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Observation of Coulomb blockade and Coulomb staircases in superconducting math xmlns="http://www.w3.org/1998/Math/MathML">mrow>ms ub>mi>Pr/mi>mrow>mn>0.8/mn>/mrow>/msub>msub> mi>Sr/mi>mrow>mn>0.2/mn>/mrow>/msub>msub>mi> NiO/mi>mn>2/mn>/msub>/mrow>/math> films Rui-Feng Wang, Yan-Ling Xiong, Hang Yan, Xiaopeng Hu, Motoki Osada, Danfeng Li, Harold Y. Hwang, Can-Li Song, Xu-Cun Ma, and Qi-Kun Xue Phys. Rev. B **107**, 115411 — Published 10 March 2023 DOI: 10.1103/PhysRevB.107.115411

Observation of Coulomb blockade and Coulomb staircases in superconducting $Pr_{0.8}Sr_{0.2}NiO_2$ films

Rui-Feng Wang,¹ Yan-Ling Xiong,¹ Hang Yan,¹ Xiaopeng Hu,¹ Motoki Osada,^{2,3}

Danfeng Li,^{4,*} Harold Y. Hwang,^{2,3} Can-Li Song,^{1,5,†} Xu-Cun Ma,^{1,5,‡} and Qi-Kun Xue^{1,5,6}

¹State Key Laboratory of Low-Dimensional Quantum Physics,

Department of Physics, Tsinghua University, Beijing 100084, China

²Stanford Institute for Materials and Energy Sciences,

SLAC National Accelerator Laboratory, Menlo Park, California 94025, United States

³Department of Applied Physics, Stanford University, Stanford, California 94305, United States

⁴Department of Physics, City University of Hong Kong, Kowloon, Hong Kong SAR 999077, China

⁵Frontier Science Center for Quantum Information, Beijing 100084, China

⁶Southern University of Science and Technology, Shenzhen 518055, China

Motivated by the discovery of superconductivity in the infinite-layer nickelate family, we report an experimental endeavor to clean the surface of nickelate superconductor $Pr_{0.8}Sr_{0.2}NiO_2$ films by Ar^+ ion sputtering and subsequent annealing, as well as study their electronic structures by cryogenic scanning tunneling microscopy and spectroscopy. The annealed surfaces are characterized by nano-sized clusters and Coulomb staircases with periodicity inversely proportional to the projected area of the nanoclusters, consistent with a double-barrier tunneling junction model. Moreover, the dynamical Coulomb blockade effects are observed and result in well-defined energy gaps around the Fermi level, which correlate closely with the specific configuration of the junctions. These Coulomb blockade-related phenomena provide an alternative plausible cause of the observed gap structure that should be considered in the spectroscopic understanding of nickelate superconductors with the nano-clustered surface.

I. INTRODUCTION

The recent discovery of the infinite-layer nickelate family $R_{1-x}(Sr, Ca)_x NiO_2$ (R = Nd, Pr, La) has provided a fascinating platform for exploring electronic correlation and superconductivity in complex oxide materials [1-4]. Unlike their cuprate counterparts [5], the nickelates exhibit a distinct phase diagram without an insulating parent state [6–9], and are considered to possess a multiorbital electronic structure [10–12]. Although surfacesensitive experimental techniques have proved powerful to clarify the electron pairing symmetry and interorbital interaction in high-temperature (T_c) superconductors [13, 14], they turn out to be challenging for the nickelate films because of the mandatory topotactic reduction process using CaH₂, which may significantly degrade the top surface. A recent scanning tunneling microscopy/spectroscopy (STM/STS) study showed the strange coexistence of a V-shaped energy gap and a fully opened energy gap on a nano-clustered $Nd_{1-x}Sr_xNiO_2$ surface after a long-time vacuum annealing [15]. Albeit several theoretical proposals [16–20], the origin of the two different types of energy gaps and the pairing symmetry of nickelate superconductors remain mysterious.

