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Third harmonic generation in graphene and few-layer graphite films

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We observe optical third harmonic generation from graphene and few-layer graphite flakes produced by exfoliation. The emission scales with the cube of the intensity of the incident near-infrared femtosecond pulses and has a wavelength that is one-third of the incident wavelength, both consistent with third harmonic generation. We extract an effective third-order susceptibility for graphene that is on the order of $10^{-16} \text{ m}^2/\text{V}^2$, which is comparable to that for materials that are resonantly excited, but larger than for materials that are transparent at the fundamental and third harmonic wavelengths.

Graphene is a monolayer of carbon atoms arranged in a hexagonal two-dimensional lattice. It has a linear dispersion relationship between energy, E, and wavenumber, k, $E(k) = \pm \hbar v_F k$, where the Fermi velocity $v_F \approx 10^6$ m/s [see Fig. 1(b)]^{1–3}. Since the material became readily available less than a decade ago⁴, it has been the subject of extensive investigations [e.g., see Refs. 5 and 6 and references therein]. Graphene exhibits a number of unusual and remarkable transport properties that make it attractive for nano-electronic applications^{7–9}, including high mobilities^{4,5,9,10} and nearly-ballistic transport at room temperature^{5,6}; however, it is the optical properties of graphene that are of primary interest here.

The linear absorbance of graphene is flat and approximately 2.3% across the entire visible spectrum^{11,12}. Thus, graphene can be considered to be both highly absorbing and/or highly transmitting, depending upon one's point of view or application. Since a negligible fraction (< 0.1%) is reflected¹², 97.7% of the incident light is transmitted. In this sense the sample is certainly transparent. On the other hand, if one were to assign an effective absorption coefficient, α , to a monolayer of thickness 0.33 nm (even though it may be questionable to use macroscopic parameters, such as α , for such thin samples), it would be very large ($\alpha \approx 7 \times 10^5$ /cm). As suggested by this large effective absorption coefficient, graphene interacts strongly with light. The strong broadband nature of the interaction of light with graphene is consistent with its linear bandstructure, where interband transitions of roughly equal strength are available throughout the visible. The combination of broadband transparency and the high mobilities mentioned earlier makes graphene a promising candidate for use as a transparent conductor¹³⁻¹⁶ in photovoltaic devices^{17,18} and touch screens¹⁴. The high broadband absorption (*i.e.*, optical conductivity) and high carrier mobility suggest that graphene may find applications in a range of optically-controlled transport devices, such as broadband and ultrafast photodetectors¹⁹⁻²⁵, optical modulators^{26,27}, plasmonic devices²⁸⁻³³, broadband polarizers³⁴, and magneto-optical devices³⁵.

The strong broadband coupling of light with graphene also suggests that it might be an attractive nonlinear material for large bandwidth photonic applications. However, second order nonlinearities in graphene are expected to be weak because of symmetry considerations. For example, graphene mounted on a substrate has C_{6v} symmetry, and therefore, the only allowed sources of second order responses are the interfaces³⁶. By comparison, for multilayer graphite, the bulk can contribute, depending upon the stacking arrangement³⁷. Indeed, second harmonic generation has been investigated both theoretically^{38–40} and experimentally^{37,41} in graphene and few-layer graphite films. Graphene flakes mounted on oxidized Si substrates have produced second harmonic signals, but the signal from the graphene is weaker than that from the substrate^{37,41}. For bilayers and few-layer graphite samples similarly mounted, the second harmonic signal is dominated by the graphite films, but it is weak^{37,41}.

In addition, the third order nonlinear optical responses associated with saturable absorption of graphene⁴²⁻⁴⁴, few-layer graphite films^{10,43-56}, and suspensions of graphene flakes⁵⁷ have been measured and time-resolved using a variety of pump-probe configurations. Typically, in these experiments, the interband absorption of the pump pulse produces nonequilibrium electron and hole populations, which subsequently relax by carrier-carrier scattering, phonon emission, diffusion and recombination. The time-delayed probe pulse is used to measure the dynamic change in the absorption coefficient caused by Pauli blocking of the final and initial states by the electron and hole distribution functions, respectively. Consequently, the emphasis in these studies has been the determination of the carrier, phonon and recombination dynamics. Because the measured nonlinearities in such experiments are dynamic, cumulative, and incoherent, they are not well suited to defining and quantifying a third-order susceptibility *per se*, and little attention has been given to quantifying the magnitude of these nonlinearities.

