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# Electronic Structure of Copper Phthalocyanine from $G_0W_0$ Calculations

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## Abstract

We present all-electron  $G_0W_0$  calculations for the electronic structure of the organic semiconductor copper phthalocyanine, based on semi-local and hybrid density functional theory (DFT) starting points. We show that  $G_0W_0$  calculations improve the quantitative agreement with high resolution photoemission and inverse photoemission experiments. However, the extent of the improvement provided by  $G_0W_0$  depends significantly on the choice of the underlying DFT functional, with the hybrid functional serving as a much better starting point than the semi-local one. In particular, strong starting point dependence is observed in the energy positions of highly localized molecular orbitals. This is attributed to self-interaction errors, due to which the orbitals obtained from semi-local DFT do not approximate the quasi-particle orbitals as well as those obtained from hybrid DFT. Our findings establish the viability of the  $G_0W_0$  approach for describing the electronic structure of metal-organic systems, given a judiciously chosen DFT-based starting point.

## 1. Introduction

In a molecular-solid form, copper phthalocyanine (CuPc), whose structure is schematically depicted in Figure 1, is a highly stable organic semiconductor with a broad range of applications. These applications include light emitting diodes, solar cells, gas sensors, and thin film transistors. It is even a candidate for single molecule devices.<sup>1</sup> Owing to these applications, there is considerable interest in investigating its electronic structure, both experimentally<sup>2-19</sup> and theoretically.<sup>2, 3, 10, 16, 20-31</sup> Beyond its technological relevance, CuPc is a prototypical molecule representative of typical interactions in many metal-organic systems and therefore an excellent benchmark for evaluation of computational methods.

To date, first principles studies of CuPc electronic structure have been dominated by density functional theory (DFT). In a previous study,<sup>26</sup> some of us have shown that use of DFT with semi-local or with hybrid functionals results in qualitatively different predictions regarding the nature and energy position of some of the frontier orbitals of CuPc, including the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO). We have further shown that hybrid functionals yield spectra that are in far better agreement with high resolution gas-phase ultraviolet photoemission spectroscopy (UPS) data.<sup>2</sup> The failure of semi-local functionals in this respect, which has subsequently been observed in other phthalocyanines and porphyrins<sup>32-35</sup> has been attributed to self-interaction errors (SIE).<sup>36,37,38</sup> SIE arise from the spurious Coulomb interaction of an electron with itself in (semi-)local approximations to the exchange-correlation functional. Such errors do not occur in Hartree-Fock theory where they are explicitly cancelled out by the exact (Fock) exchange term. It is thus possible to mitigate these errors by including a fraction of exact exchange, as done in hybrid functionals.<sup>38-41</sup>

Still, even with modern hybrid functionals the agreement of calculated spectra with experiment is not perfect. Formally, although the eigenvalues of a DFT calculation can serve as useful approximations for quasi-particle (QP) excitation energies,<sup>42-45</sup> they are

not rigorously equal to QP excitation energies. Even if semi-quantitative agreement is achieved, the issue of the origin of finer differences between theory and experiment remains open. This is very much the case for CuPc. Although agreement between theory and experiment has been achieved for the most part, some differences remain. In particular, one peak found in the high resolution UPS data<sup>2</sup> (see Figure 4), which has been denoted as “peak F” and attributed experimentally to a Cu-derived state, did not find its match in the theoretical spectra. In the absence of further experimental or computational data, it was not possible to ascertain whether this reflects the remaining limitations of DFT in general or the employed hybrid functional in particular, or whether it stems instead from further phenomena not considered by the computation, such as final state or vibrational effects.<sup>26</sup>

A logical step to take in order to answer this question is to resort to computational methods that compute quasi-particle excitation energies directly.<sup>46</sup> One of the most practical and widely employed methods is many-body perturbation theory within the GW approximation,<sup>43, 47-50</sup> where G is the one-particle Green function and W is the dynamically screened Coulomb interaction. However, calculations based on GW can be prohibitively expensive, especially for larger molecules. Indeed, we are aware of only a limited number of previous GW calculations for organic molecules in the gas phase, e.g. Refs. 34, 40, 51-67, most of which are quite recent. In particular, only recently have GW-based calculations for the free-base phthalocyanine (H<sub>2</sub>Pc) and related porphyrins begun to emerge.<sup>34, 51, 64</sup> We are aware of only one GW study of a transition metal porphyrin derivative, but there the transition metal atom (Co) was replaced with a simpler metallic atom (Ca) for calculating the dynamically screened Coulomb interaction, W.<sup>62</sup> Owing to the significant cost associated with these calculations, none of these studies has employed a fully self-consistent GW.<sup>57, 68-74</sup> Instead, as is often the case with GW calculations, a perturbative approach is used, where both the Green function and the screened Coulomb interaction are evaluated using the underlying single-electron DFT orbitals. The final QP excitation energies are then obtained as a

perturbative first-order correction to the DFT eigenvalues. This approach, which is used here, is known as  $G_0W_0$ .

An additional simplification, employed in most  $G_0W_0$  calculations, is to neglect off-diagonal terms in the self-energy operator. This amounts to assuming that the orbitals obtained from the DFT calculations mimic the quasi-particle wave-function sufficiently well, in which case only the orbital energies need to be corrected.<sup>43</sup> Although this approximation is not universally valid (see, e.g., ref. 52), it often yields excellent results. In particular, GW studies of metal-free phthalocyanines and porphyrins,<sup>34, 51, 64</sup> based on DFT with a semi-local functional as a starting point, have been found to yield satisfactory agreement with experiment.

