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Resonance energy transfer near metal nanostructures mediated by surface plasmons

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We develop a unified theory of plasmon-assisted resonance energy transfer (RET) between molecules near a metal nanostructure that maintains energy balance between transfer, dissipation and radiation. We show that in a wide range of parameters, including in the *near field*, RET is dominated by *plasmon-enhanced radiative transfer* (PERT) rather than by nonradiative transfer mechanism. Our numerical calculations performed for molecules near Ag nanoparticle indicate that RET magnitude is highly sensitive to molecules positions.

I. INTRODUCTION

Resonance energy transfer (RET) between spatially separated molecules^{1,2} plays important role in diverse phenomena across physics, chemistry and biology. Examples include photosynthesis, exciton transfer in molecular aggregates, energy exchange between proteins^{3,4} and, more recently, between excitons in quantum dots (QD)⁵ and in QD-protein assemblies.⁶ During past decade, significant advances were made in RET enhancement and control by placing molecules or QDs in microcavities⁷⁻⁹ or near metal films and nanoparticles (NP).¹⁰⁻¹⁸ The coupling between molecular dipoles and surface plasmons (SP) in metal opens up new RET channels. The ability to control RET rates by adjusting dipoles positions relative to metal surface is important in biomedical applications¹⁹ such as, e.g., SP biosensors.²⁰

Near plasmonic nanostructure, RET from a donor to an acceptor is governed by the interplay between several processes. The energy of the excited donor can either be radiated, dissipated or absorbed by the acceptor and each of these channels is affected by the nearby metal in its own way. In a closely related phenomenon – plasmon-enhanced fluorescence – the decay rates in nonradiative and radiative channels depend differently on the distance between molecule and metal surface, d , and the measured fluorescence²⁵⁻²⁸ from molecules attached to a metal NP indeed shows that, with decreasing d , SP enhancement is followed by quenching, in agreement with theory.²¹⁻²⁴ A similar, albeit somewhat more complicated, scenario is expected when a donor and an acceptor are placed nearby a plasmonic nanostructure, i.e., the energy transfer from the donor to the acceptor should be strongly affected by dissipation in metal and by plasmon-enhanced radiation. However, no RET theory including all relevant energy flow channels has yet been available. It is our goal to provide such a theory here.

To highlight the issue, recall famous Förster's formula for energy W_{ad}^F transferred from donor to acceptor¹⁻⁴

$$\frac{W_{ad}^F}{W_d} = \frac{9}{8\pi} \int \frac{d\omega}{k^4} f_d(\omega) \sigma_a(\omega) |D_{ad}^0|^2, \quad (1)$$

where W_d is donor's radiated energy, $f_d(\omega)$ is its spectral function, $\sigma_a(\omega)$ is acceptor's absorption crosssection, D_{ad}^0

is dipoles electromagnetic coupling at distance r_{ad} and k is the wavevector of light. In the near field ($kr_{ad} \ll 1$), we have $D_{ad}^0 = q_{ad}/r_{ad}^3$ (q_{ad} is orientational factor) and RET changes with distance as $(r_F/r_{ad})^6$, where r_F is Förster's radius. In the far field ($kr_{ad} \gg 1$), RET is dominated by radiative coupling $|D_{ad}^0| \propto k^2/r_{ad}$ leading to weaker r_{ad}^{-2} dependence.^{4,29} Eq. (1) is derived from *first-order* transition probability under the perturbation D_{ad}^0 .

For molecules near a plasmonic nanostructure, Eq. (1) must be modified. The standard model by Gersten and Nitzan^{30,31} and its extension to planar and composite systems³²⁻³⁴ includes SP into transition's intermediate states and so Eq. (1) holds with new coupling D_{ad} which now includes SP channels. However, this model accounts for neither dissipation in metal nor plasmon-enhanced radiation channels and, as a result, yields enormous (up to 10⁵) RET enhancement that contrasts sharply with the much more modest (~ 10) increase^{11-14,16-18} and even reduction^{10,15} of measured RET rates.

