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## Systematic variation of spin-orbit coupling with d-orbital filling: Large inverse spin Hall effect in 3d transition metals

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# Surprisingly large inverse spin Hall effect and systematic variation of spin-orbit coupling with $d$ -orbital filling in $3d$ transition metals

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## Abstract

It is generally believed that spin-orbit coupling (SOC) follows  $Z^4$  (atomic number) dependence and becomes significant only in heavy elements. Consequently, SOC in  $3d$  transition metals should be negligible given their small  $Z$ . Using dynamic spin pumping of  $\text{Y}_3\text{Fe}_5\text{O}_{12}$ -based structures, we uncover a systematic evolution of spin Hall angle ( $\theta_{\text{SH}}$ ) with  $d$ -orbital filling in a series of  $3d$  metals, reminiscent of behavior observed in  $5d$  metals. In particular, Cr and Ni show very large  $\theta_{\text{SH}}$  (half of that for Pt), indicating that  $d$ -orbital filling rather than  $Z$  plays a dominant role in spin Hall effect (SHE) in  $3d$  metals. This result enriches our understanding of SHE and broadens the scope of materials available for exploring the rich phenomena enabled by SOC as well as presenting a guidepost for testing theoretical models of spin-orbit coupling in transition metals.

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Spin-orbit coupling is the underlying mechanism for magnetocrystalline anisotropy [1], anomalous Hall effect [2], and more recently, spin Hall effect [3] and topological insulators [4]. It is generally believed that SOC varies as  $Z^4$  [5-7], implying that SOC is important only in heavy elements, while in lighter elements such as  $3d$  transition metals, SOC should be negligibly small. SHE depends on the SOC and  $\theta_{\text{SH}}$  is a measure of the strength of SOC. Because of the generally accepted  $Z^4$  dependence of SOC, measurement of  $\theta_{\text{SH}}$  has been focused on heavy elements by SHE [8] or inverse spin Hall effect (ISHE) [9-15], while  $3d$  metals have rarely been studied [16, 17].

Ferromagnetic resonance (FMR) spin pumping of pure spin currents from a ferromagnet (FM) into a nonmagnetic (NM) material provides a powerful technique for measurement of  $\theta_{\text{SH}}$  in a broad range of materials [7, 9]. We report a systematic study of the ISHE in a series of  $3d$  transition metals using FMR spin pumping from  $\text{Y}_3\text{Fe}_5\text{O}_{12}$  (YIG) epitaxial films into Ti, V, Cr, Mn,  $\text{Fe}_{50}\text{Mn}_{50}$  (FeMn),  $\text{Fe}_{20}\text{Ni}_{80}$  (Py), Ni, and Cu. The large ISHE signals in our YIG-based structures [7, 15, 18-21] provides unprecedented sensitivity for characterizing the ISHE in  $3d$  metals which are expected to have weak SOC. Surprisingly, we detect an ISHE voltage ( $V_{\text{ISHE}}$ ) exceeding 5 mV in a YIG/Cr(5 nm) bilayer, which is among the highest  $V_{\text{ISHE}}$  we observed in any materials [7, 15].

We deposit epitaxial YIG films on (111)-oriented  $\text{Gd}_3\text{Ga}_5\text{O}_{12}$  (GGG) substrates [7, 15, 22]. A  $2\theta$ - $\omega$  x-ray diffraction (XRD) scan of a 25-nm YIG film shown in Fig. 1(a) shows clear Laue oscillations. The x-ray reflectometry (XRR) spectrum of a 40-nm YIG film in Fig. 1(b) reflects the smooth YIG surface. The atomic force microscopy (AFM) image in the inset to Fig. 1(b) exhibits a roughness of only 0.106 nm. Figure 1(c) shows the derivative of a FMR absorption spectrum for a 20-nm YIG film taken in a FMR cavity at a radio-frequency (rf)  $f =$

9.65 GHz and a microwave power  $P_{\text{rf}} = 0.2$  mW, which gives a peak-to-peak linewidth ( $\Delta H$ ) of 9.5 Oe. Spin pumping measurements are carried out at room temperature on YIG/metal bilayers (approximate dimensions of 1 mm  $\times$  5 mm). A DC magnetic field  $\mathbf{H}$  is applied in the  $xz$ -plane and the ISHE voltage is measured across the  $\sim 5$ -mm long metal layer along the  $y$ -axis, as illustrated in Fig. 1(d).