Given the above-mentioned qualitative differences between semi-local and hybrid functional DFT results for CuPc, it is not at all obvious that semi-local functionals would be a good starting point for GW in this case. Significant sensitivity of perturbative GW calculations to the choice of the DFT starting point has been noted before in solid-state systems. Examples include: narrow-gap semiconductors, where semi-local functionals erroneously predict metallic behavior,<sup>75-78</sup> large-gap semiconductors and insulators, where the quasi-particle gap underestimate in semi-local DFT calculations can be very large,<sup>76, 79, 80</sup> and materials containing localized *d*-states, where semi-local DFT fails due to SIE.<sup>78, 79, 81, 82</sup>

Here, we explore whether  $G_0W_0$  calculations for CuPc yield further quantitative agreement with experiment, beyond that obtained from DFT calculations, and to what extent such further agreement depends on the DFT starting point. To this end, we perform perturbative  $G_0W_0$  calculations, based on both semi-local and hybrid functional DFT calculations, and compare our results to high-resolution gas-phase UPS data<sup>2</sup> and to thin film inverse photoemission spectroscopy (IPES) data.<sup>8, 17</sup> We find that the  $G_0W_0$  calculations yield meaningful improvements in the agreement with experimental results, as compared to those obtained from DFT with a hybrid functional. A detailed analysis reveals that these improvements are clearly discernible only upon comparison to high-resolution experimental data, and obtained only if the hybrid functional, rather

than a semi-local one, is used as the starting point for the  $G_0W_0$  calculation. We relate the observed starting point sensitivity to SIE effects, due to which the orbitals obtained from semi-local DFT do not approximate the quasi-particle (QP) orbitals as well as those obtained from hybrid DFT.

## 2. Methods

### 2.1 Computational Details

All calculations were performed using the all-electron numerical atom-centered orbital (NAO) code, FHI-aims.<sup>83, 84</sup> The NAO basis sets are grouped into a minimal basis, containing only basis functions for the core and valence electrons of the free atom, followed by four hierarchically constructed sets of additional basis functions, denoted by “*tier* 1-4”. A detailed description of these basis functions can be found in Ref. 83. The geometry of CuPc was relaxed using the generalized gradient approximation (GGA) of Perdew, Burke, and Ernzerhof (PBE)<sup>85</sup> with a *tier* 2 basis set, which has been demonstrated to approach the basis set limit for ground-state GGA calculations and to be nearly free of basis set superposition errors.<sup>83</sup> The atomic zero-order regular approximation (ZORA)<sup>83</sup> was used to account for scalar relativistic effects during geometry relaxation.

$G_0W_0$  calculations were carried out using PBE as a semi-local functional starting point and the one-parameter PBE-based hybrid functional (PBEh, also known as PBE0), with 25% of Hartree-Fock exchange,<sup>86</sup> as a hybrid functional starting point. The more accurate, but computationally more expensive, scaled ZORA<sup>87</sup> method was used to account for scalar relativistic effects in the single point calculations that served as starting points for the  $G_0W_0$  calculations. The spin state of CuPc was constrained to a doublet throughout, using the formalism of Behler *et al.*<sup>88, 89</sup>

A detailed account of the all-electron implementation of GW in FHI-aims has been given elsewhere.<sup>90</sup> Briefly, the implementation makes use of the resolution-of-identity (RI) technique, whereby a set of auxiliary basis functions is introduced to represent both

the Coulomb potential and the non-interacting response function. This allows for efficient GW calculations with NAO basis functions. The RI accuracy and NAO basis set convergence have been benchmarked in Ref <sup>90</sup>. The self-energy is first calculated on the imaginary frequency axis and then analytically continued to the real frequency axis using a two-pole fitting procedure.<sup>91</sup> As discussed in more detail below, GW calculations require a larger basis set than DFT calculations to achieve convergence with respect to the number of empty states. Here, GW calculations were performed using basis sets up to *tier 4*.

Performing GW calculations in an all-electron code has the advantage that possible pseudopotential errors are avoided. As discussed extensively in the literature, these errors, which do not affect ground-state DFT, may become significant in GW calculations if there is significant spatial overlap between core and valence wave-functions.<sup>74, 92-99</sup> In addition, the compact and inherently local nature of the NAO basis functions leads to a more rapid convergence with the number of basis functions.<sup>100</sup> The fact that periodic boundary conditions need not be imposed in FHI-aims is another advantage for GW calculations of molecular systems, as there is no need for large regions of vacuum and there can be no artifacts due to spurious interactions between periodic replicas.