By comparison, measurements of coherent third order nonlinearities are relatively rare^{58–60}. Two-photon absorption has been measured in bilayer graphite flakes⁵⁸, and a third order nonlinear susceptibility with magnitude, $|\chi^{(3)}|$, on the order of $10^{-16} \text{ m}^2/\text{V}^2$ was extracted, which is consistent with the quantum perturbation theory used by the authors. By comparison, in the same study⁵⁸, no two-photon absorption was observed in monolayer graphene, also consistent with the authors theory which predicted a $|\chi^{(3)}| \approx 10^{-18} \text{ m}^2/\text{V}^2$. In contrast, however, ballistic photocurrents have been injected into multilayer epitaxial graphene samples by quantum interference between twophoton absorption and one-photon absorption, which suggests that the strength of the two-photon absorption is significant in graphene⁵⁹. Moreover, $|\chi^{(3)}|$'s as large as $10^{-15} \text{ m}^2/\text{V}^2$ have been reported for coherent four-wave mixing experiments in graphene⁶⁰, and a study on coherent self-phase modulation in dispersion of graphene sheets containing effectively about 100 layers deduced a monolayer $|\chi^{(3)}|$ of the same order of magnitude⁶¹.

Here we report observation of third harmonic generation (THG) from graphene and few-layer graphite. The samples studied are graphene and few-layer graphite flakes produced by mechanical exfoliation and mounted on a 300-nm silicon dioxide layer grown on a 500- μ m-thick silicon substrate. Flake thicknesses are determined by their optical contrasts⁶² and atomic force microscopy. Third harmonic emission is measured using the experimental geometry schematically sketched in Fig. 1(a). The fundamental near-infrared pulses (ω , red) with an average power in the range of 1 - 10 mW are obtained from an optical parametric oscillator pumped by a Ti:sapphire laser at a repetition rate of 80 MHz. Each pulse is tightly focused onto the sample by a microscope objective, and the third harmonic generated by the sample (3ω , green) is collected in the reflected direction by the same lens. Color filters are used to block the reflected

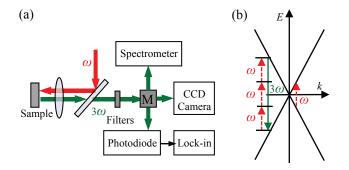


FIG. 1. (a) Experimental schematic: A fundamental (ω , red) pulse is normally incident on the sample. The third harmonic (3ω , green) is detected in the reflected direction by a CCD camera, a spectrometer or a photodiode connected to a lock-in amplifier. (b) Schematic diagram showing the linear dispersion of graphene, indicating the one-photon absorptions of ω and 3ω and illustrating the energy level description of third harmonic generation.

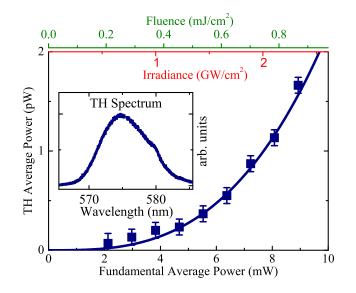


FIG. 2. The average power of the third harmonic as a function of the average power of the incident fundamental (solid squares), and the spectrum of the third harmonic (solid squares, inset). The solid line is a cubic fit ($\chi^{(3)} = 0.4 \times 10^{-16} \text{ m}^2/\text{V}^2$) of Eq. (1) to the data using parameters appropriate for our experimental conditions, as discussed in the text.

 ω beam. An adjustable mirror (M) is used to direct the 3ω beam either to an imaging charge-coupled device (CCD) camera, a spectrometer, or a silicon photodiode connected to a lock-in amplifier. The camera is used to rapidly locate a flake having the desired thickness and to spatially image the 3ω spots. The spectrometer, which is equipped with a thermoelectric cooled silicon CCD camera, allows the detection of weak 3ω spectra. The combination of the photodiode, which has an internal amplifier, and the lock-in amplifier provides for the continuous monitoring of the 3ω power as experimental parameters are varied.

