

This is the accepted manuscript made available via CHORUS. The article has been published as:

Semiconducting ferroelectric perovskites with intermediate bands via B-site Bi^{5+} doping

Lai Jiang, Ilya Grinberg, Fenggong Wang, Steve M. Young, Peter K. Davies, and Andrew M. Rappe

Phys. Rev. B **90**, 075153 — Published 29 August 2014

DOI: [10.1103/PhysRevB.90.075153](https://doi.org/10.1103/PhysRevB.90.075153)

1 Semiconducting ferroelectric perovskites with intermediate bands 2 via B -site Bi^{5+} doping

3 Lai Jiang,¹ Ilya Grinberg,¹ Fenggong Wang,¹ Steve M.
4 Young,¹ Peter K. Davies,² and Andrew M. Rappe^{1,2,*}

5 ¹*The Makineni Theoretical Laboratories, Department of Chemistry,*
6 *University of Pennsylvania, Philadelphia, PA 19104-6323*

7 ²*Department of Materials Science and Engineering,*
8 *University of Pennsylvania, Philadelphia, PA 19104-6272*

Abstract

We propose B -site Bi^{5+} -doped ferroelectric perovskite materials as suitable candidates for the bulk photovoltaic effect and related solar applications. The low-lying $6s$ empty states of the electronegative Bi atom produce empty bands in the energy gap of the parent materials, effectively lowering the band gap by 1–2 eV, depending on the composition of the ferroelectric end member and the concentration of Bi^{5+} in the solid solution. The polarization decreases but survives upon doping, which enables the “shift current” mechanism for photocurrent generation, while the decreased band gap allows absorption of much of the visible spectrum. The magnitude of shift current response is calculated for $0.75\text{Pb}_2\text{InNbO}_6\text{-}0.25\text{Ba}_2\text{InBiO}_6$ (PIN-BIB) and $0.75\text{Pb}_2\text{ScNbO}_6\text{-}0.25\text{Sr}_2\text{ScBiO}_6$ (PSN-SSB) and is predicted to exceed the visible light bulk photovoltaic response of all previously reported materials, including BiFeO_3 . Furthermore, the existence of their intermediate bands and multiple band gaps, combined with Fermi level tuning by A -site co-doping, also allows for their potential application in traditional $p - n$ junction-based solar cells as broad-spectrum photoabsorbers.

* rappe@sas.upenn.edu

9 I. INTRODUCTION

10 The capture and conversion of solar energy has recently been of great interest due to
11 its abundance, accessibility and sustainability. However, the efficiency of the current com-
12 mercially available $p - n$ junction based solar cells is limited by the Shockley-Queisser (SQ)
13 limit [1]. Additionally, fabrication of solar cells is complicated by the need to form an
14 interface to enable excited carrier separation. Polar materials, on the other hand, can
15 generate current throughout the bulk when illuminated, due to the lack of inversion sym-
16 metry [2–5]. Several mechanisms have been proposed to explain the bulk excited carrier
17 separation in ferroelectrics (FEs) and the above-band-gap photovoltages that have been
18 observed in FE-based cells [6–11]. Among them, the shift-current mechanism, in which
19 photo-excited coherent states possess intrinsic momentum and generate photocurrent, has
20 been shown to corroborate experimental observations [12]. FE ABO_3 perovskite oxides such
21 as $Pb(Zr_{1/2}Ti_{1/2})O_3$ [13] and $BiFeO_3$ [14–16] have been the subject of most of the solar
22 absorber FE investigations, due their large polarizations and robustness. However, these
23 FE oxides have band gaps (E_g) well above the visible range (≥ 3 eV) and therefore cannot
24 absorb most of the solar spectrum [17–21]. This has inspired theoretical and experimental
25 efforts to find FE oxide materials with low band gaps. [22–24] We have previously reported
26 that introducing a combination of Ni ions and oxygen vacancies into FE perovskites gives
27 rise to a smaller gap in the visible range, by modifying the relative energy levels of the band
28 edges [22, 23]. A visible light FE photovoltaic has been recently predicted and experimen-
29 tally demonstrated [25].

30 In this study, we opt for a different approach; band gap reduction is achieved by intro-
31 ducing low-lying empty intermediate bands (IBs) in the middle of the band gap through
32 dopant substitutions. In addition to the benefit of a reduced band gap, the presence of a
33 band in between the valence band (VB) and conduction band (CB) also opens the possi-
34 bility of co-doping with donors to make the intermediate band half-filled. Materials with
35 such half-filled IBs, mostly highly mismatched alloys, have been predicted to be as efficient
36 as multi-junction solar cells, while avoiding the complexity of traditional multi-junction or
37 tandem device structures. The theoretical conversion efficiency of a single IB solar cell can
38 be up to 62%, and even higher efficiency of up to 72% is predicted for materials with two
39 IBs [26–29].

We choose the Bi^{5+} cation as a substituent on the B -site of FE perovskites to create the IB state. Previous studies have shown that $\text{Ba}_2\text{ReBiO}_6$ (rare earth $\text{Re} = \text{La, Ce, Nd, Sm, Eu, Gd, Dy}$) double perovskites have a low-lying IB comprising Bi $6s$ and O $2p$ orbitals, with an additional CB ≈ 1.5 eV higher comprising Re orbitals [30]. The high electronegativity of Bi^{5+} and the $6s$ character of the orbitals lead to a low-lying CB [31] that does not involve the empty states of the other metal atoms. This is unlike the band anticrossing approach used in highly mismatched alloys, which relies on the interaction between localized dopant states and an extended semiconductor matrix to split the IB from the CB [32, 33]. The presence of an IB in $\text{Ba}_2\text{ReBiO}_6$ materials suggests that it is possible to create IB states by substitution of Bi^{5+} into a transition-metal-based FE perovskite. For example, the substitution of as little as 5% Bi^{5+} into $\text{Ba}_2\text{InTaO}_6$ reduces E_g from 2.97 eV to 1.70 eV [34]. However, there are no reports of Bi^{5+} -doped ferroelectrics. We therefore use first-principles calculations to study the structural and electronic properties of $(1-x)\text{KNbO}_3 - x\text{KBiO}_3$ (KNB), $(1-x)\text{Pb}_2\text{InNbO}_6 - x\text{Ba}_2\text{InBiO}_6$ (PIN-BIB) and $(1-x)\text{Pb}_2\text{ScNbO}_6 - x\text{Ba}_2\text{ScBiO}_6$ (PSN-BSB) solid solutions. We hypothesize that the combination of a ferroelectric end-member and Bi^{5+} on the B will reduce the band gap while preserving ferroelectricity.

