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Phys. Rev. B 87, 081202 — Published 25 February 2013

DOI: 10.1103/PhysRevB.87.081202

Ionic current and polarization effect in TIBr

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Thallium bromide (TlBr) is an ionic semiconductor which has shown great capacity for accurate radiation detection. Its application to this end, however, has been hampered by degradation of performance over time, in a process called polarization. This effect has been traditionally assigned to a build-up of ions at the electrodes, which would counteract an applied electrical bias field. Here we estimate ionic mobility in TlBr and its possible association with the polarization effect using parameter free quantum simulations. Our results indicate that in samples with up to moderate levels of impurities, ions cannot traverse distances large enough to generate zones of accumulation and depletion in the crystal, suggesting different causes for the polarization effect.

In recent years, thallium bromide has emerged as one of the most promising materials for sensitive room temperature γ and X-radiation detection, achieving resolution as fine as 1% at 662 keV or better. 1,2 The high performance stems from the material's favorable properties, namely, a moderate band gap (2.7 eV), very long carrier drift length (lifetime up to 10^{-4} s), high room-temperature resistivity (around $10^{11} \Omega.\text{cm}^{-1}$)³ and high average atomic number.⁴ However, its widespread adoption for radiation detection applications-such as medical and space imaging or port monitoring for national securityhas been prevented due to invariable performance degradation after operation times that vary from hours to several weeks.⁵ This effect, termed polarization, has been assumed to be associated with the accumulation of oppositely charged ions (Tl⁺ and Br⁻) at the electrical contacts of the device, from migration of the ions in opposite directions via vacancy hopping under an applied bias field. The resulting charge build up would counter the applied electric field and impair the collection of photo-induced carriers, degrading detection performance. Different remedies have been attempted to prevent this degradation, including using thallium contacts,6 cooling the detectors, ⁷ employing various surface treatments, ⁸ and others. No technique has yet been able to solve the degradation problem indefinitely.

In this letter we describe a quantitative theoretical estimation of ionic migration in TlBr to compare against the observed degradation times. Drift ionic mobility can be evaluated by the Einstein-Smoluchowski relation:

$$\mu = \frac{qD}{kT} \tag{1}$$

with the diffusivity given by the expression:⁹

$$D = f\nu_0 a_0^2 \sum_{i=\text{TI,Br}} \left\{ \exp\left(-\left(\Delta G_m^i + \Delta G_f^{\text{vacs}}\right)/kT\right) + \tilde{n}_{\text{vac},i}^{\text{excess}} \exp\left(-\Delta G_m^i/kT\right) \right\}$$
(2)

for the vacancy-hop mechanism, where q is the charge of the mobile species, k is the Boltzmann constant, f is a factor dependent on the lattice, a_0 is the jump distance of an ion, ν_0 is the frequency of vibration of the ion in the jump direction (attempt frequency), ΔG_m is the migration free energy barrier, and $\Delta G_f^{\rm vacs}$ is the average Gibbs free energy of formation of both types of vacancies for a given value of the Fermi level. For TIBr $(Pm\bar{3}m$ structure), the ions move in $\langle 100 \rangle$

directions on equivalent sites forming a simple cubic lattice, for which f=0.655 and a_0 equals the lattice constant. The term containing $\tilde{n}_{\text{vac},i}^{\text{excess}}$ accounts for the possibility of an extrinsic concentration of vacancies, which may form to keep charge neutrality in the presence of charged impurities, for example 10 .

In order to theoretically estimate ionic current in TlBr, all quantities in Eqs. (1) and (2) can be obtained from parameterfree quantum mechanical simulations. We use density functional theory¹¹ with the generalized gradient approximation for the exchange-correlation as developed by Perdew, Burke and Erzenhof (PBE).12 We performed tests using more accurate HSE06 hybrid functional^{13,14} in smaller cells and verified the accuracy of PBE for the analysis presented here¹⁰. The projector augmented-wave method, 15 as implemented in the VASP code, ^{16–18} is used to treat core electrons. A planewave basis with an energy cutoff of 320 eV is used. For Brillouin zone sampling, we use the tetrahedron method with a Monkhorst-Pack mesh of $5\times5\times5$ k-points for a $4\times4\times4$ supercell (128 atoms). Atomic coordinates were relaxed until all residual forces were below 0.01 eV/Å. For pristine TlBr, we obtain a direct band gap of 1.98 eV and a lattice parameter of 4.06 Å, compared to experimental values¹⁹ of 3.01 eV (direct gap) and 3.97 Å.²⁰

