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Evidence for Spin Mixing in Holmium Thin Film and Crystal Samples

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Abstract

In a number of recent experiments, holmium has been shown to promote spin triplet pairing when in proximity to a spin singlet superconductor. The condition for the support of spin triplet pairing is that the ferromagnet should have an inhomogeneous magnetic state at the interface with the superconductor. Here we use Andreev reflection spectroscopy to study the properties of single ferromagnet/superconductor interfaces formed of holmium and niobium, as a function of the contact resistance of the junction between them. We find that both single crystal and c-axis oriented thin film holmium show unusual behavior for low junction contact resistance, characteristic of spin mixing type properties, which are thought necessary to underpin spin triplet formation. We also explore whether this signature is observed when the junction is formed of Ni₁₉Pd₈₁ and niobium.

Introduction

At a superconductor/ferromagnet (S/F) junction conventional spin-singlet Cooper pairs penetrating into the ferromagnet will decay over a length of the order of $\xi_F = \sqrt{\frac{\hbar D_F}{E_{ex}}}$ due to destruction of the Cooper pair coherence as a result of the exchange field of the ferromagnet ¹ (where D_F is the diffusion coefficient and E_{ex} is the exchange energy in the ferromagnet ^{2, 3}). In strong ferromagnets E_{ex} is large and ξ_F is of the order of ~1 nm at low temperature ; however, theories have emerged recently suggesting the existence of a novel proximity effect where spin-triplet pairing is generated at the S/F interface resulting in a greatly extended decay length, $\xi_T \gg \xi_F$. This exotic proximity effect named "the long range spin triplet proximity effect" (LRSTPE)^{4,5} only exists if either some form of inhomogeneous magnetization is present at the S/F interface or if there is a spin active region (such as spin scattering in a strong spin orbit coupled medium) between the S and F layers^{4,5}. Current thinking suggests that the inhomogeneous magnetic state could either be provided by a magnetic system that offers intrinsic inhomogeneity due to a non co-linear spin arrangement or could be artificially created in a number of ways including the presence of domain walls (although domain wall density may prove an issue), or through a thin film multilayer arrangement using different types of ferromagnets⁶. Either way spin mixing must occur close to the interface with the interrogating superconductor.

It has been suggested that holmium (Ho) could provide the necessary magnetic inhomogeneity to induce the LRSTPE due to the intrinsically non-linear cone structure of its ordered magnetic moments ⁷. Indeed, two recent experiments report evidence for triplet pairing promoted by Ho^{8,9}. Sosnin *et al.* used Andreev interferometry to measure phaseperiodic conductance oscillations in Ho which formed the barrier of a Al/Ho/Al ring structure ⁸, whilst Robinson *et al.* measured the critical current behavior of Nb/Ho/Co/Ho/Nb junctions ⁹. Both experiments varied the thickness of the F layers (Ho and Co, respectively) and observed supercurrent signatures with thicknesses much greater than ξ_F .

Evidence for the LRSTPE has also been observed in other systems, including: Pd_{0.88}Ni_{0.12} and Pd_{0.987}Fe_{0.013} coupled to Co in S/F1/N/F2/N/F1/S-type junctions ²; Co nanowires with W superconducting leads ¹⁰; and CrO₂, a half-metallic oxide coupled to NbTi or MoGe superconducting leads ^{11, 12}. In these systems the origin of LRSTPE is more likely to be related to artificially created inhomogeneity, either through the difference in spin scattering generated by the choice of thin films in the multilayer stack or though the particular arrangement that a polycrystalline random alignment of grains may present to the superconducting interface. Reviewing these experimental results shows that there is a great deal more to be learnt in this new emerging field and, as predicted theoretically, the induced spin triplet pairing is intimately linked to the properties of the interface. In view of the current status of the field it seems essential to examine the transport across S/F interfaces in more detail so that nature of the spin-singlet to spin-triplet conversion process can be better understood and possibly even controlled.

For any single S/F interface theory tells us that the conductance across the interface plays a pivotal role in determining whether the conventional even-frequency singlet ¹³ proximity component or the odd frequency triplet ⁴ LRSTPE dominates ^{14, 15}. This balance between the singlet and triplet components is due to the competition between the effect of increasing spin-mixing (which acts to destroy singlet pairing) and increasing junction transparency (which acts to provide a higher proportion of singlet Cooper pairs from the superconductor).

