Multiphoton processes at cyclotron resonance subharmonics in a two-dimensional electron system under dc and microwave excitation

S. Chakraborty, A. T. Hatke, L. W. Engel, J. D. Watson, and M. J. Manfra

Phys. Rev. B 90, 195437 — Published 24 November 2014
DOI: 10.1103/PhysRevB.90.195437
Multiphoton processes at cyclotron resonance subharmonics in a 2D electron system under DC and microwave excitation

S. Chakraborty,¹ A. T. Hatke,¹ L. W. Engel,¹ J. D. Watson,²,³ and M. J. Manfra²,³

¹National High Magnetic Field Laboratory, Tallahassee, Florida 32310, USA
²Department of Physics, Purdue University, West Lafayette, Indiana 47907, USA
³Birck Nanotechnology Center, School of Materials Engineering and School of Electrical and Computer Engineering, Purdue University, West Lafayette, Indiana 47907, USA

We investigate a two dimensional electron system (2DES) under microwave illumination at cyclotron resonance subharmonics. The 2DES carries sufficient direct current, \( I \), that the differential resistivity oscillates as \( I \) is swept. At magnetic fields sufficient to resolve individual Landau levels, we find the number of oscillations within an \( I \) range systematically changes with increasing microwave power. Microwave absorption and emission of \( N \) photons, where \( N \) is controlled by the microwave power, describes our observations in the framework of the displacement mechanism of impurity scattering between Hall-field tilted Landau levels.

PACS numbers:

Low magnetic field (\( B \)) transport of two dimensional electron systems (2DESs) under nonequilibrium conditions has been a subject of intense study for over a decade. Illumination with microwave (\( ac \)) radiation results in \( 1/B \)-periodic resistance oscillations termed microwave induced resistance oscillations (MIROs)\(^1-4\). Additionally, application of sufficiently large direct current (\( dc \)) in a Hall bar geometry results in \( 1/B \)-periodic differential resistivity (\( r \)) oscillations called Hall-field induced resistance oscillations (HIROs)\(^5-7\). MIROs are periodic in \( \epsilon ac = \omega/\omega C \), where \( \omega = 2\pi f \) is the frequency of the microwave radiation and \( \omega C \) is the cyclotron frequency. MIRO maximum-minimum pairs occur symmetrically offset from integer values of \( \epsilon ac \) at \( \epsilon ac/m = \pm \phi \), where \( m \) is an integer and \( \phi \) is referred to as the phase\(^8-11\). HIROs are periodic in \( \epsilon dc = \omega H/\omega C \), where \( \omega H = \sqrt{8\pi n c I /ue} \) with \( n c \) the carrier density, \( I \) the applied direct current, and \( u e \) the Hall bar width. Maxima and minima of HIROs occur, respectively, at \( \epsilon dc = m \) and \( \epsilon dc = m - 1/2^9 \). Both oscillation types have been investigated theoretically considering two main mechanisms: the first, called the displacement mechanism\(^12-14\), is based on the modification of impurity scattering in the presence of \( ac \) or \( dc \) excitation, and the second, called the inelastic mechanism\(^15-17\), is based on microwave induced oscillations in the nonequilibrium electron distribution function versus energy. The inelastic and displacement mechanisms are argued to be valid for different experimental conditions depending on whether 1) the magnetic field is sufficiently large for the Landau levels (LLs) to be well separated, \( \omega C \tau q > \pi/2 \) where \( \tau q \) is the quantum scattering time, or 2) on whether there is \( dc \) excitation.

For large microwave intensity, MIROs can occur at rational fractions of \( \epsilon ac \), with \( \epsilon ac = 1/m \) the most readily obtainable experimental series\(^18-24\). These fractional MIROs are a result of multiphoton processes. In the displacement mechanism, transitions can occur due to sequential absorption of single photons through real intermediate states\(^24,25\), while in the inelastic mechanism, transitions occur through intermediate virtual states\(^26\). An inelastic model theory\(^26\) of fractional MIROs in the separated-LL regime incorporates virtual transitions between microwave-induced sidebands in the density of states and predicts the inelastic mechanism to overwhelm the displacement mechanism.

In this paper we study samples with applied direct current\(^27\), which is expected to suppress the inelastic mechanism relative to the displacement mechanism for \( 2\pi \epsilon dc > 1^28,29 \). Working in the regime of separated LLs, we perform a combined (\( ac + dc \))\(^30-32\) experiment, in which we subject the sample to direct current and to microwaves at fractional-\( \epsilon ac \) using a coplanar waveguide structure. We find that the number of oscillations within an \( \epsilon dc \) range changes systematically with increasing microwave power in a way that clearly depends on the number of participating photons. Our results can be described in terms of competition between scattering events involving different numbers of photons.