The formation energies of defects are given by:²¹

$$\Delta E_f = E_d - (E_p - \sum_i n_i \mu_i) + q(\mu_e + E_{VBM}),$$
 (3)

where E_d and E_p are the total energies of the defective and the pristine supercells, respectively, n_i is the number of atoms of element i removed from the supercell and added to a reservoir whose chemical potential is μ_i , and q is the charge exchanged with a reservoir at an electron chemical potential μ_e , which we reference to the energy of the valence band maximum, $E_{\rm VBM}$. Spurious periodic electrostatic interactions for supercells with charged defects were corrected with the Makov-Payne scheme²², with ε_0 =5.7²³. The chemical potentials in the stoichiometric regime are given by $\mu_{\rm Tl(Br)} = \mu_{\rm Tl(Br)}^0 + \Delta H_{f,\rm TlBr}/2$, where $\Delta H_{f,\rm TlBr} = \mu_{\rm TlBr} - \mu_{\rm Tl}^0 - \mu_{\rm Br}^0$ and $\mu_{\rm Br}^0 = -1.62$ eV (hexagonal structure) and $\mu_{\rm Br}^0 = -1.62$ eV(Br₂ gas). The equilibrium concentration of each defect is then given by $c = c_0 exp[-E_f/k_BT]$.

In Fig. 1 we show the calculated formation energies for

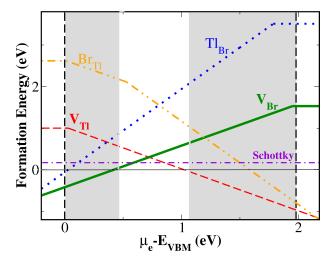


FIG. 1. (color online) Formation energies of intrinsic defects in TlBr: E_f of positively charged Br vacancies coincides with that of negatively charged Tl vacancies near the middle of the band-gap, pinning the Fermi level. Neutrally charged complexes of vacancies (Schottky pairs), Tl and Br antisites are also indicated. The vertical dashed lines indicate the positions of the calculated band edges and the shaded areas denote inaccessible values of the Fermi level, where the formation of vacancies becomes spontaneous ($E_f < 0$).

vacancies and antisite defects in TlBr as a function of electron chemical potential. The slopes of the curves indicate the charge state of the defect and kinks mark transition levels. The vertical dashed lines indicate the positions of the calculated band edges, and the shaded areas indicate physically inaccessible regions of Fermi level where the formation energy of one of the vacancies becomes negative. Because of the pinning of the fermi level near the middle of the band-gap, indicated by the crossing of the formation energy curves of $V_{\rm Tl}^-$ and $V_{\rm Br}^+$, as well as the low formation energies of these defects, TIBr is driven to generate extra charged vacancies in response to any excess charge introduced by impurities 9,10,26,27. Thus, inclusion of the $\tilde{n}_{\text{vac},i}^{\text{excess}}$ term in Eq. (2) is of fundamental importance to estimate the relationship between concentration of impurities and the ionic current. From Eq. (3), we obtain $\Delta E_f^{\rm vacs} = (\Delta E_f^{V_{\rm Br}^+} + \Delta E_f^{V_{\rm TI}^-})/2$ to be plugged into Eq. (2). We found $\Delta E_f^{\rm vacs} = 0.3$ eV using PBE with a $4\times4\times4$ supercell. The calculated values are quite lower than experimental estimates of $2\Delta G_f^{\rm vacs}=0.91~{\rm eV^{27}}$. As a result, simulations predict a larger concentration of intrinsic vacancies in TIBr and therefore larger ionic currents, as we will discuss in the sequence.