Figures 2(a) to 2(f) show  $V_{\text{ISHE}}$  vs.  $H - H_{\text{res}}$  spectra ( $H_{\text{res}}$  is the resonance field of the YIG) of YIG/metal(10 nm) bilayers for Ti, V, Cr, Mn, FeMn, and YIG/Cu(10 nm)/Ni(10 nm) trilayer at two opposite in-plane field orientations  $\theta_{\text{H}} = 90^\circ$  and  $270^\circ$  using  $P_{\text{rf}} = 200$  mW, which exhibit  $V_{\text{ISHE}} = -24.6 \mu\text{V}$ ,  $-594 \mu\text{V}$ ,  $-2.55 \text{ mV}$ ,  $-549 \mu\text{V}$ ,  $-4.65 \mu\text{V}$ , and  $39.4 \mu\text{V}$ , respectively, at  $\theta_{\text{H}} = 90^\circ$ . The negative sign in  $V_{\text{ISHE}}$  arises from the convention of positive  $V_{\text{ISHE}}$  for YIG/Pt at  $\theta_{\text{H}} = 90^\circ$ . The strong exchange coupling between YIG and Ni induces such substantial additional damping of the YIG that we use YIG/Cu/Ni trilayers to determine  $\theta_{\text{SH}}$  as reported previously [21]. The 2.5-mV ISHE signal measured in YIG/Cr(10 nm) is exceptionally large and comparable to the values detected in  $5d$  metals Ta, W, and Pt on our YIG films [7, 15]. This suggests unexpectedly large  $\theta_{\text{SH}}$  and surprisingly strong SOC in Cr. Given the relatively small  $Z$  of  $3d$  elements, we explore the potential role of  $d$ -orbital configuration and antiferromagnetism (AF), e.g., in Cr and FeMn, [23] in this surprising result. The detailed study of eight  $3d$  transition metals [7, 21] presented here uncovers unexpected role of  $d$ -orbital filling in spin Hall physics in this group of light materials.

The mV-level  $V_{\text{ISHE}}$  observed in YIG/Cr is surprising since the SOC in Cr ( $Z = 24$ ) has been considered negligible.  $\theta_{\text{SH}}$  is a measure of SOC and can be calculated from [9, 10, 12, 14],

$$V_{\text{ISHE}} = -e\theta_{\text{SH}}wR\lambda_{\text{SD}} \tanh\left(\frac{t_{\text{NM}}}{2\lambda_{\text{SD}}}\right) g^{\uparrow\downarrow} f P \left(\frac{\gamma h_{\text{rf}}}{4\pi\alpha f}\right)^2, \quad (1)$$

where  $e$  is the electron charge,  $w$ ,  $R$  and  $t_{\text{NM}}$  are the sample width, resistance and thickness,

respectively, of the Cr layer,  $\lambda_{\text{SD}}$  is the spin diffusion length of Cr,  $g^{\uparrow\downarrow}$  is the interfacial spin mixing conductance,  $P = 1.21$  is a factor arising from the ellipticity of the magnetization precession [7],  $\gamma$  is the gyromagnetic ratio,  $h_{\text{rf}} = 0.25$  Oe is the rf field at  $P_{\text{rf}} = 200$  mW [7], and  $\alpha$  is the Gilbert damping constant of YIG. To calculate  $\theta_{\text{SH}}$ , we first determine  $\lambda_{\text{SD}}$  from the Cr thickness ( $t_{\text{Cr}}$ ) dependence of  $V_{\text{ISHE}}$  [Fig. 2(g)], which is partially due to the variation in resistivity ( $\rho$ ) of the Cr films [Fig. 2(h)] similar to the behavior reported previously [24]. The ISHE-induced charge current  $I_c = V_{\text{ISHE}}/R$  is proportional to the spin current pumped into Cr [7, 15]. Figure 2(i) plots the  $t_{\text{Cr}}$  dependence of  $V_{\text{ISHE}}/Rw$ , from which we obtain  $\lambda_{\text{SD}} = 13.3 \pm 2.1$  nm by fitting to  $\frac{V_{\text{ISHE}}}{Rw} \propto \lambda_{\text{SD}} \tanh\left(\frac{t_{\text{Cr}}}{2\lambda_{\text{SD}}}\right)$  [25].  $g^{\uparrow\downarrow}$  can be obtained from the spin-pumping enhancement of damping [9-12],

$$g^{\uparrow\downarrow} = \frac{4\pi M_s t_{\text{YIG}}}{g\mu_B} (\alpha_{\text{YIG/NM}} - \alpha_{\text{YIG}}), \quad (2)$$

