



This is the accepted manuscript made available via CHORUS. The article has been published as:

Pressure-induced phase transitions in AgClO_{4}

D. Errandonea, L. Gracia, A. Beltrán, A. Vegas, and Y. Meng Phys. Rev. B **84**, 064103 — Published 18 August 2011

DOI: 10.1103/PhysRevB.84.064103

Pressure-induced phase transitions in AgClO₄

D. Errandonea¹, L. Gracia², A. Beltrán², A. Vegas³, and Y. Meng⁴

¹Departamento de Física Aplicada-ICMUV, MALTA Consolider Team, Universitat de Valencia,

Edificio de Investigación, c/ Dr. Moliner 50, 46100 Burjassot (Valencia), Spain

²Departament de Química Física I Analítica, MALTA Consolider Team, Universitat

Jaume I, Campus de Riu Sec, 12080 Castelló, Spain

³Instituto de Química-Física Rocasolano, CSIC, c/ Serrano 119, 28006 Madrid, Spain

⁴HPCAT, Carnegie Institution of Washington, Advanced Photon Source, Building 434E,

Argonne National Laboratory, 9700 South Cass Avenue, Argonne, IL 60439, USA

Abstract: AgClO₄ has been studied under compression by X-ray diffraction and

density-functional theory calculations. Experimental evidence of a structural phase

transition from the tetragonal structure of AgClO₄ to an orthorhombic barite-type

structure has been found at 5.1 GPa. The transition is supported by total-energy

calculations. In addition, a second transition to a monoclinic structure is theoretically

proposed to take place beyond 17 GPa. The equation of state of the different phases is

reported as well as the calculated Raman-active phonons and their pressure evolution.

Finally, we provide a description of all the structures of AgClO₄ and discuss their

relationships. The structures are also compared with those of AgCl in order to explain

the structural sequence determined for AgClO₄.

PACS Numbers: 62.50.-p, 64.70.K-, 61.50.Ks, 64.30.-t

1

I. Introduction

A number of structure types of ABO₄ oxides consist of AO₈ bisdisphenoids and BO₄ tetrahedra. They include important mineral structures such as zircon (ZrSiO₄), anhydrite (CaSO₄), silver perchlorate (AgClO₄), and scheelite (CaWO₄). These structures are closely and simply related via crystallographic operations [1] and, because of their compositional diversity and structural simplicity, played a key role in developing comparative crystal chemistry. After pioneering work in the 1960s – 1980s on the pressure effects on the structure of ABO₄ oxides [2, 3], there has been a large effort to determine systematic trends in pressure-induced phase transitions. Many zircon-structured oxides have been found to transform under compression either to a scheelite-type structure or to a monazite-type (CePO₄) structure [4–8]. In some cases, the zircon-monazite-scheelite sequence has been observed [9]. These transitions are consistent with crystal-chemistry arguments supporting that pressure increase can be mirror by changing the ratio of A/B cation sizes [10]. These arguments are also consistent with the anhydrite-monazite-barite (BaSO₄) high-pressure (HP) sequence found in CaSO₄ [11] and with several high-pressure transitions detected in scheelites and related oxides [12 - 18]. In contrast with zircon, scheelite, and anhydrite, the effects of pressure on the crystal structure of silver perchlorate have not been studied yet. Here, in order to improve the understanding the high-pressure behavior of ABO₄ oxides, we report a combined experimental and theoretical study of AgClO₄. Our results verify predictions of the high-pressure structural systematic of ABO₄ oxides. In particular we observed one phase transition and identify the structure of the high-pressure phase. In addition, the occurrence of a second transition is proposed and axial and bulk compressibility of different phases are determined.

II. Experimental details

We performed high-pressure X-ray diffraction experiments at room temperature up to 20.5 GPa. Studies were carried out with a symmetric diamond-anvil cell (DAC) with 480- μ m-diameter culet diamonds and a 150- μ m-drilled rhenium gasket, at 16-IDB beamline of the HPCAT at the Advanced Photon Source (APS). We used a monochromatic X-ray beam (λ = 0.36802 Å) focused down to 10 μ m x 10 μ m. The diffraction patterns were recorded on a MAR345 image plate located at 350 mm from the sample and integrated using FIT2D. To perform the experiments, we used micronsize fresh powder of anhydrous AgClO₄ with purity higher than 99.9% (Aldrich). The powder was loaded in the diamond-anvil cell using neon (Ne) as the pressure-transmitting medium to guarantee quasi-hydrostatic conditions in the pressure range covered by the experiments. Special care was taken during the loading to avoid hydration of AgClO₄. The pressure was measured by means of the ruby fluorescence technique. It was also confirmed with the equation of state (EOS) of Ne [19]. The indexation of the Bragg reflections was done with UNITCELL [20] and DICVOL [21]. GSAS [22] was used to carry out structural refinements.

III. Overview of the calculations

Density-functional theory (DFT) calculations were performed with the CRYSTAL09 program package [23]. Chlorine and silver atoms have been described by HAYWLC-31G and HAYWSC-311d31G pseudo-potential basis set, respectively, while for oxygen atom it has been used the standard 6-31G*. The Becke's three-parameter hybrid non-local exchange functional [24] combined with the Lee-Yang-Parr gradient-corrected correlation functional, B3LYP [25], has been used. Hybrid density-functional methods have been extensively used for molecules and provide an accurate description of crystalline structures, bond lengths, and binding energies [26]. The diagonalization of

the Fock matrix was performed at adequate k-points grids in the reciprocal space being the Pack-Monkhorst/Gilat shrinking factors IS = ISP = 4. The thresholds controlling the accuracy of Coulomb and exchange integrals were set to 10^{-8} and 10^{-14} , whereas the percent of Fock/Kohn-Sham matrices mixing was set to 40 [23]. Fittings of the computed energy–volume data provide values of zero-pressure bulk modulus and its pressure derivative as well as enthalpy–pressure curves for the four studied polymorphs [27]. Vibrational-frequencies calculation in CRYSTAL is performed at the Γ point within the harmonic approximation, and the dynamical matrix is computed by numerical evaluation of the first-derivative of the analytical atomic gradients.

IV. Results

a. X-ray diffraction experiments

At ambient conditions AgClO₄ has a tetragonal structure, space group (SG) **142m** (No. 121), with Z = 2 [28]. At high-temperature there is transition to a cubic structure, space group **F43m** (No. 216), with Z = 4 [29]. X-ray diffraction measurements show that our samples have the tetragonal structure with unit-cell parameters a = 4.976(3) and c = 6.746(4) Å. These values and the obtained atomic coordinates (see Table I) agree with those previously reported [28]. The structure of AgClO₄ is shown in Fig.1a. Following the classical description, it consists of layers of ClO₄ tetrahedra sharing corners with AgO₈ bisdisphenoids. The four Cl-O bond distances are 1.469 Å and the eight Ag-O bond distances are 2.528 Å (×4) and 2.726 Å (×4).

