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Magnetotransport of proton irradiated \( \text{BaFe}_2\text{As}_2 \) and \( \text{BaFe}_{1.985}\text{Co}_{0.015}\text{As}_2 \) single crystals

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Abstract

Here we study the magnetotransport properties of the ferropnictide crystals \( \text{BaFe}_2\text{As}_2 \) and \( \text{BaFe}_{1.985}\text{Co}_{0.015}\text{As}_2 \). These materials exhibit a high field linear magnetoresistance that has been attributed to the quantum linear magnetoresistance model. In this model, the linear magnetoresistance is dependent on the concentration of scattering centers in the material. By using proton-beam irradiation to change the defect scattering density, we find that the dependence of the magnitude of the linear magnetoresistance on scattering quite clearly contravenes this prediction. A number of other scaling trends in the magnetoresistance and high field Hall data are observed and discussed.

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The ferropnictides are a remarkable system where the competing influences of electron correlations, magnetic ordering effects and crystal structure combine to create a range of extraordinary properties including superconductivity\textsuperscript{1-3}. In all underdoped ferropnictides, associated structural (tetragonal to orthorhombic) and antiferromagnetic (AFM) transitions occur, which in parent BaFe\textsubscript{2}As\textsubscript{2} are coupled at around 134 K\textsuperscript{2,4}. At the magnetic transition\textsuperscript{1,5}, a spin-density wave (SDW) striped magnetic state is produced, with the spins aligned antiparallel along the \textit{a}- and \textit{c}-axis direction and parallel in \textit{b}-axis direction. Discrepancies between the experimental and theoretical local moment calculations\textsuperscript{6,7} indicate that the system fits neither entirely local or itinerant models. Simultaneous to the establishment of the AFM ordering is the creation of extremely small Fermi surface (FS) pockets\textsuperscript{8}. It has been theoretically predicted\textsuperscript{9} and verified by ARPES measurements\textsuperscript{10} that some of these FS pockets have Dirac Cone (DC) characteristics, where a linear relationship between momentum and energy is expected. DCs have been recently discovered in a wide variety of different materials, with many possessing a two dimensional structure similar to BaFe\textsubscript{2}As\textsubscript{2}\textsuperscript{11}, making the study of DC physics a topic of general interest in condensed matter physics today.

Large positive linear magnetoresistance (MR) is rather rare but is often found in DC systems. Generally in the ferropnictides this has been attributed to the Abrikosov quantum linear magnetoresistance (QLM) model\textsuperscript{8,12-14} on the basis that the extreme quantum limit (EQL) condition of the model (all carriers occupying a single Landau level) is accessible at much lower fields in Dirac systems. However, doubts have been raised about the robustness of this phenomenon\textsuperscript{15}. The QLM model predicts a strong dependence of the MR on the concentration of scattering centers, \(N_i\). Two regimes have been identified; in the compensated regime the MR is inversely proportional to \(N_i\) and in the uncompensated regime the MR is linearly proportional to \(N_i\). Thus a systematic study of the MR as a function of \(N_i\) is a good test of the applicability of the QLM model in these systems.

Proton irradiation has been shown to introduce defects, which are recognized to be predominantly of a point defect character, without significantly altering the electronic structure of the material\textsuperscript{16,17}. In contrast, Co doping is expected to modulate both the scattering and carrier concentration. In this paper, we present resistivity, MR and Hall effect measurements on pristine and proton irradiated single crystals of BaFe\textsubscript{2}As\textsubscript{2} and BaFe\textsubscript{1.985}Co\textsubscript{0.015}As\textsubscript{2} and compare our findings with the predictions of the QLM model.

The in-plane MR shows unsaturated linear magnetic field dependence in all crystals
below the structural and magnetic transitions. The crossover to linear MR behavior occurs at a temperature dependent critical field \(B^*\) which we find is unaffected by the proton irradiation. A number of other scaling trends in the MR and high field Hall data are observed, which are discussed in light of both the multiband and anisotropic quasiparticle lifetime models.