## 2.2 Basis set convergence

First, we examine the basis set convergence of our  $G_0W_0$  calculations. The standard implementation of the GW self-energy contains an infinite sum over states,<sup>43</sup> which, in practice translates into a finite sum over a very large number of unoccupied states. This leads to notoriously slow convergence of GW calculations with respect to the number of unoccupied states.<sup>101, 102</sup> We conducted  $G_0W_0$  calculations of CuPc, based on both PBE and PBEh (denoted throughout as GW@PBE and GW@PBEh, respectively) with increasingly large hierarchically constructed NAO basis sets<sup>103</sup> and compared the resulting QP HOMO energy to the experimental ionization potential (IP) value of 6.38 eV, obtained from gas phase UPS.<sup>2, 3, 5</sup> The results are shown in Figure 2. The largest change in the QP HOMO energy is from *tier 1* to *tier 2*. At the *tier 2* level, the QP HOMO

energy is less than 0.3 eV away from experiment, whereas at the tier 1 level the QP HOMO energy is  $\sim 0.5$  eV higher than experiment. At the *tier 4* level, both the GW@PBE QP HOMO energy of 6.26 eV and the GW@PBEh QP HOMO of 6.31 eV are within  $\sim 0.1$  eV from experiment. Our findings regarding basis set convergence are in agreement with those of Ren et al.<sup>90</sup> We also note that the spectra obtained at the *tier 2* level (not shown for brevity) were found to be qualitatively similar to those obtained at the *tier 4* level, with the difference being predominantly a rigid shift of the QP energies by  $\sim 0.2$  eV. All results presented in the following were obtained at the *tier 4* basis set level, which we consider to be adequately converged.

### 3. Results and discussion

The calculated spectra obtained with PBE, PBEh, GW@PBE, and GW@PBEh are shown in Figure 3. They are compared to the gas phase UPS data of Evangelista et al.<sup>2</sup> and to two thin film IPES experiments.<sup>8, 17</sup> We note that the comparison to additional gas phase UPS<sup>3, 5</sup> and IPES<sup>9, 18</sup> experiments is similar. The calculated spectra were obtained from computed single-particle energy levels, broadened by convolution with a 0.35 eV wide Gaussian, in order to simulate the experimental resolution. First, it is important to understand how the energy levels in the different calculations were aligned. Because GW eigenvalues correspond directly to electron removal or addition energies, the GW energies were not modified. However, it is well-known that for either PBE or PBEh the HOMO and LUMO do not correspond to the ionization potential or the electron affinity, respectively,<sup>42</sup> causing an uncontrolled shift of the entire simulated photoemission curve. In theoretical simulations of photoemission from gas-phase clusters,<sup>104-106</sup> this was remedied without fitting to experimental data by computing the ionization potential as the total energy difference between the neutral species and the cation<sup>107</sup> and rigidly shifting the filled-state eigenvalue spectrum such that the HOMO coincided with the computed ionization potential. Here, we employ the same procedure with the PBE and PBEh HOMO set at the total energy difference values of 6.57 and 6.27 eV, respectively. For the empty states, a similar rigid shift was performed to align the



LUMO with the computed electron affinity of 2.04 eV for both PBE and PBEh. The electron affinity was obtained by computing the total energy difference between the neutral species and the anion.<sup>108</sup> In addition, the experimental IPES data are for thin films, where due to polarization effects the experimentally reported fundamental gap (i.e., the difference of the ionization potential and the electron affinity) of 3.1 eV is considerably smaller than the same gap in the isolated molecule. To preserve the computational gas-phase data, the *experimental* IPES spectra were shifted to align their leading peak with the leading peak of the GW@PBEh spectrum. We note that although cross-section effects can be taken into account to improve line-shape agreement between theory and experiment, as recently shown by Vogel et al. for CuPc,<sup>3</sup> this was not included here because our focus is on peak positions.

As mentioned above and discussed in Ref. <sup>42</sup>, although QP energies are not given exactly by DFT eigenvalues, the latter can still often usefully approximate QP energies. At the experimental resolution of the data in Fig. 3, this appears to be the case. All four calculated spectra exhibit the main features of the experimental spectra, namely, the HOMO peak followed by three broader peaks in the UPS data, and the three main peaks in the IPES data. The main difference between the DFT data and the GW data (or experiment) at this resolution is that the PBE spectrum is significantly compressed relative to experiment and that the PBEh spectrum is still somewhat compressed. The two  $G_0W_0$  spectra generally offer good quantitative agreement with experiment and with each other. For example, although the PBE and PBEh HOMO-LUMO gaps are very different (1.12 eV and 2.33 eV, respectively), this leads to a difference of only 0.24 eV between the GW@PBE gap (3.70 eV) and the GW@PBEh gap (3.94 eV). Naively it would appear that: (1) As known for inorganic semiconductors since the early days of  $G_0W_0$  calculations,<sup>43</sup> the main effect of GW is to “shift and stretch” the DFT eigenvalues; (2) The DFT starting point is of little consequence for the final  $G_0W_0$  result. We demonstrate that neither conclusion holds up to scrutiny at a higher resolution.

The same theoretical spectra of Fig. 3, but broadened by convolution with a narrower, 0.15 eV wide Gaussian, are compared in Fig. 4 to high-resolution gas phase

UPS data<sup>2</sup> taken in the region of the HOMO peak and the first lower main peak. The recent gas phase UPS data of Ref. <sup>3</sup> exhibit the same peak positions and are not shown for brevity. Now that sub-features of Fig. 3 can also be considered, the differences in accuracy of the theoretical spectra are revealed. We first focus on the position of the HOMO-1 peak, because it affects the spectral shape noticeably and because lessons learned from it are directly applicable to other spectral features. Both Fig. 4 and Fig. 3 illustrate the positions of the  $a_{1u}$  and  $b_{1g\uparrow}$  energy levels (the corresponding orbitals are visualized in Fig. 5). As discussed previously,<sup>26</sup> owing to a large self-interaction error in the PBE calculation, the  $b_{1g\uparrow}$  orbital, which is highly localized around the Cu atom, is shifted to a higher energy. This shift causes PBE to predict an incorrect ordering of the frontier orbitals, where the  $b_{1g\uparrow}$  orbital is the HOMO, located  $\sim 0.1$  eV above the  $a_{1u}$  orbital.<sup>109</sup> This error is strongly reduced in the PBEh spectrum – the correct ordering is restored, and the overall agreement with experiment is much improved. This is consistent with the higher SIE attributed to the localized  $b_{1g\uparrow}$  orbital, as compared to the  $a_{1u}$  orbital, which is delocalized over the organic macrocycle.

