EXAFS and PDF analyses are consistent within error bars; however, the PDF results do not indicate any significant anomalous enhancement in the LTT phase. While small atomic displacements associated with stripe order are certainly present, as indicated by single-crystal diffraction [10, 65], the present work indicates that they are significantly smaller than the zero-point bond-length fluctuations.

Next, we turn to the doping dependence of the Cu-O bond anisotropy, where we have two competing trends. One of these involves the decrease in the average octahedral tilt with doping. The shortening of the inplane Cu-O bond length reduces the mismatch with bond lengths in the La₂O₂ layer, resulting in one contribution to the reduction in average tilt. Another comes from the quenched disorder associated with substituting Ba²⁺



FIG. 19. (Color online) (x, T) evolution of δ shown in Fig. 11(d)-(f). Solid lines mark structural transition temperature: T_{HT} (red) and T_{LT} (blue).

for La³⁺. The Ba acts effectively as a negative defect, repelling the neighboring apical oxygens and disrupting the octahedral tilt pattern. These effects lead to the decrease in the average orthorhombic strain with x, as summarized in Fig. 18. The competing trend involves the onset temperature for the LTT (LTLO) transition, resulting in ordering of OI tilts. The empirical trend is that this should grow with Ba concentration (as it depends on the average ionic radius of the 2+ ions relative to that of the 3+ ions [67]). These competing trends lead to the bondlength anisotropy reaching a maximum that appears to occur coincidentally near x = 0.125, where stripe order is strongest [17].

We get a somewhat different perspective from the temperature and doping dependence of parameter δ , defined in Eq. (2), which measures the LTT-like component of the octahedral tilts; a false color representation is shown in Fig. 19. Here we see that the OI tilts appear in a significant way at the onset of LTO order. Furthermore, the relative magnitude is largest at x = 0.125 even before LTT order is achieved. This behavior is suggestive that the degree of Cu-O(1) bond-length splitting might be influenced by electron-phonon coupling and the particular stability of the stripe-ordered phase at x = 0.125. Regarding stability, it is interesting to note the results of recent optical pump probe studies. Pumping the x = 0.125 phase in La_{1.8-x}Eu_{0.2}Sr_xCuO₄ with 80-meV photons with polarization *parallel* to the planes induces interlayer superconducting coherence for $T \lesssim 15$ K [68]; this also causes stripe melting in $La_{2-x}Ba_xCuO_4$ [69]. In contrast, pumping $La_{2-x}Ba_xCuO_4$ with polarization perpendicular to the planes enhances interlayer superconducting coherence for x = 0.115, but not for x = 0.125[70].

It is also relevant to compare with observations of

charge-density-wave (CDW) order in YBa₂Cu₃O_{6+d} [71, 72]. While there are differences in the doping dependence of the charge-ordering wave vectors and the connection to the spin correlations, the CDW order in YBa₂Cu₃O_{6+d} is strongest for hole concentration near 0.12 [73, 74], a remarkable similarity to La_{2-x}Ba_xCuO₄ [17] and La_{1.6-x}Nd_{0.4}Sr_xCuO₄ [75]. The CDW order in YBa₂Cu₃O_{6+d} appears at temperatures as high as ~ 150 K in a lattice with OI order present to above room temperature.

Finally, we note that charge-stripe order has recently been detected by x-ray diffraction in $La_{2-x}Sr_xCuO_4$ with $x \sim 0.12$ [76–79], confirming an earlier identification by nuclear magnetic resonance [80]. This result is somewhat surprising, as the average structure of $La_{2-x}Sr_xCuO_4$ is LTO (although electron diffraction studies have indicated LTT-like regions at LTO twin boundaries for x = 0.12[81] and LTLO order for x = 0.115 [82]). A key difference from $La_{2-x}Ba_xCuO_4$ is that the average orientation of the charge stripes is rotated away from the Cu-O bond direction by a small amount. Despite this difference, it seems relevant to ask whether dynamic or quasi-static OI tilts may be present in $La_{2-x}Sr_xCuO_4$. We hope to test this possibility in the future.

V. SUMMARY

Experimental evidence for the persistence, on a nanometer lengthscale, of CuO₆ LTT-like octahedral tilt correlations deep into the LTO crystallographic phase in $La_{2-x}Ba_xCuO_4$ with 0.095 $\leq x \leq 0.155$ has been presented. Despite the average structure becoming orthorhombic above T_{LT} as evidenced by Rietveld refinements of neutron scattering data, PDF analysis of the same data shows that the local structure retains its base temperature signatures consistent with orthogonal inequivalent state up to at least T_{HT} , where LTO transforms to HTT. The analysis also suggests that there is little preference between OI and OE tilts at high temperature, consistent with the idea that, in the HTT phase, the Cu-O(2) bond precesses rather smoothly around the c axis. The bond-length modulation that pins stripe order is found to be remarkably subtle, with no anomalous bond length disorder at low temperature, placing an upper limit on in-plane Cu-O bondlength anisotropy of 0.005 Å. Complementary inelastic neutron scattering measurements on x = 1/8 single crystal sample reveal that upon heating across T_{LT} the tilt correlations become extremely short-range and dynamic. The finite width of excitations around $\mathbf{Q} = (3, 3, L)$ along Q_z further indicates that the LTT tilt fluctuations have 3D character. The relative magnitude of the effect is maximum at x = 1/8 doping where bulk superconductivity is most strongly suppressed, suggesting that the splitting of Cu-O(1) bond lengths might be influenced by electronphonon coupling and the particular stability of the stripeordered phase at this composition.

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