II. METHODOLOGY

We performed density functional theory (DFT) calculations using the norm-conserving nonlocal pseudopotential plane-wave method [35]. The pseudopotentials [36] are generated using the OPIUM package [37] with a 50 Ry cutoff of the kinetic energy. DFT calculations were done with the QUANTUM-ESPRESSO package [38] using the local density approximation [39] and PBEsol [40] for the exchange-correlation functional for both structural optimization and electronic structure calculations. For a $2 \times 2 \times 2$ perovskite supercell, we used shifted $4 \times 4 \times 4$ and $8 \times 8 \times 8$ Monkhorst-Pack k -point grids [41] for the ground state and the density of states (DOS) calculations, respectively. Polarization was calculated by the Berry phase approach [42, 43] on an unshifted $4 \times 4 \times 20$ k -point grid, where the densely sampled direction is permuted in order to obtain all three polarization components. Due to the multi-valued nature of polarization, we calculated the polarization change when the centrosymmetric non-polar structure deforms to the relaxed low-symmetry structure. To explore the photovoltaic activity for the two Pb-based materials, we evaluate the short-circuit

current under linearly polarized light [44] using shift current calculations. We chose the $2 \times 2 \times 2$ supercell to allow for modeling different doping fractions of Bi^{5+} . For structural optimization, both internal coordinates and lattice vectors are relaxed. In order to correct for the band gap underestimation in DFT due to the unphysical delocalization of the Kohn-Sham states [45] (especially prominent when the band edges are composed of strongly correlated d and f orbitals), we used the DFT+ U method, in which the Hubbard U term accounts for the on-site repulsion of the correlated electrons [46].

For the KNB system, we performed calculations at $x = 0.125$, where one of the eight Nb atoms in the supercell is replaced by a Bi atom. For the Pb-based materials, the two B cations form a rock-salt ordering to reduce the long-range Coulombic interaction [47]. Electronic structures are calculated for $x = 0, 0.25, 0.5, 0.75$ and 1. The positions of the dopant Bi atoms are chosen so that the high-symmetry structure possesses inversion symmetry and has no spontaneous polarization.

III. RESULTS AND DISCUSSION

A. Bi^{5+} doping in KNbO_3

The calculated band structures and projected densities of states (PDOS) of KNbO_3 (KNO) and KNB with LDA+ U functionals are shown in Fig. 1. We added U terms to both the Nb $4d$ and the Bi $5d$ orbitals. The effective U values are determined by a linear response approach [48] to be 3.86 eV (Nb $4d$) for KNO, and 3.94 eV (Nb $4d$) and 1.11 eV (Bi $5d$) for KNB, respectively. The electronic properties of KNO and KNB are summarized in Table I. Note that the only significant effect of the Hubbard U term is to increase the E_g of KNO from 1.7 eV to 2.1 eV, by raising the CB energy. The KNB band gap is insensitive to the addition of U because its IB has negligible Nb $4d$ or Bi $5d$ characters. The LDA+ U band gap for KNO, although improved, is still 1 eV below the experimental value, in agreement with other theoretical predictions [49]. Use of PBEsol+ U (which is designed for solids), LDA, and LDA+ U all yield similar results for KNB. Therefore we expect that the general trend of band gap reduction by Bi^{5+} doping in KNbO_3 is accurately reproduced by LDA calculations.

Inspection of the KNB electronic structure (Fig. 1b) shows that when Bi^{5+} is substituted

TABLE I. Electronic properties of KNO and KNB. Experimental band gap [50] and polarization [51] are available for KNO but not for KNB.

Method	E_g (eV)		P (C/m ²)	
	KNO	KNB	KNO	KNB
Experiment	3.1	N/A	0.41	N/A
LDA	1.7	0.8	0.42	0.26
LDA+ U	2.1	0.8	0.40	0.25
PBEsol+ U	2.4	0.9	0.42	0.24

for Nb^{5+} an IB emerges, while the CB and VB do not change significantly. From the PDOS it is evident that the IB mainly comprises Bi 6s and O 2p. Due to the presence of the IB, the LDA+ U E_g drops from 2.1 eV for KNO to 0.8 eV for KNB. The 0.25 C/m² calculated polarization value of KNB shows that the solid solution is still FE after Bi^{5+} doping. Inspection of the KNB band structure shows strong dispersion of the IB, such that there is only a small band gap between the IB and the original CB. This is unfavorable for the potential use of KNB in multi-gap solar cells.

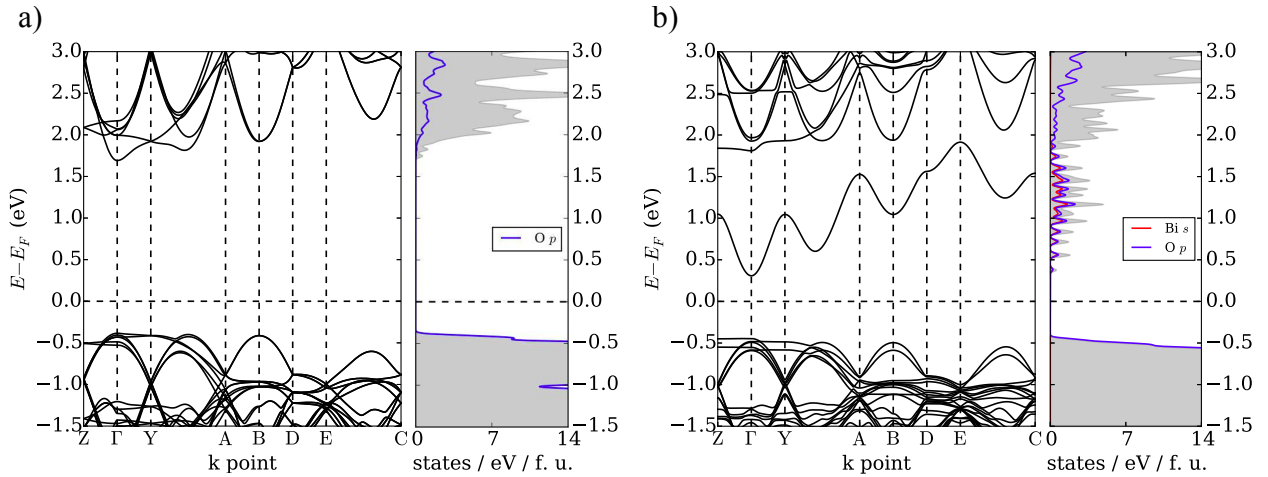


FIG. 1. LDA+ U band structures and PDOS of (a) KNO and (b) KNB, shaded areas indicate total DOS.

Due to the large ionic radius mismatch between Nb^{5+} (0.64 Å) and Bi^{5+} (0.76 Å) on the B -site and the fact that the end-member KBiO_3 does not form a stable perovskite phase [52], the KNB solid solution is unlikely to form with normal solid-state synthesis methods. It

nevertheless serves as a proof-of-concept that lowering the band gap by “IB insertion” while maintaining strong P is possible for FE oxides.