Similarly to PBEh, GW@PBE reorders the  $b_{1g\uparrow}$  and  $a_{1u}$  orbitals, correctly making the  $a_{1u}$  orbital the HOMO. However, the  $b_{1g\uparrow}$  orbital is placed only  $\sim 0.4$  eV lower, leading to a doubling of the first peak of the simulated spectrum, which is in disagreement with experiment. The GW@PBEh spectrum is significantly better – not only is the correct orbital ordering obtained, but the  $b_{1g\uparrow}$  orbital is found  $\sim 1.4$  eV below the  $a_{1u}$  orbital. At this position, the  $b_{1g\uparrow}$  related feature is in very close agreement with the position of “peak F” in the UPS data. Furthermore, this is consistent with the attribution of “peak F” to a Cu-derived orbital in the experimental work of Evangelista et al.<sup>2</sup> Importantly, in the PBEh spectrum, the  $b_{1g\uparrow}$  orbital is somewhat lower, lying  $\sim 1.6$  eV below the  $a_{1u}$  HOMO. At this position, and with the theoretical broadening used to simulate experiment, the  $b_{1g\uparrow}$  orbital forms a shoulder on the second peak of the simulated spectrum, rather than a separate peak, so that “peak F” could not be unequivocally identified from the PBEh data.

Our calculations also yield significant differences between GW@PBE and GW@PBEh in the ordering of the LUMO and LUMO+1 orbitals, as shown in Fig. 3. Visualization of the LUMO and LUMO+1 orbitals, given in Fig. 5, reveals that these differences are related to the energy position of the empty counterpart of the spin-split  $b_{1g}$  orbital,  $b_{1g\downarrow}$ . The PBE calculation erroneously predicts this orbital to be the LUMO, lying  $\sim 0.25$  eV below the non-spin-split  $e_g$  orbital. We have previously postulated that because the SIE shifts the occupied  $b_{1g\uparrow}$  orbital to a higher energy, it also shifts its empty counterpart,  $b_{1g\downarrow}$ , to a lower energy, with the overall spin-split energy severely underestimated.<sup>26</sup> Just as for the filled states, the correct ordering is restored by PBEh, which places the  $b_{1g\downarrow}$  orbital  $\sim 1.1$  eV above the  $e_g$  LUMO. Similarly to the valence spectrum, the empty-state spectrum is not satisfactorily corrected by GW@PBE. In the GW@PBE spectrum the  $b_{1g\downarrow}$  orbital is essentially degenerate with the  $e_g$  LUMO, lying only  $\sim 0.03$  eV above it. In contrast, the GW@PBEh calculation maintains the PBEh orbital ordering, with a similar energy difference between the  $b_{1g\downarrow}$  orbital and the  $e_g$  LUMO. At this position, the  $b_{1g\downarrow}$  orbital is in close agreement with the position of a “weak” peak in the experimental spectrum, identified by Murdey et al.<sup>17</sup> via curve fitting (shown in Fig. 3) and assigned by them to a Cu-derived  $b_{1g}$  state. This indicates yet again that PBEh is superior to PBE, as a starting point for  $G_0W_0$ , not only with respect to the occupied states, but also with respect to the empty ones.

The deficiency of GW@PBE, with regard to either GW@PBEh or experiment, indicates that the spurious upward shift of the  $b_{1g\uparrow}$  orbital and the corresponding downward shift of the  $b_{1g\downarrow}$  orbital in the PBE calculation are only partially corrected. This suggests that in this case the PBE starting point is too far removed from the correct solution to result in an accurate perturbative  $G_0W_0$  calculation. In contrast, the GW@PBEh correction to the energy of the  $b_{1g\uparrow}$  orbital is only slightly less negative than that for the  $a_{1u}$  orbital, indicating that PBEh is a much better starting point with respect to the position of the  $b_{1g\uparrow}$  orbital. To identify the origin of this starting point sensitivity, additional  $G_0W_0$  calculations were performed, where PBEh was used to calculate the dynamic dielectric function,  $\epsilon$ , in an otherwise PBE based GW calculation, and vice versa.

A *tier 2* basis set was employed for these calculations. The resulting QP energies of the frontier orbitals of CuPc are shown in Table 1.

