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Pressure evolution of the normal-state and superconducting-state properties of the line-nodal material CaSb_2 revealed by ^{123}Sb -nuclear quadrupole resonance

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CaSb_2 is the Dirac line-nodal material that exhibits superconducting (SC) transition at 1.7 K. In spite of its conventional SC state at ambient pressure, the transition temperature T_c shows a peak structure against hydrostatic pressure. We performed AC magnetic susceptibility and ^{123}Sb -nuclear quadrupole resonance (NQR) measurements on single crystalline CaSb_2 under pressures up to 2.08 GPa. T_c monotonically increased in this pressure region, which is consistent with the previous study. We observed continuous broadening of NQR spectrum against pressure, which is a sign of unique compression behavior of the lattice. In the normal state, the nuclear spin-lattice relaxation rate $1/T_1$ is proportional to temperature in all pressure values; typical of a metal. However, $1/T_1T$ in the normal state is independent of pressure, indicating that the density of states at the Fermi energy $N(E_F)$, which is one of the parameters governing T_c , is insensitive to pressure. From these results, we conclude that $N(E_F)$ does not govern the origin of the enhancement in T_c . This is unusual for a weak electron-phonon coupling superconductor. In the SC state, we revealed that SC gap becomes larger and more isotropic under pressure.

INTRODUCTION

Materials with nontrivial topological features have been the central part of the research target in condensed matter physics. In particular, topological superconductivity has been attracting much attention since it could be a host of exotic bound states. One of the promising candidates for bulk topological superconductivity is superconductivity in semimetals with nontrivial topological numbers. In such materials, chemical doping is not necessary for the emergence of superconductivity. This ensures the “clean” topological superconductivity. So far, a lot of studies have been performed to discover superconductivity in topological semimetals such as Dirac [1–5], Weyl [6–14], and line-nodal semimetals [15–23]. Dirac and Weyl semimetals have topologically protected point nodes in their bulk electronic bands, while nodes form lines in the $\mathbf{k}$ space in line-nodal semimetals. In terms of superconductivity, line-nodal semimetals seem to be especially advantageous due to their moderate density of states (DOS). As a matter of fact, a large part of superconducting (SC) line-nodal semimetals exhibit superconductivity without pressure or other techniques [15–19, 21–23]. Therefore, line-nodal semimetal is a good platform for exploring topological superconductivity and for understanding the relationship between nodal lines and superconductivity in detail.

CaSb_2 is a superconductor [23] which was predicted as a line-nodal material [24]. It crystallizes in a monoclinic structure with a nonsymmorphic space group ($P2_1/m$, No. 11, C_{2h}^2) with two nonequivalent crystallographic Sb sites, Sb(1) and Sb(2) [Fig. 1(a)]. In most line-nodal

materials, line nodes are gapped by spin-orbit coupling (SOC). However, the line nodes in CaSb_2 are protected against SOC by nonsymmorphic crystalline symmetry [24], making CaSb_2 suitable for investigating the superconductivity in line-nodal materials.

First-principles calculation predicts that CaSb_2 has two kinds of Fermi surfaces: a topologically trivial three-dimensional hole pocket stems from Sb(2) and a pair of quasi-two-dimensional electron pockets related to the nodal lines stems from Sb(1) [25]. Some of the authors of this paper observed both of them by quantum oscillation measurements [26]. Regarding superconductivity, we succeeded in observing the nuclear quadrupole resonance (NQR) signals of $^{121/123}\text{Sb}(1)$ and revealed a full-gap s -wave SC behavior at ambient pressure [25]. A full-gap behavior was also reported from magnetic penetration depth measurements [27]. Micro-focused angle-resolved photoemission spectroscopy (μ -ARPES) reported that the existence of electron pockets is sample dependent and pointed out that topologically trivial hole pockets play a dominant role in superconductivity [28]. These results indicate that, at least at ambient pressure, the SC state of CaSb_2 is conventional.

On the contrary, the deviation from the Bardeen-Cooper-Schrieffer (BCS) behavior in specific heat was reported [29]. Furthermore, we observed nonmonotonic behavior of SC transition temperature T_c against hydrostatic pressure, indicating the unconventional character of the SC state in CaSb_2 [30]. The origin of the pressure dependence of T_c remains unexplained. We note that this kind of behavior in T_c is also observed in a SC line-nodal metal NaAlSi [31], whose origin is not revealed either.