The paper will first introduce the QLM model then describe our experimental efforts to compare systematic changes in the scattering density to the predictions of the QLM model. Finally we will discuss the high field Hall resistance data and observation of scaling relationships.

I. INTRODUCTION TO QUANTUM LINEAR MAGNETORESISTANCE

Previous work has reported a linear MR occurring at low magnetic fields in twinned crystals.\(^{8,13,14}\) There are a number of potential explanations for the advent of linear MR\(^{18–22}\) however, the QLM model\(^{23,24}\) has been generally applied to the ferropnictides.\(^{8,13,14}\) The requirements for QLM are extremely stringent, as the carriers within the dominant bands must be confined to a single Landau level. This condition can only be satisfied at the fields utilized within this work if the dominant transport bands are extremely small DCs.\(^{8,13,14,25}\) Using the separation of Landau levels within DCs it is possible to write down the conditions for the EQL:

\[
n_0 \ll \left( \frac{e\mu_0 H}{\hbar} \right)^{3/2} T_0 < v_f \sqrt{e\mu_0 H \hbar} \tag{1}\]

where \(n_0\) and \(T_0\) are the EQL threshold values for the carrier density and temperature respectively. It has therefore been interpreted that the linear MR is evidence for the existence of DCs. In most instances, the linear MR originates at fields above 1 T. At low fields, a semi-classical parabolic shape is perceived \((MR \approx A_2(\mu_0 H)^2)\). At \(B^*\), a transition from the low field parabolic behavior to the high field linear MR is discerned, therefore, above and below \(B^*\) we write:

\[
MR \approx \begin{cases} 
A_2[\mu_0 H]^2, & \mu_0 H < B^* \\
A_1 \mu_0 H + O[\mu_0 H]^2 & \mu_0 H > B^*
\end{cases} \tag{2}
\]
Furthermore, by rearranging the temperature condition for the EQL (right hand condition of equation 1) it is possible to determine an expected temperature dependence of $B^*$.  

$$B^*(T) = \frac{1}{2\hbar c v_f^2} (k_B T + E_F)^2$$  

(3)

from which the Fermi velocity and energy can be calculated.

There are a number of different forms of the QLM model each dependent on the electronic structure of the material. In the case of BaFe$_2$As$_2$ and BaFe$_{1.985}$Co$_{0.015}$As$_2$, the situation of small pockets of high mobility carriers within a FS is most applicable. Within this scheme there are two forms for ideally compensated or uncompensated metals, where compensated specifically refers to the equal numbers of carriers within the high mobility pockets. The simplification for the compensated case leads to:

$$\rho_{xx}(\mu_0 H) = \frac{\pi \mu_0 H}{f(n) e N_i}$$  

(4)

where $f(n)$ is a function with a value close to unity. However, in the uncompensated situation:

$$\rho_{xx}(\mu_0 H) = \frac{f(n) N_i \mu_0 H}{e (n_e - n_h)^2} = \frac{f(n) N_i \mu_0 H}{en_e^2 n_{eff}}$$  

(5)

where $n_e$ and $n_h$ are the electron and hole carrier densities respectively and $n_{eff}$ is the effective carrier density within the DCs.

As illustrated by equations 4 and 5, the compensated and uncompensated models have different dependences on the scattering density, with the compensated (uncompensated) models displaying indirect (direct) proportionality. A variation of equation 5 has been applied throughout the literature where the difference between the electron and hole carrier densities has been replaced by the ‘effective’ carrier density ($n_{eff}$) for the DC states derived from the low field Hall resistivity.