As is well-known, the geometry of an object can profoundly affect the electronic properties as its dimensions are reduced to that comparable to characteristic length scales [21, 22]. Specifically, if the charging energy $e^2/2C$

(e is the electron charge and C is the capacitance) of a nano-sized object is larger than the energy of thermal fluctuations $(k_B T)$ $(k_B$ is the Boltzmann constant), the effect of single-electron tunneling (SET) arises. In widely studied systems such as metal nanoparticles [23–27] and discontinuous films [28], a double-barrier tunneling junction (DBTJ) model based on the orthodox theory fairly describes the experimental spectra [29–31]. Controlled by the impedance of the internal junctions, the tunneling current often exhibits equally spaced Coulomb staircases with increasing bias voltage. On the other hand, in a single junction dominating system, quantum fluctuations exert a significant influence on the SET and lead to dynamic Coulomb blockade (DCB) [32, 33], yielding an energy gap near the Fermi level (E_F) [34, 35]. Here, we report such behaviors on the surface of superconducting $Pr_{0.8}Sr_{0.2}NiO_2$ (PSNO) films. Our results call for a more comprehensive understanding of the gap-like features of tunneling spectra on the nano-clustered surface of nickelate superconductors.

II. METHODS

The infinite-layer PSNO films were prepared on $SrTiO_3$ (STO) substrates by reducing the precursor $Pr_{0.8}Sr_{0.2}NiO_3$ thin films grown by the pulsed laser deposition, as detailed elsewhere [2]. Afterward, the samples were *ex situ* transferred to our UHV chamber connected to a Unisoku USM 1300 ³He STM system. Prior to STM measurements, we cleaned the samples with Ar^+ ion sputtering at energies of 500~1000 eV for 10~45 minutes under a pressure of 1×10^{-5} Torr and then annealed

^{*} danfeng.li@cityu.edu.hk

 $^{^\}dagger$ clsong
07@mail.tsinghua.edu.cn

[‡] xucunma@mail.tsinghua.edu.cn

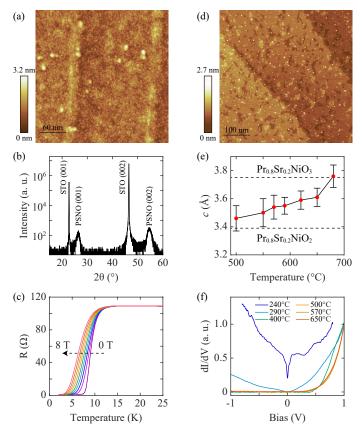


FIG. 1. (a) STM topographic image of PNSO after Ar⁺ sputtering and annealing at 200°C (300 nm \times 300 nm, V = -3.0 V, I = 10 pA). (b) XRD pattern (wavelength of the X-ray: 1.5406 Å) of PNSO after treatments at 200°C, showing the infinite-layer PSNO phase. (c) Temperature dependent resistance curves of the PSNO sample in (b) under varied magnetic fields. The superconducting onset temperature of 10.8 K is similar to the films before Ar^+ sputtering and annealing. (d) STM topographic image of PNSO after Ar⁺ sputtering and annealing at 650°C (500 nm \times 500 nm, V=2.7 V, I=10pA). (e) Step heights of PSNO films as a function of annealing temperatures. Each point comes from the measurements of 20 profiles, and the error bar indicates the standard deviation. (f) Spatially averaged dI/dV spectra measured at 4.2 K on the surface of PSNO samples after various annealing temperatures.

them in UHV to improve the crystalline quality at varied temperatures. Unless otherwise specified, the STM measurements were conducted at 0.4 K with a polycrystalline PtIr tip, which was cleaned by *e*-beam heating in UHV and calibrated on MBE-grown Ag/Si(111) films. Tunneling spectra were measured using a standard lock-in technique with a small bias modulation at 931 Hz.