Fig. 2 shows a selection of diffraction patterns measured at different pressures. From ambient pressure up to 4.2 GPa all the diffraction patterns can be assigned to the low-pressure tetragonal structure. At 4.2 GPa three additional reflections appear as due to the solidification of Ne [29]. These peaks are identified with asterisks in the figure. From 4.2 GPa we increased the pressure up to 5.1 GPa. At this pressure we observed

considerable changes in the diffraction pattern, indicating that in that pressure range a phase transition took place. No additional changes were detected up to the maximum pressure. We also found that the phase transition is non-reversible as can be seen in the upper trace of Fig. 2.

As described in the introduction, the high-pressure structural sequence of many ABO₄ oxides can be understood considering crystal-chemistry arguments. According with these arguments, under pressure AgClO₄ (like CaSO₄) could take the structure of related sulphates and chromates that crystallize with the monazite- and barite-type structures. Considering these arguments, to analyze the high-pressure data we considered as potential high-pressure structures of AgClO₄: monoclinic monazite (SG $P2_1/n$), orthorhombic barite (SG Pnma), and AgMnO₄-type (SG $P2_1/n$), a monoclinic distortion of the barite-type structure. We found that the diffraction patters, collected at 5.1 GPa and higher pressure, could be indexed with an orthorhombic unit cell. A subsequent Rietveld refinement of the diffraction pattern measured at 5.1 GPa showed that it could be well matched with a barite-type structure. The structure is shown in Fig. 1b. In Fig. 2 we show for comparison, the measured and calculated patters in addition to the residuals of the refinement. There it can be seen that the agreement between theoretical and experimental diffraction patterns is quite good. The residuals are R_{WP} = 3.04 %, $R_P = 1.25$ %, and $R(F^2) = 0.92$ % (154 reflections). The obtained structural parameters are given in Table II and are in good agreement with those of the aristotype barite [30] and also with those of the isostructural KClO₄ compound [31]. This result is consistent with the idea that oxides under compression prefer to take the structure of related compounds with larger cations [10]. According with our results the transition to the barite-type phase involves a volume collapse of 7 %, indicating that the transition is a first-order transformation. This fact is also consistent with the fact that the highpressure phase can be recovered at ambient pressure upon decompression. As can be seen in Fig. 1, the transition to the barite-type phase does not only involve an increase of the packing efficiency, but also an increase in the Ag coordination number from 8 to 8 + 4. In contrast the ClO₄ tetrahedra are only slightly modified. According with our experiments, at 5.1 GPa in the barite-type phase there are a double-degenerated short Cl-O distances (1.335 Å) and two longer distances 1.350 Å and 1.352 Å. In the other hand, for the Ag-O bonds we obtained the following distances: 2.537 Å (×2), 2.556 Å, 2.622 Å, 2.723 Å (×2), 2.753 Å (×2), 2.889 Å (×2), and 3.175 Å (×2). Therefore, the slightly distorted ClO₄ tetrahedra and the 12-coordinated Ag units resemble very much that of divalent-metal sulfate minerals isomorphic to barite (celestine, anglesite, and barite) [32].

From our experimental results we obtained the pressure evolution of the unit-cell parameters of the low- and high-pressure phase. The structural refinements performed for data collected for pressures larger than 5.1 GPa were of similar quality than the one performed at 5.1 GPa (see details above). The results are shown in Fig. 3 together with the pressure evolution of the volume. In this figure it can be seen that in the low-pressure phase the *c*-axis is more compressible than the *a*-axis. In the high-pressure phase the *a*-axis is also the most compressible one. The pressure–volume curves shown in Figure 3 were analyzed in the standard way using a third-order Birch–Murnaghan equation of state [33]. The bulk modulus (B₀), its pressure derivative (B₀'), and the atomic volume (V₀) at zero pressure were obtained for both phases. For the low-pressure phase we got: $V_0 = 167(1) \text{ Å}^3$, $B_0 = 29(4) \text{ GPa}$, and $B_0' = 4.1(2)$. For the high-pressure phase we got: $V_0 = 310.9(9) \text{ Å}^3$, $B_0 = 38(8) \text{ GPa}$, and $B_0' = 5.1(6)$. The obtained bulk moduli indicate that AgClO₄ is a quite compressible compound. The origin of this phenomenon is probably the weakness of the Ag-O bonds. Previously, it

has been empirically determined that the bulk modulus in many ABO₄ compounds is related to the cation charge density of the AO₈ polyhedra [10]. In particular, it has been established that B₀ (GPa) = 610 Z/d^3 , where Z is the cationic formal charge of A and d is the mean A–O distance at ambient pressure in Å. From our data we obtained an average Ag–O distance of 2.627 Å. Applying the formula given above, a bulk modulus of 33 GPa is obtained, which agrees with the value obtained from the fitted equation of state for the low-pressure phase of AgClO₄.

b. Theoretical study of the structural properties

First-principle calculations support the experimental findings. Fig. 4 shows the calculated total energy as a function of volume for relevant structures of AgClO₄. These are the tetragonal ambient-pressure structure (142m), an orthorhombic barite-type structure (Pnma), and a monoclinic structure which belongs to space group $P2_1/m$ (No. 11). This structure will be later described in detail. In addition to these three structures, based upon crystal-chemistry arguments, we also performed calculations for other candidate structures as scheelite, zircon, AgMnO₄-type, monazite, anhydrite, KAlF₄, Cmcm-type NaClO₄, and high-temperature AgClO₄. From Fig. 4, the enthalpy as function of pressure can be calculated for each phase and the relative stability and coexistence pressures of the phases can be extracted by the common-tangent construction. We found in agreement with experiments that the most stable structure at ambient conditions is the tetragonal structure of AgClO₄ (142m). The calculated lattice parameters are summarized in Table III. They slightly overestimated the experimental values, although the differences are within the typical reported systematic errors in density-functional theory calculations [34, 35]. Under compression, the orthorhombic barite-type structure becomes the most stable structure. According with the calculations, the tetragonal-to-barite transition takes place at 2 GPa. This pressure is smaller than the experimental value (5.1 GPa). The difference in the transition pressure is comparable with differences found in related oxides and can be caused by the presence of kinetic barriers [36]. The lattice parameters calculated for the barite phase at 5.4 GPa are summarized in Table III. Calculations underestimate the experimental value of the a-axis and overestimate the experimental value of the other two axes. In spite of these differences, calculations predict the same crystal symmetry for the high-pressure phase, supporting that it could have a barite-type structure. On the other hand, as in the experiments, in the calculations we obtain a large volume collapse associated to the transition (6%), which indicates that the transition has a first-order character. This fact is consistent with the non-reversibility of the transition detected by experiments. From the calculations the pressure evolution of the lattice parameters and unit-cell volume, qualitatively agree with the experimental evolution as shown by the equation of state parameters determined for the tetragonal (orthorhombic phase): $B_0 = 27$ GPa and $B_0' = 4$ ($B_0 = 37$ GPa and $B_0' = 5$).

Upon further compression, calculations predict a second transition to a monoclinic structure with symmetry $P2_1/m$ which is shown in Fig. 1c. This structure was considered following the structural relationship between cations and alloys proposed by O'Keeffe and Hyde [37], later generalized by Vegas [38, 39]. Among the several possible structures, that of the high-temperature phase of deuterated RbD₂PO₄ [40] was considered as one of the most plausible candidates, being so the object of the theoretical calculations, as described below.