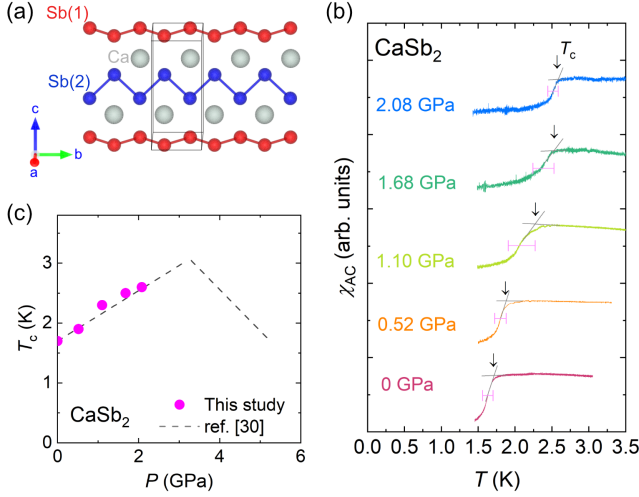


FIG. 1. (Color online) (a) Crystal structure of CaSb₂ with two nonequivalent Sb sites drawn by VESTA [32]. (b) Temperature dependence of the AC susceptibility χ_{AC} measured by a self-inductance method using a frequency range of 83.5-89.7 MHz under various pressure values. (c) Pressure dependence of T_c . The broken lines are visual guidance identical to those in Ref. [30].

We consider that it is important to clarify the origin of nonmonotonic change in T_c to understand the SC properties of CaSb₂ and line-nodal materials, particularly those relating to band topology.

In this paper, we report AC magnetic susceptibility measurements and NQR measurements on ¹²³Sb(1) site, at which the nodal behavior is expected, under hydrostatic pressures up to 2.08 GPa to reveal the origin of the increase in T_c . The increase in T_c by pressure reported for polycrystalline samples was reproduced in the single crystals. In the normal state, the nuclear spin-lattice relaxation rate $1/T_1$ is proportional to temperature, namely the value of $1/T_1T$ is constant in all pressure values. The constant value of $1/T_1T$, associated with DOS at the Fermi energy E_F , is almost pressure independent. This indicates that $N(E_F)$ (DOS at E_F) is pressure independent. From this result, we conclude that the change in T_c is not ascribed to any changes in $N(E_F)$. In the SC state, a higher coherence peak was observed under pressure, suggesting that anisotropy in the SC full gap is reduced under pressure.

METHODS

We used single crystals of CaSb₂ with slab-like shape grown by the self-flux method as reported in Ref. [26]. AC magnetic susceptibility χ_{AC} was measured by the NQR tank circuit to determine T_c . A standard spin-echo technique was used for the ¹²³Sb-NQR measurements (nuclear spin $I = 7/2$). The value of $1/T_1$ was

obtained by measuring the time dependence of the spin-echo intensity after saturation of the nuclear magnetization $M(t)$. Obtained data were fitted by the theoretical relaxation function [33]

$$m(t) = \frac{2}{21} \exp\left(-\frac{3t}{T_1}\right) + \frac{25}{154} \exp\left(-\frac{10t}{T_1}\right) + \frac{49}{66} \exp\left(-\frac{21t}{T_1}\right) \quad (1)$$

in the same way as Ref. [25] where $m(t) = [M(\infty) - M(t)]/M(\infty)$. Pressure was applied using a NiCrAl-BeCu piston-cylinder-type cell with Daphne 7373 oil as pressure medium. The diameter of the initial sample space is 3.7 mm. Pressure was determined by Pb manometer using the relationship [34]

$$P \text{ (GPa)} = \frac{7.18 \text{ (K)} - T_c \text{ (K)}}{0.364 \text{ (K/GPa)}}. \quad (2)$$

RESULTS AND DISCUSSION

Figure 1(b) shows the temperature dependence of χ_{AC} measured at various pressures. Clear diamagnetic signal due to the SC transition was observed. The width of the transition, which is shown with an errorbar, becomes broader up to 1.10 GPa. The broadening of the SC transition can be attributed to the inhomogeneity of pressure, while the origin of the sharpening beyond 1.10 GPa is not clear. T_c is defined as the onset temperature of the SC transition. The pressure dependence of T_c is plotted in Fig. 1(c). In this pressure range, T_c monotonically increases. This is consistent with the previous result shown with the dashed line [30].