The 3ω signal produced by a graphene flake when it is irradiated by an ω beam with horizontal linear polarization is summarized in Fig. 2. The spectrum of the emitted 3ω light produced by an ω beam with an average power of 10 mW is shown in the inset of Fig. 2. The central wavelength of 575.5 nm is within 0.4% of the separately measured ω wavelength (1720.4 nm) divided by 3 (*i.e.*, 573.5 nm), which confirms that we are measuring the third harmonic [see Fig. 1(b) for the energy diagram of THG]. When the laser spot is moved from the flake to the bare substrate, no 3ω signal is observed under the same conditions. Also, the second-harmonic signals from the graphene flakes, the Si/SiO₂ substrate, and their interfaces, which were previously observed in similarly mounted samples^{37,41}, are much smaller than the third harmonic and are not measurable under our conditions. In addition, by using an analyzing polarizer in front of the spectrometer, we find that the emitted 3ω radiation is linearly polarized along the same direction as the ω pulse.

The main panel of Fig. 2 shows the 3ω average power as a function of the ω average power. For convenience, the corresponding ω peak on-axis irradiance and pulse fluence are also shown on the top axis. The average 3ω power

is calibrated by comparing the measured 3ω signal on the spectrometer to that produced by a laser pulse of known power at 560 nm incident on the substrate. In this way, the reflection of the substrate, the loss of all optics, and the sensitivity of the spectrometer are included in the detector calibration. The measured signal is consistent with a cubic dependence on incident ω power, as indicated by the comparison with solid line in the main panel of Fig. 2 and as expected for third harmonic signal. The small deviation from cubic behavior at extremely low power levels can be attributed to unremoved noise background in the signal.

In an attempt to quantify the strength of the third harmonic signal produced by graphene, we now extract an effective third-order susceptibility, $\chi^{(3)}$, by comparing the 3ω signal shown in Fig. 2 with the well-known result for a thin bulk sample in the limit of an undepleted fundamental³⁶:

$$\mathcal{E}_{3\omega} = \frac{1}{4} \frac{i3\omega}{2n_{3\omega}c} d\chi^{(3)} \mathcal{E}^3_{\omega},\tag{1}$$

where c is the speed of light in a vacuum, d is the sample thickness, $n_{3\omega}$ is the index of refraction of the material at 3ω , and $\mathcal{E}_{3\omega}$ (\mathcal{E}_{ω}) is the magnitude of the 3ω (ω) field and where each field is related to its irradiance by $I_i = n_i \epsilon_0 c \mathcal{E}_i \mathcal{E}_i^*/2$. Furthermore, if the irradiance associated with each fundamental pulse is taken to be Gaussian in space and time,

$$I_{\omega}(r,t) = I_0 e^{-4\ln 2(r/W)^2} e^{-4\ln 2(t/\tau)^2},\tag{2}$$

with a diameter W and a pulsewidth τ (both in full width at half maxima), the peak on-axis irradiance, I_0 , is related to the average power, \bar{P}_{ω} , by

$$\bar{P}_{\omega} = f \frac{\sqrt{\pi\tau}}{\sqrt{4\ln 2}} \frac{\pi W^2}{4\ln 2} I_0,\tag{3}$$

where f is the repetition rate of the laser. While the use of bulk concepts, such as susceptibilities and indices of refraction, to describe a single atomic layer is questionable, this procedure allows us to assign an effective material parameter that allows comparison of THG in graphene to that in other well-known bulk materials. Using values appropriate to our experiment [i.e., d = 0.33 nm, $n_{\omega} \approx n_{3\omega} = 2.4$, $W = 3.5 \ \mu m$, $\tau = 320$ fs, $\lambda = 1720.4$ nm, and f = 81 MHz], these expressions are used to extract a value of $|\chi^{(3)}| \sim 0.4 \times 10^{-16} \text{ m}^2/\text{V}^2$ from Fig. 2.