where  $g$ ,  $\mu_B$ , and  $t_{\text{YIG}}$  are the Landé factor, Bohr magneton, and YIG thickness, respectively. We determine the damping constants of a bare YIG film ( $\alpha_{\text{YIG}}$ ) and a YIG/Cr bilayer ( $\alpha_{\text{YIG/NM}}$ ) from the frequency dependencies of the FMR linewidth measured using a microstrip transmission line [Fig. 3(a)]. The linewidth increases linearly with frequency:  $\Delta H = \Delta H_{\text{inh}} + \frac{4\pi\alpha f}{\sqrt{3}\gamma}$  [26], where  $\Delta H_{\text{inh}}$  is the inhomogeneous broadening. Table I shows the damping enhancement due to spin pumping:  $\alpha_{\text{sp}} = \alpha_{\text{YIG/NM}} - \alpha_{\text{YIG}}$ , where  $\alpha_{\text{YIG/NM}}$  and  $\alpha_{\text{YIG}} = (8.7 \pm 0.6) \times 10^{-4}$  are obtained from the least-squares fits in Fig. 3(a). Thus, we calculate  $g^{\uparrow\downarrow} = (8.3 \pm 0.7) \times 10^{17} \text{ m}^{-2}$  for the YIG/Cr interface and  $\theta_{\text{SH}} = -0.051 \pm 0.005$  for Cr. This surprisingly large  $\theta_{\text{SH}}$  is half the value of Pt [7].

Using the same approach, we obtain  $\theta_{\text{SH}}$  for other  $3d$  metals. The spin diffusion lengths of V, Mn, and Ni are determined to be  $14.9 \pm 2.4$ ,  $10.7 \pm 1.1$ , and  $3.2 \pm 0.1$  nm as shown in Figs.

2(j), 2(k), and 2(l), respectively. Considering that V, Cr, and Mn all have similar spin diffusion lengths, and since  $\theta_{\text{SH}}$  is virtually insensitive to  $\lambda_{\text{SD}}$  when  $\lambda_{\text{SD}} \geq t_{\text{NM}}$  [due to the term  $\lambda_{\text{SD}} \tanh(\frac{t_{\text{NM}}}{2\lambda_{\text{SD}}})$  in Eq. (2)], it is safe to assume  $\lambda_{\text{SD}}$  of Ti is similar to Cr. The calculated values of  $\theta_{\text{SH}}$  for Ti and Mn are very small (Table I) while the spin Hall angles for V and Ni are quite large for  $3d$  metals.

To highlight the systematic behavior of  $\theta_{\text{SH}}$ , we plot  $\theta_{\text{SH}}$  vs.  $Z$  in Fig. 3(b) for the eight  $3d$  metals. We note that V, Cr, and Ni with large  $\theta_{\text{SH}}$  sit directly above Ta, W, and Pt in the periodic table, respectively, which exhibit some of the largest  $\theta_{\text{SH}}$ . This suggests that the  $d$ -electron configuration of the transition metals plays a very important role in SHE, consistent with the prediction of Tanaka *et al.* [27] who illuminated the role of the total number of  $4d$  ( $5d$ ) and  $5s$  ( $6s$ ) electrons in the SHE in the  $4d$  ( $5d$ ) metals. To understand the role of  $d$ -electrons, we list in Table I the total number of  $3d$  and  $4s$  electrons,  $n_{3d+4s}$ . We note that  $\theta_{\text{SH}}$  varies significantly both in sign and magnitude:  $\theta_{\text{SH}}$  is negative from Ti ( $n_{3d+4s} = 4$ ) to FeMn ( $n_{3d+4s} = 7.5$ ) and changes to positive for Py ( $n_{3d+4s} = 9.6$ ), Ni ( $n_{3d+4s} = 10$ ) and Cu ( $n_{3d+4s} = 11$ ) while its magnitude reaches maximum at Cr ( $n_{3d+4s} = 6$ ) and Ni ( $n_{3d+4s} = 10$ ). The sign change in  $\theta_{\text{SH}}$  mimics the trend observed in  $5d$  metals [7, 13, 27, 28], while the magnitude of  $\theta_{\text{SH}}$  spans a range of almost three orders of magnitude. From Fig. 3(b) and our previous result on  $5d$  metals [7], we can gain insights into the underlying mechanisms responsible for the SHE and SOC in transition metals.

There are three mechanisms that could be responsible for SHE in transition metals: 1) atomic number, 2)  $d$ -electron count, and 3) magnetic ordering; we address these separately below. First, while the atomic number may play a role in SHE in  $3d$  metals, it is not a dominant factor: for example, between Cr and W which belong to the same VIB transition metal group, the

$Z^4$  dependence predicts a difference of 90 times in their SOC strengths and  $\theta_{\text{SH}}$ , while our experimental values show a factor of 2.7 in  $\theta_{\text{SH}}$  between the two elements.

Secondly, we can also rule out magnetic ordering in the  $3d$  metals as the dominant factor. While Cr and Ni exhibit large  $\theta_{\text{SH}}$ , they also possess magnetic ordering: Cr is an AF [23] and Ni is a FM. To probe the role of AF ordering in ISHE in  $3d$  metals, we compare the spin Hall angles of Cr and FeMn, a robust AF. The  $\theta_{\text{SH}}$  of Cr is 689 times larger than that of FeMn (Table I). The dramatic difference in the two  $3d$  AF metals suggests that the surprisingly large  $\theta_{\text{SH}}$  in Cr does not arise from its AF order [29]. The very small  $\theta_{\text{SH}}$  of FeMn also agrees with the theoretical prediction for  $4d$  and  $5d$  metals [27] in that at  $n_{3d+4s} \approx 7.5$ , the spin Hall conductivity (SHC) crosses zero.