III. RESULTS AND DISCUSSIONS

Figure 1(a) shows a typical STM topographic image of the PSNO films upon sputtering at 500 eV for 10 minutes

and annealing at 200°C for 1 hour. The film exhibits a corrugated surface covered with nano-sized clusters. This topography is highly reproducible for all PSNO samples under similar treatments. The samples retain the infinite-layer crystal structure and bulk superconductivity with a T_c^{onset} of 10.8 K (the temperature where the resistance reduces to 90% of the value at 20 K), as confirmed by X-ray diffraction (XRD) [Fig. 1(b)] and macroscopic transport measurements [Fig. 1(c)]. This nanoclustered topography is little affected by further Ar^+ ion sputtering. However, it undergoes an evident transformation into an atomically flat step-terrace structure as the annealing temperature is increased above 500°C, as shown in Fig. 1(d). The step height gradually changes from near the *c*-axis length of the PSNO phase (3.39 Å) to that of the $Pr_{0.8}Sr_{0.2}NiO_3$ phase (3.75 Å) with increasing temperature [Fig. 1(e)]. Meanwhile, the tunneling spectra change from metallic characteristics to insulating ones [Fig. 1(f)]. We therefore focus on the spectral measurements on the nano-clustered surface after lowtemperature annealing $(180 \sim 240^{\circ} C)$.

The PSNO nanoclusters are clearly imaged by a magnified STM image shown in Fig. 2(a). They are shaped in irregular polygons and mostly approximated as hemispheres. This allows us to measure their sizes by the diameter (labeled as d) of the outmost peripherv of various nanoclusters. Figure 2(b) shows spatially resolved dI/dVspectra straddling various nanoclusters taken at 4.2 K. These spectra exhibit a remarkable size d dependence and can be divided into two categories. One is on the small nanoclusters that exhibits an energy gap around the Fermi level (E_F) and additional oscillatory peaks outside the low-energy gap. The other one is characteristic of a metal-like feature with an obvious spectral dip at E_F . To clarify the relationship between the spectra and the size of PSNO nanoclusters, we systematically measured the dI/dV spectra as well as effective diameters for various nanoclusters, as illustrated in Figs. 2(c) and 2(d). In general, all the spectra exhibit equidistant oscillatory peaks with increasing bias, reminiscent of Coulomb staircases for the single electron tunneling. According to this scenario, each peak means the number of electrons in the nanoclusters changes by one. As described in the DBTJ model [29–31], the barrier increases with the decrease of the nanocluster size via $E_C = e/C_2$, where C_2 is the effective capacitance between the nanocluster and the continuous film beneath it. Figure 2(e) shows the dependence of E_C on d for various nanoclusters, justifying an inversely quadratic relationship between them via $E_C \propto 1/d^2$, because the capacitance of a metal island is proportional to the projected area in scale with d^2 . Therefore, this result provides strong evidence for the notion that the equally spaced conductance peaks originate from Coulomb blockade effects in the PSNO nanoclusters.

Note that the equidistant conductance peaks of the tunneling dI/dV spectra hold true only for those well above and below E_F , whereas the energy spacing be-

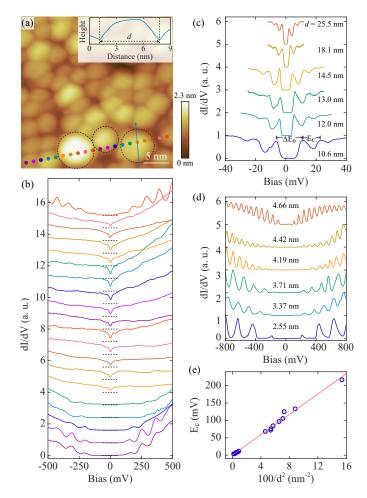


FIG. 2. (a) STM topographic image of PNSO nanoclusters (30 nm × 30 nm, V = -3.0 V, I = 10 pA). The nanoclusters are marked by dashed circles with various effective diameters (d). Inset: line profile along the blue arrow to determine the d value. (b) A series of dI/dV spectra (setpoints: V = -500 mV, I = 100 pA) acquired on the correspondingly colored spots in (a). (c, d) Representative spectra on the nanoclusters of different sizes, as labeled. The setpoints in (c) are V = 40 mV, 30 mV, 25 mV, 25 mV, 12 mV, 12 mV, I = 1.5 nA, 8.0 nA, 6 nA, 6 nA, 1.3 nA, 2.0 nA for the spectra from bottom up. The setpoints in (d) are V = -800 mV, I = 1.0 nA for the sized nanoclusters. (e) Relationship between Coulomb staircase periodicity (E_C) and size parameters $1/d^2$. The red curve shows the best linear fit between them.