We note that the error bars shown in Fig. 2 reflect the day-to-day accuracy in measuring the average power; however, other uncertainties limit the extraction of an accurate value for $\chi^{(3)}$ from the data. For example, the pulsewidth, τ , the diameter of the spatial profile, W, (which enters squared) and the repetition rate, f, for the laser are used to calculate the peak on axis irradiance I_0 from the measured average power P_{ω} . Therefore, since I_0 enters cubed in the extraction of $\chi^{(3)}$, any errors in the measurement of τ , W and f are greatly multiplied. Also, the sample used for these measurements is shaped like a rectangle with a width ~ 1 μ m and a length much larger than the focused laser spot diameter. Thus, the overlap between fundamental focused laser spot and the sample is imperfect. The fit shown in Fig. 2 is numerically corrected for this incomplete overlap. The fit shown in Fig. 2 is not corrected for multiple reflections associated with the layered oxide-Si structure. A calculation based on light propagation through our specific layered structure, ^{41,63} which incorporates third harmonic polarizations, indicates that the $\chi^{(3)}$ value extracted in this case is changed only by roughly a factor of two, which is within the experimental uncertainty discussed above, and for pedagogical simplification, we ignore those complications here. For these reasons, the absolute value of $\chi^{(3)}$ given in the previous paragraph should be taken as an order of magnitude determination. The upper limit on the fluence (and irradiance) shown in Fig. 2 is determined by damage to the sample.

We also investigate the nonlinear optical response as the sample evolves from monolaver graphene to multi-laver graphite by measuring the third harmonic from flakes of thickesses ranging from 1 to 6 atomic layers mounted on a single Si/SiO₂ substrate for an average power of 1 mW, as shown in Fig. 3. The solid curve in Fig. 3 is a fit of Eq. 1, which assumes that $\chi^{(3)}$ is independent of layer number, to the data for an effective third-order susceptibility of $|\chi^{(3)}| \sim 0.8 \times 10^{-16} \text{ m}^2/\text{V}^2$. Notice that this value is ~ twice larger than that extracted from Fig. 2. To the degree possible, the experimental conditions are held constant for the two sets of measurements; however, they are performed on different days, on different flakes, of different sizes, mounted on different substrates. Given the cubic dependence of the third order interaction on the field and given the inherent uncertainties and variation in the experimental parameters, this represents reasonable agreement between the two measurements. For these reasons, $|\chi^{(3)}| \sim 10^{-16} \text{ m}^2/\text{V}^2$ should be regarded as an order of magnitude estimate of the susceptibility. This magnitude is one order of magnitude smaller than those estimated from recent four-wave mixing⁶⁰ and self-phase modulation⁶¹ experiments, but more than two orders of magnitude larger than that from two-photon absorption experiment and quantum perturbation calculation⁵⁸. Further efforts, from both theoretical and experimental sides, are needed to fully understand third order response of graphene. We also note that the uncertainties are relatively large in this set of measurement, mainly due to necessary adjustments of the alignment when changing flakes and samples. Hence, although Eq. 1 appears to be consistent with the data, we do not view this as a proof of the quadratic dependence.

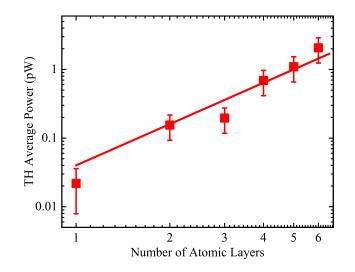


FIG. 3. The average power of the third harmonic as a function of the number of atomic layers for an average fundamental power of 1 mW (solid squares). The solid line is a quadratic fit ($\chi^{(3)} = 0.8 \times 10^{-16} \text{ m}^2/\text{V}^2$) of Eq. (1) to the data using parameters appropriate for our experimental conditions, as discussed in the text.

The deduced effective $\chi^{(3)}$ is several orders of magnitude larger than that for transparent materials³⁶. This is because third order response is dramatically enhanced by the resonant nature of the intermediate and final transitions needed for the THG³⁶. The nonlinear response of graphene is also broadband, owing to its bandstructure. On the other hand, however, $\chi^{(3)}$ of graphene is comparable to those associated with resonant transitions in other materials (*e.g.* metal nanoparticles)³⁶. The presence of resonant transitions at ω and 3ω in graphene not only enhances $\chi^{(3)}$, but also ensures strong linear (and nonlinear) absorption at both frequencies. This absorption is a detriment to the third order processes, because it reduces the fundamental intensity needed for THG and leads to the subsequent absorption of the third harmonic⁶⁴. In fact, one can define a figure of merit (FOM) for the THG as the ratio of the total number of third harmonic photons generated to the total number of photons (ω and 3ω) absorbed. It is straightforward to show that this FOM is, in turn, proportional to the ratio $\chi^{(3)}/\alpha$. Thus, while graphene and thin graphite films (and indeed all materials with resonant transitions) have large $\chi^{(3)}$'s, they do not have unusually large FOMs. For example, for our experimental conditions, a pulse with a fluence of 100 μ J/cm² (peak intensity of ~ 0.3 GW/cm²) would have a third harmonic conversion efficiency of less than 10⁻¹⁰, but would lose 0.023 of its energy to linear absorption.