According with these calculations, the second transition takes place at 17.2 GPa. Experiments were performed up to 20.5 GPa and this transition was not found. Probably it will be found upon further compression (note that the first transition was found in experiments at a pressure 3.2 GPa higher than calculated). Unfortunately, beyond 20.5

GPa the diffraction patterns broadens and distorts, not allowing to obtain any reliable results from them. Reasons for these changes are beyond the scope of this work and may be related either to the occurrence of pressure-induced phase transitions or to pressure-induced chemical decomposition of AgClO₄. The lattice parameters calculated for the high-pressure monoclinic phase are summarized in Table III. Apparently the compression of this phase is isotropic. We found also that the monoclinic β angle is basically not affected by compression. According with calculations there is a volume change of about a 1.5 % at the orthorhombic-monoclinic transition. It also involves a change of the Ag coordination to 11, but the Cl coordination remains 4. For the monoclinic phase we determined the equation of state being $B_0 = 43.4$ GPa and $B_0' = 4$. Among all the structures included in the calculations the monoclinic phase remains the most stable one up to 40 GPa. In this structure, as in the other two, again it is observed that most of the compression of the crystal is accounted by the reduction of the Ag-O bonds, being the ClO₄ tetrahedra highly uncompressible units.

Changes in crystal structures induced by the phase transitions can be also related to different local atomic rearrangements in the crystals. Thus the higher density of the high-pressure structures can be traced back to the unit-cell volume reduction due to a more effective packing of the O atoms surrounding the Ag atoms. To analyze pressure effects from this perspective we calculated the pressure-evolution of Ag-O and Cl-O bond distances for the three reported phases. Results are summarized in Figure 5. Calculated bond distances are slightly different than experimental distances. However calculations are capable to accurately describe the evolution and changes induced by pressure in atomic bonds. In the figure, clearly it can be seen that in the three phases the Ag-O bonds are more compressible than the Cl-O bonds; i.e. the ClO₄ tetrahedra behave like rigid units. The differential bond compressibility is more notorious in the low-

pressure tetragonal phase. Another fact to remark is that at the first phase transition, the induced coordination change produces an enlargement of the Ag-O bonds in order to accommodate four oxygen atoms more surrounding the Ag atoms. Regarding the second transition, calculations show that the distortion of the ClO₄ tetrahedra is enhanced in the monoclinic phase and that the Ag-O bonds are strongly reduced at the orthorhombic-monoclinic transition. The average Ag-O bond distances are reduced a 5% at the transition.

There is a last comment we would like to add about theoretical results. As we already mentioned, calculations found the high-temperature phase of AgClO₄ (F43m) to be not stable in comparison with the tetragonal phase. However, if we consider a volume expansion (negative pressures) we found that AgClO₄ prefers to take the cubic structure instead the tetragonal one. The high-temperature F43m phase [41] has an AgCl-subarray of the zincblende-type and is consistent with the stabilization of the cubic phase upon heating, as it was reported for many other compounds [15, 16]. This feature, in turn, agrees with the concept that relates oxidation and pressure [42] which will be discussed below. Following this concept, compression induces a volume and symmetry reduction in AgClO₄, but heating of the oxide releases pressure producing a reversion of the structural changes. Therefore, if we start the structural sequence in the high-temperature structure of AgClO₄, volume reduction causes in AgClO₄ a gradual symmetry reduction following the sequence cubic-tetragonal-orthorhombic-monoclinic.

c. Lattice-dynamics calculations

Lattice vibrations play an important role for materials modelling and their behaviour under pressure provides useful information regarding structural instabilities and phase transformations. The frequencies (ω) of Raman-active modes for the tetragonal, orthorhombic, and monoclinic structures have been calculated as well as the

Grüneisen parameters ($\gamma = B_0 \ \partial ln\omega/\partial P$) from its pressure dependences. Group theoretical considerations lead to 12 zone-center Raman-active modes in the tetragonal phase of AgClO₄: $\Gamma = 2A_1 + B_1 + 4B_2 + 5E$. The calculated ambient-pressure frequencies are summarized in Table IV. There it can be seen that the modes can be organized in three different groups. One group is composed by the six low-frequency modes with frequencies smaller than 251.5 cm⁻¹. These modes are separated by a phonon-gap of nearly 90 cm⁻¹ from three modes which follow the sequence $A_1 \le E \le B_2$. At high frequency, there are also three modes organized following the same symmetry order, which is separated from the second group by a phonon gap of about 150 cm⁻¹. The last three modes are associated to internal vibrations within the ClO₄ tetrahedra. In Table IV we also reported the pressure coefficient $(\partial \omega/\partial P)$ for each mode and the Grüneisen parameter. The two modes more affected by pressure are the B_2 mode with frequency 107.3 cm⁻¹ and the E mode with frequency 182.6 cm⁻¹. The last mode is associated with an Ag-O stretching. In addition, in the table it can be seen that the tetragonal structure presents two soft modes (at 64 and 251 cm⁻¹) characterized by a decrease of the vibrational frequency with pressure. These modes have symmetry E and B_I and both are associated to a bending between O-Ag-O units. Finally, we can see that Grüneisen parameters are much smaller in tetragonal AgClO₄ than in related compounds like zircon-type and scheelite-type ABO₄ oxides [43, 44]. In contrast they are comparable with those reported for barite-type ABO₄ oxides [45]. This indicates that in AgClO₄ and barite-type oxides the restoring force acting on an atom displaced from its equilibrium position is smaller than in other ABO₄ oxides. This is consistent with the fact that both barite-type oxides and AgClO₄ are the most compressible compounds within the ABO₄ family [46].

We will comment now on the Raman-active modes of the barite-type phase. Group theoretical considerations lead to 36 zone-center Raman-active modes: $\Gamma = 11A_g$ + $7B_{1g}$ + $11B_{2g}$ + $7B_{3g}$. The calculated sequence of modes resembles very much that of barite-type oxides. In our case, calculations show that lattice modes for frequencies smaller than 280 cm⁻¹ are basically ascribed to the motion of the Ag cation and tetrahedral ClO₄ units. The internal vibrations of the ClO₄ tetrahedron spanned the frequency range from 280 - 880 cm⁻¹, but with a gap between 406 and 609 cm⁻¹. The modes located between 610 and 785 cm⁻¹ can be associated to the v₁ and v₃ bands of barite [47]. For this structure the pressure coefficients of the different modes are comparable to those of the low-pressure phase. In particular, the modes with larger pressure coefficient are those located between 140 and 195 cm⁻¹. In addition, the barite structure presents one soft mode A_g (at 375 cm⁻¹) characterized by a negative Grüneisen parameter which corresponds to a bending of O-Cl-O units (rotation of ClO₄ tetrahedra). This feature is typical of scheelite-structure oxides [43], suggesting that at higher pressure orthorhombic phases should undergo a transition involving a strong coupling between a zone-centre optic mode and a strain of A_g symmetry.