The microwave setup is shown schematically in Fig.1 (a). We lithographically defined a Hall bar of width \( w = 20 \mu m \), etched from a symmetrically doped GaAs/AlGaAs quantum well, and deposited Ge/Au/Ni contacts. A coplanar waveguide\(^33\) with slot width \( S = 100 \mu m \), defined as the distance between the driven center conductor and the ground plane, was superimposed on the sample surface with the Hall bar oriented along the slot. The slot confined the microwave electric field. The contacts were located \( \sim 6S \) from the slot and were shielded by the ground plane. The density, \( n \approx 3.7 \times 10^{11} \) \( cm^{-2} \), and mobility, \( \mu \approx 5.7 \times 10^{6} \) \( cm^2/Vs \), were obtained by brief illumination with a red light emitting diode at a few Kelvin. The sample was mounted on a brass block and was kept at \( T = 1.4K \) in vacuum for the measurements. The differential resistivity, \( r = dV/dI \), was measured with a lock-in amplifier at a few Hz. In this paper, \( 0 dB \) corresponds to a microwave rms voltage of \( \sim 4.3 \) mV on the center conductor\(^34\).

In Fig.1 (b) we plot \( r \) vs \( B \) obtained while driving the transmission line at frequency \( f \approx 30.5 \) GHz, power +3 dB, and fixed currents from \( I = 0 \) to \( 24 \mu A \) in steps of...
eral well-defined HIROs up to a baseline in each plot. The 0 dB trace contains several well-defined HIROs up to \( \epsilon = 31 \) GHz. A 0 dB trace (dotted line) is presented at fixed \( I \) again match those in the 0 dB trace. Vertical dashed lines denote the cyclotron resonance and its second harmonic and the dotted lines mark its second and third subharmonic. Traces are vertically offset for clarity.

For \( I = 0 \mu A \) trace \( \phi < 1/4 \) at \( \epsilon_{ac} = 2 \), which is consistent with a high power regime of previous work. Additionally, fractional MIROs centered at \( \epsilon_{ac} = 1/2 \) and 1/3 are observed. For \( I = 4 \mu A \), at \( \epsilon_{ac} = 1 (\epsilon_{dc} \sim 1/2) \) and \( \epsilon_{ac} = 1/2 (\epsilon_{dc} \sim 1/4) \), the oscillations have flipped. Maxima at \( 4 \mu A \) replace minima at \( 0 \mu A \) while minima at \( 4 \mu A \) replace maxima at \( 0 \mu A \). At \( I = 8 \mu A \) the \( \epsilon_{ac} = 1 (\epsilon_{dc} \sim 1) \) and \( \epsilon_{ac} = 1/2 (\epsilon_{dc} \sim 1/2) \) oscillation extrema again match those in the \( I = 0 \mu A \) trace. For \( I > 8 \mu A \) additional maxima and minima are observed near \( \epsilon_{ac} = 1 \) and \( \epsilon_{ac} = 1/2 \). On the \( I = 16 \mu A \) trace these extrema are marked by \( \downarrow \) and \( \uparrow \). The additional maximum and minimum near \( \epsilon_{ac} = 1 \) agree with previous high microwave power and strong direct current observations. In what follows we restrict our measurements to the separated LL regime.

In Figs. 2 and 3 we show \( r \) vs \( \epsilon_{dc} \) taken by sweeping \( I \) at fixed \( B \). Figure 2 shows data for \( \epsilon_{ac} = 1/2 \) and \( f = 31 \) GHz. A 0 dB trace (dotted line) is presented as a baseline in each plot. The 0 dB trace contains several well-defined HIROs up to \( \epsilon_{dc} = 3 \), with maxima at \( \epsilon_{dc} = m \) and minima at \( \epsilon_{dc} = m - 1/2 \). In Fig. 2(a) we show the effect of increasing the microwave power by +3 dB. Here, maxima are observed near \( \epsilon_{dc} = 1/2, 3/2 \) and \( 5/2 \). In addition, maxima at \( \epsilon_{dc} = m \) are still present, though with reduced amplitude compared to the 0 dB trace, hence the entire +3 dB trace vs \( \epsilon_{dc} \) trace in Fig. 2(a) shows a microwave power induced doubling of the \( \epsilon_{dc} \)-frequency for up to six oscillations.

Figure 2(b) shows data taken with an increased microwave power of +6 dB. The strength of the \( \epsilon_{dc} = 1/2 \) maximum is little changed, though the \( \epsilon_{dc} = 3/2 \) maximum is almost completely suppressed. The maximum at \( \epsilon_{dc} = 5/2 \) has become a minimum, now more closely resembling the 0 dB trace than the +3 dB trace. In addition, the amplitudes of the maxima at \( \epsilon_{dc} = m \) are increased relative to their values at +3 dB. For the highest microwave power, +10 dB, as shown in Fig. 2(c), \( \epsilon_{dc} = 3/2 \) is a minimum. Throughout the power dependence shown in Fig. 2, the \( \epsilon_{dc} = 1/2 \) maximum persists with only weak amplitude variation.