For FM metal Ni, we consider the two elements directly below Ni in the periodic table, Pd and Pt. Tanaka *et al.* [27] calculate that the SHC of Pd is  $\sim 70\%$  of that for Pt, much larger than the 11% predicted from the  $Z^4$  dependence. If we similarly assume a 70% ratio in SHC for Ni relative to Pd, we would conclude that the SHC for Ni is 49% that of Pt: very close to our experimentally measured ratio. This is without considering the FM ordering in Ni. Thus, the surprisingly large values and significant variation in  $\theta_{\text{SH}}$  of  $3d$  metals arise mainly from the  $d$ -electron configuration, indicating its dominant role in spin Hall physics [7, 13, 27, 28].

Taken together, our results in  $3d$  and  $5d$  [7] metals reveal a surprising feature of ISHE: the effects of atomic number and  $d$ -orbital filling are additive—not multiplicative—indicating they operate independently, and each of these mechanisms can be of comparable importance. This means that if either contribution ( $Z$  or  $d$ ) is large, the SHE is large, not that if either one is small, the SHE is small. For example, the  $Z^4$  dependence is clearly dominant in the Cu, Ag, and Au series [7] whose filled  $d$ -shells have zero orbital moment and do not contribute to the ISHE;

while for transition metals with partially filled  $d$ -orbitals, the  $d$ -orbital contribution to the ISHE is dominant, as demonstrated by the variation of sign and magnitude of  $\theta_{\text{SH}}$  in both  $3d$  and  $5d$  transition metals.

Furthermore, we confirm the influence of Cr antiferromagnetism on the static and dynamic magnetization of YIG. Cr is an incommensurate AF with a Néel temperature of 311 K in the bulk [23]. In Cr thin films, the AF ordering temperature is reduced. The static or dynamic AF ordered spins in Cr are expected to couple to the YIG magnetization via interfacial exchange interaction [30], resulting in possible exchange bias and enhanced coercivity ( $H_c$ ) [31]. The room temperature, in-plane magnetic hysteresis loops for a 20-nm YIG film and YIG/Cr( $t_{\text{Cr}}$ ) bilayers with  $t_{\text{Cr}} = 10, 35, 50,$  and  $100$  nm shown in Fig. 4 demonstrate that this is in fact the case. The bare YIG film exhibits a square hysteresis loop with a very small  $H_c = 0.35$  Oe and a very sharp magnetic switching. At  $t_{\text{Cr}} = 10$  nm,  $H_c$  only increases slightly to 0.52 Oe, suggesting that at 10 nm, the correlation of Cr spins is fairly weak. As  $t_{\text{Cr}}$  increases,  $H_c$  continuously rises and reaches 1.73 Oe, indicating strengthening AF correlation with increasing  $t_{\text{Cr}}$ . This observation is further verified by the magnetic damping enhancement shown in the inset to Fig. 4, where the YIG/Cr(100 nm) exhibits a much larger damping constant than the YIG/Cr(10 nm). As a comparison, both the 10-nm and 100-nm vanadium films induce similar damping in YIG due to its nonmagnetic nature.

In conclusion, we observe surprisingly large, mV-level ISHE voltages in YIG/Cr bilayers and robust spin pumping signals in other  $3d$  metals. By measuring ISHE voltages and damping enhancement, we determine the spin Hall angles of eight  $3d$  metals, which reveal unexpected systematic behavior involving both sign change and dramatic variation in magnitude, implying the dominant role of  $d$ -electron configuration in SHE of  $3d$  metals. Theoretical calculations



similar to those performed for  $4d$  and  $5d$  transition metals [27] are needed for thorough understanding of the underlying mechanisms responsible for the observed large SHE in  $3d$  transition metals.

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**Table I.** Total number of 3d and 4s electrons ( $n_{3d+4s}$ ), ISHE voltages at  $f = 9.65$  GHz and  $P_{\text{rf}} = 200$  mW, Gilbert damping enhancement due to spin pumping  $\alpha_{\text{sp}} = \alpha_{\text{YIG/NM}} - \alpha_{\text{YIG}}$  ( $\alpha_{\text{YIG}} = 8.7 \pm 0.6 \times 10^{-4}$ ) and the calculated interfacial spin mixing conductance, electrical resistivity, spin diffusion length, and spin Hall angle for each metal (alloy).