Evidently, the QP energies of the localized  $b_{1g\uparrow,\downarrow}$  orbitals depend more strongly on G and W than on  $\epsilon$ . Therefore, one cannot ascribe the unsatisfactory results of the GW@PBE calculations merely to over-screening, resulting from an over-estimated polarization due to the small HOMO-LUMO gap of PBE. This means that for highly localized orbitals that carry a large SIE, the orbitals obtained from semi-local DFT are not a satisfactory approximation to the QP orbitals. This conclusion is further supported by calculating the electron density difference between the  $b_{1g\uparrow}$  orbital obtained from PBEh and from PBE, visualized in Figure 5. The difference in the density is small compared to the densities themselves, and has to be magnified by a factor of ten with respect to the other orbital densities visualized in Figure 5. Still, such small differences are known to be significant for GW calculations.<sup>81</sup> For the  $b_{1g\uparrow}$  orbital, the difference between PBEh and PBE amounts to a lower density around the Cu atom and a higher density around the neighboring N atoms for PBEh. In comparison, the differences between the PBEh and PBE densities of the  $a_{1u\uparrow}$  and  $e_g\uparrow$  orbitals are invisible even at this magnification. This is consistent with the weaker starting point dependence of the QP energies of these orbitals. The strong dependence of the QP-correction of the DFT energies on the spatial distribution of the KS orbitals, rather than just on the KS eigenvalues, may indicate that partial self-consistency only in the eigenvalues would not be sufficient to remedy severe SIE issues.

Our findings are reminiscent of those reported in Refs.<sup>78, 79, 81, 82</sup> for several semiconductors. There, it was shown that the underbinding of the *d*-band by semi-local functionals owing to SIE leads to changes in hybridization. Similarly to the case of CuPc, the inadequacy of the semi-local starting point for these semiconductors carries over to  $G_0W_0$  calculations and a hybrid starting point proves to be superior. Interestingly, although both the  $b_{1g}$  and the  $e_g$  orbitals have Cu-*d* contributions, this leads to a change in hybridization and starting point sensitivity only for the  $b_{1g}$  orbital. We also note that this issue is not restricted to systems with *d*-orbitals and may arise in any system

afflicted with SIE. For example, the starting point sensitivity observed for isonicotinic acid is caused by SIE in orbitals associated with the localized nitrogen lone pair.<sup>66</sup>

So far we have focused mostly on the spin-split  $b_{1g}$  orbital as an important special case. Fig. 6 exhibits the QP corrections to the PBE and PBEh for a wider range of energies. Generally, the QP corrections over the PBEh starting point are smaller than the QP energy corrections over the PBE starting point, making PBEh a better starting point. Contrary to the “shift and stretch”  $G_0W_0$  corrections often observed in typical inorganic semiconductors,<sup>43</sup> here the QP corrections to the different orbitals found here are quite scattered and do not form an obvious straight line. We attribute this to the different degree of localization and resulting SIE for each orbital.<sup>37,38</sup> In such cases, a simple stretch of the DFT spectrum is not sufficient to compensate for SIE. This demonstrates clearly that SIE-related differences in the DFT starting point are generally carried over to the  $G_0W_0$  calculations.

#### 4. Conclusions

We conducted  $G_0W_0$  calculations for the electronic structure of CuPc, based on semi-local (PBE) and hybrid (PBEh) functional starting points, and compared the results to available gas phase UPS and thin film IPES data. We found that, GW@PBEh yields excellent agreement with experimental results, especially compared to the positions of the peaks associated with the leading Cu-derived  $b_{1g}$  orbital, but GW@PBE does not. We attribute the observed starting point sensitivity of  $G_0W_0$  calculations to self-interaction errors in the semi-local DFT calculations, which partly carry over to the perturbative  $G_0W_0$  results. The localization and hybridization of orbitals exhibiting significant SIE is affected, making them unsatisfactory approximations to the quasi-particle orbitals. This problem cannot be remedied by correction schemes that only shift the DFT eigenvalues without changing the spatial distribution of the orbitals and would require off-diagonal correction terms that could be prohibitively expensive computationally. In such cases, the orbitals obtained from hybrid DFT provide a better approximation to the QP orbitals and thus a more reliable starting point for  $G_0W_0$  calculations. Our findings establish the

viability of the  $G_0W_0$  approach for describing the electronic structure of metal-organic systems, given a judiciously chosen DFT-based starting point.

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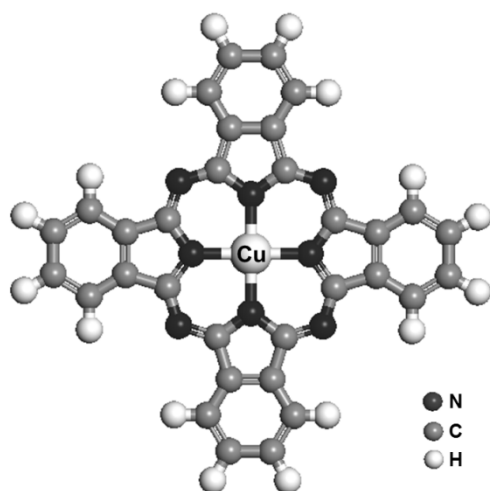