Consequently, for constant, but sufficient, spin mixing conditions, lower junction transparency (higher interface resistance) should promote the LRSTPE phase whilst for cleaner junctions (low interface resistance) singlet pairing will dominate. Point contact Andreev reflection (PCAR) offers a potentially ideal probe as the conductance of the contact (and therefore the S/F interface resistance) can be controlled by varying the pressure on the tip-sample contact. In this paper we examine the properties of single S/F interfaces, primarily those formed between Nb and Ho, and use Andreev spectroscopy to extract details on how the properties of the interface change as the interface transparency is varied. We compare the Nb/Ho results to those obtained from junctions formed between Nb and a $Ni_{19}Pd_{81}$ thin film.

Experimental

Holmium is a rare earth metal with a complex magnetic phase diagram ^{16, 17}. As the temperature is reduced from room temperature, Ho first undergoes a transition to a spin-spiral antiferromagnetic (AFM) state with a Néel temperature of $T_N \sim 133$ K ¹⁶. In a previous study it was shown using polarised X-ray Bragg diffraction that there were domains of different chirality in the AFM state of a Ho single crystal ¹⁸. Below 19 K (the Curie temperature, T_C) there is a transition to a weak ferromagnetic alignment with a cone-like structure where the cone axis lies along the crystallographic c-axis in zero applied magnetic field (see illustration in the inset to Fig. 1(b)).

The Ho single crystal studied here was $(2.44 \times 1.82 \times 0.9)$ mm in size and was grown at the Ames Laboratory using strain annealing ¹⁹. The 300nm thick Ho thin film was prepared in a UHV system by dc magnetron sputtering onto a 200nm thick Nb buffer on \sim (5 × 5) mm area heated (~873K) c-plane sapphire. The Ho target was pre-sputtered for 15 minutes prior to film growth and the system's base pressure was better than 10⁻⁸ Pa. The films are epitaxial and c-axis oriented as determined by X-ray diffraction. The total Ho thin film thickness was determined by low angle X-ray diffraction and by fitting the period of the Kiessig fringes using simulation software. The films were capped with a 10nm protective layer of gold to prevent surface oxidation. A number of polycrystalline Ni₁₉Pd₈₁ thin films (108 nm) were also prepared for comparative measurements. These films were grown by sputterdeposition in a UHV chamber on a Si substrate, as described previously ²⁰. The Ni₁₉Pd₈₁ films have a Curie temperature of 230K determined from magnetometry measurements and an easy axis out of the plane. The slightly higher Curie temperature in comparison to the earlier report²⁰ is probably due to a small change in the surface composition of the target. A copper film prepared by sputtering was used as a benchmark to show how the extracted parameters vary with tip pressure for a non magnetic film.

PCAR measurements were taken at 4.2K using superconducting tips that were mechanically cut from 0.25mm diameter Nb wire ²¹. Spectra were also taken using platinum tips to identify non-superconductivity related components to the "background" conductance

spectra ²². All measurements were performed with the tip aligned parallel to the c-axis of the Ho crystal or Ho thin film, which is the ideal crystallographic direction as it lies along the spin cone axis [see inset to Fig 1(b)]. The tip-sample distance was controlled by a stepper-motor connected to a differential screw such that systematic measurements could be made as a function of contact pressure. In addition to PCAR measurements, the surfaces of the Ho single crystal and thin film were scanned using a Hall probe ²³ to identify any variation in the magnetic properties between the crystal and the thin film.

The Andreev spectra were fitted as described previously ²¹ using the Blonder-Tinkham-Klapwijk (BTK) equations modified for spin polarization by Mazin *et al.*, ^{24, 25}. Spectra were fitted for the polarization, P, the dimensionless parameter Z, which incorporates the interface scattering and a smearing parameter, ω , which accounts for both thermal and inelastic broadening effects. As any effect of the LRSTPE on the conductance spectra is expected to be subtle, the spectra were fitted using a fixed value for the gap voltage of Δ = 1.5 meV, i.e. the Nb gap value at low temperature ²⁶. Restricting the fitting routine to a three parameter fit ensured that the fitting was robust and that any error introduced by the fitting procedure was systematic across the series. It is usual to define the contact resistance of a junction at zero bias, R_{C0} . However, as the interface properties change drastically with tip pressure, we have extracted the 30mV resistance at each junction (R_{CB}), and use this value to define the contact resistance.