Bilayer/ Trilayer	$n_{3d+4s}$	$ V_{\text{ISHE}} $	$\alpha_{\text{sp}}$	$g^{\uparrow\downarrow}$ ( $\text{m}^{-2}$ )	$\rho$ ( $\Omega \text{ m}$ )	$\lambda_{\text{SD}}$ (nm)	$\theta_{\text{SH}}$
YIG/Ti	4	24.6 $\mu\text{V}$	$(1.8 \pm 0.1) \times 10^{-3}$	$(3.5 \pm 0.3) \times 10^{18}$	$3.0 \times 10^{-6}$	$\sim 13.3$	$-(3.6 \pm 0.4) \times 10^{-4}$
YIG/V	5	594 $\mu\text{V}$	$(1.6 \pm 0.1) \times 10^{-3}$	$(3.1 \pm 0.3) \times 10^{18}$	$2.9 \times 10^{-6}$	14.9	$-(1.0 \pm 0.1) \times 10^{-2}$
YIG/Cr	6	2.55 mV	$(4.3 \pm 0.3) \times 10^{-4}$	$(8.3 \pm 0.7) \times 10^{17}$	$8.3 \times 10^{-6}$	13.3	$-(5.1 \pm 0.5) \times 10^{-2}$
YIG/Mn	7	549 $\mu\text{V}$	$(2.3 \pm 0.2) \times 10^{-3}$	$(4.5 \pm 0.4) \times 10^{18}$	$9.8 \times 10^{-6}$	10.7	$-(1.9 \pm 0.1) \times 10^{-3}$
YIG/FeMn	7.5	4.65 $\mu\text{V}$	$(2.5 \pm 0.2) \times 10^{-3}$	$(4.9 \pm 0.4) \times 10^{18}$	$2.8 \times 10^{-6}$	3.8 [32]	$-(7.4 \pm 0.8) \times 10^{-5}$
YIG/Cu/Py	9.6	23.7 $\mu\text{V}$	$(3.3 \pm 0.3) \times 10^{-3}$	$(6.3 \pm 0.5) \times 10^{18}$		1.7	$(2.0 \pm 0.5) \times 10^{-2}$
YIG/Cu/Ni	10	39.4 $\mu\text{V}$	$(1.0 \pm 0.1) \times 10^{-3}$	$(2.0 \pm 0.2) \times 10^{18}$		3.2	$(4.9 \pm 0.5) \times 10^{-2}$
YIG/Cu	11	0.99 $\mu\text{V}$	$(8.1 \pm 0.6) \times 10^{-4}$	$(1.6 \pm 0.1) \times 10^{18}$	$6.3 \times 10^{-8}$	500	$(3.2 \pm 0.3) \times 10^{-3}$

## Figure captions:

**Figure 1.** (a) Semi-log  $2\theta$ - $\omega$  XRD scan of a 25-nm YIG film, which exhibits clear Laue oscillations. (b) X-ray reflectometry spectrum of a YIG(40 nm) film on GGG. Inset: AFM image of a 25-nm YIG film with a roughness of 0.106 nm. (c) A room-temperature FMR derivative spectrum of a YIG film with an in-plane field at  $P_{\text{rf}} = 0.2$  mW, which gives  $\Delta H = 9.5$  Oe. (d) Schematic of experimental setup for ISHE measurements.

**Figure 2.**  $V_{\text{ISHE}}$  vs.  $H - H_{\text{res}}$  spectra of (a) YIG/Ti, (b) YIG/V, (c) YIG/Cr, (d) YIG/Mn, (e) YIG/Fe<sub>50</sub>Mn<sub>50</sub> bilayers and (f) YIG/Cu/Ni trilayer at  $\theta_{\text{H}} = 90^\circ$  (red) and  $270^\circ$  (blue) using  $P_{\text{rf}} = 200$  mW. Cr thickness dependence of (g) ISHE voltage, (h) resistivity, and (i) ISHE-induced charge current ( $V_{\text{ISHE}}/R$ ) normalized by sample width  $w$  of YIG/Cr( $t_{\text{Cr}}$ ) bilayers. A spin diffusion length of  $\lambda_{\text{SD}} = 13.3 \pm 2.1$  nm is obtained from (i). (j) V, (k) Mn, and (l) Ni thickness dependencies of ISHE-induced charge currents normalized by  $w$  of the YIG/V( $t_{\text{V}}$ ), YIG/Mn( $t_{\text{Mn}}$ ), and YIG/Ni( $t_{\text{Ni}}$ ) bilayers give  $\lambda_{\text{SD}} = 14.9 \pm 2.4$ ,  $10.7 \pm 1.1$ , and  $3.2 \pm 0.1$  nm for V, Mn, and Ni, respectively.