We observed ¹²³Sb(1)-NQR spectrum corresponding to $\pm 3/2 \leftrightarrow \pm 5/2$ transition. The site assignment of Sb(1)-NQR signal was described in the previous study [25]. The NQR spectra measured at 4.2 K under various pressure values are presented in Fig. 2(a). The full width at half maximum (FWHM) at ambient pressure is 0.079 MHz. This is about 1/3 of FWHM in the powder samples [25], indicating much higher quality of the single crystalline samples. The spectrum at 0 GPa is compared with that of the powder samples in the inset of Fig. 2(a). As pressure increases, the peak frequency decreases. This indicates that the electric field gradient around the observed nuclei varied owing to compression. In addition, the linewidth of the spectrum monotonically increases with applying pressure as shown in Fig. 2(b). If the environment around the observed nuclei is homogeneous throughout the compressed sample, the linewidth would not increase. In general, measurements under pressure is influenced by the inhomogeneity of pressure, which may cause the broadening of NQR spectra. When using a piston-cylinder type cell and Daphne 7373 oil, it was reported that pressure inhomogeneity is small up to 2.2

GPa above which Daphne 7373 oil becomes solid at room temperature, and that the inhomogeneity is almost constant between 1 GPa and 2.2 GPa [35, 36]. Therefore, the observed continuous increase in the FWHM above 1.10 GPa cannot be attributed to the inhomogeneity of pressure. Another possibility is plastic deformation of the crystal. We can exclude this for the following reason. After the compression process, we relieved pressure and measured NQR spectrum at ambient pressure again. The shift of the resonance frequency was much smaller than the original FWHM and the value of FWHM was almost unchanged compared to the change caused by pressure, indicating the shrinkage is reversible in the pressure region below 2.08 GPa. We believe that the non-saturating broadening of the NQR spectrum reflects the unique features of the compression of CaSb_2 . Specifically, lattice anomaly occurring at higher pressure as seen in $\text{Cd}_2\text{Re}_2\text{O}_7$ is anticipated [37]. In order to understand the evolution of structural parameters and electric field gradient against pressure, detection of all NQR signals is desirable.

Figure 3(a) shows the normalized temperature T/T_c dependence of $1/T_1T$ at each pressure. Above T_c , $1/T_1T$ is almost constant in all pressure values. This so-called Korringa behavior is a characteristic of Fermi liquid systems. Considering $1/T_1T \propto N(E_F)^2$, pressure independent $1/T_1T$ indicates that $N(E_F)$ is independent of pressure. This suggests that the increase in T_c cannot be explained by that in $N(E_F)$. We discuss this point later.

We measured $1/T_1T$ below T_c at 0 GPa and 1.68 GPa to compare the SC properties under pressure with those at ambient pressure. In the SC state, a clear coherence peak was observed just below T_c at 1.68 GPa as shown in Fig. 3(a). This suggests that BCS superconductivity continues in this pressure region. We also normalize $1/T_1T$ with the mean value of that above T_c and plot it for 1.68 GPa along with that at ambient pressure [25] as shown in Fig. 4. The normalized coherence peak becomes higher under pressure. We fitted the data using the BCS model [38],

$$\frac{T_{1n}}{T_{1s}} = \frac{2}{k_B T} \int_0^\infty dE N_s(E) \left[1 + \frac{|\Delta(T)|^2}{E^2} \right] f(E) [1 - f(E)], \quad (3)$$

where T_{1n} (T_{1s}) is T_1 in the normal (SC) state, $N_s(E)$ is the quasi-particle DOS in the SC state, $\Delta(T)$ is the T dependent energy gap, and $f(E)$ is the Fermi distribution function. The effect of the energy broadening in $N_s(E)$ was introduced by the convolution with a rectangular broadening function whose width and height are 2δ and $1/2\delta$, respectively. δ corresponds to the distribution of SC gap. Although the existence of two SC gaps was discussed from the temperature dependence of SC upper critical field H_{c2} [26] and magnetic penetration depth [27], single gap was sufficient for the fitting of $1/T_1T$ in the SC state. (We also performed the fitting with a two-