Here we present a unified theory for RET near metal nanostructures based on classical approach that accounts accurately for the full energy flow in the system. We show that Eq. (1) is replaced with

$$\frac{W_{ad}}{W_d} = \frac{9}{8\pi} \int \frac{d\omega}{k^4} \frac{\gamma_d^r}{\Gamma_d(\omega)} \tilde{f}_d(\omega) \tilde{\sigma}_a(\omega) |\tilde{D}_{da}(\omega)|^2, \quad (2)$$

where γ_d^r is donor's *free space* radiative decay rate, Γ_d is its *full* decay rate, \tilde{f}_d and $\tilde{\sigma}_a$ are modified spectral function and absorption crosssection, respectively, and the coupling \tilde{D}_{da} includes high-order SP-assisted transitions. For a low-yield donor, γ_d^r should be replaced with free space fluorescence rate γ_d . We also identify *plasmon-enhanced radiative transfer* (PERT) as dominant RET mechanism in a wide parameter range. In the *far field*, we extract from Eq. (2) a general formula for PERT from remote donors to an acceptor near metal surface that extends radiative RET theory^{4,29} to plasmonic systems. In the *near field*, our numerical calculations of RET near Ag NP (see inset in Fig. 1) show that PERT is dominant mechanism here as well. Depending on system geometry, RET can either be enhanced or reduced as compared to Förster's transfer, consistent with experiment.¹⁰⁻¹⁸

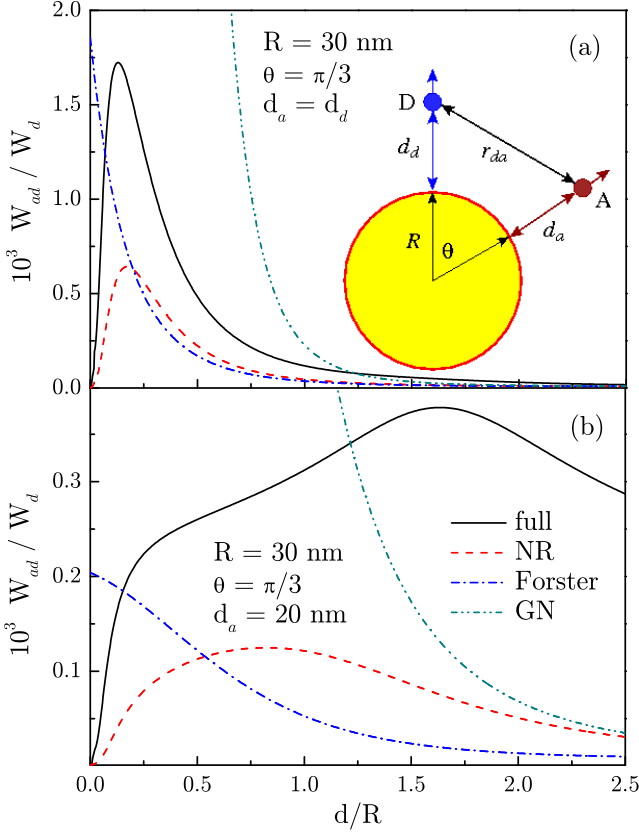


FIG. 1: (Color online) RET vs. distance for $R = 30$ nm Ag NP is shown at $\theta = \pi/3$ with (a) $d_a = d_d = d$ and (b) $d_a = 20$ nm $d_d = d$ using full Eq. (2), non-radiative (NR) channel only, Förster's transfer Eq. (1) and Gersten-Nitzan (GN) model.^{30,31}