II. EXPERIMENTAL DETAILS

Large single crystals of BaFe$_2$As$_2$ and BaFe$_{1.985}$Co$_{0.015}$As$_2$, grown using the self-flux method, were cleaved using a micromechanical exfoliation technique. All crystals were cleaved from the same crystal for each compound. Proton irradiation was performed such
that protons doses of $0.5 \times 10^{16}$ and $1 \times 10^{16}$ cm$^{-2}$ were achieved for the BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystals and $0.5 \times 10^{16}$ cm$^{-2}$ for BaFe$_2$As$_2$. Crystal sizes were of the order of 2 millimeters in the $ab$ plane and below 40 micrometres along the c-axis. This is sufficiently thin ($< 50 \mu m$) to achieve homogeneous irradiation damage using 3-MeV H$^+$ irradiation for BaFe$_2$As$_2$ according to calculations using the SRIM code\textsuperscript{17}. All transport measurements were taken using the van der Pauw technique\textsuperscript{27} with the magnetic field applied along the $c$-axis and current within the $ab$-plane. Data was symmetrized by combining the MR responses of 0 T to 7 T positive (0 T to -7 T negative) magnetic sweep to the -7 T to 0 T negative (7 T to 0 T positive) sweep creating 2 continuous sets of data. The MR response for all sweep directions was then averaged to ensure the elimination of the Hall voltage signal. Two forms of the MR will be presented in this work, the MR is defined as $(\rho(\mu_0 H) - \rho(0 T))$ (defined as MR throughout) and the normalized MR (NMR) as $(\frac{(\rho(\mu_0 H) - \rho(0 T))}{\rho(0 T)})$.

A rigorous treatment of the transport characteristics requires a multiband approach\textsuperscript{28}, nevertheless to examine trends between unirradiated and irradiated undoped and Co doped crystals we restrict our analysis to low fields and consider a single carrier approximation to extract $n_{eff}$ from the low field Hall resistivity as:

$$n_{eff} = \frac{1}{R_{He}}$$  \hspace{1cm} (6)

where $R_{He}$ is the Hall coefficient. From this and the longitudinal resistivity we can also extract the effective single carrier Hall mobility $\mu_H$.

III. RESULTS

A. Testing the QLM model

In order to test the QLM model we first must demonstrate that we have changed the scattering density in our crystals without significantly altering other properties. Fig. 1 shows the zero field resistivity ($\rho_0$) vs. T for all crystals. The magnetic and structural transition at 134 K is clearly visible for the BaFe$_2$As$_2$ crystals and displays a similar shape to previous reports\textsuperscript{4,14,29}. There is no significant variation in the temperature of the structural and magnetic transition with proton irradiation for any crystals, nor in the shape of the resistivity with temperature curves. Taken together these imply that the fundamental
electronic structure remains unperturbed by the damage. The most important observation, within the context of this study, is that the proton damage systematically increases the residual resistivity in both families of crystals implying that only temperature independent disorder has been added.

This observation is further supported by examining the low field Hall resistivity ($\rho_{xy}(\mu_0 H)$) data. For all crystals, a negative Hall coefficient indicative of electron carrier dominance is measured, as indicated in Fig. 2A. The important observation is that the Hall coefficient is unaffected by the proton irradiation. This implies that the carrier density is unchanged by the proton damage, supporting the observation that the change in $\rho_0$ is primarily due to changes in scattering density and not changes in carrier concentration.

The temperature dependence of the Hall coefficient is quite different in the two compounds. We can compare behavior most simply by plotting the Hall coefficient against the temperature normalized by the magnetic transition temperature ($T_N$), as shown in Fig. 2A. The difference between the curves suggests that Co doping significantly alters the electronic structure. Note that as in other studies, we observe an increase in the magnitude of the Hall coefficient with Co doping. Within the Boltzmann transport model (see equation 6), this signifies a decrease in carrier concentration rather than the expected increase in electron density with the addition of Co, as shown in Fig. 2B. In Fig. 2C, a direct comparison of $\rho_{xy}(\mu_0 H)$ at 25 K is shown for all crystals. The curves are nonlinear and more significantly so in the parent compounds. This curvature has been analyzed simply in terms of multi-carrier behavior. Due to the complexity of the electronic structure of these materials, no conclusive explanation has been generated to explain these trends.