B. Bi^{5+} doping in more feasible double perovskite systems

To suggest more feasible candidates for efficient solar energy conversion, we examine solid solutions in which one end member is a naturally occurring perovskite with Bi^{5+} on the B -site and the other is a FE perovskite. For better solubility, the lattice mismatch between end members should be kept to a minimum. Therefore, we studied the structural and electronic properties of PIN-BIB and PSN-BSB. The lattice parameters of these end members in the perovskite phase are PIN (4.11 Å) [53], BIB (4.23 Å) [54], PSN (4.08 Å) [55], and BSB (4.18 Å) [56], both alloy pairs differing by less than 3%. We study the rock-salt ordered B -cation arrangement because it minimizes the Coulombic interaction between B -cations with different charges. This B -cation ordering can be achieved in PSN and PIN with slow annealing, and both PSN and PIN exhibit ferroelectricity for ordered or partially ordered B -cation arrangements. [57, 58].

The calculated band gaps and polarizations for the two solid solutions at different doping concentrations are shown in Fig. 2. The polarization values generally decrease with increasing Bi^{5+} concentration, consistent with the decrease in the concentration of ferroelectrically active Pb and Nb ions. The effect of Bi^{5+} doping on the band gap is more complicated. For PIN-BIB E_g decreases monotonically with increasing x , while for PSN-BSB there is a minimum E_g at $x = 0.25$. At this concentration, Bi^{5+} causes a substantial decrease in E_g while still preserving a substantial polarization. In addition, the formation energy of PIN-BIB and PSN-BSB at $x = 0.25$ are both negative, indicating that these solid solutions are energetically more favorable than their parent materials (See Fig. S1 in the supplementary material). Therefore, we examine PIN-BIB and PSN-BSB at $x = 0.25$ more closely. The properties of PIN-BIB and PSN-BSB at $x = 0.25$ are summarized in Table II.

The band structures and PDOS with LDA functionals for the two solid solutions at $x = 0.25$ are shown in Fig. 3. From here on, we focus on studying solid solutions at $x = 0.25$, and the doping concentration will not be explicitly denoted. The reduction in band gap is caused by IBs that are of Bi 6s and O 2p origin. Comparison of KNB, PIN-BIB and PSN-BSB band structures shows that Bi^{5+} introduces IBs, independent of the composition of

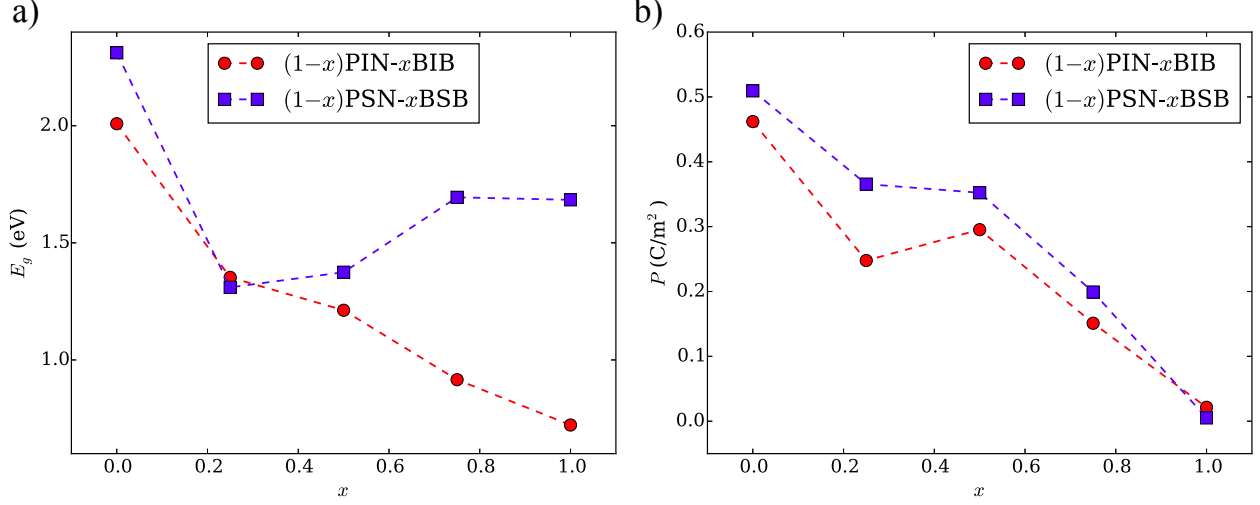


FIG. 2. (a) LDA band gap and (b) polarization vs. composition for PIN-BIB and PSN-BSB. x is the concentration of end member BIB or BSB.

TABLE II. Band gap E_g , polarization P and lattice constants a , b and c of 0.75PIN-0.25BIB and 0.75PSN-0.25BSB. Numbers in parenthesis denote the three components of polarization.

	E_g (eV)	P (C/m ²)	a (Å)	b (Å)	c (Å)
PIN-BIB	1.4	0.25 (0.07, 0.21, 0.11)	8.26	8.25	8.34
PSN-BSB	1.3	0.37 (0.11, 0.33, 0.11)	8.16	8.16	8.16

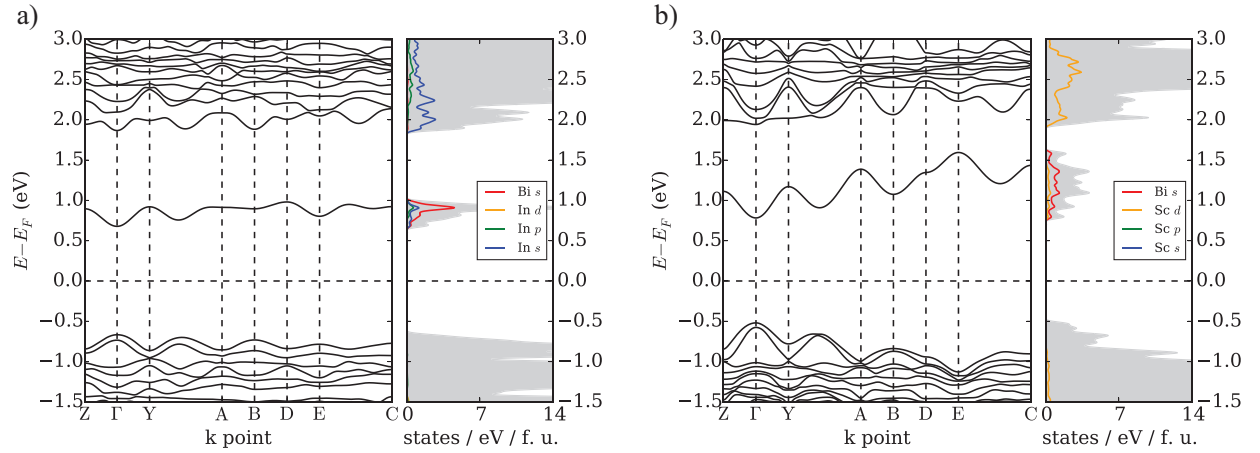


FIG. 3. Band structures and PDOS for (a) PIN-BIB and (b) PSN-BSB, shaded areas indicate total DOS.