II. THEORY OF PLASMON-ASSISTED RESONANCE ENERGY TRANSFER

We consider a donor and an acceptor near the surface of a metal nanostructure which are represented by point-like dipoles located at \mathbf{r}_j with induced moments $\mathbf{p}_j(\omega) = p_j(\omega)\mathbf{e}_j$ oriented along \mathbf{e}_j ($j = a, d$). The dipoles are driven by the common electric field,

$$\mathbf{p}_j(\omega) = \alpha_j(\omega)\mathbf{E}(\mathbf{r}_j, \omega) + \delta_{jd}\mathbf{p}_d^0(\omega), \quad (3)$$

where $\alpha_j(\omega) = \alpha'_j(\omega) + i\alpha''_j(\omega)$ is complex polarizability assumed here isotropic, $\mathbf{p}_d^0(\omega) = \alpha_d(\omega)\mathbf{e}_d E_0$ is donor's initial dipole moment with some constant E_0 depending on excitation, and δ_{jk} is Kroniker's symbol. The electric field \mathbf{E} is, in turn, the solution of Maxwell's equation with dipole sources³⁵

$$\mathbf{E}(\mathbf{r}, \omega) = \frac{4\pi\omega^2}{c^2} \sum_j \mathbf{G}(\mathbf{r}, \mathbf{r}_j; \omega) \cdot \mathbf{p}_j(\omega), \quad (4)$$

where $\mathbf{G}(\mathbf{r}, \mathbf{r}'; \omega)$ is Maxwell's equation Green's dyadic, satisfying $\nabla \times \nabla \times \hat{\mathbf{G}} - \epsilon(\mathbf{r}, \omega)(\omega/c)^2 \hat{\mathbf{G}} = \hat{\mathbf{I}}$, and $\epsilon(\mathbf{r}, \omega)$

equals metal permittivity, $\epsilon(\omega)$, inside the metal region and that of outside medium, ϵ_0 , otherwise. The quantity of interest is energy absorbed by the acceptor in unit frequency interval,

$$\frac{dW_{ad}}{d\omega} = -\frac{\omega}{\pi} \text{Im} [\mathbf{p}_a^*(\omega) \cdot \mathbf{E}(\mathbf{r}_a, \omega)] = \frac{\omega\alpha_a''}{\pi} \left| \frac{p_a}{\alpha_a} \right|^2, \quad (5)$$

where we used $\mathbf{E}(\mathbf{r}_a, \omega) = \mathbf{p}_a(\omega)/\alpha_a(\omega)$ from Eq. (3). A closed system for $p_j(\omega)$ is obtained by using Eq. (4) to eliminate the electric field from Eq. (3),

$$p_j(\omega) + \alpha_j \sum_k D_{jk}(\omega) p_k(\omega) = \delta_{jd} p_d^0(\omega), \quad (6)$$

where we introduced frequency-dependent matrix

$$D_{jk}(\omega) = -\frac{4\pi\omega^2}{c^2} \mathbf{e}_j \cdot \mathbf{G}(\mathbf{r}_j, \mathbf{r}_k; \omega) \cdot \mathbf{e}_k. \quad (7)$$

Expressing p_a from Eq. (6), we obtain

$$\frac{dW_{ad}}{d\omega} = \frac{\omega E_0^2}{\pi} \frac{|\tilde{\alpha}_d|^2 \alpha_a''}{|1 + \alpha_a D_{aa}|^2} |\tilde{D}_{ad}|^2, \quad (8)$$

where $\tilde{D}_{ad} = D_{ad} [1 - \tilde{\alpha}_d D_{da} \tilde{\alpha}_a D_{ad}]^{-1}$ is donor-acceptor coupling that includes high-order transitions, and

$$\tilde{\alpha}_j(\omega) = \frac{\alpha_j(\omega)}{1 + D_{jj}(\omega)\alpha_j(\omega)} \quad (9)$$

is molecule's *dressed* polarizability satisfying the relation

$$\tilde{\alpha}_j'' + D_{jj}'' |\tilde{\alpha}_j|^2 = \frac{\alpha_j''}{|1 + D_{jj}\alpha_j|^2}, \quad (10)$$

which expresses *energy balance* between total extinction described by $\tilde{\alpha}_j''$, external losses such as radiation and dissipation in metal encoded in $D_{jj}''(\omega)$, and absorption in the presence of environment (r.h.s.).