Finally, for the monoclinic phase, group theoretical considerations lead to 18 zone-center Raman-active modes: $\Gamma = 11A_g + 7B_g$. The calculated modes are summarized in Table IV. There it can be seen that modes more sensitive to pressure are those located between 200 and 300 cm⁻¹. In contrast with the other two structures there are no soft modes present in the monoclinic phase. Another typical feature of this phase is the increase of the frequency of the modes associated to internal vibrations of the ClO₄ tetrahedron in comparison with the other two phases. These frequencies increase following the structural sequence tetragonal-orthorhombic-monoclinic. This fact could be associated to the increase of the force constants of the internal vibrations.

V. Crystal chemistry of AgClO₄

The two previously-known phases of AgClO₄ and the high-pressure transitions can be rationalized when the structures are analyzed in terms of their cation sub-arrays (AgCl) and simultaneously compared with the structural changes undergone by the parent binary halide AgCl. This approach has proved to be fruitful in the analysis of many other structures of oxides [38, 39, 48] and is based upon the following simple features:

- i) There is a general trend by which the cation arrays in the oxides try to maintain the structure of the parent alloy/metal [38, 39].
- ii) In many instances, the insertion of O atoms to form the oxides produces the same effect as the application of physical pressure, so that cations, in the oxides, can adopt structures typical of high-pressure phases of the alloy/metal. The behavior of the BaSn/BaSnO₃ pair of compounds is paradigmatic [42, 49].
- iii) In those oxides that stabilize in structures associated to high-pressure phases of the parent alloys, usually at high temperature (HT) a phase transition takes place, in such a way that the structure of the HT-phase recovers that of the ambient pressure phase of the alloy [39, 48].
- iv) In many instances, the cation subarrays of oxides and their corresponding alloys have concurrent pathways in their phase transitions, as if the O atoms would not be present [48].

Figure 6 clearly shows that the tetragonal structure of AgClO₄ is a small distortion of the cubic rock-salt-type AgCl. The importance of this comparison resides in that the volumes of both unit cells is almost identical, with values of 170 and 167 Å³ for AgClO₄ and AgCl, respectively. That means that the insertion of four O atoms per formula unit does not alter significantly the volume of the cell. The unique effect we

might assign to the oxidation should be the tetragonal distortion of the rock-salt AgCl array. It should be remarked, however, that the distortion occurs in a concerted manner, so that the contraction of the a and b axes equals the elongation of the c axis and hence, the average value of the three axes in the tetragonal AgClO₄ phase (5.567 Å) coincides with the unit-cell parameter of the halide AgCl (5.55 Å).

It has also been reported that, above 430 K, the tetragonal phase of AgClO₄ transforms into a cubic structure (**F43m**, a = 6.95 Å, V = 347 Å³) where the cell volume is doubled and the O atoms show positional disorder [29]. In this structure the parent structure of the AgCl subarray is not modified resembling also rock-salt-type AgCl.

As discussed above, the tetragonal AgClO₄ converts at 5.1 GPa into a barite-type structure. Like BaSO₄, the structure is orthorhombic (*Pnma*) and can be described following O'Keeffe & Hyde [37] as an oxygen-stuffed AgCl-subarray of the FeB-type which is represented in Figure 7. The structure is formed by columns of trigonal prisms of Ag (Ba, Fe) atoms running parallel to *b* and where the ClO₄ (SO₄, B) groups/atoms are inserted. The final coordination number of the ClO₄ increases from 6 in the NaCl-like phase to 7 in the barite-type structure.

At this point, we can conclude that unlike the high-temperature rock-salt-type and the tetragonal phases of AgClO₄, in which the parent structure of AgCl (NaCl-type) is maintained, the AgCl-subarray of the high pressure barite-type structure does not correspond to any known structure for the binary AgCl compound. This discrepancy, which at first glance could inquire the assertions quoted above, admits an explanation looking at the high-pressure behavior of AgCl [50, 51]. At increasing pressure AgCl undergoes the transition sequence NaCl \rightarrow $P2_1/m \rightarrow$ TlI (B33) \rightarrow CsCl (a = 3.20 Å). Although the B33 structure is also identified with CrB alloy, in this article, we will use the correspondence $B33 \leftrightarrow$ TlI-type.

The reason for this choice is that, in the TII-type structure, the Ag atoms (grey spheres in Figures 8d, f) are displaced from the center of the trigonal prisms towards the line connecting two Cl atoms. It is noteworthy that in TII itself the Tl atoms are located just on that line, and that the same pattern is obtained whether the connected atoms are I or Tl. In this ideal case, both I and Tl atoms have a CN = 7. Looking at Figures 8d and 8f, we see that, in the isostructural AgCl-III the situation is almost identical. When the prisms are defined by Cl atoms (Figure 8) the Ag atoms lie into the prisms. On the contrary, when the prisms are formed by the Ag atoms, the Cl atoms deviate slightly (~0.2 Å) out the Ag-Ag line. It is a matter of choice to decide the best model. The factors which can influence these results are the applied pressure and the accuracy of the structure refinement depending, in turn, on the quality of the X-ray diffraction patterns.

In this context, two important features should be remarked. The first one is, that in some compounds, such as BaSn, the $B33 \rightarrow B2$ transition is induced under pressure [44], so that the complete transition path becomes $B1(\text{NaCl}) \rightarrow P2_1/m \rightarrow \text{TII}$ ($B33) \rightarrow B2$ (CsCl) as it has been observed for AgCl itself [49, 50]. Recall that the double $B1 \rightarrow B33 \rightarrow B2$ transition has been observed in TII itself and also in some alkali-metal halides. The second feature is that the FeB and the CrB (TII)-type structures are intimately related. In fact, the FeB-type is considered as a stacking variant of the CrB-type structure. In fact, in the FeB boride itself, the B33-phase (Cmcm) has been induced at low temperature [52].

The similarities between both structural types are illustrated in Figure 9. Note that the coordination polyhedron around the B atom, in FeB (Cmcm) (Figure 9a) is quite similar to that surrounding the ClO₄ group in the barite-type AgClO₄ (FeB-type, Pnma) represented in Figure 9b. On the other hand, when the barite structure is projected onto

the (3 0 1) plane, one obtains the pattern drawn in Figure 9c which is part of the *B*33 structure represented in Figure 9d.

In this context, the structure of the high pressure phase AgCl-II, represented in Figures 8d and 10c, can be contemplated as an intermediate structure between the FeB and the *B*33 structures. Thus, if in the blue network of Figure 10c, the blocks of trigonal prisms would displace horizontally from each other, the *B*33 structure is formed. A similar result is obtained if the displacement occurs in the red network.

In Figure 8b we represented an alternative description of the high-pressure phase AgCl-II ($P2_1$ /m) which was not discussed above. This view of the structure is, in fact, a highly distorted B1 structure (Figure 8a). This fact is important because it gives sense to the complete transition path of AgCl under pressure i.e. B1 (NaCl) $\rightarrow P2_1/m \rightarrow TII$ (B33) $\rightarrow B2$ (CsCl), so that the $P2_1$ /m phase can be seen as a B1 structure taking form to convert into the B33. As already shown, in AgCl–II ($P2_1$ /m), fragments of both structures are recognizable.