tween the two peaks on both sides of E_F (labeled as ΔE_0) is commonly larger than E_C . A straightforward explanation may be that the gap ΔE_0 contain the superconducting gap (Δ_S) in PSNO. For most size-confined superconducting systems, the relationship $\Delta E_0 = E_C + 2\Delta_S$ holds when the cluster size exceeds the Anderson limit [27, 28, 36]. At elevated temperature or magnetic field, the superconducting gap is suppressed and the gap ΔE_0 will reduce from $E_C + 2\Delta_S$ to E_C , which provides a feasible criterion to distinguish superconductivity from the coupled Coulomb effect. To this purpose, temperaturedependent spectral investigations have been carried out on two typical nanoclusters with d = 12.0 nm and d = 25.5nm [Figs. 3(a-d)], respectively. The extracted ΔE_0 and E_C from these spectra are shown in Figs. 3(b, d), where the E_C are extracted from the average of the energy differences between the first and second oscillatory peaks (marked by short rods) on both energy sides. Surprisingly, the gap ΔE_0 never approaches E_C with temperature, and the thermal broadening effect even broadens the two E_F -near conductance peaks such that ΔE_0 phenomenally increases with temperature. At elevated temperatures, the gap-like features and conductance peaks gradually weaken and eventually disappear at the same time. The closing temperature of ΔE_0 (6 K) in the 25.5-nm nanocluster is less than that (15 K) in the 12.0nm nanocluster, which seems to be contradictory to the quantum size effect of superconductors that generally present a weaker superconductivity in smaller-sized nanoclusters [37]. Furthermore, we have also measured a series of dI/dV spectra on varying magnetic fields in Figs. 3(e, f), from which the extracted ΔE_0 and E_C change little with the increasing field. These results compellingly indicate that ΔE_0 completely originates from the Coulomb effect and gets smeared out at elevated temperatures. No clear signature of the superconducting gap is found from our careful spectral measurements on the nano-clustered surface, even though the bulk superconductivity of the samples has been confirmed by transport measurements. Our results suggest that the nano-clustered surface has different stoichiometry from the bulk of the PSNO superconductors, where more caution should be paid in interpreting the gap-like features in the nickelate system.

Having excluded the involved superconductivity, the DCB is considered as an alternative cause for the widened ΔE_0 . Experimentally, the DCB induced conductance gaps appear at high environmental impedance and are critically dependent on the tip-sample distances [34, 35]. To check this scenario, Fig. 4(a) shows a series of sitespecific normalized tunneling spectra on a 25.5-nm nanocluster at varied current setpoints. Evidently, there exists only a gap ΔE_0 in the dI/dV spectra measured at I < 0.5 nA, while the Coulomb staircases become more and more remarkable and ΔE_0 gradually decreases to E_C at larger I [Fig. 4(b)]. These results show a salient crossover from Coulomb blockade (a dominant single junction) to Coulomb staircases (double-barrier junctions). As illustrated in Fig. 4(c), the whole experimental setup can be simplified to two tunneling junctions, just as in the DBTJ model. The first junction is between the tip and the surface PSNO nanocluster with an effective resistance R_1 and capacitance C_1 , and the other one is between the surface PSNO nanocluster and the underlying PSNO film with effective parameters R_2 and C_2 . When the distance between the tip and the sample is large enough, where R_1 is much larger than R_2 , the first tunneling channel is dominant. However, as the tip approaches the sample surface so that R_1 is comparable