In summary we have observed third harmonic generation from graphene and few-layer graphite films. The emission is at one third of the fundamental wavelength, and scales with the cube of the fundamental intensity. It is characterized by an effective third-order susceptibility of the order of $\chi^{(3)}(3\omega;\omega,\omega,\omega) \sim 10^{-16} \text{ m}^2/\text{V}^2$. Such a strong third order response originates from the resonant nature of the light-graphene interaction, which also causes strong absorption of light.

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- ⁵ C. Berger, Z. Song, X. Li, X. Wu, N. Brown, C. Naud, D. Mayou, T. Li, J. Hass, A. N. Marchenkov, E. H. Conrad, P. N. First, and W. A. de Heer, Science **312**, 1191 (2006).
- ⁶ F. Bonaccorso, Z. Sun, T. Hasan, and A. C. Ferrari, Nat. Photonics 4, 611 (2010).
- ⁷ M. C. Lemme, T. J. Echtermeyer, M. Baus, and H. Kurz, IEEE Electr. Device Lett. 28, 282 (2007).
- ⁸ M. T. Han, B. Özyilmaz, Y. B. Zhang, and P. Kim, Phys. Rev. Lett. **98**, 206805 (2007).
- ⁹ Y. M. Lin, C. Dimitrakopoulos, K. A. Jenkins, D. B. Farmer, H. Y. Chiu, A. Grill, and P. Avouris, Science **327**, 662 (2010).

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¹ P. R. Wallace, Phys. Rev. **71**, 622 (1947).

² K. S. Novoselov, A. K. Geim, S. V. Morozov, D. Jiang, M. I. Katsnelson, I. V. Grigorieva, S. V. Dubonos, and A. A. Firsov, Nature 438, 197 (2005).

³ A. H. C. Neto, F. Guinea, N. M. R. Peres, K. S. Novoselov, and A. K. Geim, Rev. Mod. Phys. 81, 109 (2009).

⁴ K. S. Novoselov, A. K. Geim, S. V. Morozov, D. Jiang, Y. Zhang, S. V. Dubonos, I. V. Grigorieva, and A. A. Firsov, Science **306**, 666 (2004).