Results

Fig. 1 shows the scanning Hall probe images of the out-of-plane magnetic moment in the single crystal oriented in the c-axis and in zero applied magnetic field. The noise floor of the 5 micron Hall probe used was ~ 0.3μ V with a 7.7mV/T sensitivity. While the crystal shows a considerable moment directed along the c-axis [Fig. 1(a)], the signal from the film (which has approximately three orders of magnitude smaller volume) is below the noise floor of the Hall probe sensor [Fig. 1(b)]. We show the results on the film for completeness. The line scans taken across the centre of both samples are shown in the top frames in Fig. 1(a) and 1(b). Although it is not possible to determine the chiral sense of the domains with the scanning Hall probe, the size and distribution of the domains indicated in Fig. 1(a) are consistent with (and remarkably similar to) the chiral domain structures in the AFM state observed using circularly polarized X-rays by Lang *et al.* [2].

The evolution of the PCAR spectra with contact resistance (R_{CB}) for the Ho single crystal and Ho thin film are shown in Fig. 2(a) and 2(d) respectively. The data for the Ni₁₉Pd₈₁ film is shown in figure 2(f). The high bias dips on the spectra have been associated with the critical current being exceeded in the contact region ²⁷. In order to fit the data, the spectra for the single crystal were normalized to the conductance spectra obtained using a nonsuperconducting Pt tip, as shown in Fig. 2(b). For the crystal, the background conductance

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was typically 'V' shaped using either the Pt or Nb tip and because of the similarity of this feature, we were able to normalize the spectra taken with the Nb tip using the Pt tip spectra as shown in Fig. 2(c). Compared to the crystal, the background spectra obtained on the film were consistently featureless and flat which meant that the spectra could be normalized by the high bias conductance value directly (Fig. 2e). The fitted spectra generated using the Mazin model are shown in Fig. 2(c), and (e) for the crystal and film, respectively and Fig. 2(g) for the Ni₁₉Pd₈₁ film.

Fitting to the spectra shown in Fig. 2 allows the extraction of the polarization P and (dimensionless) interface parameter Z and the relationship between P and Z for crystal and film are shown in Fig. 3(a) and 3(b) respectively. The P–Z relationship of an S/F interface always takes a similar form in that high P is associated with low Z and vice versa and the origin of this dependence has been widely discussed in the literature ²⁸⁻³². The 'intrinsic' polarization is usually obtained by extrapolating a P–Z plot to low Z - although not usually to $Z = 0^{29}$ because Z also includes the effect of Fermi velocity mismatch between the S/F materials ³³. The trends we find for the P–Z relationship are not unusual in this respect. However, when we show the explicit relationship of P and Z with the contact resistance, R_{CB} , of the junction, it becomes clear that the P–Z plot masks a much less obvious relationship.

Fig. 4(a, b) shows the behavior of three separate contacts made to the single crystal and Fig. 4 (c, d) shows the equivalent for two separate contacts made to the thin film. Both sets of spectra change in an unusual way with increased tip pressure. In both types of sample, as tip pressure is increased (decreasing R_{CB}), Z increases anomalously and sharply, and P shows a corresponding precipitous drop. By direct examination of the spectra shown in Fig. 2, it is clear that the sharpening of spectral features as R_{CB} drops indicate that the effective interface barrier is increasing. This is most clear in Fig. 2(a), the series of spectra taken on the Ho crystal. We are confident that these changes to the Z and P parameters are real (i.e. not an artifact of the fitting process). Futhermore, in case of the crystal, the data for $P(R_{CB})$ and $Z(R_{CB})$ show a 'dome'-like and a dip-like non-monotonic dependence. We make this more clear in Fig.4a,b by plotting P, Z as function of $R_{CB}/R_{CB-Peak}$, where $R_{CB-Peak}$ is the value of R_{CB} at the peak in the polarization. For the film, the peak in polarization or dip in Zvalue is not observed [Fig. 4(c)]. Instead, at higher, R_{CB} , the polarization is constant then starts to decrease with decreasing R_{CB} . The differences between the Ho film and crystal are subtle, they have in common that both show the anomalous rise in Z and drop in P at high tip pressure.