**Figure 3.** (a) Frequency dependencies of FMR linewidth of a bare YIG film, five YIG/metal bilayers, and a YIG/Cu/Ni trilayer. (b)  $Z$  dependence of the calculated  $\theta_{\text{SH}}$  of  $3d$  transition metals shows a surprisingly large variation of  $\theta_{\text{SH}}$  with  $n_{3d+4s}$ .

**Figure 4.** Influence of film thickness on Cr antiferromagnetism: room temperature magnetic hysteresis loops of a single YIG(20 nm) film and YIG/Cr bilayers with  $t_{\text{Cr}} = 10, 35, 50,$  and  $100$  nm, which give coercivities of 0.35, 0.52, 0.74, 1.26, and 1.73 Oe, respectively. The inset shows the frequency dependencies of FMR linewidth of YIG/Cr(10 nm) and YIG/Cr(100 nm).

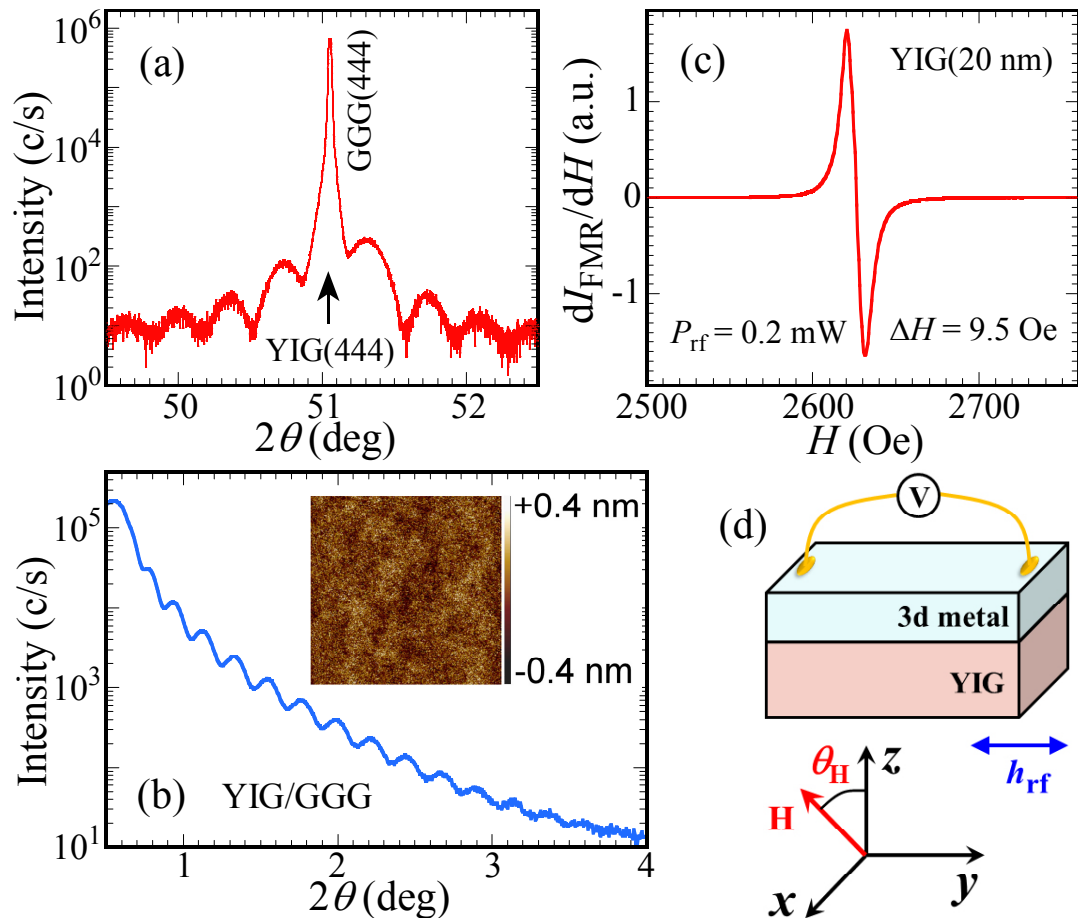
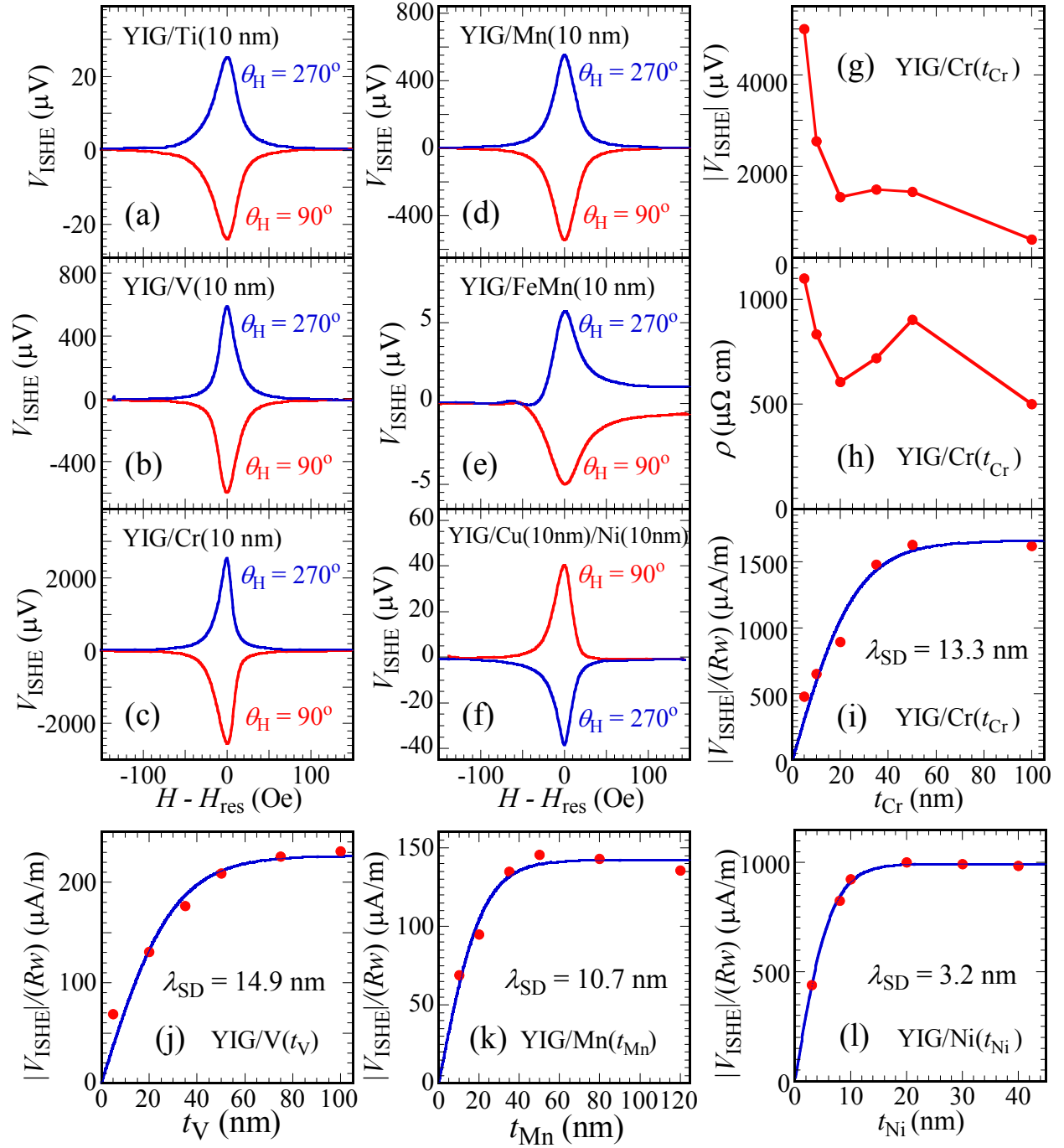