139 the parent FE material. This suggests that Bi^{5+} substitution, if experimentally achievable,
 140 would lower the band gap of other FE perovskites as well. Fig. 3 shows that PSN-BSB
 141 has an IB with a larger bandwidth than that of PIN-BIB. A more dispersive IB implies
 142 a lower effective mass for the electrons and more mobile carriers, which could allow for
 143 better conductivity for photoexcited electrons, whereas a narrower band (such as the one in
 144 PIN-BIB) indicates isolated Bi 6s states and lower probability of electron hopping between
 145 sites.

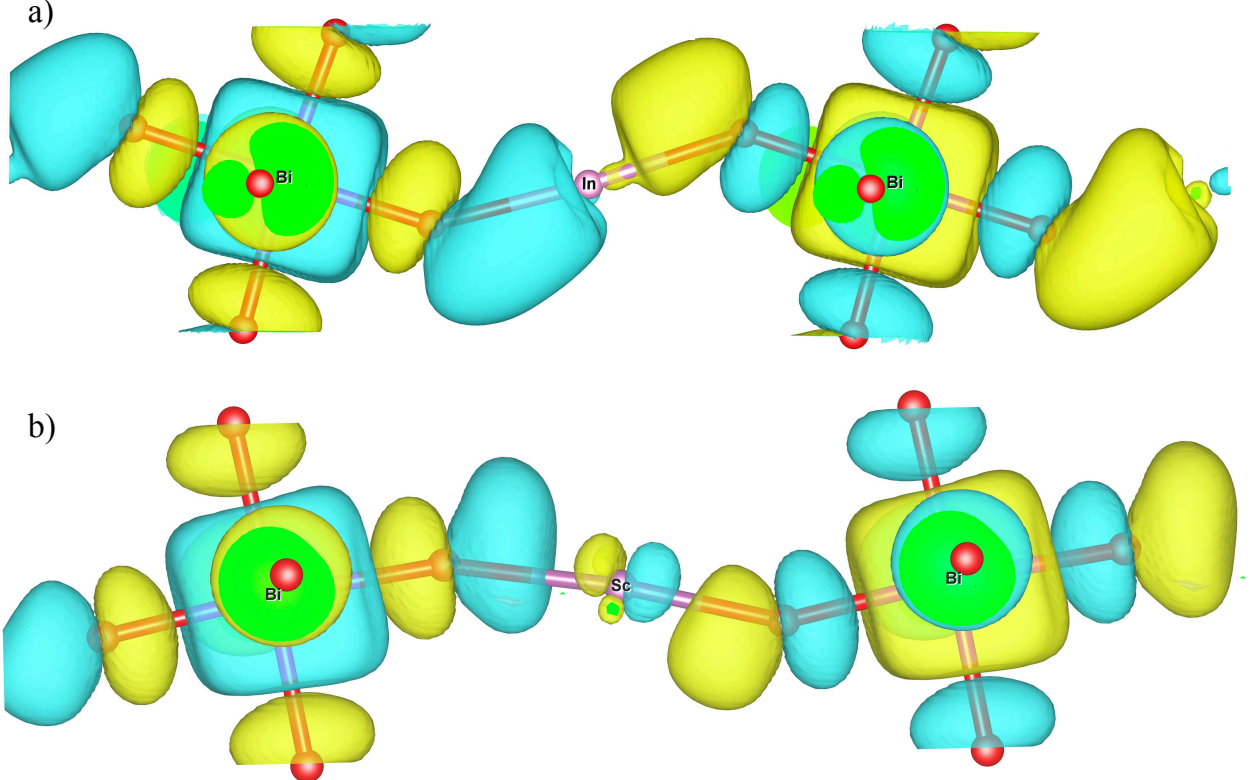


FIG. 4. E point intermediate band wavefunctions along the Bi - O - B' - O - Bi chain in (a)
 PIN-BIB and (b) PSN-BSB.

146 By comparing Fig. 3a to Fig. 3b it is evident that the difference in bandwidth is mostly
 147 the result of different dispersion behaviors of the IB at the E point $(1/2, 1/2, 1/2)$, i.e., the IB
 148 energy at E point is at minimum in PIN-BIB, but at maximum in PSN-BSB. At other high
 149 symmetry points in the Brillouin zone, the dispersion trend is generally the same between
 150 the two solid solutions, with differences in the magnitude. We attribute the differing E
 151 point dispersions to the atomic orbitals of In or Sc available to participate in IB formation.
 152 Consider a Bi-O- B' -O-Bi chain, at E point the wavefunction periodicity requires that the

153 two Bi atoms at the ends of the chain (in any direction) provide s orbitals of opposite
 154 phases to the IB, shown in Fig. 4. For B' , all orbitals that are symmetric with respect to
 155 the plane perpendicular to the O- B' -O line have effectively non-bonding contribution to
 156 the IB, because their constructive and destructive overlap with the two opposite phase O $2p$
 157 lobes cancel each other. This leaves only p orbitals as possible participating orbitals to the
 158 IB. From PDOS of PIN-BIB (Fig. 3a), we see that the valance $5p$ in In^{3+} is readily available
 159 in the IB, which is reflected in the In p -O p σ bond shown in Fig. 4a. On the other hand
 160 for Sc^{3+} , $4p$ orbitals are too high in energy and $3p$ orbitals are too low, compared to the
 161 valance $3d$. The PDOS of PSN-BSB (Fig. 3b) shows negligible p contribution to the IB,
 162 and the wavefunction in Fig. 4b contains very small fraction of Sc p -O p σ^* bond, possibly
 163 from anti-bonding interaction of the low energy Sc $3p$ in the core state. The bonding vs.
 164 anti-bonding characteristic explains the energy minimum in In-containing vs maximum in
 165 Sc-containing solid solutions.