- ¹⁰ B. A. Ruzicka, S. Wang, L. K. Werake, B. Weintrub, K. P. Loh, and H. Zhao, Phys. Rev. B 82, 195414 (2010).
- ¹¹ R. R. Nair, P. Blake, A. N. Grigorenko, K. S. Novoselov, T. J. Booth, T. Stauber, N. M. R. Peres, and A. K. Geim, Science 320, 1308 (2008).
- ¹² K. F. Mak, M. Y. Sfeir, Y. Wu, C. H. Lui, J. A. Misewich, and T. F. Heinz, Phys. Rev. Lett. **101**, 196405 (2008).
- ¹³ K. S. Kim, Y. Zhao, H. Jang, S. Y. Lee, J. M. Kim, K. S. Kim, J. H. Ahn, P. Kim, J. Y. Choi, and B. H. Hong, Nature 457, 706 (2009).
- ¹⁴ S. Bae, H. Kim, Y. Lee, X. F. Xu, J. S. Park, Y. Zheng, J. Balakrishnan, T. Lei, H. R. Kim, Y. I. Song, Y. J. Kim, K. S. Kim, B. Ozyilmaz, J. H. Ahn, B. H. Hong, and S. Iijima, Nat. Nanotechnol. 5, 574 (2010).
- ¹⁵ S. Gilje, S. Han, M. Wang, K. L. Wang, and R. B. Kaner, Nano Lett. 7, 3394 (2007).
- ¹⁶ H. A. Becerril, J. Mao, Z. Liu, R. M. Stoltenberg, Z. Bao, and Y. Chen, ACS Nano 2, 463 (2008).
- ¹⁷ X. Wang, L. J. Zhi, and K. Mullen, Nano Lett. 8, 323 (2008).
- ¹⁸ H. Park, P. R. Brown, V. Buloyic, and J. Kong, Nano Lett. **12**, 133 (2012).
- ¹⁹ F. N. Xia, T. Mueller, R. Golizadeh-Mojarad, M. Freitag, Y. M. Lin, J. Tsang, V. Perebeinos, and P. Avouris, Nano Lett. 9, 1039 (2009).
- ²⁰ F. N. Xia, T. Mueller, Y. M. Lin, A. Valdes-Garcia, and P. Avouris, Nat. Nanotechnol. 4, 839 (2009).
- ²¹ T. Mueller, F. N. A. Xia, and P. Avouris, Nat. Photonics 4, 297 (2010).
- ²² N. M. Gabor, J. C. W. Song, Q. Ma, N. L. Nair, T. Taychatanapat, K. Watanabe, T. Taniguchi, L. S. Levitov, and P. Jarillo-Herrero, Science **334**, 648 (2011).
- ²³ M. C. Lemme, F. H. L. Koppens, A. L. Falk, M. S. Rudner, H. Park, L. S. Levitov, and C. M. Marcus, Nano Lett. **11**, 4134 (2011).
- ²⁴ A. Urich, K. Unterrainer, and T. Mueller, Nano Lett. **11**, 2804 (2011).
- ²⁵ D. Sun, G. Aivazian, A. M. Jones, J. S. Ross, W. Yao, D. Cobden, and X. D. Xu, Nat. Nanotechnol. 7, 114 (2012).
- ²⁶ M. Liu, X. B. Yin, E. Ulin-Avila, B. S. Geng, T. Zentgraf, L. Ju, F. Wang, and X. Zhang, Nature 474, 64 (2011).
- ²⁷ M. Liu, X. B. Yin, and X. Zhang, Nano Lett. **12**, 1482 (2012).
- ²⁸ L. Ju, B. S. Geng, J. Horng, C. Girit, M. Martin, Z. Hao, H. A. Bechtel, X. G. Liang, A. Zettl, Y. R. Shen, and F. Wang, Nat. Nanotechnol. 6, 630 (2011).
- ²⁹ F. H. L. Koppens, D. E. Chang, and F. J. G. de Abajo, Nano Lett. **11**, 3370 (2011).
- ³⁰ S. F. Shi, X. D. Xu, D. C. Ralph, and P. L. McEuen, Nano Lett. **11**, 1814 (2011).
- ³¹ A. Vakil and N. Engheta, Science **332**, 1291 (2011).
- ³² P. Tassin, T. Koschny, M. Kafesaki, and C. M. Soukoulis, Nat. Photonics 6, 259 (2012).
- ³³ W. Zhou, J. Lee, J. Nanda, S. T. Pantelides, S. J. Pennycook, and J. C. Idrobo, Nat. Nanotechnol. 7, 161 (2012).
- ³⁴ Q. L. Bao, H. Zhang, B. Wang, Z. H. Ni, C. Lim, Y. Wang, D. Y. Tang, and K. P. Loh, Nat. Photonics 5, 411 (2011).
- ³⁵ I. Crassee, J. Levallois, A. L. Walter, M. Ostler, A. Bostwick, E. Rotenberg, T. Seyller, D. van der Marel, and A. B. Kuzmenko, Nat. Phys. 7, 48 (2011).
- ³⁶ R. W. Boyd, Nonlinear Optics, 3rd ed. (Academy Press, San Diego, USA, 2008).