Figure 1



**Figure 2**



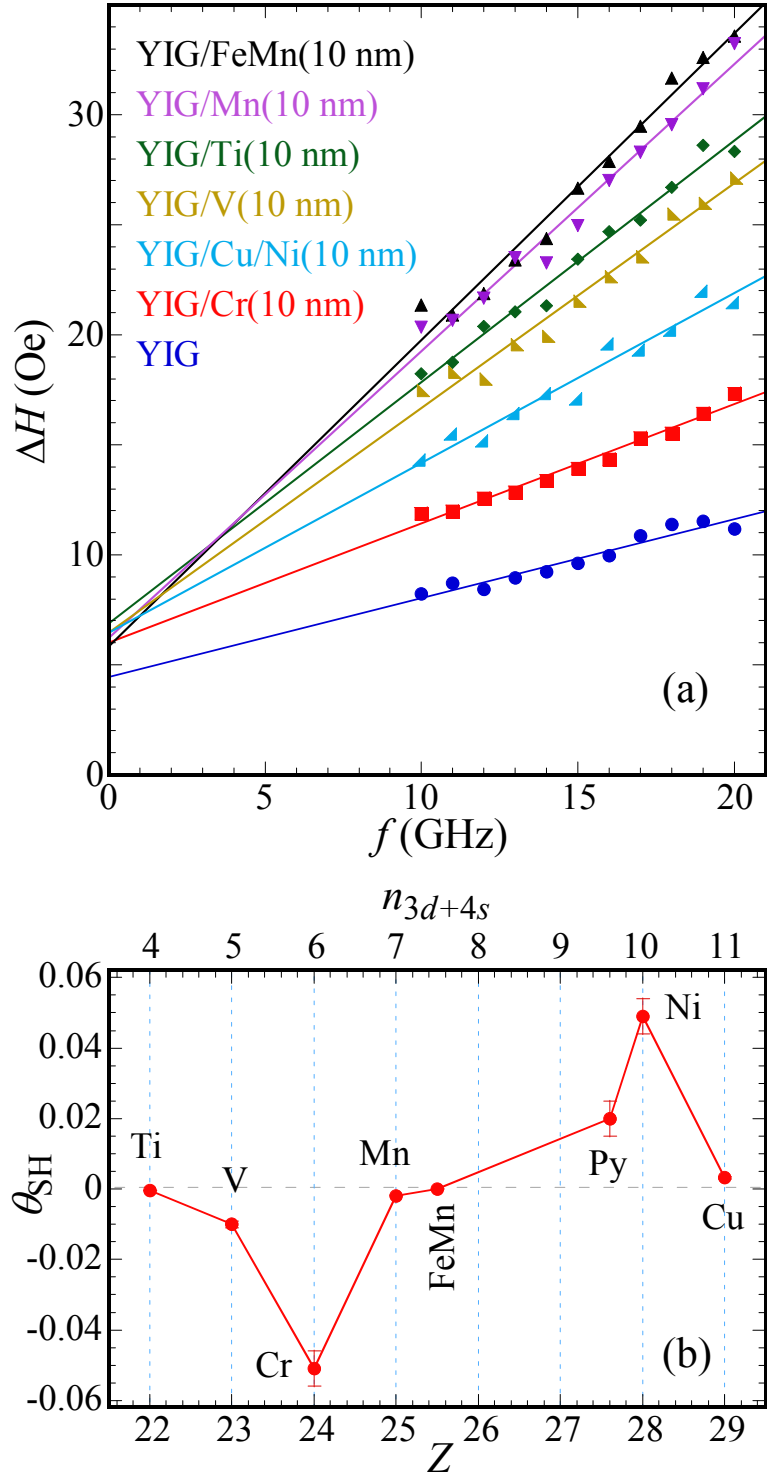


Figure 3

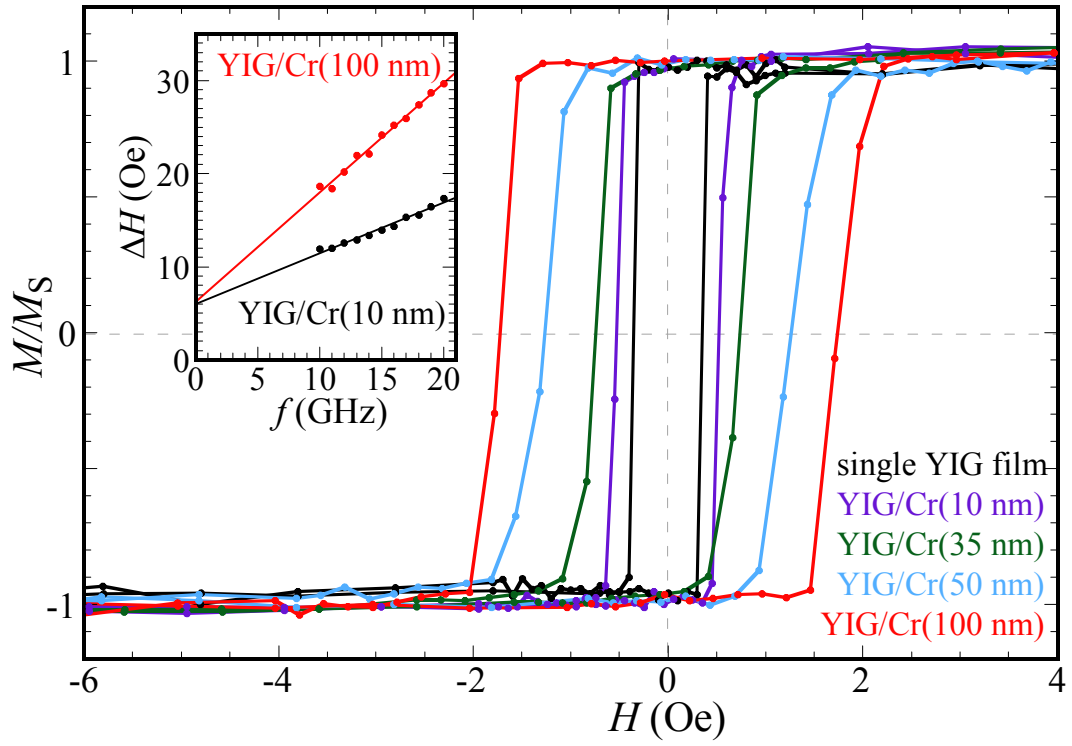


Figure 4