We note that the insensitivity of the $\rho_{xy}(\mu_0 H)$ to changes in the scattering density ($N_i$)
observed in this study is in contrast to the work conducted by Ishida et al.\textsuperscript{15}. In that work, the magnetotransport properties were strongly influenced by annealing leading to an eradication of the linear MR. This would suggest that extrinsic scatterers play a fundamental role in determining the magnetotransport properties. Furthermore, the study by Urata et al.\textsuperscript{33} on Mn doped BaFe\textsubscript{2}As\textsubscript{2} observed that both the magnitude and shape of the $\rho_{xy}(\mu_0 H)$ was affected by the introduction of magnetic scatterers caused by Mn doping. Our work would suggest, however, that both annealing and Mn doping do not solely reduce/increase the number of scattering centers and therefore the exact nature of defects existent in the undoped and underdoped ferropnictides plays an essential role in determining the magnetotransport properties.

Let us now turn to the MR. We find that all crystals show a large linear component to the MR below the magnetic transition. Figs. 3 A and B show the characteristic field dependence for the symmetrized MR data for the unirradiated and 0.5 $\times 10^{16}$ cm$^{-2}$ proton damaged BaFe\textsubscript{2}As\textsubscript{2} crystals respectively. In Fig. 3 C, the MR is compared at 10 K for both crystals. Figs. 4 A, B and C show the characteristic field dependence for the symmetrized MR data for the unirradiated, 0.5 $\times 10^{16}$ cm$^{-2}$ and 1 $\times 10^{16}$ cm$^{-2}$ proton damaged BaFe\textsubscript{1.985}Co\textsubscript{0.015}As\textsubscript{2} crystals respectively. In Fig. 4 D, the MR is compared at 10 K for all BaFe\textsubscript{1.985}Co\textsubscript{0.015}As\textsubscript{2} crystals. Both the temperature dependence and magnitude is comparable to previous studies for both compounds\textsuperscript{14,15}. The changes with irradiation are subtle.
FIG. 3. (Color online) The field dependence of the symmetrised MR for unirradiated (A) and $0.5 \times 10^{16} \text{ cm}^{-2}$ irradiated (B) BaFe$_2$As$_2$ crystals. C) Comparison between unirradiated (solid black line) and $0.5 \times 10^{16} \text{ cm}^{-2}$ irradiated (dashed red line) MR at 10 K for BaFe$_2$As$_2$ crystals. Green dotted lines represent ± 10 % change in MR.

By taking the derivative of the symmetrised MR data the functional form of the MR response can be observed. As shown in the Fig. 5 A, the BaFe$_2$As$_2$ crystals show a linear contribution to the MR originating at fields above 1 T. The undoped crystals display a noticeable curvature at high fields, similar to earlier studies$^{14,34}$. However, with Co doping the high field behavior of the unirradiated BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystal shows increased linearity, reminiscent of the work of Kuo et al$^{14}$. However, with increasing irradiation the high field MR of the BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystals becomes increasingly non-linear, as shown in Fig. 5 B.

The $B^*$ is extracted and plotted against reduced temperature in Fig. 5 C and D for the BaFe$_2$As$_2$ and BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystals, respectively. The expected $T^2$ relationship is coarsely perceived, as indicated by previous studies$^{8,35}$. From this region, the Fermi velocity ($\sim 2 \times 10^5 \text{m} \text{s}^{-1}$) and energy ($\sim 3 \text{ meV}$) have been calculated using equation 3. These values correspond well with previous transport$^8$ and quantum oscillation work$^{36}$. However, near $T_N$ the data appears to deviate from this $T^2$ temperature dependence. Note that this deviation of $B^*$ has been predicted theoretically$^{28}$.