In order to show how anomalous this behaviour is, we show the equivalent P and Z behaviour when a Nb tip is pressed into a copper foil, or for a Nb tip on a Ni_{0.19}Pd_{0.81} film, plotted in Fig.4c,d In the case of Cu, Z decreases slightly as R_{CB} is reduced owing to the increasing transparency of the tip-sample interface²¹ (for Cu, P = 0%). In the case of Ni_{0.19}Pd_{0.81}, hardly a change in P or Z is found. Note that the difference in behaviour of Z in

the Ho cannot be explained purely by an increase in the smearing parameter with decreasing contact resistance as both the Ho crystal and the Cu sample show the same trend of decreased smearing as the contact resistance is reduced²⁸.

Before drawing any definitive conclusion, it is also important to try to eliminate any artificial trend in P and Z in the case of the Nb/Ho contact due to the effects of stray magnetic fields on tip properties³¹. In order to examine this in more detail we have taken the spectrum at the onset to the anomalous rise in Z (and precipitous drop in P) and modelled the effect on this spectrum of the presence of an external magnetic field. We do this by using a model we developed previously called "the two channel model", which we have shown simulates the effect of a magnetic field on the tip properties up to a field of about 80% of the upper critical field , H_{C2} , of the Nb tip (i.e., $h = H/H_{C2} = 0.8$). The results of this simulation are shown in the inset to Fig. 3(a) up to h = 0.3. The plots show that if the effect of increasing tip pressure was simply to experience an increasing magnetic field, P would increase and Z would decrease. This is opposite to the observations that we have made in the main plots of Fig. 4 and therefore we can rule out any possible effects from stray fields. The apparent increase in the Z parameter as the contact resistance drops indeed appears to be a real and anomalous effect. We suggest that it is indicative of a novel form of spin scattering which also results in a reduced P.

Discussion

Theoretical calculations of the expected Andreev conductance spectra in the presence of the LRSTPE ³⁴⁻³⁷ indicate that spin mixing at the S/F interface leads to an enhancement of the sub-gap conductance, either via a direct increase in the conductance ³⁴ or via the formation of Andreev bound states ³⁶. A number of experimental reports have shown possible signatures of the LRSTPE ³⁸⁻⁴⁰, although it remains to be determined what the 'signature' of the LRSTPE is in the Andreev reflection spectra. It is clear, however, from both theoretical and experimental works that if the LRSTPE can be reliably turned 'on' and 'off', changes should be observed in the parameters used to *fit* the spectra that indicate the sub-gap conductance, i.e. P and Z. Although we see clear changes in P and Z with *R_{CB}*, we do not see any evidence of a sub-gap structure in the spectra (Fig. 2). However the magnitude of the sub-gap conductance expected as a result of spin-mixing or the LRSTPE may be below the resolution of the spectra shown ⁴¹⁻⁴³. The changes in P and Z suggest that the scattering mechanism probed by the PCAR, at low *R_{CB}* is an indication of spin-mixing that is the precursor to the LRSTPE (i.e. P is reduced as the scattering increases).

The dependence of P, $Z(R_{CB})$ can be understood qualitatively using a simple schematic, as shown in Fig. 5. The behavior of Z at high R_{CB} in the Ho crystal implies the existence of a surface layer, probably an oxide, as proposed for other systems ⁴⁴. For the crystal, as the Nb tip first approaches the Ho [Fig. 5(a)], the surface layer acts as a spin scattering layer resulting in a low P (and high Z) in the conventional way. As the tip is pushed further into the crystal surface [Fig. 5(b)], the Andreev reflection probes the spin alignment of the Ho with a Z parameter that is indicative of a clean interface and the observed P is maximal. Finally, as the tip goes through this surface layer completely [Fig. 5(c)], the spin-mixing of the Ho becomes dominant (Z increases) and so P is once again reduced. In the case of the film, the thin Au capping layer prevents the oxide from forming and so as the tip first approaches the capped film surface the intrinsic P of the Ho is preserved through the thin metallic capping layer and P is approximately constant with R_{CB} . Once the tip punctures the capping layer the intrinsic spin-mixing of the Ho results in the same high Z value and low P behavior as observed in the Ho crystal. The results indicate that at low R_c in both the crystal and the film spin-mixing occurs. Note that in PCAR R_{CB} can decrease either due to a cleaner interface or due to an increase in the physical size of the contact ^{30, 44}. This may explain why the effects observed here vary in magnitude between different contacts [for example the square and star datasets in Fig. 4(a)].