166 For a more mathematical description of the IB dispersion difference between the Sc-
 167 and In-containing perovskites, we construct and fit a tight-binding model for perfect cubic
 168 PIN-BIB and PSN-BSB where O p , Bi s , B' s , B' p and B' d are the basis orbitals, whose
 169 on-site energies are e_p , e_s , e'_s , e'_p and e'_d , respectively. The hopping matrix elements that
 170 are considered in our model include t_{sp} ($\sigma_{\text{Bi } s \rightarrow \text{O } p}$), t'_{sp} ($\sigma_{B' s \rightarrow \text{O } p}$), t'_{pp} ($\sigma_{B' p \rightarrow \text{O } p}$) and t'_{dp}
 171 ($\sigma_{B' d \rightarrow \text{O } p}$). By minimizing the difference between the tight-binding band structure and
 172 the corresponding DFT band structure, we obtained the on-site energies and hopping terms
 173 listed in Table III. We show in Fig. 5 the comparison of DFT and tight binding band
 174 structure for the two solid solutions, with the IB plotted as a band whose width at each
 175 k-point represents the relative contribution from different B' atomic orbitals, in order to
 176 illustrate the difference in orbital contributions between PIN-BIB and PSN-BSB. Bi s and
 177 O p contributions are not shown because they are too large and overshadow the more delicate
 178 B' orbital contributions at different k-points. It is clear that in PIN-BIB, the IB consists of
 179 mostly In s and some In p at E point, whereas in PSN-BSB, the majority Sc orbital is Sc
 180 d . Note that in the DFT bands we use a relaxed distorted structure, which allows a little
 181 Sc d contribution at the E point; whereas in the tight binding model for simplicity a high
 182 symmetry cubic structure is used, in which symmetry forbids any Sc d contribution at the
 183 E point.

184 From the fitting data, it is evident that in PIN-BIB both s and p on-site energies are

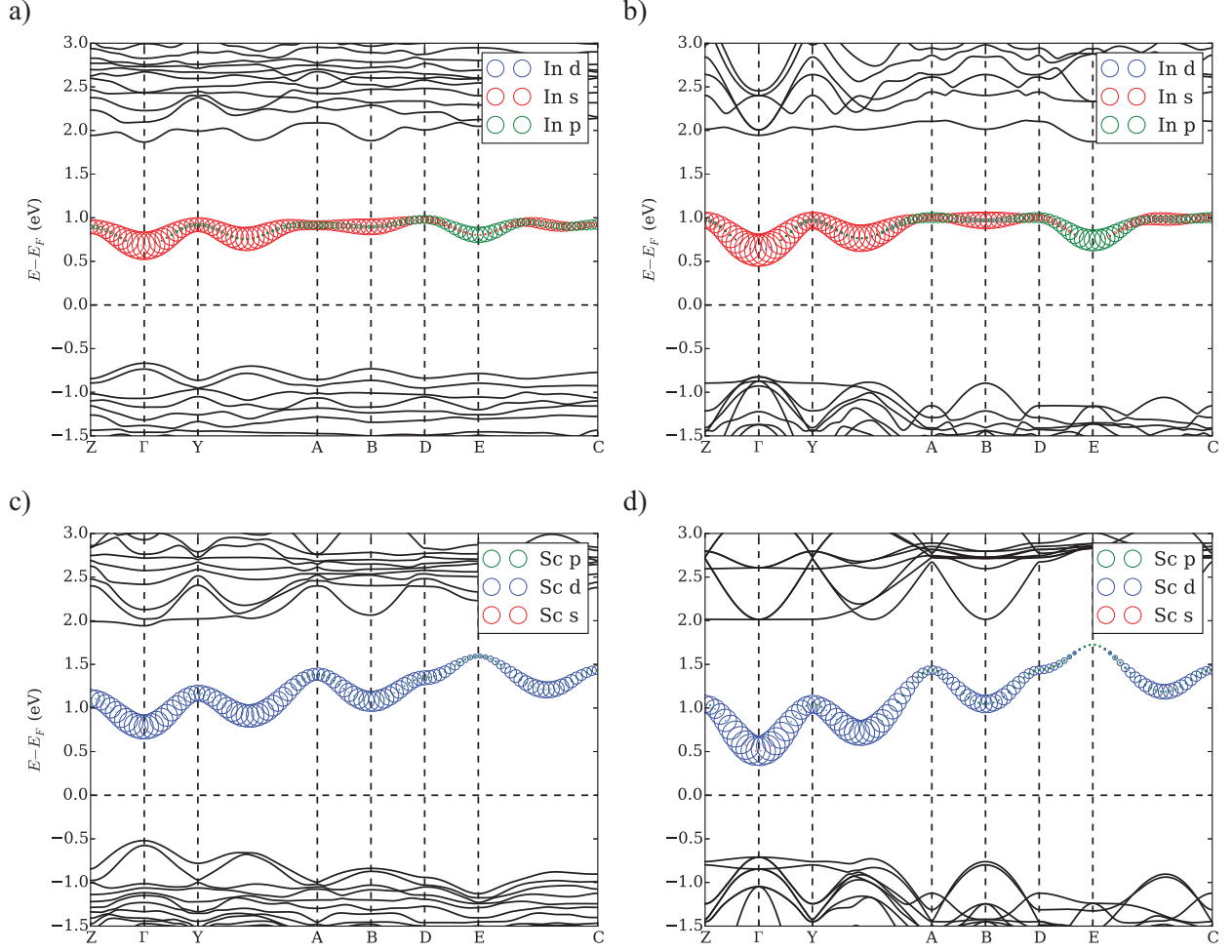


FIG. 5. Comparison between (a, c) DFT and (b, d) tight-binding electronic bands for (a, b) PIN-BIB and (c, d) PSN-BSB. The intermediate bands are composed of circles whose centers reside on the corresponding energy levels and whose radii are proportional to the norm of the coefficients of the atomic orbital basis for the eigenstates at each k-point.

TABLE III. Tight binding model parameters of PIN-BIB and PSN-BSB fitted from corresponding DFT band structures.

e (eV)	PIN-BIB	PSN-BSB	t (eV)	PIN-BIB	PSN-BSB
Bi e_s	6s 1.25	6s 1.38	t_{sp} ($\sigma_{\text{Bi } s \rightarrow \text{O } p}$)	4.22	4.39
In/Sc e'_s	5s 2.69	4s 5.51	t'_{sp} ($\sigma_{\text{B}' s \rightarrow \text{O } p}$)	1.39	0.41
In/Sc e'_p	5p 6.88	3p -17.28	t'_{pp} ($\sigma_{\text{B}' p \rightarrow \text{O } p}$)	2.03	0.39
In/Sc e'_d	4d -6.72	3d 4.16	t'_{dp} ($\sigma_{\text{B}' d \rightarrow \text{O } p}$)	0.55	2.91
In/Sc e_p	2p 0.00	2p 0.00			

185 higher than the filled d orbitals, and the hopping from In s and In p to O p is more significant
 186 compared to the hopping from In d . For PSN-BSB the p state is the filled core state with
 187 low on-site energy and interacts weakly with O p compared to the valence d states. The Sc
 188 s is valence, but still has smaller interaction with O p , leaving Sc d as the only orbital that
 189 has significant mixing with O. These results demonstrate that In s , In p and Sc d are mostly
 190 favorable to participate in IB formation, with remarkable agreement between the DFT and
 191 tight binding bands shown in Fig. 5.