To close this section we would like to make some comments on the predicted high-pressure structure of the RbD₂PO₄-type. The theoretical calculations carried out on several structures concluded that a second HP-transition to be undergone by AgClO₄ should be the barite-type \rightarrow RbD₂PO₄-type. This phase is monoclinic ($P2_1/m$) and its structure is represented in Figure 11a projected on the ab plane. In projection, the Ag atoms form rhombs which in 3D are highly distorted cubes (average edge a = 4.17 Å) centered by the ClO₄ groups. Consequently, the AgCl substructure is a distorted B2 (CsCl-type) structure which is represented in Figure 11b.

When the monoclinic structure of AgClO₄ is projected onto the *ac* plane, one can perceive that the distortion of the Ag cubes is such that preserves some structural

features of a *B*33 structure (related to the FeB-type array of the barite structure) which appears as an intermediate phase in the process of conversion of *B1* into *B*2.

We have also analyzed the structure of other related compounds such as AgClO₃ which undergoes the transition $P4/m \rightarrow P2_13$ at 413 K. In this cubic phase of AgClO₃, the AgCl subarray also forms a distorted B2 structure but with much more regular cubes. The structure is represented in Figure 11c and its average unit cell (a = 3.85 Å) is smaller than that of AgClO₄.

The magnitude of the distortions occurred in the two *B*2 structures of both AgClO₄ and AgClO₃ cannot be explained at present unless we admit the size of the respective anions as the dominant factor. What is important, however, is that the transitions sequence undergone by AgClO₄ can be identified with that of the parent AgCl, as summarized below:

6.6 GPa 10.8 GPa 17 GPa & 500K
$$AgCl: B1 \rightarrow P2_1/m \rightarrow B33 \rightarrow B2$$

$$T < 429K \qquad 5.2 GPa \qquad 17.5 GPa$$

$$AgClO_4: B1 \rightarrow I\overline{4}2m \rightarrow Barite \rightarrow RbD_2PO_4$$

Note that in the above scheme the transitions of AgClO₄ start with the high temperature NaCl-type which at room temperature becomes distorted-NaCl. The lowering of temperature is equivalent to the application of pressure. These similarities provide new examples of how the structures of oxides are governed by cations and that these cations undergo their own phase transitions in spite of being embedded in an oxygen matrix.

VI. Concluding Remarks

In this work we reported an experimental and theoretical study of the structural stability of AgClO₄ under compression. X-ray-diffraction experiments together with calculations have allowed us to determine the occurrence of a phase transition from the

tetragonal structure of AgClO₄ to a barite-type structure. In addition, total-energy calculations predict the occurrence of a second transition to a structure with monoclinic symmetry. The whole sequence of structures reported for AgClO₄, indicates that their AgCl-subarrays follow a similar sequence as the high-pressure phases of the parent AgCl. The room-temperature equations of state of different phases are also reported. Furthermore, lattice-dynamics calculations of Raman-active modes of different phases are also presented.

Acknowledgements

We acknowledge the financial support of the Spanish MICINN under Grants No. MAT2010-21270-C04-01 and No. CSD2007-00045. X-ray-diffraction experiments were performed at HPCAT (Sector 16), Advanced Photon Source (APS), Argonne National Laboratory. HPCAT is supported by CIW, CDAC, UNLV, and LLNL through funding from DOENNSA, DOE-BES, and NSF. A.P.S. was supported by DOE-BES, under Grant No. DE-AC02-06CH11357.

References

- [1] H. Nyman, B.G. Hyde, and S. Andersson, Acta Cryst. B 40, 441 (1984).
- [2] O. Fukunaga and S. Yamaoka, Phys. Chem. of Minerals **5**, 167 (1979) and references therein.
- [3] J. P. Bastide, J. Solid State Chem. 71, 115 (1987) and references therein.
- [4] H. P. Scott, Q. Williams, and E. Knittle, Phys. Rev. Lett. 88, 015506 (2001).
- [5] L. Gracia, A. Beltrán, and D. Errandonea, Phys. Rev. B **80**, 094105 (2009).
- [6] D. Errandonea, R. S. Kumar, L. Gracia, A. Beltrán, S. N.Achary, and A. K. Tyagi, Phys. Rev. B 80, 094101 (2009).
- [7] D. Errandonea, R. Lacomba-Perales, J. Ruiz-Fuertes, A. Segura, S. N. Achary, and A. K. Tyagi, Phys. Rev. B **79**, 184104 (2009).
- [8] R. Lacomba-Perales, D. Errandonea, Y. Meng, and M. Bettinelli, Phys. Rev. B 81, 064113 (2010).
- [9] F. X. Zhang, J. W. Wang, M. Lang, J. M. Zhang, and R. C. Ewing, Phys. Rev. B 80, 184114 (2009).
- [10] D. Errandonea and F. J. Manjón, Prog. Mater. Sci. 53, 711 (2008).
- [11] W. A. Crichton, J. B. Parise, S. M. Antao, and A. Grzechnik, Am. Mineral. 90, 22 (2005).
- [12] D. Errandonea, J. Pellicer-Porres, F. J. Manjón, A. Segura, Ch. Ferrer-Roca, R. S.
- Kumar, O. Tschauner, P. Rodríguez-Hernández, J. López-Solano, S. Radescu, A. Mujica, A. Muñoz, and G. Aquilanti, Phys. Rev. B **72**, 174106 (2005).
- [13] D. Errandonea, Phys. Status Solidi B **242**, R125 (2005).
- [14] D. Errandonea, J. Pellicer-Porres, F. J. Manjón, A. Segura, Ch. Ferrer-Roca, R. S.
- Kumar, O. Tschauner, J. López-Solano, P.Rodríguez-Hernández, S. Radescu, A. Mújica, A. Muñoz, and G. Aquilanti, Phys. Rev. B **73**, 224103 (2006).

- [15] D. Errandonea, R. S. Kumar, X. Ma, and C. Y. Tu, J. Solid State Chem. 181, 355 (2008).
- [16] J. Ruiz-Fuertes, S. López-Moreno, D. Errandonea, J. Pellicer-Porres, R. Lacomba-Perales, A. Segura, P. Rodríguez-Hernández, A. Muñoz, A. H. Romero, and J. González, J. Appl. Phys. **107**, 083506 (2010).
- [17] J. Ruiz-Fuertes, D. Errandonea, R. Lacomba-Perales, A. Segura, J. González, F. Rodríguez, F. J. Manjón, S. Ray, P. Rodríguez-Hernández, A. Muñoz, Zh. Zhu, and C. Y. Tu, Phys. Rev. B **81**, 224115 (2010).
- [18] R. Lacomba-Perales, D. Martínez-García, D. Errandonea, Y. Le Godec, J. Philippe, G. Le Marchand, J. C. Chervin, A. Polian, A. Muñoz, and J. López-Solano, Phys. Rev. 81, 144117 (2010).
- [19] A. Dewaele, F. Datchi, P. Loubeyre, and M. Mezouar, Phys. Rev. B 77, 094106 (2008).
- [20] T. J. B. Holland and S. A. T. Redfern, Miner. Magazine **61**, 65 (1997).
- [21] A. Boultif and D. Louer, J. Appl. Cryst. 37, 724 (2004).
- [22] A.C. Larson and R.B. Von Dreele, General Structure Analysis System (GSAS), Los Alamos National Laboratory Report LAUR 86-748 (2000).
- [23] R. Dovesi, V. R. Saunders, C. Roetti, R. Orlando, C. M. Zicovich-Wilson, F. Pascale, B. Civalleri, K. Doll, N. M. Harrison, I. J. Bush, Ph. D'Arco and M. Llunell, CRYSTAL09 User's Manual (University of Torino, 2009).
- [24] A. Becke, J. Chem. Phys. 98, 5648 (1993).
- [25] C. Lee, W. Yang, and R. Parr, Phys. Rev. B 37, 785 (1988).
- [26] C. H. Hu and D. P. Chong, Encyclopedia of Computational Chemistry (Wiley, Chichester, 1998).