Fig. 4(c, d) also shows our first results on a 108nm thick $Ni_{0.19}Pd_{0.89}$ film. The spectra and fit to a spectrum are shown in Fig. 2(f) and 2(g). Interestingly, although reports that thin films (<4nm) of $Pd_{0.88}Ni_{0.12}$ promote triplet behavior ², here we see no significant anomalous upturn in Z as compared with Ho. However, this result is consistent with the view that whereas in Ho the spin triplet state is promoted by the intrinsic inhomogeneity of the spin state of the material, in the multilayer stack, the inhomogeneous magnetization has been created artificially and that a $Ni_{0.19}Pd_{0.89}$ film would not necessarily be expected to support proximity induced spin triplet behaviour in isolation. Our inference concerning NiPd agrees with the recent publication from the Birge group⁴⁵.

In conclusion, we have shown an anomalous dependence of the polarization P and the interface scattering parameter Z on contact resistance R_{CB} in the magnetically inhomogeneous system Ho, using point contact Andreev reflection spectroscopy. Similarities in the PCAR spectra taken on both single crystal and thin film Ho, suggest a common scattering mechanism. This scattering results in reduced polarization and strongly suggests increased spin mixing, a fundamental precursor to the LRSTPE effect. We do not see this effect when we perform the same experiments using copper foil or Ni_{0.19}Pd_{0.89} thin films.

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Figure Captions

FIG. 1. Hall images of a) single crystal and b) thin film Ho at zero field and 6K. Black regions represent negative induction and bright represent positive induction. Line scans across the centre of the images (white dashed lines) are shown in the top panels. Inset to (b) shows a schematic of the cone structure in Ho for T < 19K, dashed arrow corresponds to the direction of the c-axis and solid arrows represent the ferromagnetic vectors locked out-of-plane.

FIG. 2. Point contact Andreev reflection data at 4.2 K, C_N is the normalised conductance: (a) Normalised conductance spectra as a function of R_{CB} for the Ho crystal. (b) High R_{CB} spectrum taken with a Nb tip (black line) and with a Pt tip (grey line) for the Ho crystal. (c) Same spectrum as (b), but after normalisation and fitting (with fitted parameters $\Delta = 1.5 \text{meV}$, $\omega = 1.24 \text{meV}$, P = 19.5%, Z = 0.63). (d) Normalised conductance spectra as a function of R_{CB} for the Ho film. (e) Spectrum taken with a Nb tip shows a flatter background than in the crystal case, so can be fitted using the high bias conductance as shown (fitted parameters $\Delta = 1.5 \text{meV}$, $\omega = 1.18 \text{meV}$, P = 35.5%, Z = 0.32). (f) C_N as a function of R_{CB} for a Ni₁₉Pd₈₁ film. (g) Normalised spectrum and fit from the data set in (f) (with fitted parameters $\Delta = 1.5 \text{meV}$, $\omega = 0.72 \text{meV}$, P = 27.5%, Z = 0.41). The arrows in (a), (d) and (f) indicate decreasing contact resistance. All curves have been offset in the vertical scale for clarity.

FIG. 3. P(Z) relation on the Ho crystal (a) and Ho thin film (b), symbols represent different contacts. The inset to (a) is a simulation of the effects of increasing the normalised field $h = H/H_{C2}$ (where H_{C2} is the upper critical field of Nb) using the datum point associated with $R_{CB-peak}$ shown in Fig. 4(a).

FIG. 4. Dependence of P (a) and Z (b) for the Ho crystal as function of $R_{CB}/R_{CB-Peak}$, where $R_{CB-Peak}$ is the value of R_{CB} at the peak in the polarization with $R_{CB-Peak} = 20\Omega$, 39Ω and 41Ω for the squares, triangles and stars in Fig.4 (a, b), respectively. The dependence of P (c) and Z (d) on R_{CB} for the spectra taken on the Ho thin film (unfilled symbols), the Ni₁₉Pd₈₁ thin film (filled circles), and copper foil (cross symbols).

FIG. 5. Schematic illustrating the behaviour of P and Z as a function of tip pressure for a system with a surface scattering layer. Layer (1) is a thin surface oxide and layer (2) represents bulk Ho.



Figure 1, Usman et al.



Figure 2, Usman et al.



Figure 3, Usman et al.



Figure 4, Usman et al.



Figure 5. Usman et al.

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