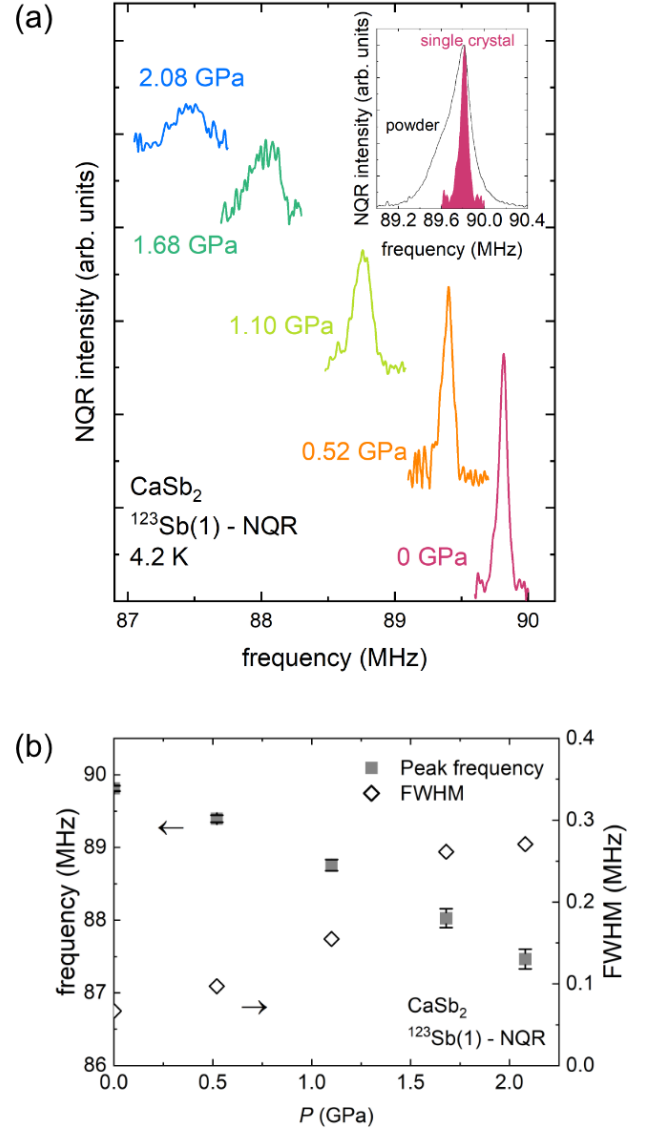


FIG. 2. (Color online) (a) $^{123}\text{Sb}(1)$ -NQR spectrum of CaSb_2 measured at 4.2 K under various pressure values. Inset: $^{123}\text{Sb}(1)$ -NQR spectrum at 0 GPa with that of powder samples. (b) Pressure dependence of peak frequency and FWHM of the NQR spectrum.

gap model, but the two obtained gaps had nearly the same values.) The results are shown as dashed curves in Fig. 4. At 1.68 GPa, we obtained $\Delta(0)/k_B T_c = 1.72$ and $\delta/\Delta(0) = 0.17$. Compared with the values at ambient pressure ($\Delta(0)/k_B T_c = 1.52$ and $\delta/\Delta(0) = 0.35$) [25], the size of SC gap became larger and the distribution of the gap became smaller. The distribution of the gap mainly comes from intrinsic gap anisotropy and the inhomogeneity of sample. We note that the data just below T_c measured in the single crystalline samples at ambient pressure was almost the same as those in the powder sample [25]. To be more specific, there is lit-