Let us review our findings. From the in plane and transverse resistivity we have established that the proton damage has changed the scattering density and in no other way changed the crystal properties. Figs. 3 C and 4 D show that the changes to the MR as a result of the irradiation are subtle. We are now able to examine the influence of this increased scattering density on the high-field MR in comparison with the trends indicated by equations 4 or 5 of the QLM model. To consider this we have fitted the high field MR
above $B^*$ using equation \ref{eq3} and extracted the coefficients: $A_1$ and $O$. A significant linear $A_1$ component exists for both the BaFe$_2$As$_2$ and BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystals, as shown in Figs. \ref{fig4} A and D respectively. Both the $A_1$ and $O$ coefficients in the BaFe$_2$As$_2$ crystals are insensitive to the increased scattering (see Figs. \ref{fig4} A and B).

It might be argued that the change in scattering density due to proton irradiation over the pre-existing background defect scattering is small, and therefore changes in $A_1$ might be difficult to determine. Considering the change in the residual $\rho_0$ value as a rule of thumb guide to the change in scattering density, we estimate that the residual resistivity changes by 10 % and 25 % for $0.5 \times 10^{16}$ cm$^{-2}$ proton irradiation for the BaFe$_2$As$_2$ and BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystals, respectively. In order to show whether changes of this order of magnitude are discernable we include curves in Fig. \ref{fig4} C and \ref{fig4} D that show how a $\pm$ 10 % or $\pm$ 25 % change to the MR would manifest. We conclude that changes in the scattering density of this order of magnitude would be discernable if equations \ref{eq4} or \ref{eq5} were applicable.

In BaFe$_{1.985}$Co$_{0.015}$As$_2$ the fitting procedure we have applied appears to show that the $A_1$ coefficient decreases by 30 % at the highest irradiation commensurate with a significant increase in the quadratic component (see Fig. \ref{fig4} D, E), leaving the MR curve relatively unchanged (as shown in Fig. \ref{fig4} D). We cannot rule out that this might be a feature of the fitting procedure rather than a physical change in the scattering properties of the various bands given that the overall change in the MR as a result of the irradiation are in fact rather
FIG. 5. (Color online). A) NMR at 25 K for BaFe$_2$As$_2$ crystals; at low fields (dark red line) MR shows the conventional $(\mu_0H)^2$ dependence, however, at high fields the MR has a significant linear component (green line). B) NMR at 25 K for BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystals. Black solid lines: unirradiated, Red dashed lines: $0.5 \times 10^{16}$ cm$^{-2}$, Blue dotted line: $1 \times 10^{16}$ cm$^{-2}$. C) and D) Critical field vs. scaled temperature for BaFe$_2$As$_2$ (closed symbols) and BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystals (open symbols) respectively. Unirradiated: , $0.5 \times 10^{16}$ cm$^{-2}$: , $1 \times 10^{16}$ cm$^{-2}$:.

subtle. A decrease of $A_1$ with increased $N_i$ corresponds to the compensated QLM prediction expressed in equation 4. However, it is extremely unlikely that the ideal compensation within the DCs is achieved in the electron doped BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystals. Clearly the MR behaviour in the BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystals contravenes the QLM prediction as set out in equations 4 and 5.

For completeness we also fit the low field parabolic behavior below $B^*$ and this is parameterized using a coefficient $A_2$, which is shown in Figs. 6 C and F for the undoped and Co doped crystals, respectively. No systematic change in the $A_2$ coefficient is observed in either compound with irradiation.