The same measurements except at \( \epsilon_{ac} = 1/3 \) are presented in Fig. 3. The baseline, 0 dB, trace shows only a single HIRO maximum at \( \epsilon_{dc} = 1 \) and a strong zero bias peak. In Fig. 3(a) the +3 dB trace shows a weakening of the \( \epsilon_{dc} = 1 \) maximum relative to the one at 0 dB and two additional maxima at \( \epsilon_{dc} = 2/3 \) and 4/3. For the +6 dB trace, oscillation maxima are present at \( \epsilon_{dc} = 1/3, 2/3, 1 \) and 4/3, with the \( \epsilon_{dc} = 1 \) maximum...
The main result of this paper is that the observed emission of varying photon numbers. In the separated LL regime the condition for maxima in the +3 dB trace in Fig. 3 (a) shows that ǫ_ac = 1/3 processes remain in competition with N = 2 processes. The +3 dB trace in Fig. 3 (a) shows N = ±1 processes are operational by maxima at ǫ_ac = 2/3 and ǫ_dc = 4/3, while the ǫ_ac = 1/3 maximum demonstrates that N = 0 processes remain. For the +6 dB trace in Fig. 3 (b) a combination of N = ±1 and N = 2 processes are present; N = 1 processes produce a maximum at ǫ_dc = 2/3, N = 2 processes produce a maximum at ǫ_dc = 1/3, and both N = −1 and N = 2 contribute to the maximum at ǫ_dc = 4/3. For ǫ_dc = 4/3 the N = 2 processes occur for absorption and scattering but the N = −1 process results in a maximum only if photon emission occurs, and N = +1 processes do not terminate at the center of a LL. For the +10 dB trace in Fig. 3 (c) N = 2 processes become more important than N = 1 processes at ǫ_ac = 2/3 so that a minimum is formed, instead of the maximum seen at +3 dB and +6 dB.

Though Eq. 1 compactly describes our observations, the numerical results of Ref. 29 do not discuss the role of microwave power. For the separated LL regime, Ref. 29 reproduced the experimentally observed ǫ_dc-frequency doubling of Ref. 41 and predicted a rough ǫ_dc-frequency tripling at ǫ_ac = 1/3. An extension of 29 to an analytic theory 42, using the overlapping LL simplification, failed to produce the additional oscillations near ǫ_ac = 1/2 in Fig. 1 (b) and did not show the presently reported ǫ_dc-frequency change at fractional MIROs.

Previous works do not adequately predict our observations, which are explainable within the displacement mechanism framework of Eq. 1. Reference 43 advanced a displacement description of the inversion of extrema observed in r vs I at ǫ_ac = 3/2 for overlapping LLs at large microwave power, but that picture does not match our observed ǫ_dc-frequency change at ǫ_ac = 1/2 or ǫ_ac = 1/3.
Lastly, a theory of the displacement mechanism that incorporated multiphoton processes in the overlapping LL regime near $\varepsilon_{\text{ac}} = 1$ does not extend to the fractional-$\varepsilon_{\text{ac}}$ regime.

In summary we have investigated the direct current response of fractional microwave induced resistance oscillations under variable microwave radiation power using a coplanar waveguide technique. With the reasonable expectation that larger $N$ processes succeed small $N$ processes at larger microwave power, we find the simple, separated-Landau-level displacement description of Eq. 1 describes the observed $\varepsilon_{\text{ac}}$-frequency change. Our results suggest that a theoretical treatment of combined dc excitation and microwave photons of arbitrary number when the levels are well separated is necessary.

We would like to thank M. A. Zudov for enlightening conversations and critical comments of the manuscript. The work was supported through DOE grant DE-FG02-05-ER46212 (NHMFL/FSU) and DE-SC0006671 (Purdue). The National High Magnetic Field Laboratory, is supported by NSF Cooperative Agreement No. DMR-0654118, by the State of Florida, and by the DOE.

25. I. V. Pechenezhskii, S. I. Dorozhkin, and I. A. Dmitriev,
We obtain the power, $P$, at the sample as the average of the input and output powers at cryostat top and calculated the voltage as $V = \sqrt{2(50\Omega)P}$. Additionally, we estimated the loss due to the sample by comparing the transmission at $B = 5$ T and $B = 0$ T. The loss is not present at 5 T, at which the sample conductivity is very small. We estimate the sample to remove $<2$ dB from the transmitted signal in the magnetic field of the experiments.

In Ref.\textsuperscript{31} there was a transition in the MIRO amplitude versus power from linear to sublinear as power was increased. This transition was concurrent with $\phi$ at $\epsilon_{ac} = 2$ decreasing from $1/4$. We define the regime of microwave power above this transition as the high power regime.

The position of the $\epsilon_{dc} = 1/2$ maximum appears slightly lower than 1/2, a result which was seen both in experiment\textsuperscript{41} and theory\textsuperscript{29}. For ease of discussion we will continue to refer to this maximum as $\epsilon_{dc} = 1/2$.

In the absence of microwave radiation the HIRO period is given by $\epsilon_{dc}$ with maxima at $\epsilon_{dc} = m$. Under microwave radiation at $\epsilon_{ac} = 1/2$ a maximum at $\epsilon_{dc} = 1/2$ was observed\textsuperscript{41} resulting in reduction of the HIRO period, or doubling of the $\epsilon_{dc}$-frequency, but restricted to only two oscillations.