Figure 1: Schematic illustration of a CuPc molecule

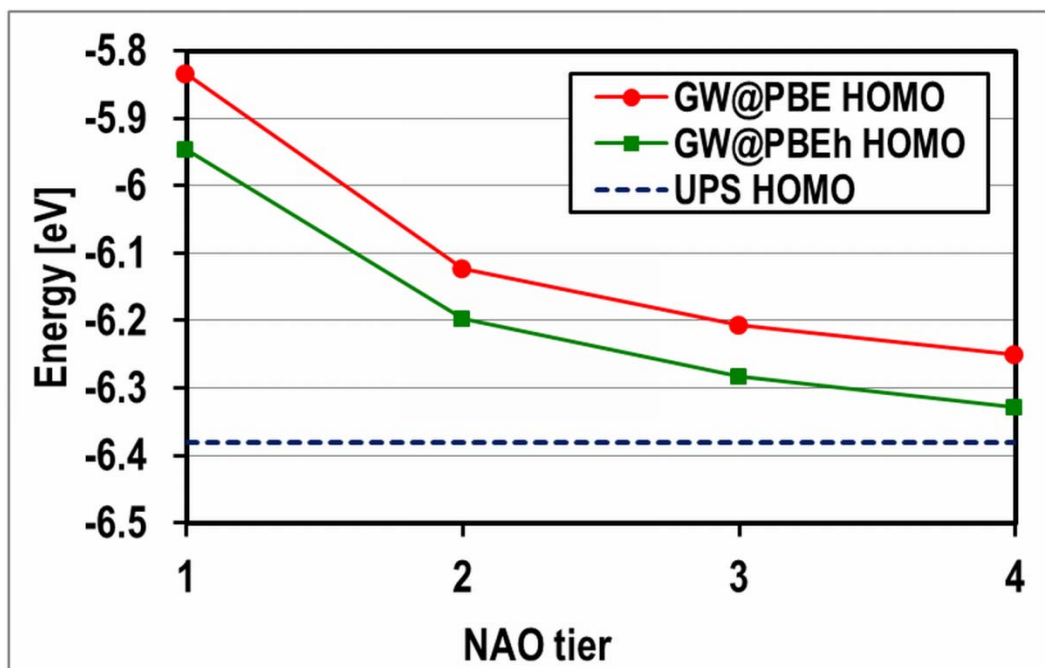


Figure 2: Comparison of the experimental ionization potential value<sup>2, 3, 5</sup> to the theoretical ionization potential, given by the lowest quasi-hole energy, obtained from  $G_0W_0$  based on the semi-local PBE functional and the hybrid PBEh functional as starting points.

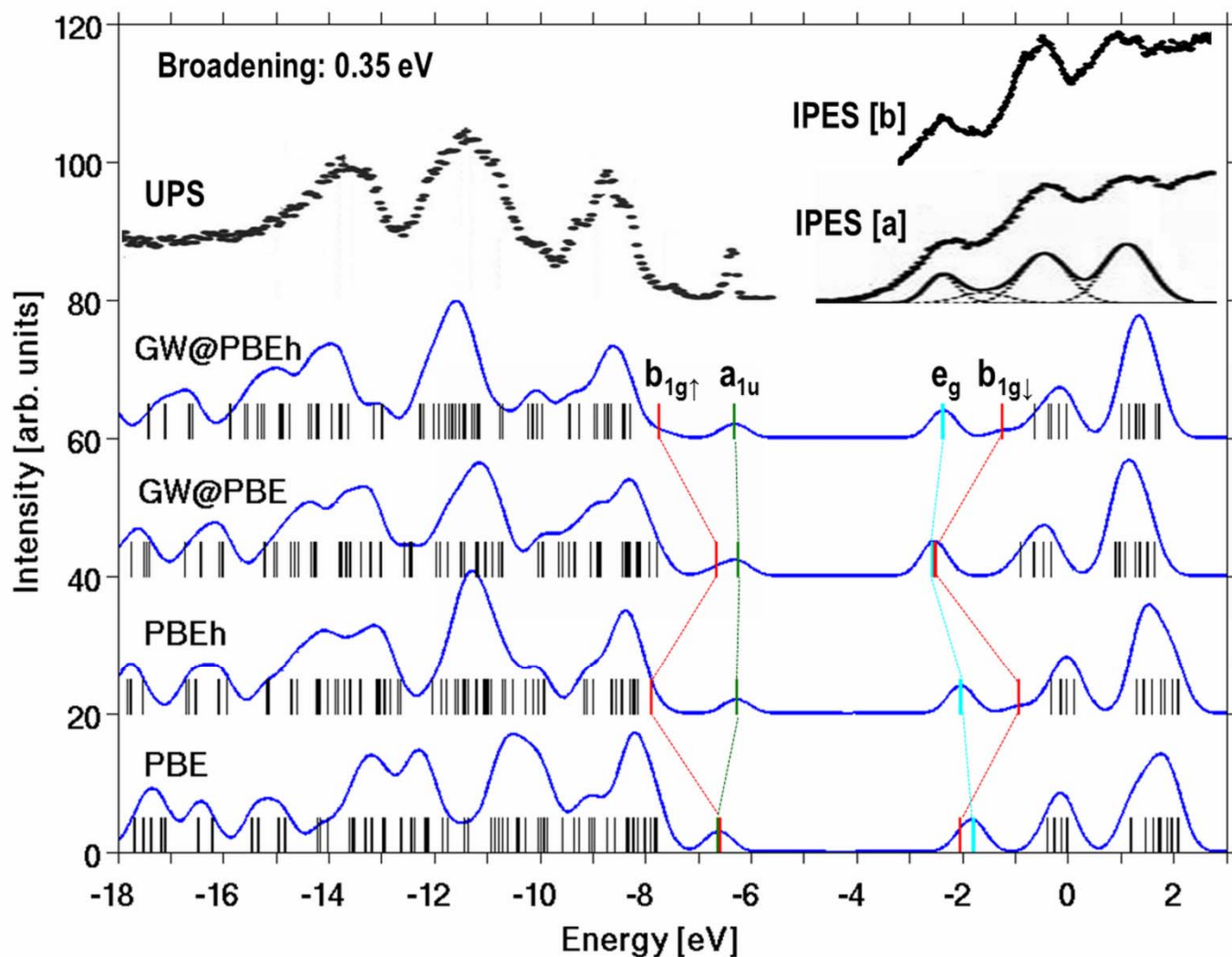


Figure 3: Calculated DFT and QP spectra, obtained from computed energy levels (shown as sticks) by broadening via convolution with a 0.35 eV wide Gaussian, compared to gas phase UPS of Evangelista et al.<sup>2</sup> and to thin film IPES data of a) Murdey et al.<sup>17</sup> (shown with curve fitting results) and b) Hill et al.<sup>8</sup> DFT spectra were shifted so as to align the HOMO and LUMO levels with computed ionization potential and electron affinity values – see text for details. Experimental IPES spectra were shifted so as to align the LUMO peak with the computed GW@PBEh LUMO peak.