To gain more insight, recover first Förster's RET from Eq. (8). For a *high-yield* donor ($\alpha_d'' = 0$), Eq. (10) yields the optical theorem, $\tilde{\alpha}_{d0}'' = \frac{2}{3}k^3 |\tilde{\alpha}_{d0}|^2$, where

$$\tilde{\alpha}_{j0} = \frac{\alpha_j}{1 - i\frac{2}{3}k^3 \alpha_j} \quad (11)$$

is polarizability in radiation field and we used free space expression for $D_{jj}^0 = -i\frac{2}{3}k^3$. The near field coupling is

$$D_{ad}^0 = [\mathbf{e}_a \cdot \mathbf{e}_d - 3(\mathbf{e}_a \cdot \hat{\mathbf{r}}_{ad})(\mathbf{e}_d \cdot \hat{\mathbf{r}}_{ad})]/r_{ad}^3 \quad (12)$$

with $\hat{\mathbf{r}} = \mathbf{r}/r$, while $\alpha_a D_{aa}^0 \sim \alpha_a k^3$ is negligible. The radiated energy of an isolated donor can be derived in a similar manner as

$$W_d = \frac{E_0^2}{\pi} \int d\omega \omega \tilde{\alpha}_{d0}''(\omega). \quad (13)$$

Using the optical theorem, Eq. (8) leads to Eq. (1) with

$$\sigma_a(\omega) = \frac{4\pi}{3} k \alpha_a''(\omega), \quad f_d(\omega) = \frac{\omega \tilde{\alpha}_{d0}''(\omega)}{\int d\omega \omega \tilde{\alpha}_{d0}''(\omega)}, \quad (14)$$

where free space donor's spectral function $f_d(\omega)$ is integral-normalized to unity.

Turning to the general case, we note that the energy balance relation Eq. (10) implies the optical theorem in absorptive environment (i.e., for high-yield donor),

$$\tilde{\alpha}_d'' = -D_{dd}'' |\tilde{\alpha}_d|^2 = \frac{2}{3} k^3 |\tilde{\alpha}_d|^2 \frac{\Gamma_d}{\gamma_d^r}, \quad (15)$$

where $\Gamma_j = -\mu_j^2 D_{jj}''$ is molecule's *full* decay rate³⁵ and $\gamma_j^r = \frac{2}{3} k^3 \mu_j^2$ is its radiative decay rate (μ_j is dipole matrix element). Using this relation and normalizing Eq. (8) to radiated energy of *isolated* donor Eq. (13), we obtain

$$\frac{1}{W_d} \frac{dW_{ad}}{d\omega} = \frac{9}{8\pi k^4} \frac{\gamma_d^r}{\Gamma_d(\omega)} \tilde{f}_d(\omega) \tilde{\sigma}_a(\omega) \left| \tilde{D}_{da} \right|^2, \quad (16)$$

which leads to Eq. (2) after frequency integration. Here

$$\tilde{\sigma}_a = \frac{4\pi k}{3} \frac{\alpha_a''}{|1 + \alpha_a D_{aa}|^2}, \quad \tilde{f}_d(\omega) = \frac{\omega \tilde{\alpha}_d''(\omega)}{\int d\omega \omega \tilde{\alpha}_d''(\omega)} \quad (17)$$

are acceptor's absorption crosssection and donor's spectral function modified by the environment [compare to Eq. (14)]. Note that, in the presence of metal, $\tilde{f}_d(\omega)$ is no longer integral-normalized to unity.

Eq. (16) includes *all* relevant energy flow channels in the system. Interactions of the molecules with the metal alter the positions and shapes of optical bands. While the coupling D_{ad} is enhanced due to plasmon-mediated channels, the factor γ_d^r/Γ_d accounts for RET *quenching* due to donor's energy transfer to the metal followed by dissipation and radiation. The absence of this factor leads to spuriously large RET.^{30–34} Note that Eq. (2) was obtained for a high-yield donor with no assumptions on molecules emission or absorption spectral bands, which are usually broad and asymmetric due to vibrational and rotational modes. Rigorous treatment of molecules internal relaxation processes would require fully quantum-mechanical consideration which is beyond our scope. However, if we assume Lorentzian lineshape for donor's effective polarizability $\tilde{\alpha}_d(\omega)$, which is a reasonable approximation in most cases, then it is easy to show that Eq. (2) is valid for low-yield donor as well upon replacing γ_d^r with free space fluorescence rate γ_d .