- [27] M. A. Blanco, E. Francisco, and V. Luaña, Comput. Phys. Commun. 158, 57 (2004).
- [28] H. J. Berthold, J. M. Molepo, and R. Wartchow, Z. Kristallogr. 144, 116 (1976).
- [29] K. Herrmann and W. Ilge, Z. Kristallogr. 75, 41 (1930).
- [30] M. Miyake, I. Minato, H. Morikawa, and S. I. Iwai, Am. Mineral. 63, 506 (1978).
- [31] G. B. Johansson and O. Lindqvist, Acta Crystallogr. B 33, 2918 (1977).
- [32] S. D. Jacobsen, J. R. Smyth, and R. J. Swope, Can. Mineral. 36, 1053 (1998).
- [33] F. Birch, J. Geophys. Res. **83**, 1257 (1978).
- [34] R. Lacomba-Perales, D. Errandonea, D. Martínez-García, P. Rodríguez-Hernández,
- S. Radescu, A. Mújica, A. Muñoz, J. C. Chervin, and A. Polian, Phys. Rev. B 79, 094105 (2009).
- [35] D. Errandonea, C. Ferrer Roca, D. Martinez-Garcia, A. Segura, O. GOmis, A. Muñoz, P. Rodriguez-Hernandez, J. Lopez-Solano, S. Alconchel, and F. Sapiña, Phys. Rev. B 82, 174105 (2010).
- [36] D. Errandonea, R. Kumar, J. López-Solano, P. Rodríguez-Hernández, A. Muñoz, M. G. Rabie and R. Sáez-Puche, Phys. Rev B 83, 134109 (2011).
- [37] M. O'Keeffe, B. G. Hyde, Struc. Bond. 61, 77 (1985).
- [38] A.Vegas, Crystallogr. Rev. 7, 189 (2000).
- [39] A. Vegas and M. Jansen, Acta Crystallogr. Section B 58, 38 (2002).
- [40] C. Moriyoshi, T. Fujii, K. Itoh and M. Komukae, Ferroelectrics 269, 273 (2002).
- [41] W. Ludwig, R. Wartchow and H. J. Berthold, Z. Kristallogr. 175, 283 (1986).
- [42] L. A. Martínez-Cruz, A. Ramos and A. Vegas, J. Solid State Chem. 110, 397 (1994).
- [43] D. Errandonea and F. J. Manjon, Mater. Res. Bull 44, 807 (2009).

- [44] V. Panchal, F. J. Manjon, D. Errandonea, P. Rodriguez-Hernandez, J. Lopez-Solano, A. Muñoz, S. N. Achary, and A. K. Tyagi, Phys. Rev. 83, 064111 (2011).
- [45] T. Huang, S. Shieh, A. Akhmetov, X. Liu, C.M. Lin and J.S. Lee, Phys. Rev. B 81 214117 (2010).
- [46] D. Santamaria-Perez, L. Gracia, G. Garbarino, A. Beltrán, R. Chuliá-Jordán, O. Gomis, D. Errandonea, Ch. Ferrer-Roca, D. Martínez-García, and A. Segura, Phys. Rev. B **84**, (2011).
- [47] Y.H. Chen, E. Huang and S. C. Yu, Solid State Comm. 149, 2050 (2009).
- [48] A. Vegas and V. García-Baonza, Acta Crystallogr. B 63, 339 (2007).
- [49] H. P. Beck and G. Lederer, Z. Anorg. Allg. Chem. 619, 897 (1993).
- [50] S. Hull and D. A. Keen, Phys. Rev. B **59**, 750 (1999).
- [51] K. Kusaba, Y. Syono, T. Kikegawa and O. Shimomura, J. Phys Chem. Solids **56**, 751 (1995).
- [52] V.A. Barinov, G. A. Dorofeef, L. V. Ovechkin, E.P. Elsukov and A.E. Ermakov, Phys. Status Solidi A **123**, 527 (1991).

Table I: Unit-cell parameters and atomic coordinates for AgClO₄ obtained from powder diffraction at RT.

a = 4.976(3) Å and $c = 6.746(4)$ Å; $V = 167.0(3)$ Å ³ ; $Z = 2$							
Atom	Site	X	у	Z			
Ag	2b	0	0	0.5			
Cl	2a	0	0	0			
О	8i	0.1645(9)	0.1645(9)	0.1341(9)			

Table II: Unit-cell parameters and atomic coordinates for barite-type AgClO₄ obtained from experiments at 5.1 GPa.

$a = 8.214(8) \text{ Å}, b = 5.160(5) \text{ Å}, \text{ and } c = 6.651(6) \text{ Å}; V = 281.9(8) \text{ Å}^3; Z = 4$							
Atom	Site	X	у	Z			
Ag	4c	0.1822(2)	0.25	0.3345(3)			
C1	4c	0.0697(1)	0.25	0.8122(9)			
O	4c	0.1902(2)	0.25	0.9503(9)			
O	8d	0.4033(4)	0.5433(4)	0.1961(2)			
О	4c	0.4253(4)	0.25	0.5901(5)			

Table III: Calculated parameters and atomic coordinates for different phases of AgClO₄. (top) low-pressure phase at ambient pressure, (center) barite phase at 5.4 GPa, (bottom) high-pressure monoclinic phase at 21.4 GPa.

$a = 5.091 \text{ Å and } c = 6.944 \text{ Å}; V = 180.0 \text{ Å}^3; Z = 2$								
Atom	Site	X	у	Z				
Ag	2b	0	0	0.5				
Cl	2a	0	0					
O	8i	0.1829	0.1829	0.1416				
$a = 7.934 \text{ Å}, b = 5.473, \text{ and } c = 7.139 \text{ Å}; V = 310.0\text{Å}^3; Z = 4$								
Atom	Site	X	y	Z				
Ag	4c	0.1823	0.25	0.2958				
Cl	4c	0.0660	0.25	0.8130				
O	4c	0.2351	0.9409					
O	8d	0.4295	0.5080	0.1768				
O	4c	0.3971	0.25	0.5597				
$a = 6.201 \text{ Å}, b = 4.953 \text{ Å}, \text{ and } c = 4.535 \text{ Å}, \beta = 111.02 \text{ °}; V = 130.0 \text{ Å}^3; Z = 2$								
Atom	Site	X	у	Z				
Ag	2e	0.2494	0.25	0.9453				
C1	2e	0.2657	0.4617					
O	2e	0.4983	0.75 0.3881					
O	2e	0.3424	0.8503					
O	4f	0.1107						

Table IV: Calculated phonon frequencies (cm⁻¹), pressure coefficients (cm⁻¹/GPa), and Grüneisen parameters for different phases of AgClO₄. Low-pressure phase at ambient pressure, barite phase at 5.4 GPa, and high-pressure monoclinic phase at 17.2 GPa.