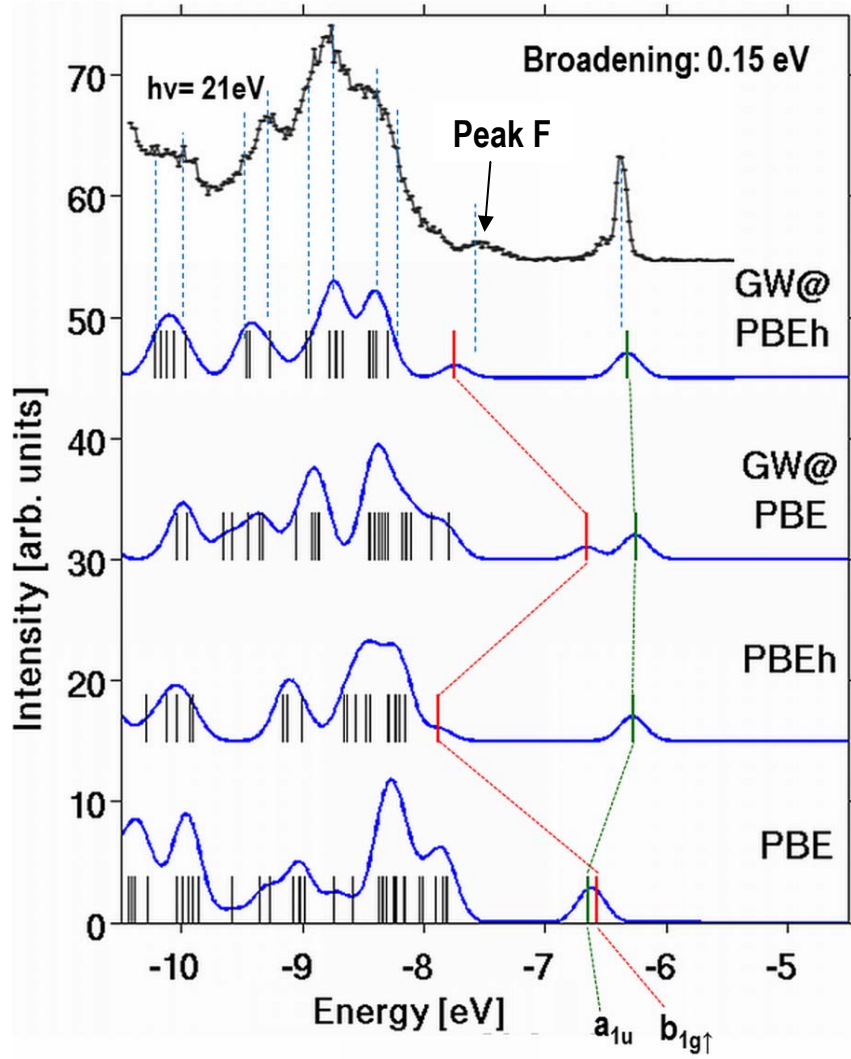


Figure 4: Calculated DFT and QP spectra, broadened by convolution with a 0.15 eV wide Gaussian, compared to high-resolution gas phase UPS data.<sup>2</sup> The DFT spectra were shifted as in Fig. 3.

TABLE I. QP energies (in eV) of the frontier orbitals of CuPc, obtained using different combinations of DFT functionals for the  $GW$  quasiparticle orbitals and calculation of the dielectric matrix  $\epsilon$ . These calculations were performed with a tier 2 basis set.

$GW$	$\epsilon$	$b_{1g\uparrow}$	$a_{1u\uparrow}$	$a_{1u\downarrow}$	$e_{g\uparrow}$	$e_{g\downarrow}$	$b_{1g\downarrow}$
PBE	PBE	-6.346	-6.123	-6.130	-2.371	-2.348	-2.193
PBEh	PBEh	-7.488	-6.197	-6.212	-2.215	-2.193	-0.918
PBE	PBEh	-6.656	-6.163	-6.173	-2.276	-2.252	-1.937
PBEh	PBE	-7.267	-6.160	-6.175	-2.294	-2.273	-1.226