Other terms in Eq. (2) can be estimated from the potential energy surface, which we sample using the nudged elastic band method with the climbing image implementation. The height of the migration barrier in Figure 2 give ΔG_m . The attempt frequency ν_0 in Eq. (2) can be obtained within harmonic transition-state theory via the Vineyard equation, which involves the ratio of the product of the system's stable vibrational modes in the ground vs. transition state. If we make the reasonable assumption that only the degree of freedom of the hopping atom in the direction of the vacancy

hop is important, ν_0 can be extracted from the curvature at the bottom of the migration barrier within the harmonic approximation. From the data in Fig. 2, we obtained ΔG_m of 0.31 eV and 0.10 eV for the migration barriers of Tl⁺ ($V_{\rm Tl}^-$) and Br⁻ ($V_{\rm Br}^+$), respectively, and ν_0 of 0.43 THz and 0.38 THz for Tl⁺ and Br⁻, respectively. These values of ν_0 are similar to the short-wavelength transverse acoustic phonon frequency in the X direction (the hop direction).

To properly estimate the diffusivities with Eq. (2), we also must consider that vacancies can bind with oppositely charged species and become less mobile. To account for such binding, we must replace $\Delta E_m (= \Delta G_m + T \Delta S_m)$ with an effective migration barrier given by $\Delta E_{m,\text{eff}} = \Delta E_m - 0.5 \Delta E_{\text{bind}}$, where the binding energy of defect complexes is given by 30

$$\Delta E_{\text{bind}} = \sum_{i} E_{d,i} - E_{\text{complex}}.$$
 (4)

Here, $E_{\rm complex}$ is the formation energy of the defect complex, $E_{d,i}$ are the formation energies of each individual defect that comprise the complex, and $\Delta E_{\rm bind} > 0$ denotes binding, following the convention adopted in ref. Ref. 31. For TlBr, we calculate the binding energy for Schottky pairs $(V_{\rm Tl}^- - V_{\rm Br}^+)$ as 0.44 eV, resulting in effective migration barriers of 0.53 eV and 0.32 eV for Tl⁺ and Br⁻, respectively, for vacancies bound as Schottky pairs. These effective barriers also have been estimated experimentally as 0.51 eV and 0.28 eV for Tl⁺ and Br⁻, respectively, by Bishop *et al.*²⁷ and as 0.56 eV and 0.25 eV, respectively, by Samara.

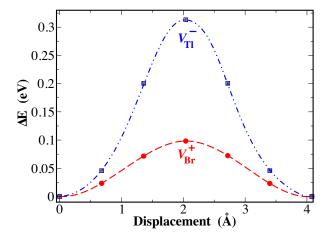


FIG. 2. (color online) Calculated migration barriers of charged TI (blue squares) and Br (red circles) vacancies obtained using the nudged elastic band method. The lines are guides to the eye.

To assess the agreement between the measured effective barriers and the theoretical results, we need to estimate the relative proportion of bound to free vacancies in TlBr. An estimate can be made by evaluating: ^{31,33}

$$p = \frac{n_{\text{pair}}}{n_{\text{free}}} = z \exp(\frac{\Delta G_{\text{bind}} - \Delta G_f^{\text{vacs}}}{k_B T}), \tag{5}$$

where z is the coordination number of vacancy pairs (*i.e.*, the number of ways of forming the pair at a particular site) and

Extrinsic conc.(cm ⁻³)	0	10 ¹⁶	10 ¹⁷	10 ¹⁸	10 ¹⁹
Experiment.params. ^a	270	9.3	0.96	0.10	0.01
Associated vacancies	2.7	2.5	1.5	0.32	0.036

 $^{a}\Delta G_{m}$ and ΔG_{f} from Ref. 27

TABLE I. Time in years for the more mobile Br⁻ ions to drift a distance of 1 mm at room temperature under an applied bias of 1000 V/cm in TlBr crystals with different concentrations of extrinsic vacancies at room temperature. Times are shown using both the experimental and theoretical estimates for the relevant parameters.