To highlight the role of PERT in the *far field* RET, consider energy transfer from *remote* donors to an acceptor located *near* the metal surface. In this case, donor's decay rate and spectral function are unaffected by metal and RET is dominated by the following process: a donor first *radiatively* excites SP in the metal which then *nonradiatively* transfers its energy to the acceptor. The coupling D_{ad} can be derived from Dyson's equation for Green's dyadic,

$$\mathbf{G}(\mathbf{r}, \mathbf{r}') = \mathbf{G}^0(\mathbf{r}, \mathbf{r}') + k^2 \bar{\epsilon} \int dV_m \mathbf{G}^0(\mathbf{r}, \mathbf{r}_m) \cdot \mathbf{G}(\mathbf{r}_m, \mathbf{r}'), \quad (18)$$

where integration is restricted to metal region and $\bar{\epsilon}(\omega) = \epsilon(\omega)/\epsilon_0 - 1$. For remote donors, using the far field

limit ($kr \gg 1$ and $kr' \ll 1$) of free Green's dyadic,³⁵ $\mathbf{G}^0(\mathbf{r}, \mathbf{r}') = \frac{e^{ikr}}{4\pi r} (\delta_{\mu\nu} - \hat{\mathbf{r}}_\mu \hat{\mathbf{r}}_\nu)$, and averaging out over donors angular positions and their dipoles orientations, we obtain PERT *per donor*

$$\frac{W_{ad}^r}{W_d} \approx \frac{1}{4\pi r_{ad}^2} \int d\omega f_d(\omega) \tilde{\sigma}_a(\omega) A(\omega), \quad (19)$$

where

$$A = \left| \mathbf{e}_a + k^2 \bar{\epsilon} \int dV_m \mathbf{G}(\mathbf{r}_m, \mathbf{r}_a) \cdot \mathbf{e}_a \right|^2 \quad (20)$$

is SP enhancement factor for a metal region of general shape. If the acceptor located at distance r_a from the center of a spherical NP, we get $A = A^\perp \cos^2 \phi + A^\parallel \sin^2 \phi$, where

$$A^\perp = \left| 1 + 2 \frac{\alpha_1}{r_a^3} \right|^2, \quad A^\parallel = \left| 1 - \frac{\alpha_1}{r_a^3} \right|^2 \quad (21)$$

are enhancement factors for normal and parallel dipole orientations,²¹ $\alpha_1(\omega)$ is NP dipole polarizability, and $\cos \phi = \hat{\mathbf{r}}_a \cdot \mathbf{e}_a$. Eq. (19) extends the *far field* radiative RET theory^{4,29} to plasmonic systems. In fact, PERT mechanism can dominate RET even in the *near field*, as our numerical calculations below demonstrate.

III. NUMERICAL RESULTS FOR NEAR FIELD ENERGY TRANSFER

As an example, consider donor and acceptor near spherical Ag NP in water with normal dipole orientations (see Fig. 1). The near field matrix D_{jk} is readily obtained from Mie's theory Green's dyadic²² as $D_{jk} = D_{jk}^0 + D_{jk}^r + D_{jk}^{nr}$, where²⁴

$$D_{jk}^r = -i \frac{2}{3} k^3 \left[1 + 2\alpha_1 \left(\frac{1}{r_j^3} + \frac{1}{r_k^3} \right) + \frac{4|\alpha_1|^2}{r_j^3 r_k^3} \right] (\hat{\mathbf{r}}_j \cdot \hat{\mathbf{r}}_k),$$

$$D_{jk}^{nr} = - \sum_l \frac{\alpha_l(l+1)^2}{r_j^{l+2} r_k^{l+2}} P_l(\hat{\mathbf{r}}_j \cdot \hat{\mathbf{r}}_k) \quad (22)$$