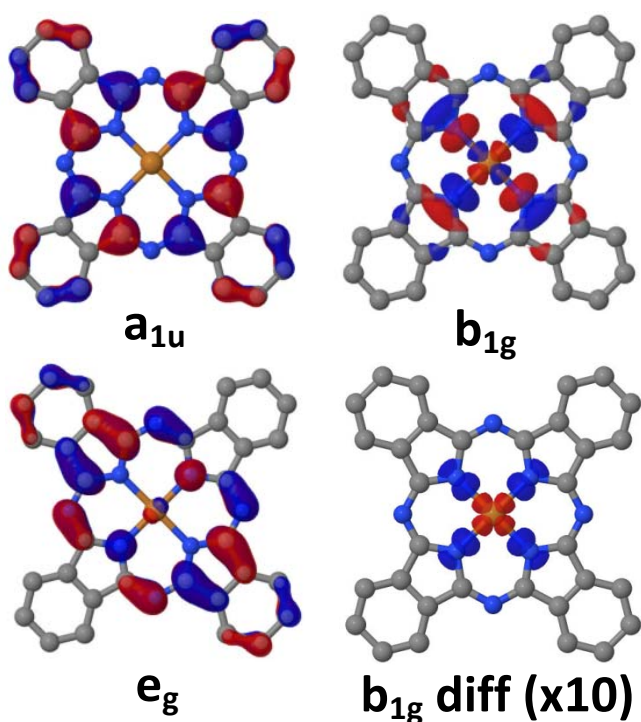


Figure 5: Visualizations of selected leading molecular orbitals of CuPc. Also shown is the density difference between the  $b_{1g\uparrow}$  orbitals obtained at the PBEh and PBE levels of theory, multiplied by a factor of ten for clarity of visualization. Red indicates a higher density in the PBE orbital and blue indicates a higher density in the PBEh orbital.

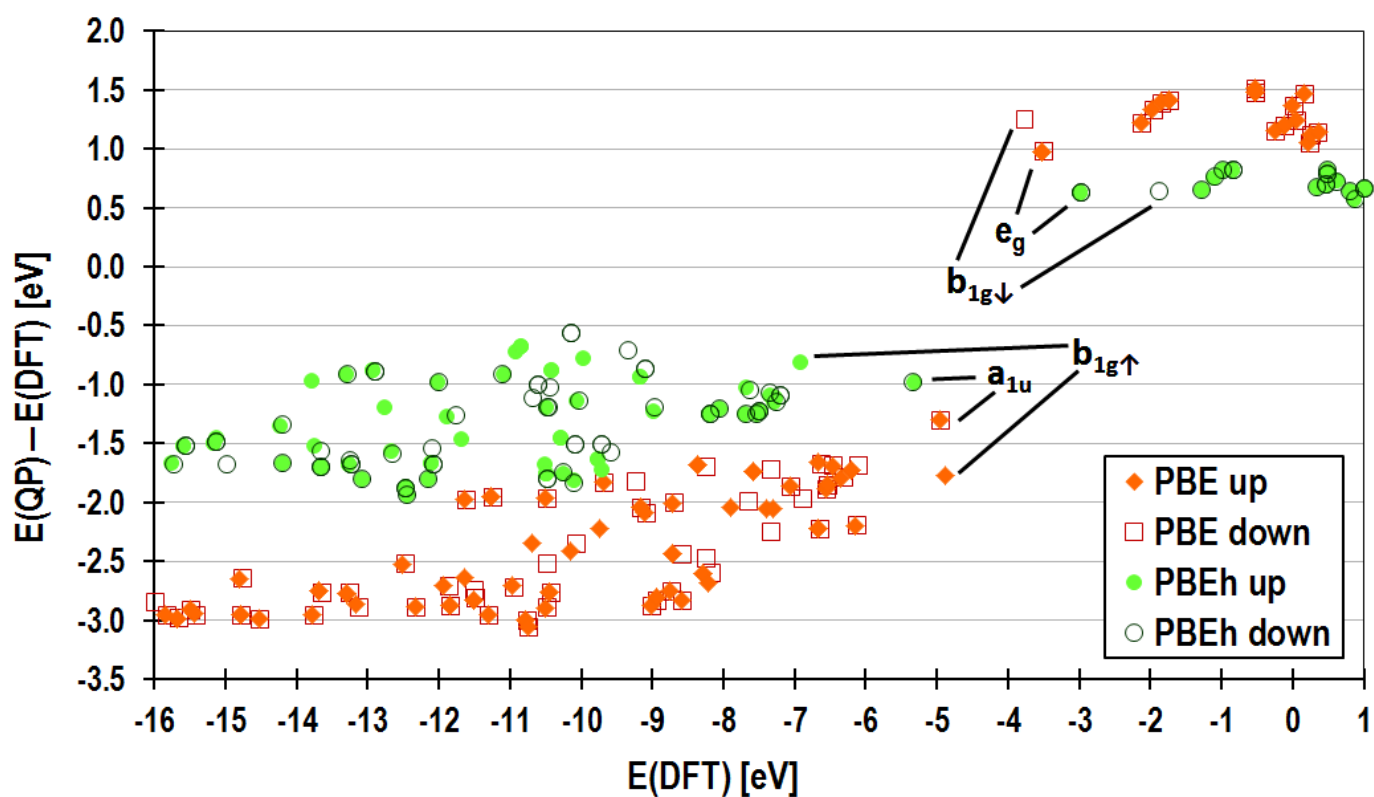


Figure 6: QP corrections as a function of DFT energies for both the PBE and PBEh starting points.

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 PBEh the electron is removed from the doubly occupied a1u orbital

108 The anion is a triplet with both PBE and PBEh

109 In ref. 26, a different orbital ordering has been reported for a PBE calculation of  
 CuPc, with the a1u orbital as the HOMO and the b1g $\uparrow$  orbital as the HOMO-1. This  
 difference is a result of the more converged basis set used here.