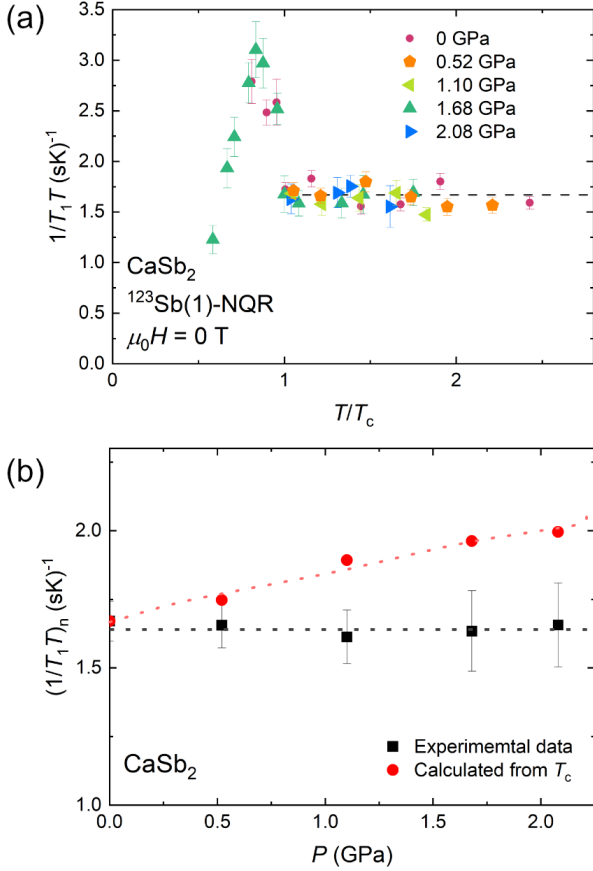


FIG. 3. (Color online) (a) T/T_c dependence of $1/T_1T$ under various pressure values. (b) Pressure dependence of observed Korringa value (black squares) and calculated ones (red circles).

the change in the height of the coherence peak, which is a decisive factor for $\delta/\Delta(0)$. Thus, the reduction of the distribution is not due to the sample quality, but to the suppression of the gap anisotropy under pressure. The origin of more isotropic gap by applying pressure is unclear, but it might be related to the pressure dependence of phonons. **We consider that the electron scattering by low-energy phonon might be enhanced because of the pressure-induced structural fluctuations, averaging the electronic states over the Fermi surfaces. As a result, the effective electron-electron interaction is averaged out and becomes momentum independent, making the SC gap more isotropic. The enhancement of the electron scattering by phonons can also explain the broadening of the NQR spectrum by the disturbance of the electric field gradient.**

Here we discuss the origin of the enhancement in T_c by applying pressure. In weak coupling BCS superconductors,

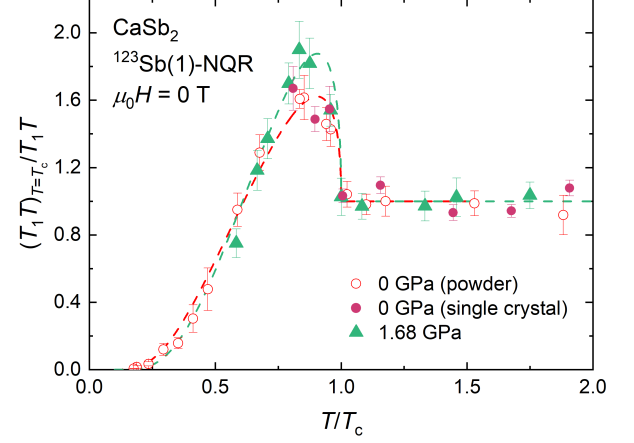


FIG. 4. (Color online) T/T_c dependence of normalized $1/T_1T$ in low temperature region at ambient pressure and 1.68 GPa. Dashed curves show the fitting results using the BCS model.