In order to scrutinise the behaviour of the undoped crystals in more detail the temperature dependence of the $A_1$ coefficient is compared directly with the QLM predictions expressed in equations 4 and 5 as shown in Fig. 7 A. To estimate $N_i$ it is necessary to derive the mean free path ($mfp$):

$$mfp = \frac{m^* v_F}{\rho_0 e^2 n} = \frac{m^* v_F \mu_H}{e} = \frac{E_F \mu_H}{e v_F}$$

(7)

where $m^*$ is the effective mass. The $E_F$ and $v_F$ values have been taken from the ARPES data from Richard et al.$^{10}$. Using the $mfp$ it is then possible to calculate $N_i$: 

10
The linear MR is inconsistent with the QLM prediction for both undoped and Co doped crystal families. As others have discussed in the context of applying the QLM to topological insulators, the necessary carrier density to satisfy the EQL is orders of magnitude too small. Using the experimental $B^*$ value the required density is $\sim 10^{17}$ cm$^{-3}$ whereas the experimentally derived carrier density is $2 \times 10^{20}$ cm$^{-3}$ for BaFe$_2$As$_2$ at 2 K. While the single carrier model that we have used to derive the carrier density may be subject to error

$$N_i = \frac{1}{\left(\frac{4}{3} m_f \mu^2\right)^3}. \hspace{1cm} (8)$$

The 2 K $N_i$ values are found to be $1.5 \times 10^{26}$ m$^{-3}$ for the unirradiated and $2.05 \times 10^{26}$ m$^{-3}$ for the irradiated parent crystals, (suggesting a change in the scattering density due to $0.5 \times 10^{16}$ cm$^{-2}$ proton damaged of the order of 30%). The theoretical temperature dependences of the compensated (equation 4) and uncompensated (equation 5) plotted using the derived 2K $N_i$ values, clearly do not reflect the experimental $A_1$ temperature dependence.

Taken together, we can state with some certainty that the irradiation study shows that the linear MR is inconsistent with the QLM prediction for both undoped and Co doped crystal families. As others have discussed in the context of applying the QLM to topological insulators, the necessary carrier density to satisfy the EQL is orders of magnitude too small. Using the experimental $B^*$ value the required density is $\sim 10^{17}$ cm$^{-3}$ whereas the experimentally derived carrier density is $2 \times 10^{20}$ cm$^{-3}$ for BaFe$_2$As$_2$ at 2 K. While the single carrier model that we have used to derive the carrier density may be subject to error.
FIG. 7. (Color online). Experimental ( ), QLM compensated equation $4$ ( ) and QLM uncompensated equation $5$ ( ) $A_1$ coefficients for BaFe$_2$As$_2$ crystals for temperatures below 100 K. Black unirradiated, Red $0.5 \times 10^{16}$ cm$^{-2}$. $A_1$ coefficient multiplied by $n_{eff}^2$ vs. $n_{eff}$ for unirradiated (B) BaFe$_2$As$_2$ and (C) BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystals. D) $\mu_H$ and MR $A_1$ coefficient as a function of inverse temperature for unirradiated BaFe$_2$As$_2$ ( ) and BaFe$_{1.985}$Co$_{0.015}$As$_2$ ( ) crystals.

it is clear that for any reasonable carrier concentration to achieve the EQL leads to an $A_1$ coefficient substantially larger than the experimental value.