Tetragonal			Orthorhombic				Monoclinic				
Mode	ω	δω/δΡ	γ	Mode	ω	δω/δΡ	γ	Mode	ω	δω/δΡ	γ
E	11.5	0.28	0.66	B_{Ig}	11.0	0.43	1.56	B_g	59.5	1.89	3.05
B_2	35.4	0.35	0.27	A_g	39.2	1.42	1.75	A_g	85.6	2.55	2.65
E	63.8	-3.86	-1.63	A_g	60.8	3.61	4.02	B_{g}	92.4	2.38	2.01
B_2	107.3	5.65	1.42	B_{2g}	33.1	0.85	0.86	A_g	104.4	2.37	1.61
E	182.6	7.97	1.18	B_{3g}	52.2	0.33	0.24	A_{g}	174.4	4.02	1.66
B_I	251.5	-1.07	-0.11	B_{2g}	60.7	1.85	1.26	B_g	217.1	6.01	2.30
A_{I}	339.1	3.26	0.26	B_{Ig}	84.2	1.62	0.69	B_g	254.0	6.42	1.94
E	357.0	-0.02	0.00	A_g	115.4	3.14	1.22	A_{g}	238.3	5.34	1.58
B_2	408.7	1.77	0.12	B_{2g}	113.2	3.63	1.41	A_g	289.6	5.87	1.35
A_I	586.7	1.93	0.09	B_{Ig}	111.3	3.26	1.25	B_{g}	348.7	3.69	0.56
E	699.3	1.87	0.07	B_{3g}	114.0	2.17	0.79	A_g	335.9	1.75	0.25
B_2	718.2	2.56	0.10	B_{2g}	125.1	3.10	1.09	A_g	391.1	0.97	0.11
				B_{3g}	140.0	4.21	1.42	B_g	416.9	2.40	0.28
				B_{Ig}	150.5	5.72	1.88	A_{g}	429.2	0.81	0.09
				A_g	155.0	5.30	1.63	A_g	584.5	0.13	0.01
				B_{3g}	168.7	6.00	1.70	A_g	702.9	0.72	0.05
				B_{3g}	172.3	4.60	1.13	B_g	801.1	4.10	0.24
				A_g	194.8	5.84	1.33	A_g	811.8	1.87	0.10
				B_{3g}	283.8	1.36	0.18				
				B_{Ig}	286.1	0.99	0.13				
				A_g	293.3	1.42	0.18				
				B_{2g}	307.6	1.32	0.16				
				A_g	369.5	-0.41	-0.04				
				B_{Ig}	375.8	0.23	0.02				
				B_{2g}	382.3	0.49	0.05				
				B_{3g}	386.6	0.86	0.08				
				A_g	393.5	0.77	0.07				
				B_{3g}	406.3	0.65	0.06				
				B_{3g}	609.9	2.53	0.16				
				A_g	614.5	2.84	0.18				
				B_{2g}	710.1	4.37	0.24				
				B_{Ig}	718.0	4.42	0.24				
				A_g	734.3	4.27	0.22				
				B_{3g}	776.3	4.20	0.21				
				A_g	758.8	0.36	0.02				
				B_{3g}	784.6	1.92	0.09				

Figure captions

Figure 1: (Color online). Different structures of AgClO₄: (a) ambient pressure tetragonal structure, (b) barite-type, and (c) high-pressure monoclinic. Different polyhedra are shown. Ag: large grey spheres, Cl: medium green spheres, and O: small red spheres.

Figure 2: Selection of X-ray diffraction patterns. Pressures are indicated. (r) indicates the pattern collected after pressure release. Neon peaks are shown identified with asterisks. Background was subtracted. In the pattern collected at 5.1 the dots represent the experiment and the solid line the calculated diffraction pattern. The residuals of the refinement are also shown.

Figure 3: Pressure evolution of unit-cell parameters and volume of AgClO₄. In the upper part the lines are a guide to the eye, in the lower part they represent the obtained EOS. For the barite-type phase we plotted V/2 to facilitate comparison. Squares: experiments. Circles: calculations.

Figure 4: (Color online) Total energy as a function of volume per formula unit for the tetragonal structure, barite-type and high-pressure monoclinic.

Figure 5: Pressure evolution of Ag-O (squares) and Cl-O (circles) distances for the different phases of AgClO₄. Empty symbols: tetragonal structure, solid symbols: baritetype, and gray symbols high-pressure monoclinic

Figure 6: (color online) (a) tetragonal structure (**M2m**) of AgClO₄ at ambient conditions (a = 4.976 and c = 6.746 Å). (b) rock-salt structure (**F45m**) of AgCl at ambient conditions (a = 5.55 Å). Ag (grey), Cl (green), and O (red).

Figure 7: (color online) (a) barite-type structure of AgClO₄ (*Pnma*) viewed along *b*. The trigonal prism centering the cell in (a) has been magnified in (b) to outline the complete coordination polyhedron. Ag (grey), Cl (green), and O (red). The Ag-Ag contacts are drawn with blue lines. (c) The structure of the FeB alloy, projected on the same plane, to show its similarity with the cation array of AgClO₄. Fe-green, B-yellow.

Figure 8: (color online) Sequence of structures of AgCl by increasing pressure. (a) ambient pressure rock-salt AgCl structure. (b) high-pressure $P2_1$ /m phase also called AgCl-II. (c) B33 structure assigned to CrB- and TlI-type. (d) Alternative description of the AgCl-II structure viewed as a distortion of the B33 structure drawn in (b). (e) The same as in (d) but out of plane to show the trigonal prisms of Cl atoms centered by the Ag atoms. (f) B33 structure rotated 90° around the b axis to show its similarities with the AgCl-II. (g) B2 (CsCl-type) structure of AgCl.

Figure 9: (color online) (a) Coordination polyhedron around the B atom in the B33 phase of FeB. (b) The same polyhedron formed by Ag atoms around the ClO₄ group in barite-type AgClO₄. (c) Fragment of the barite-type structure projected onto the (3 0 1) plane showing its similarity with the HP B33 structure of AgCl–III, represented in (d).

Figure 10: (color online) (a) The anti-structure of AgCl-III (*B*33), viewed along *a*. Ag atoms (grey) are connected with red lines to show the trigonal prisms occupied by Cl atoms (green). Compare with Fig. 9c. (b) The same structure, viewed along the *c* axis, showing how that Cl atoms are slightly out of the trigonal prisms. Compare with Fig. 9f. (c) The structure of monoclinic AgCl-II, viewed along the *b* axis. Both structure and anti-structure have been drawn with red and blue lines, respectively. Note that the red network is the same as that drawn in Fig. 9d. The blue lattice shows that the Cl atoms are slightly out of the horizontal trigonal prisms but inserted into the vertical trigonal prisms.