tors, T_c is expressed as

$$T_c = 1.13 \frac{\hbar\omega_D}{k_B} \exp \left[-\frac{1}{N(E_F)V} \right], \quad (4)$$

where ω_D is the Debye frequency, V is the effective interaction between electrons mediated by phonons, and k_B is Boltzmann's constant. Accordingly, $N(E_F)$ is one of the parameters governing T_c . In conventional metallic systems, $1/T_1$ follows the Korringa law expressed as

$$\frac{1}{T_1T} = \frac{\pi}{\hbar} A^2 N(E_F)^2 k_B, \quad (5)$$

where $\hbar$ and A are Dirac's constant and the hyperfine coupling constant, respectively. By measuring the value of $1/T_1T$, we can detect the change in $N(E_F)$ and confirm whether the increase in T_c is related to $N(E_F)$ or not [39, 40]. In CaSb_2 , we observed a conventional metallic behavior originating from Fermi-surface portions away from the topological line nodes above T_c , and BCS SC behavior below T_c [25]. Therefore, we can apply the above method to CaSb_2 . In our experimental results, $1/T_1T$ was unchanged by pressure, indicating that $N(E_F)$ is independent of applied pressure. Note that the increase in $N(E_F)$ accompanied by the decrease in the hyperfine coupling, which results in constant $1/T_1T$, is not expected in weak coupling electron systems. In most cases, the hyperfine coupling is kept constant or increased by compression in nonmagnetic metals [41–43]. **Since CaSb_2 has multiple bands crossing the Fermi energy, if some of the bands have weak hyperfine coupling, those bands may not be seen by NQR. However, The possibility that the pressure-dependent band is essentially invisible due to the weak hyperfine coupling is also excluded because $1/T_1T$ at 1.68 GPa shows a clear coherence peak just below the enhanced T_c . Our measurements reliably**

captured the electronic states changed by pressure. For a more detailed discussion, we estimated the expected pressure variation of $1/T_1T$ by assuming that the increase in T_c is caused only by that in $N(E_F)$. Here we used $\hbar\omega_D/k_B = 231$ K [29] and assumed that ω_D and V are pressure independent. The result is shown in Fig. 3(b) with experimental data. Clearly, there is a discrepancy between calculation and experimental data. From this result, we conclude that pressure dependence of T_c does not arise from $N(E_F)$. As in Eq. (4), T_c is tuned by three parameters $N(E_F)$, ω_D , and V . Therefore, the origin is considered to be the Debye frequency ω_D or the effective interaction V . This is surprising because in a weak electron-phonon coupling superconductor, the pressure dependence of V and ω_D is usually weaker than that of $N(E_F)$ [44]. Whichever the origin is, there should be a change in the lattice properties. The peak in T_c suggests that the pressure variation of the lattice properties would have anomaly. As the superconductivity of CaSb_2 is likely to be mediated by electron-phonon coupling, this anomaly might cause interesting phenomena such as a drastic change of the SC state. In particular, it is predicted that the SC symmetry other than s -wave in this material is topologically nontrivial [45]. **Another fascinating possibility for the realization of topological superconductivity is the formation of interband pairing. In CaSb_2 , the interband coupling could be strong because of the band degeneracy at the nodal lines. If such coupling becomes stronger by pressure, the interband pairing would be promoted. Notably, T_c is always enhanced when interband pairing is additionally formed [46].** Experimental investigation that can probe the pressure variation of ω_D or V such as specific-heat measurement is desired.

CONCLUSIONS

In conclusion, we performed AC magnetic susceptibility and $^{123}\text{Sb}(1)$ -NQR measurements on single-crystal CaSb_2 to investigate the origin of the enhancement in T_c by pressure. We confirmed the enhancement in T_c of the current samples up to 2.08 GPa. The NQR spectral peak of the single-crystal samples is much sharper than that of the powder samples, ensuring the higher quality of the single crystals. We observed nonsaturating spectral broadening against pressure that probably reflects unique compression behavior of CaSb_2 , rather than pressure inhomogeneity. At all pressure values, $1/T_1$ exhibits Korringa behavior above T_c . The constant value of $1/T_1T$ against pressure indicates that $N(E_F)$ is independent of pressure. This result excludes enhancement of $N(E_F)$ from the possible causes of the enhancement in T_c . According to the BCS theory, remaining candidates are ω_D and V , both of which are related to the crystal lattice. As for the SC properties, the gap becomes larger and more

isotropic by applying pressure. For further investigation of the pressure evolution of the electronic state, NQR measurements at higher pressures with a different type of cell would be useful. It is an interesting future issue to clarify the origin of the peak in T_c against pressure in CaSb_2 , as well as its SC symmetry in higher pressure region.

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