192 **C. Shift current study of the Bi^{5+} doped double perovskites**

193 Several mechanisms have been proposed to account for the photocurrent produced by FE
 194 materials under illumination. In thin films, excited carrier separation and the resulting pho-
 195 tovoltage and photocurrent have been ascribed to extrinsic effects such as engineered domain
 196 wall structures and the depolarizing field due to incomplete polarization charge compensa-
 197 tion at the ferroelectric-electrode interfaces [6, 7]. In addition, an intrinsic bulk photovoltaic
 198 effect can also arise in a homogeneous noncentrosymmetric material, which is mainly gov-
 199 erned by the “shift current” mechanism [8–11]. Like the normal linear (in light intensity)
 200 interfacial photovoltaic effect, shift current is a second-order nonlinear optical effect with
 201 the photocurrent quadratic in the electric field (therefore linear in intensity). However, shift
 202 current does not rely on an external engineered asymmetry or an internal depolarization
 203 field to separate charge. Under sustained illumination, electrons are continuously excited to
 204 a quasiparticle coherent state that is entangled with the radiation source, resulting in a net
 205 direct current due to the broken inversion symmetry. While we make clear that our designed
 206 materials can be useful as absorbers in conventional photovoltaic or by using the depolar-
 207 ization field at interfaces to separate charge (See Fig. S2 in the supplementary material for
 208 the optical transition property), here we also study the bulk shift current performance of
 209 these materials.

210 We calculated the shift current susceptibility with respect to light intensity and the Glass
 211 coefficients of PIN-BIB and PSN-BSB. The shift current involves nonlinear optical processes
 212 that arise from the second-order interaction with incident electric field, in which electrons
 213 are excited to coherent superpositions, resulting in a net current flow in the presence of
 214 an asymmetric potential. The susceptibility σ_q^{rs} determines the current density J_q due to

interaction with electric field E_r and E_s : $J_q = \sigma_q^{rs} E_r E_s$. For simplicity, we assume that both excitations are caused by the same monochromatic light, and thus only the diagonal terms σ_q^{rr} are reported. The Glass coefficient G_q^{rr} [4] is another measure of photovoltaic efficiency, the shift current density for material of width w with incident light intensity I and frequency ω : $J_q(\omega) = G_q^{rr} I w$, assuming that the material is thick enough to absorb all incident light.

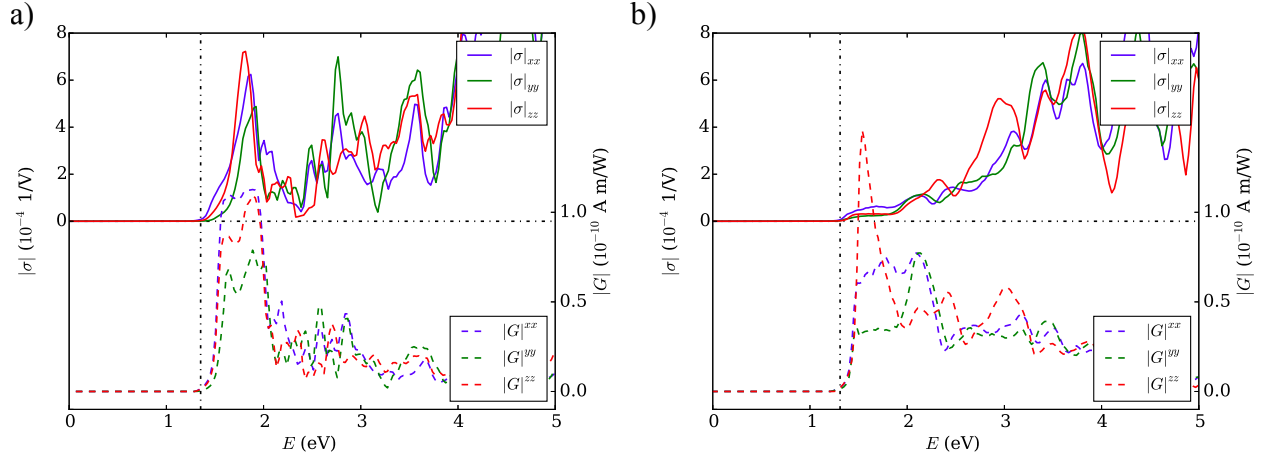


FIG. 6. Total susceptibility (solid line) and Glass coefficient (dashed line) of (a) PIN-BIB and (b) PSN-BSB.

Fig. 6 shows the calculated shift current susceptibilities and the Glass coefficient spectra of PIN-BIB and PSN-BSB. It is immediately obvious that the photocurrent response thresholds of both materials are located at relatively low photon energies — essentially at the theoretical band gap edge. This verifies our expectation that the introduction of low-lying IB states would shift the light absorption and photocurrent response well into the visible light range. Nevertheless, the two materials show quite different shift current susceptibility behaviors. For PIN-BIB, one large peak appears in the near-band-gap region (at 1.9 eV) while no such peak is found in PSN-BSB. As the photon energy increases, the photocurrent response of PIN-BIB decreases and reaches minimum at 2.3 eV. As illustrated by the band structure of PIN-BIB (Fig. 3), the large peak at 1.9 eV is mainly due to the transitions from the O $2p$ VB to the Bi $6s$ IB. Since this IB state is relatively localized and separated from the fundamental CB states, the photon absorption at higher energy is suppressed until the photon energy is large enough for a transition to the CB. For PSN-BSB, the shift current susceptibility increases as a function of photon energy up to 4 eV. This broad spectrum light absorption and photocurrent evolution is consistent with the dispersive IB in PSN-

TABLE IV. The calculated largest shift current susceptibility σ and Glass coefficient G of various materials between the band gap E_g and 1 eV above it. For BFO, the numbers are calculated with the GGA+ U method [12], and those in parentheses are the experimental values with a photon energy of 2.85 eV [44, 59].

	PIN-BIB	PSN-BSB	PTO	BTO	BFO	KNO
σ (10^{-4} V $^{-1}$)	7.2	1.7	3.9	1.4	0.9 (1.1)	11.1
G (10^{-10} A·m/W)	1.1	1.4	1.2	0.2	0.05 (0.05)	0.3
E_g (eV)	1.4	1.3	3.4	3.2	2.7	3.1

BSB. In addition, the magnitude of the shift current susceptibility at the band edge is not as large as that in PIN-BIB. For both materials, the shift current susceptibility exhibits similar behavior in terms of magnitude and spectrum shape under different polarizations of incident illumination.