are NP-induced radiative and nonradiative terms, $\alpha_l = R^{2l+1} \frac{l(\epsilon - \epsilon_0)}{l\epsilon + (l+1)\epsilon_0}$ is NP polarizability, $P_l(x)$ is Legendre polynomial, $D_{ad}^0 = (1 + \sin^2 \theta/2)/r_{ad}^3$, $\hat{\mathbf{r}}_a \cdot \hat{\mathbf{r}}_d = \cos \theta$, and angular momenta up to $l = 50$ were included. Full decay rates are $\Gamma_j = -(3/2k^3) \gamma_j^r D_{jj}''$. We consider, for simplicity, a high-yield donor with a broad emission band due to the vibrational modes. Molecules optical bands are Lorentzians of width 0.05 eV centered at 2.95 eV and 3.2 eV with maximal overlap at about SP energy of 3.08 eV [see inset in Fig. 2(a)], $\sigma_a(\omega)$ was normalized to its total $\int d\omega \sigma_a(\omega)$, and modified $\tilde{\sigma}_a$, \tilde{f}_d and \tilde{D}_{ad} were found using Eq. (22).

In Fig. 1, we plot W_{ad} vs. molecules distance d from $R = 30$ nm NP surface at $\theta = \pi/3$ with equal $d_a = d_d = d$ and with changing $d_d = d$ at fixed d_a . Three models

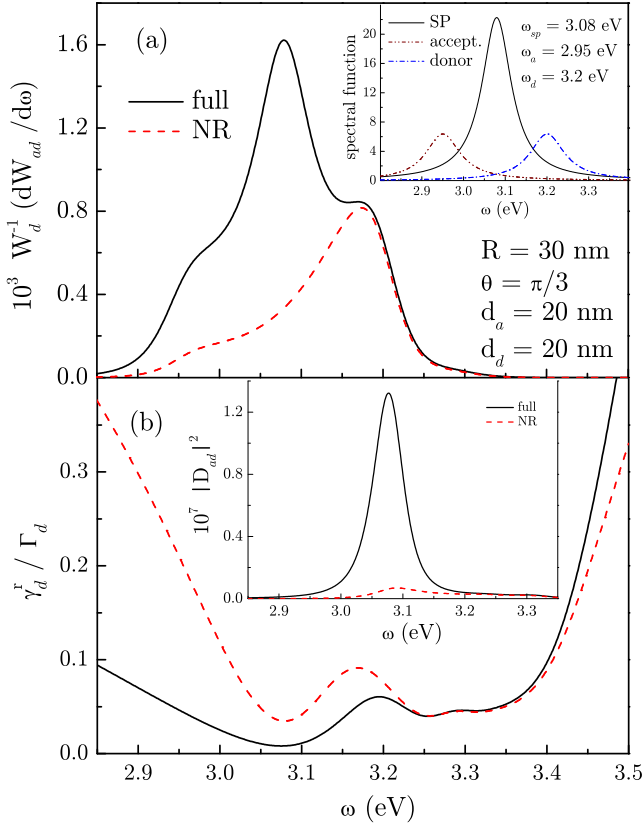


FIG. 2: (Color online) (a) Spectral function Eq. (16) and molecules optical bands relative to SP band α_1/R^3 (inset) are shown together with (b) quenching factor γ_d^r/Γ_d and coupling $|D_{ad}|^2$ (inset) using full and nonradiative (NR) models.

– full Eq. (2), its nonradiative part only, and Gersten-Nitzan model^{30,31} – are compared to Förster’s transfer Eq. (1). For $d_d = d_a$, W_{ad} is about three times larger than W_{ad}^F and rapidly decays with d , while for $d/R \ll 1$ it is quenched by metal. There is no enhancement if only nonradiative channel is included in Eq. (2). In contrast, Gersten-Nitzan model yields much greater enhancement (up to 10^5) for $d/R \ll 1$ since it includes no quenching effects. However, at fixed d_a and $d_d/R \gtrsim 1$, the full W_{ad} is the largest one [see Fig. 1(b)] due to the dominant role of PERT mechanism, as discussed above.