- ³⁷ J. J. Dean and H. M. van Driel, Appl. Phys. Lett. **95**, 261910 (2009).
- ³⁸ M. M. Glazov, JETP Lett. **93**, 366 (2011).
- ³⁹ S. A. Mikhailov, Phys. Rev. B **84**, 045432 (2011).
- ⁴⁰ S. F. Wu, L. Mao, A. M. Jones, W. Yao, C. W. Zhang, and X. D. Xu, Nano Lett. **12**, 2032 (2012).
- ⁴¹ J. J. Dean and H. M. van Driel, Phys. Rev. B 82, 125411 (2010).
- ⁴² M. Breusing, S. Kuehn, T. Winzer, E. Malicacute, F. Milde, N. Severin, J. P. Rabe, C. Ropers, A. Knorr, and T. Elsaesser, Phys. Rev. B 83, 153410 (2011).
- ⁴³ P. J. Hale, S. M. Hornett, J. Moger, D. W. Horsell, and E. Hendry, Phys. Rev. B 83, 121404 (2011).
- ⁴⁴ P. A. George, J. Strait, J. Dawlaty, S. Shivaraman, M. Chandrashekhar, F. Rana, and M. G. Spencer, Nano Lett. 8, 4248 (2008).
- ⁴⁵ J. M. Dawlaty, S. Shivaraman, M. Chandrashekhar, F. Rana, and M. G. Spencer, Appl. Phys. Lett. 92, 042116 (2008).
- ⁴⁶ D. Sun, Z. K. Wu, C. Divin, X. B. Li, C. Berger, W. A. de Heer, P. N. First, and T. B. Norris, Phys. Rev. Lett. **101**, 157402 (2008).
- ⁴⁷ H. Choi, F. Borondics, D. A. Siegel, S. Y. Zhou, M. C. Martin, A. Lanzara, and R. A. Kaindl, Appl. Phys. Lett. 94, 172102 (2009).
- ⁴⁸ P. Plochocka, P. Kossacki, A. Golnik, T. Kazimierczuk, C. Berger, W. A. de Heer, and M. Potemski, Phys. Rev. B 80, 245415 (2009).
- ⁴⁹ D. Sun, C. Divin, C. Berger, W. A. de Heer, P. N. First, and T. B. Norris, Phys. Rev. Lett. **104**, 136802 (2010).
- ⁵⁰ J. Z. Shang, Z. Q. Luo, C. X. Cong, J. Y. Lin, T. Yu, and G. G. Gurzadyan, Appl. Phys. Lett. **97** (2010).
- ⁵¹ L. Huang, G. V. Hartland, L. Q. Chu, Luxmi, R. M. Feenstra, C. Lian, K. Tahy, and H. Xing, Nano Lett. 10, 1308 (2010).
- ⁵² H. Wang, J. H. Strait, P. A. George, S. Shivaraman, V. B. Shields, M. Chandrashekhar, J. Hwang, F. Rana, M. G. Spencer, C. S. Ruiz-Vargas, and J. Park, Appl. Phys. Lett. **96**, 081917 (2010).
- ⁵³ B. A. Ruzicka, L. K. Werake, H. Zhao, S. Wang, and K. P. Loh, Appl. Phys. Lett. **96**, 173106 (2010).
- ⁵⁴ B. A. Ruzicka, N. Kumar, S. Wang, K. P. Loh, and H. Zhao, J. Appl. Phys. **109**, 084322 (2011).
- ⁵⁵ J. Z. Shang, T. Yu, J. Y. Lin, and G. G. Gurzadyan, ACS Nano 5, 3278 (2011).
- ⁵⁶ P. A. Obraztsov, M. G. Rybin, A. V. Tyurnina, S. V. Garnov, E. D. Obraztsova, A. N. Obtraztsov, and Y. P. Svirko, Nano Lett. **11**, 1540 (2011).
- ⁵⁷ S. S. Chu, S. F. Wang, and Q. H. Gong, Chem. Phys. Lett. **523**, 104 (2012).
- ⁵⁸ H. Z. Yang, X. B. Feng, Q. Wang, H. Huang, W. Chen, A. T. S. Wee, and W. Ji, Nano Lett. **11**, 2622 (2011).

- ⁵⁹ D. Sun, C. Divin, J. Rioux, J. E. Sipe, C. Berger, W. A. de Heer, P. N. First, and T. B. Norris, Nano. Lett. 10, 1293 (2010).
 ⁶⁰ E. Hendry, P. J. Hale, J. Moger, A. K. Savchenko, and S. A. Mikhailov, Phys. Rev. Lett. 105, 097401 (2010).
- ⁶¹ R. Wu, Y. L. Zhang, S. C. Yan, F. Bian, W. L. Wang, X. D. Bai, X. H. Lu, J. M. Zhao, and E. G. Wang, Nano Lett. **11**, 5159 (2011).
- ⁶² P. Blake, E. W. Hill, A. H. C. Neto, K. S. Novoselov, D. Jiang, R. Yang, T. J. Booth, and A. K. Geim, Appl. Phys. Lett. ⁶³ Z. S. Yang, N. H. Kwong, R. Binder, and A. L. Smirl, J. Opt. Soc. Am. B 22, 2144 (2005).
 ⁶⁴ S. A. Mikhailov, Physica E 44, 924 (2012).