 $\Delta G_{\rm bind} = \Delta E_{\rm bind} - \Delta S_{\rm bind} T$, with $\Delta S_{\rm bind}$ the entropy change due to the association of the vacancies. Considering bound pairs of vacancies occupying nearest neighbor sites, for TlBr we have z=8. The entropies of formation and association of the pairs can be estimated using the expressions:³¹

$$\Delta S_f = (10.8E_{\text{bind}} - 2.56) k_B$$
 (6)

and

$$\Delta S_{\text{bind}} = \left(\ln([V_c]) + \frac{4L}{Nk_B T_m}\right) 2k_B,\tag{7}$$

where $[V_c]$ is the critical mole fraction of vacancies at melting $(8.5 \times 10^{-4} \text{for TlCl}^{31})$, T_m is the melting temperature (732) K for TlBr³¹), L is the heat of fusion (16.3 kJ/mol for TlBr³¹) and N is Avogadro's constant. Equation 6 is empirical and was obtained by fitting several experimental results, whereas equation 7 comes from assuming that melting occurs when the concentration of thermally generated vacancies reaches a critical value. Using these expressions with the formation energy from Ref. 27 and an association energy of 0.44 eV from our calculations, we get that at room temperature there are about 20 times more vacancies bound in neutrally charged pairs than isolated ones. Using instead the calculated formation energy for Schottky pairs, we get that at room temperature the number of vacancy pairs is four orders of magnitude higher than that of free vacancies in the crystal. We note that even disregarding the entropy terms approximated by equations 6 and 7 these conclusions are maintained. Moreover, our results show that oppositely charged vacancies are not only bound on nearestneighbor sites, but also at least for second nearest neighbor sites; therefore, the effective value of z in equation 5 is underestimated and should be at least as high as 24. Thus, the values of p given above are lower estimates. Consequently, we conclude that most vacancies will be paired in neutral complexes rather than being isolated in TlBr at room temperature, explaining the good agreement between the experimental and theoretical results for the migration barriers of Tl⁺ and Br⁻ ions the vacancies are considered to be largely bound in neutral pairs.

In Fig. 3 we plot the ionic mobilities \times T(K) vs. T⁻¹ for different concentrations of extrinsic vacancies using Eqs. (1) and (2). This data is based on considering complete association of vacancies into neutral pairs, using the binding energy between $V_{\rm Tl}$ and $V_{\rm Br}$ as a common value for binding between

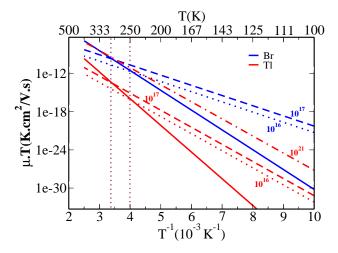


FIG. 3. (color online) Ionic mobility, μ , as a function of T^{-1} for Br^- (blue) and Tl^+ (red) ions in TlBr. The solid lines are plotted for the case of intrinsic concentrations of vacancies, while the dotted and dashed lines correspond to cases with additional extrinsic concentrations of vacancies as indicated next to each line (in cm $^{-3}$). These results were obtained using our calculated parameters, assuming that all vacancies are associated in pairs with oppositely charged defects. The binding energy assumed was the same as that of Schottky pairs. The dash-dotted curves correspond to the required extrinsic concentration of Tl vacancies so that Tl^+ ions become the majority carriers at room temperature, given intrinsic concentrations of V_{Br}^+ . The vertical dotted lines indicate room temperature and $-20\,^{\circ}$ C.

vacancies and any charged defect, which was shown to be reasonably accurate for several impurities in Ref 10. Excess vacancy concentrations must be higher than 10^{17} cm⁻³ to affect ionic mobilities at room temperature. Using the data from Ref. 27 this threshold changes to 10^{15} cm⁻³, because of the smaller concentration of vacancies due to the higher formation energy relative to the theoretical estimate. Overall, however, the qualitative behavior is similar in either case. We also show the extrinsic concentrations needed to affect the mobilities at -20 °C, a temperature at which the polarization effect significantly slows down⁷. We further show the required extrinsic concentrations of V_{Tl} to make Tl^+ ions more mobile than Br⁻ (assuming intrinsic concentration of $V_{\rm Br}$): $10^{21} \, {\rm cm}^{-3} \, V_{\rm Tl}$ with completely associated vacancies, a concentration so high that the crystal would likely become unstable and melt.³¹ Using the experimental data results that $10^{19} \, \mathrm{cm}^{-3}$ extrinsic V_{Tl} would be needed to change the majority carriers to Tl⁺. At such high concentrations of defects, many of the approximations we used become less reliable³³, therefore these results involve larger errors than the ones with concentrations below 10^{19} cm^{-3} .