The Glass coefficient gives the photocurrent density per unit sample width assuming full absorption, and includes the light attenuation effect due to absorption coefficient. As shown in Fig. 6, the Glass coefficient plots of both PIN-BIB and PSN-BSB exhibit a similar trend: a near-band-gap peak followed by decreasing intensity with higher incident photon energy, in contrast to the susceptibility plots in which PIN-BIB and PSN-BSB differ significantly. This is attributed to the relatively small absorption coefficients of PSN-BSB near the band gap with respect to PIN-BIB. The Glass coefficients in both materials show good photovoltaic activity within the visible range.

To evaluate the prospect of using these two materials for solar energy conversion, we compare the calculated results to those of the prototype FE materials PbTiO₃ (PTO), BaTiO₃ (BTO), BiFeO₃ (BFO) and KNO. As shown in Table IV, the susceptibility magnitude of PIN-BIB near its band gap is larger than that of PTO and BTO. Although the shift current response of PSN-BSB near the band gap is not as large as that of PTO, the response at higher photon energy is stronger. The Glass coefficient magnitudes of both PIN-BIB and PSN-BSB in the near-band-gap region are also comparable to that of PTO and larger than that of BTO. Clearly, the shift current responses of PIN-BIB and PSN-BSB near their band gaps are much larger than that of BFO (near its higher E_g). Furthermore, the Glass coefficients of both PIN-BIB and PSN-BSB are at least one order of magnitude larger than

that of BFO, implying their potential use as photovoltaic materials. Though the shift current responses of PIN-BIB and PSN-BSB are not as large as that of KNO, the onset of photon absorption energy is again lower (1.4 eV vs. 3.1 eV) and their Glass coefficients are more than twice that of KNO. Based on these comparisons and the fact that the shift current response of PIN-BIB and PSN-BSB occurs at low photon energy, we propose that these two materials are promising candidates for bulk photovoltaic solar energy conversion. Furthermore, PIN-BIB is more appropriate for monochromatic illumination with photon energy at the band gap while PSN-BSB should offer good photovoltaic performance under broad-spectrum solar light illumination. Since the excitations from the IB to the CB are not included in the shift current, these materials could be more appealing for photovoltaic applications than the shift current results shown here after appropriate doping.

IV. CONCLUSIONS

In conclusion, we have shown that semiconducting ferroelectrics with band gaps in the visible range can be designed by Bi^{5+} substitution on the perovskite B -site. The introduction of empty Bi 6s empty states in the band gap of the parent material leads to an E_g lowering of ≈ 1.5 eV, enabling the absorption of much more of the solar spectrum in FE-based devices. The resulting materials exhibit several interesting electronic structure features, most notably a dispersive intermediate band due to the Bi 6s states. We propose that PIN-BIB and PSN-BSB are promising candidates for bulk photovoltaic solar energy conversion based on their band gaps, polarization, solubility and photocurrent response, with PIN-BIB more appropriate for monochromatic illumination and PSN-BSB more suitable for solar light illumination.

ACKNOWLEDGMENTS

L. J. was supported by the Air Force Office of Scientific Research under Grant No. FA9550-10-1-0248. I. G. was supported by the Office of Naval Research under Grant No. N00014-12-1-1033. F. W. was supported by the Department of Energy under Grant No. DE-FG02-07ER46431. S. M. Y. was supported by the National Science Foundation, under Grant No. DMR11-24696. P. K. D and A. M. R. were supported by the Energy Commercial-

ization Institute of BFTP. Computational support was provided by the High Performance
Computing Modernization Office of the Department of Defense, and the National Energy
Research Scientific Computing Center of the Department of Energy. We would like to thank
Fan Zheng for fruitful discussions.

-
- [1] W. Shockley and H. Queisser, J. Appl. Phys. **32**, 510 (1961).
 - [2] A. G. Chynoweth, Phys. Rev. **102**, 705 (1956).
 - [3] F. S. Chen, J. Appl. Phys. **40**, 3389 (1969).
 - [4] A. M. Glass, D. von der Linde, and T. J. Negran, Appl. Phys. Lett. **25**, 233 (1974).
 - [5] V. M. Fridkin, Crystallog. Rep. **46**, 654 (2001).
 - [6] M. Qin, K. Yao, and Y. C. Liang, Appl. Phys. Lett. **95**, 022912 (2009).
 - [7] M. Qin, K. Yao, and Y. C. Liang, Appl. Phys. Lett. **93**, 122904 (2008).
 - [8] G. Dalba, Y. Soldo, F. Rocca, V. M. Fridkin, and P. Sainctavit, Phys. Rev. Lett. **74**, 988 (1995).
 - [9] R. von Baltz and W. Kraut, Phys. Rev. B **23**, 5590 (1981).
 - [10] K. Tonooka, P. Poosanaas, and K. Uchino (International Society for Optics and Photonics, 1994) pp. 224–232.
 - [11] B. I. Sturman and V. M. Fridkin, *The Photovoltaic and Photorefractive Effects in Noncentrosymmetric Materials*, edited by G. W. Taylor, Ferroelectricity and Related Phenomena, Vol. 8 (Gordon and Breach Science Publishers, 1992).
 - [12] S. M. Young, F. Zheng, and A. M. Rappe, Phys. Rev. Lett. **109**, 236601 (2012).
 - [13] K. Nonaka, M. Akiyama, T. Hagio, and A. Takase, J. Eur. Ceram. Soc. **19**, 1143 (1999).
 - [14] T. Choi, S. Lee, Y. Choi, V. Kiryukhin, and S.-W. Cheong, Science **324**, 63 (2009).
 - [15] S. Y. Yang, J. Seidel, S. J. Byrnes, P. Shafer, C. H. Yang, M. D. Rossell, P. Yu, Y. H. Chu, J. F. Scott, J. W. Ager, L. W. Martin, and R. Ramesh, Nature Nanotechnology **5**, 143 (2010).
 - [16] J. Seidel, D. Y. Fu, S. Y. Yang, E. Alarcon-Llado, J. Q. Wu, R. Ramesh, and J. W. Ager, Physical Review Letters **107**, 126805 (2011).
 - [17] P. C. Joshi and S. B. Desu, Thin Solid Films **300**, 289 (1997).
 - [18] D. Bao, X. Yao, K. Shinozaki, and N. Mizutani, J. Physics D: App. Phys. **36**, 2141 (2003).