B. Exploration of Alternative Models

Non-saturating linear MR has been observed in a variety of materials such as: topological insulators$^{37-39}$, SrTiO$_3$$^{40}$, cuprates$^{41-43}$, bismuth-based layered magnetic$^{44}$ and non-magnetic$^{11}$ compounds, metal oxides$^{45}$, silver chalcogenides$^{46}$, graphene$^{47}$ and bismuth$^{48}$. The QLM model appears to be good description for the final three materials whilst the mechanism is less clear for the others. Recently, the balance equation proposal has been applied by Wang and Lei$^{49}$ to explain linear MR in the 2D surface states of 3D topological insulators. In its original form, the balance equation proposal is potentially applicable to the ferropnictides$^{50}$. The proposal suggests that the high field MR magnitude should be proportional to the carrier density$^{49}$. We have explored this by plotting the $A_1$ coefficient multiplied by $n_{eff}^2$ against $n_{eff}$. As shown in Figs. 7B and C, discrepancies appear between the compounds. In the BaFe$_2$As$_2$ unirradiated crystal, a linear relationship is observed which not the case for the unirradiated BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystal. However, the balance equation approach is predicted to be directly proportional to the effective magnetic g-factor$^{49}$. In the ferropnictides, the magnetic g-factor is relatively small$^{51}$ suggesting this model is unlikely to be applicable.
A recent paper by Koshelev\textsuperscript{28} has explained the linear MR in terms of the FS reconstruction generated at the SDW magnetic transition. The SDW order leads to the mixing of the hole and electron bands and the creation of areas within the FS where the velocity of the carriers abruptly changes, so-called turning points. At these turning points, the normal orbital motion of the carriers in an applied magnetic field is disrupted, producing at low field an increased quadratic MR response and, above a crossover magnetic field, linear magnetoconductivity. Both the linear magnetoconductivity coefficient and $B^*$ should depend on scattering within this model. $B^*$ should vary proportionally with the inverse of the scattering time i.e. $B^*$ should increase with increased $N_i$. The extraction of $B^*$ from our data is subject to significant uncertainty (see error bars shown in Figs. 5 C and D) and within these limits it is difficult to determine the trends. However we find that the difference in magnitude of $B^*$ between the parent and the Co doped crystals is consistent with this theory.

Further clues lie in the observation that we find a correspondence in the temperature evolution of $\mu_H$ and MR $A_1$ coefficient. As shown in Fig. 7 D, the temperature dependence for both parameters is shown to be consistent throughout the entire temperature range in both compounds. This finding echoes the work in the topological insulators\textsuperscript{52}, Heusler alloys\textsuperscript{52} and MnAs-GaAs semiconductors\textsuperscript{54} indicating that the linear MR may be proportional to the $\mu_H$.

The non-linearity and shape of $\rho_{xy}(\mu_0 H)$ in BaFe$_2$As$_2$ and BaFe$_{1.983}$Co$_{0.015}$As$_2$ as shown in Fig. 2 C), bears a similarity to that of the heavy fermion\textsuperscript{55} and cuprate\textsuperscript{41} superconductors. This non-linearity is still not fully understood in any of these material families, although the anomalous Hall effect has been proposed as an explanation\textsuperscript{56}. However, as has been pointed out by many authors, the ferropnictides, heavy fermion materials and cuprates share a number of similar properties: AFM magnetic ground state, the two dimensional nature of the electronic structure and the existence of high temperature superconductivity\textsuperscript{57}; suggesting a common explanation\textsuperscript{56} for the magnetotransport behavior.

To study the high field behavior of the Hall resistivity systematically, the high field (5-7 T) linear slope of the Hall resistivity has been calculated. An extremely surprising result emerges, as shown in Figs. 8 A and B. It appears that the intercept of high field Hall (HFH) resistivity linear fitting is independent of Co doping. Without a conclusive theoretical model for the origin of the $\rho_{xy}(\mu_0 H)$ non-linearity it is impossible to understand the significance of
FIG. 8. (Color online). A) Hall resistivity for unirradiated BaFe$_2$As$_2$ (solid line) and BaFe$_{1.985}$Co$_{0.015}$As$_2$ (dashed line) crystal at 10K. Dotted lines are linear fit of high field Hall resistivity. B) high field Hall resistivity intercept against temperature for unirradiated crystals. BaFe$_2$As$_2$: , BaFe$_{1.985}$Co$_{0.015}$As$_2$: C) Kohler plots for unirradiated BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystal. D) modified Kohler plots for unirradiated BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystal.

this observation. However, it would suggest that an intrinsic property of the magnetic state is retained despite Co doping.