In Table I we show the calculated time it would take a Br⁻ ion to traverse a distance of 1 mm in the crystal under an applied bias of 1000 V/cm to estimate the mobility at room temperature, for different concentrations of extrinsic vacancies. Taking the experimental parameters and considering reasonably high extrinsic concentrations of V_{Br}^+ , up to $10^{17}~{\rm cm}^{-3}$, the times are in order of years, which is inconsistent with the longest observed stable operation of a TIBr radiation detector

at room temperature—on the order of a few months.^{1,2} Thus, for a time-dependent polarization effect to be caused by drift of Br ions, extrinsic concentrations of vacancies must be significantly higher than 10^{17} cm⁻³. Otherwise, our calculations show that the experimental estimate of the migration barrier for Br would have to wrong by nearly 300% to accommodate the hypothesis of detector degradation within a few hours due to intrinsic charge gradients within the crystal. For example, if ΔE_m^{Br} were only 0.1 eV- a discrepancy of 70% from the experimental estimate - it would take about 8.5 hours for a Br⁻ ion to traverse a distance of 1 mm within an intrinsic TIBr crystal. If ΔE_m^{Br} were 0.25 eV a discrepancy of 21% from the experimental estimate, a Br- ion would take about 75 days to move 1 mm in an impurity free crystal. In Ref. 10 we calculated the effect of co-doping TlBr with Se and Pb, showing that in this case there is occurrence of defect complexes involving both dopants and both types of vacancies that bind more than three times more strongly than the Schottky pairs. Reproducing the analysis above for the material treated in this way, we find that migration times for the vacancies, even with extrinsic concentrations of vacancies of 10^{19} cm⁻³. would be of the order of 10⁶ years. This indicates that such a treatment would be a very effective alternative to ultra purification of TIBr. This hints at either a high concentrations of extrinsic vacancies in TlBr, meaning high impurity levels, or different causes for the degradation of the energy resolution of these radiation detectors than that commonly accepted. This important conclusion has been overlooked in current efforts to construct stable and accurate TlBr radiation detectors.

In summary, we have estimated the diffusivities of intrinsic

ions in TlBr using DFT with the PBE and HSE06 exchangecorrelation functionals. By accounting of the binding of oppositely charged vacancies into pairs, very good agreement between the theoretical effective migration barriers and the experimental measurements is obtained. We estimate that there are more bound than free vacancies in TlBr at room temperature. Using both the experimental and our theoretical data, we estimated the time required for the faster species, Br⁻ ions, to traverse a distance of 1 mm in the crystal under 1000 V/cm bias at room temperature. We showed that this migration takes too long to account for the observed degradation of TlBr detectors in less than about 1 year, unless if the samples have very large levels of contamination (at least around 10^{17} cm⁻³), which is not consistent with measured impurity concentrations. For a TlBr crystal co-doped with Pb and Se ions, as discussed in Ref. Ref. 10 these migration times are extremely high, indicating an alternative to purification. Our results strongly indicate that the origin of the loss of resolution and sensitivity over time of TIBr radiation detectors is not exclusively the accumulation of $\mathrm{Br}^-/\mathrm{Tl}^+$ at the contacts.

ACKNOWLEDGMENTS

This work performed under the auspices of the U.S. Dept. of Energy by Lawrence Livermore National Laboratory under Contract DE-AC52-07NA27344, with support from the National Nuclear Security Administration Office of Nonproliferation and Verification Research and Development (NA-22).