The interplay of different RET contributions is shown in Fig. 2 featuring spectral density Eq. (16) together with quenching factor γ_d^r/Γ_d and coupling $|D_{ad}|^2$ at fixed d . $dW_{ad}/d\omega$ has a sharp SP peak which disappears if only nonradiative channel is included [see Fig. 2(a)]. PERT channel *reduces* γ_d^r/Γ_d due to SP-enhanced radiation but it strongly *enhances* D_{ad} [see Fig. 2(b)], the net result being RET increase, while in nonradiative channel the enhancement and quenching effects nearly cancel out. Weak high-frequency oscillations are due to high- l SPs.

The relative rates of SP-assisted RET and Förster’s transfer are highly sensitive to system’s geometry. RET

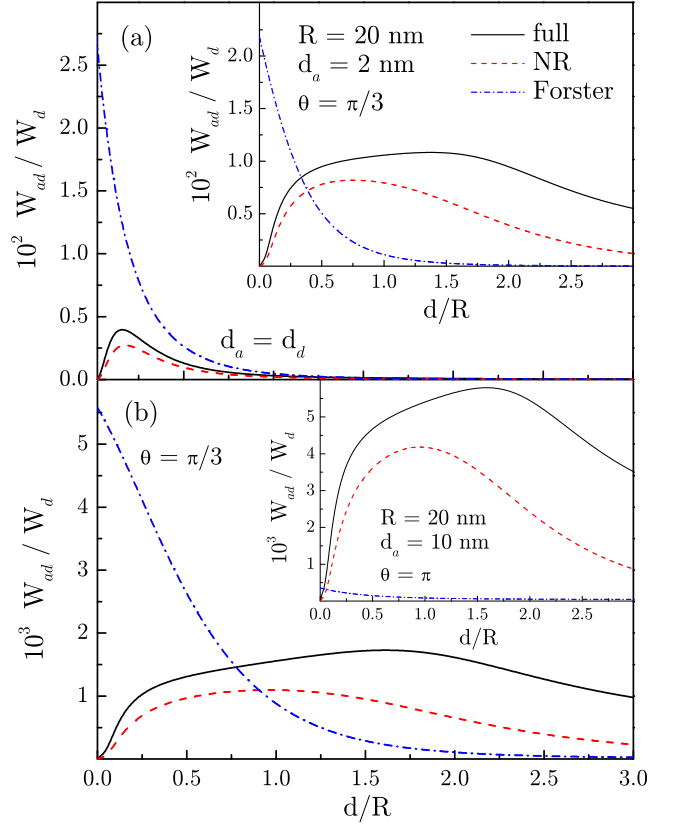


FIG. 3: (Color online) RET vs. distance for $R = 20$ nm Ag NP is shown (a) at $\theta = \pi/3$ with $d_a = d_d$ and $d_a = 2$ nm (inset) and (b) with $d_a = 10$ nm at $\theta = \pi/3$ and $\theta = \pi$ (inset) using full, nonradiative (NR) and Förster models.

is quenched if both molecules are close to NP surface [see Fig. 3(a)] but it becomes enhanced if donor-NP distance increases (inset). For $\theta = \pi/3$ RET is enhanced if $d_d \gtrsim R$ [see Fig. 3(b)], but for $\theta = \pi$ it is strongly enhanced for nearly all d (inset). In fact, NP acts as a *hub* that couples equally well nearby and remote molecules with different θ while Förster’s transfer drops for large r_{ad} . For smaller NP sizes, the role of PERT becomes less pronounced yet it remains dominant for larger donor-NP distances.

IV. CONCLUSIONS

In summary, a theory of resonance energy transfer between energy donors and acceptors near a plasmonic structure is presented which maintains correct energy balance between transfer, dissipation and radiation that is essential for interpretation of experimental data. The plasmon-enhanced radiative transfer is shown to be the dominant mechanism in a wide parameter range. This work was supported by the NSF under Grant Nos. DMR-0906945 and HRD-0833178, and EPSCOR program.

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