- [19] S. Pandeya, A. Jamesa, R. Ramana, S. Chatterjeea, A. Goyala, C. Prakasha, and T. Goelb,
Physica B **369**, 135 (2005).
- [20] K. Y. Chan, W. S. Tsang, C. L. Mak, K. H. Wong, and P. M. Hui, Phys. Rev B **69**, 144111
(2004).
- [21] X. Wan, H. L. W. Chan, C. L. Choy, X. Zhao, and H. Luo, J. Appl. Phys. **96**, 1387 (2004).
- [22] J. W. Bennett, I. Grinberg, and A. M. Rappe, J. Am. Chem. Soc. **130**, 17409 (2008).
- [23] G. Y. Gou, J. W. Bennett, H. Takenaka, and A. M. Rappe, Phys. Rev. B **83**, 205115 (2011).
- [24] W. S. Choi, M. F. Chisholm, D. J. Singh, T. Choi, G. E. J. Jr., and H. N. Lee, Nat. Commnu.
3, 689 (2012).
- [25] I. Grinberg, D. V. West, M. Torres, G. Gou, D. M. Stein, L. Wu, G. Chen, E. M. Gallo, A. R.
Akbashev, P. K. Davies, J. E. Spanier, and A. M. Rappe, Nature **503**, 509 (2013).
- [26] A. Luque and A. Martí, Phys. Rev. Lett. **78**, 5014 (1997).
- [27] A. Martí, E. Antolín, C. R. Stanley, C. D. Farmer, N. López, P. Díaz, E. Cánovas, P. G.
Linares, and A. Luque, Phys. Rev. Lett. **97**, 247701 (2006).
- [28] A. Luque, A. Martí, and C. Stanley, Nature Photonics **6**, 146 (2012).
- [29] N. López, L. A. Reichertz, K. M. Yu, K. Campman, and W. Walukiewicz, Phys. Rev. Lett.
106, 028701 (2011).
- [30] T. Hatakeyama, S. Takeda, F. Ishikawa, A. Ohmura, A. Kakayama, Y. Yamada, A. Mat-
sushita, and J. Yea, J. Cer. Soc. J **118**, 91 (2010).
- [31] S. G. Hur, T. W. Kim, S. J. Hwang, H. Park, W. Choi, S. J. Kim, and J. H. Choy, J. Phys.
Chem. B **109**, 15001 (2005).
- [32] W. Shan, W. Walukiewicz, J. W. Ager, E. E. Haller, J. F. Geisz, D. J. Friedman, J. M. Olson,
and S. R. Kurtz, Phys. Rev. Lett. **82**, 1221 (1999).
- [33] K. M. Yu, W. Walukiewicz, J. Wu, W. Shan, J. W. Beeman, M. A. Scarpulla, O. D. Dubon,
and P. Becla, Phys. Rev. Lett. **91**, 246403 (2003).
- [34] T. W. Kim, S. G. Hur, S. J. Hwang, H. Park, Y. Park, W. Choi, and J. H. Choy, Mater. Res.
Bull. **42**, 1914 (2007).
- [35] M. C. Payne, M. P. Teter, D. C. Allan, T. A. Arias, and J. D. Joannopoulos, Rev. Mod.
Phys. **64**, 1045 (1992).
- [36] A. M. Rappe, K. M. Rabe, E. Kaxiras, and J. D. Joannopoulos, Phys. Rev. B Rapid Comm.
41, 1227 (1990).

- [37] <http://opium.sourceforge.net>.
- [38] P. Giannozzi, S. Baroni, N. Bonini, M. Calandra, R. Car, C. Cavazzoni, D. Ceresoli, G. L. Chiarotti, M. Cococcioni, I. Dabo, A. D. Corso, S. de Gironcoli, S. Fabris, G. Fratesi, R. Gebauer, U. Gerstmann, C. Gougoussis, A. Kokalj, M. Lazzeri, L. Martin-Samos, N. Marzari, F. Mauri, R. Mazzarello, S. Paolini, A. Pasquarello, L. Paulatto, C. Sbraccia, S. Scandolo, G. Sciauzero, A. P. Seitsonen, A. Smogunov, P. Umari, and R. M. Wentzcovitch, *J. Phys.: Condens. Matter* **21**, 395502 (2009).
- [39] J. P. Perdew and A. Zunger, *Phys. Rev. B* **23**, 5048 (1981).
- [40] J. P. Perdew, A. Ruzsinszky, G. I. Csonka, O. A. Vydrov, G. E. Scuseria, L. A. Constantin, X. Zhou, and K. Burke, *Phys. Rev. Lett.* **100**, 136406 (2008).
- [41] H. J. Monkhorst and J. D. Pack, *Phys. Rev. B* **13**, 5188 (1976).
- [42] R. D. King-Smith and D. Vanderbilt, *Phys. Rev. B* **47**, 1651 (1993).
- [43] R. Resta, *Ferroelectrics* **136**, 51 (1992).
- [44] S. M. Young and A. M. Rappe, *Phys. Rev. Lett.* **109**, 116601 (2012).
- [45] W. Kohn and L. J. Sham, *Phys. Rev.* **140**, A1133 (1965).
- [46] K. A. Johnson and N. W. Ashcroft, *Phys. Rev. B* **58**, 15548 (1998).
- [47] L. Bellaiche and D. Vanderbilt, *Phys. Rev. Lett.* **81**, 1318 (1998).
- [48] M. Cococcioni and S. de Gironcoli, *Phys. Rev. B* **71**, 035105 (2005).
- [49] C. Duan, W. N. Mei, J. Liu, and J. R. Hardy, *J. Phys.: Condes. Matt.* **13**, 8189 (2001).
- [50] B. T. Matthias, *Phys. Rev.* **75**, 1771 (1949).
- [51] P. Günter, *J. Appl. Phys.* **48**, 3475 (1977).
- [52] T. N. Nguyen, D. M. Giaquinta, W. M. Davis, and H. zur Loye, *Chem. Mater.* **5**, 1273 (1993).
- [53] S. G. Zhukov, A. V. Yatsenko, and S. B. Vakhrushev, *J. Struct. Chem.* **38**, 486 (1997).
- [54] W. T. Fua, M. J. Polderman, and F. M. Mulder, *Mater. Res. Bull.* **35**, 1205 (2000).
- [55] K. S. Knight and K. Z. Baba-Kishi, *Ferroelectrics* **173**, 341 (1995).
- [56] M. W. Lufaso, P. W. Barnes, and P. M. Woodward, *Acta Crystallog. Sec. B* **B62**, 397 (2006).
- [57] K. Ohwada and Y. Tomita, *J. Phys. Soc. Jpn* **79**, 011012 (2010).
- [58] J. Zhang, Q. Li, and D. Feng, *Chin. Phys. Lett.* **9**, 355 (1992).
- [59] W. Ji, K. Yao, and Y. C. Liang, *Physical Review B* **84**, 094115 (2011).