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- ¹ M. Shorohov, M. Kouznetsov, I. Lisitskiy, V. Ivanov, V. Gostilo, and A. Owens, IEEE Trans. Nucl. Sci. 56, 1855 (2009).
- ² K. Hitomi, M. Matsumoto, O. Muroi, T. Shoji, and Y. Hiratate, IEEE Trans. Nucl. Sci. **49**, 2526 (2002).
- ³ A. Churilov, G. Ciampi, H. Kim, L. Cirignano, W. Higgins, F. Olschner, and K. Shah, IEEE Trans. Nucl. Sci. **56**, 1875 (2009).
- ⁴ T. E. Schlesinger, J. E. Toney, H. Yoon, E. Y. Lee, B. A. Brunett, L. Franks, and R. B. James, Mat. Sci. and Eng.: R: Reports 32, 103 (2001).
- ⁵ K. Hitomi, Y. Kikuchi, T. Shoji, and K. Ishii, IEEE Trans. Nucl. Sci. **56**, 1859 (2009).
- ⁶ K. Hitomi, T. Shoji, and Y. Nlizeki, Nucl. Instrum. Methods Phys. Res., Sec. A **585**, 102 (2008).
- ⁷ T. Onodera, K. Hitomi, and T. Shoji, IEEE Trans. Nucl. Sci. 54, 860 (2007).
- ⁸ I. B. Oliveira, F. E. Costa, P. K. Kiyohara, and M. M. Hamada, IEEE Trans. Nucl. Sci. 52, 2058 (2005).
- ⁹ P. Knauth and H. Tuller, J. Am. Ceram. Soc **85**, 1654 (2002).
- ¹⁰ C. Rocha Leão and V. Lordi, submitted (2011).
- ¹¹ P. Hohenberg and W. Kohn, Phys. Rev. **136**, B864 (1964).
- ¹² J. P. Perdew, K. Burke, and M. Ernzerhof, Phys. Rev. Lett. 77, 3865 (1996).
- ¹³ J. Heyd, G. Scuseria, and M. Ernzerhof, J. Chem. Phys. **118**, 8207 (2003).
- ¹⁴ J. Heyd, G. Scuseria, and M. Ernzerhof, J. Chem. Phys. **124**,

- 219906 (2006).
- ¹⁵ P. E. Blöchl, Phys. Rev. B **50**, 17953 (1994).
- ¹⁶ G. Kresse and D. Joubert, Phys. Rev. B **59**, 1758 (1999).
- ¹⁷ G. Kresse and J. Furthmüller, Phys. Rev. B **54**, 11169 (1996).
- ¹⁸ G. Kresse and J. Furthmüller, Comput. Mater. Sci. 6, 15 (1996).
- ¹⁹ R. Z. Bachrach and F. C. Brown, Phys. Rev. B **1**, 818 (1970).
- We neglect spin-orbit coupling (SOC), which was verified to be inconsequential for the properties of interest here (see Ref. Ref. 10.
- ²¹ S. B. Zhang and J. E. Northrup, Phys. Rev. Lett. **67**, 2339 (1991).
- ²² G. Makov and M. C. Payne, Phys. Rev. B **51**, 4014 (1995).
- ²³ R. Lowndes and D. Martin, Proc. Roy. Soc. London A **308**, 473 (1969).
- ²⁴ C. Persson, Y.-J. Zhao, S. Lany, and A. Zunger, Phys. Rev. B 72, 035211 (2005).
- ²⁵ C. Rocha Leão and V. Lordi, Phys. Rev. B **84**, 165206 (2011).
- ²⁶ G. A. Samara, Phys. Rev. B **23**, 575 (1981).
- ²⁷ S. R. Bishop, W. Higgins, G. Ciampi, A. Churilov, K. S. Shah, and L. Tuller, J. Electrochem. Soc. **158**, J47 (2011).
- ²⁸ G. Henkelman, B. P. Uberuaga, and H. Jónsson, The Journal of Chemical Physics **113**, 9901 (2000).
- ²⁹ G. Vineyard, J. Phys. Chem. Solids **3**, 121 (1957).
- ³⁰ C. G. Van de Walle and J. Neugebauer, J. Appl. Phys. **95**, 3851 (2004).
- ³¹ W. Bollmann, Crystal Research and Technology **17**, 849 (1982).
- 32 We performed tests on the $3\times3\times3$ supercell, as used in Ref. ? where the association energy of vacancy pairs was disregarded,

and we obtained a a migration barrier of 0.15~eV for Br vacancies. This value did not change appreciably when employing the HSE06 functional. These results, although attesting the good qual-

- ity of the PBE-NEB calculations, are less reliable due to larger finite size errors.
- P. Fahey, P. Griffin, and J. Plummer, Rev. Mod. Phys. **61**, 289 (1989).