It is useful if we now revisit the MR properties in light of the high field Hall Effect observations. Due to the complexities of producing analytical models for the magnetotransport properties, scaling techniques are conventionally used. Kohler’s rule is the traditionally used scaling method for understanding the temperature evolution of the MR ratio. When a single species of charge carrier exists such that $m^*/n_e$ remains constant then MR can be rescaled by dividing the applied magnetic field by the $\rho_0$:

$$\text{MR ratio(}\mu_0H, T\text{)} = f\left(\frac{\mu_0H}{\rho(0, T)}\right)$$

(9)

In Fig. 8C, the Kohler plots for 10 K, 25 K, 50 K and 70 K are shown for the unirradiated BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystal. As indicated by the failure of the lines to fall upon a single curve, Kohler’s rule is clearly contravened. Furthermore, the refined Kohler rule$^{58}$, where the temperature dependence of the scattering is taken into account, does not illustrate any clear scaling. To explain violations of the Kohler rule a modified form of Kohler scaling has been developed where the MR is scaled by the Hall angle ($\tan\theta_H = \frac{\rho_{xy}}{\rho_{xx}}$):

$$\text{MR ratio(}\mu_0H, T\text{)} = f\left(\frac{\mu_0H}{\tan^2\theta_H}\right)$$

(10)
This has been shown to more accurately scale both the cuprate$^{59}$ and heavy fermion$^{60}$ superconductors. The compounds studied in this work display intriguing differences. For BaFe$_2$As$_2$, the modified Kohler form does not provide any improvement at any temperature below $T_N$, as indicated by the inset of Fig. 8 D. In contrast, the modified Kohler analysis illustrates a strong correlation at low temperatures for BaFe$_{1.985}$Co$_{0.015}$As$_2$. This pattern follows that of Ru doping indicated by Eom et al.$^{61}$. It has been suggested that the modified Kohler rule could originate from an anisotropic scattering rate due to spin fluctuations$^{61}$. In the anisotropic scattering rate scenario, the dominant electron-electron scattering process shows a large disparity within the FS due to the SDW magnetic order$^{62}$. This produces locations of larger/smaller electron and hole scattering rates, leading to so-called hot/cold spots which dominate the magnetotransport properties. It is important to note that the anisotropic scattering model has been shown to recreate the unusual Hall coefficient dependence of Co doping discussed previously$^{62}$. Nevertheless, the model would have to reconcile the differences we find between the undoped and Co doped crystals where the former shows similar non-linear high field Hall but yet its MR does not scale according to the modified Kohler rule.

IV. CONCLUSION

In summary, using the systematic introduction of scattering centers through 3-MeV proton irradiation we have studied the effect of defects on the normal state magnetotransport properties of high quality undoped BaFe$_2$As$_2$ and electron doped BaFe$_{1.985}$Co$_{0.015}$As$_2$ single crystals. We have demonstrated that the proton damage increases the scattering density and does not strongly affect other properties. The high field MR exhibits a non-saturating linear MR in all crystals, as seen in previous studies. However, we observe discrepancies between the compounds. In the undoped BaFe$_2$As$_2$ crystals, no change in the high field linear component is observed upon irradiation. In contrast, the BaFe$_{1.985}$Co$_{0.015}$As$_2$ crystals appear to display a decrease in the $A_1$ coefficient with proton irradiation, and an increasing quadratic component, although the changes to the MR curves with irradiation are in fact quite subtle. These observations are not consistent with the application of the QLM model in the ferropnictides. In addition, the Hall resistivity has been measured with increasing irradiation dose and displays a consistent non-linearity at high fields and below 100 K for all
crystals, irrespective of proton irradiation. Furthermore, the magnitude of the Hall coefficient is unaffected by the introduction of scattering defects. We have compared our observed trends with theoretical predictions. The multiband nature of the materials makes the magnetotransport trends complex and a simple explanation elusive. Nevertheless setting out how these crystal families react to systematic increase in scattering density helps to lay the foundations for further theoretical developments.

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