Figure 11: (color online) (a) HP structure of AgClO₄ predicted by calculations. It is monoclinic (*P*2₁/m) and isostructural to RbD₂PO₄. The Ag atoms (grey) form a distorted simple-cubic array centered by the ClO₄ groups [Cl (green) and O (red)]. (b) An isolated Ag₈ cube showing the distorted CsCl-type structure formed by the AgCl subarray. (c) The cubic HT-phase of AgClO₃ showing the CsCl-type structure. Colors as in (a).

Figure 1

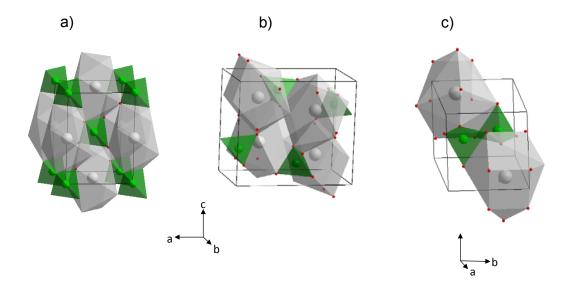


Figure 2

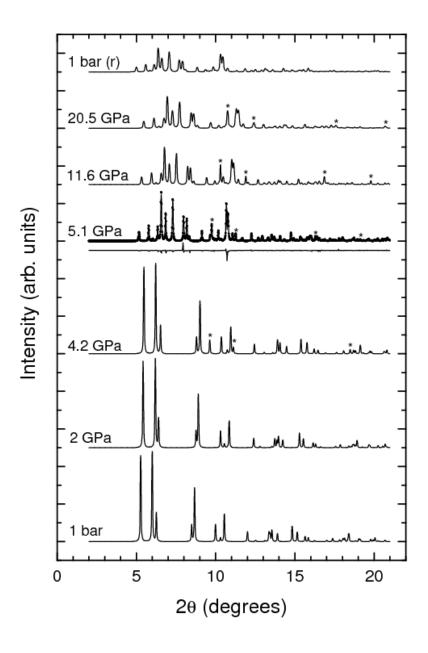


Figure 3

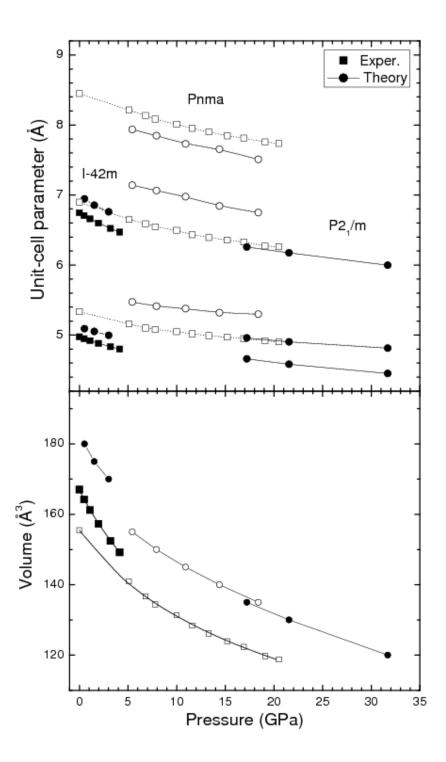


Figure 4

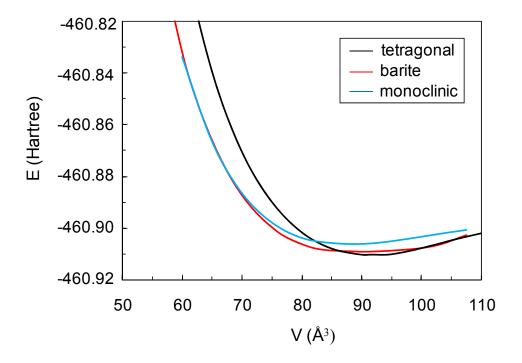


Figure 5

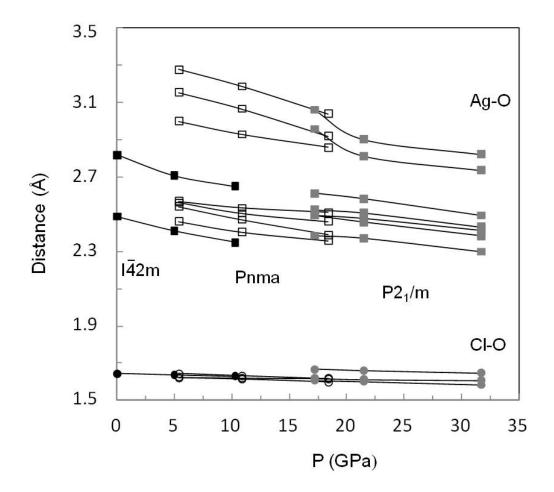


Figure 6

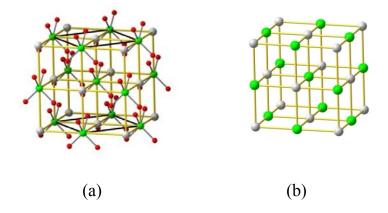


Figure 7

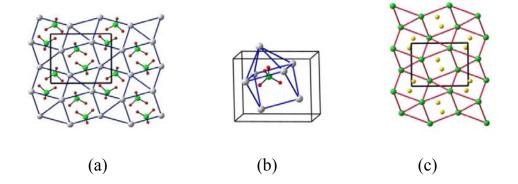


Figure 8

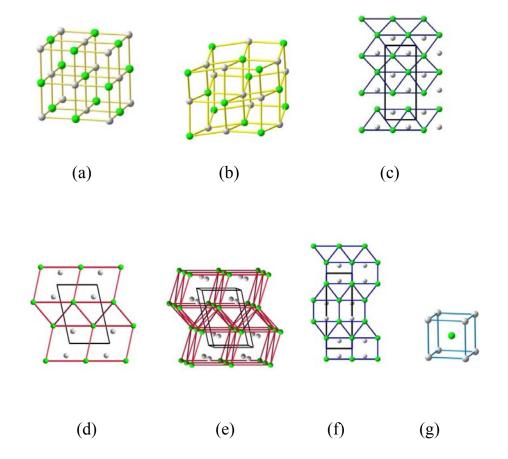


Figure 9

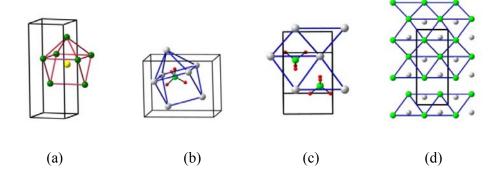


Figure 10

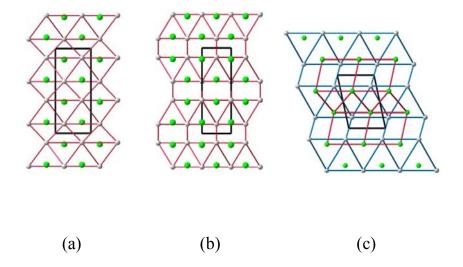


Figure 11