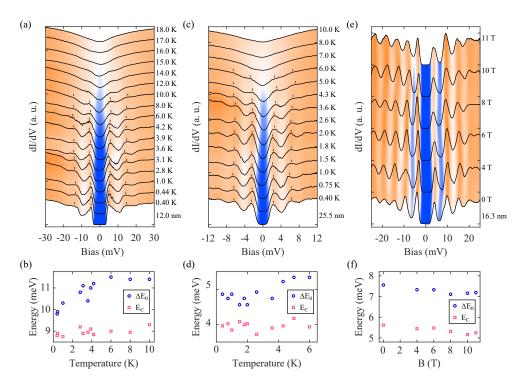


FIG. 3. (a) Temperature dependent dI/dV spectra (setpoints: V = 30 mV, I = 8.0 nA) measured in a 12.0-nm PSNO nanocluster. (b) The extract ΔE_0 and E_C of spectra in (a) as a function of temperatures. (c, d) Same to (a, b) but on a 25.5-nm PSNO nanocluster. The setpoints are V = 12 mV, I = 2.0 nA. (e) A series of dI/dV spectra (setpoints: V = 25 mV, I = 4.0 nA) measured in a 16.3-nm PSNO nanocluster under different magnetic fields. (f) The extract ΔE_0 and E_C of spectra in (e) as a function of magnetic fields.

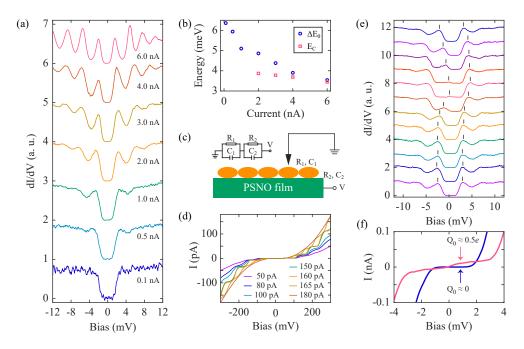


FIG. 4. (a) A series of dI/dV spectra on a 25.5-nm PSNO nanocluster as a function of tunneling current setpoints. The bias setpoints are stabilized at 12 mV. (b) The extract ΔE_0 and E_C as a function of the current setpoints. (c) Schematic illustration of the DBTJ model on the PSNO surface and equivalent circuit of this structure. (d) A series of I-V curves measured on a 4.66-nm PSNO nanocluster at different tunneling current setpoints. The bias setpoints are fixed at 300 mV. (e) A series of dI/dV spectra (setpoints: V = 12 mV, I = 1.3 nA) acquired along a trajectory of 8.0 nm in an 18.1-nm PSNO nanocluster. (f) Comparison of I-V curves between $Q_0 \approx 0$ and $Q_0 \approx 0.5e$.

with R_2 , the second tunneling channel comes into play and the double junctions jointly cause the equidistant oscillatory peaks with the periodicity $E_C = e/C_2$. In special conditions (e.g. I = 6 nA), the *I*-V spectrum exhibits equally spaced staircases and the dI/dV spectrum exhibits discrete peaks, where the influence of DCB is negligible. Figure 4(d) shows another series of measurements on a 4.66-nm nanocluster with larger R_2 . One can immediately notice that the similar Coulomb staircases happen only for intermediate tunneling current setpoints (80 pA $\leq I \leq 165$ pA). Too small or too large current setpoint I means $R_1 \gg R_2$ or $R_1 \ll R_2$, which changes the configuration to a single junction model dominated by the first or the second tunneling junction.

In addition to the effective resistances and capacitances, the fractional residual charge Q_0 is another important parameter in the DBTJ model, which represents the effective initial charge in the central electrode. Figure 4(e) illustrates the influence of Q_0 via a series of Coulomb staircases along a trajectory of 8.0 nm in an 18.1-nm nanocluster. These spectra are not symmetric with respect to E_F but are shifted in energy because of the local variation of Q_0 . In principle, the locations of the first spectral peaks below and above E_F have analytical expressions $x_1 = (-e/2 + Q_0)/C_2$ and $x_2 = (e/2 + Q_0)/C_2$. As Q_0 approaches e/2, x_1 moves to the E_F with minimum intensity. Figure 4(f) exhibits magnified *I-V* spectra between $Q_0 \approx 0$ and $Q_0 \approx e/2$. At $Q_0 \approx 0$, the spectrum is characteristic of a Coulomb gap, while at $Q_0 \approx e/2$, the gap vanished and the *I-V* curve shows a nonzero slope everywhere. The residual charge is considered to originate from the site-varying work functions and capacitances of the junctions [29]. Given the almost same shape of spectra beyond the first peaks, the capacitances should remain unchanged when the tip moves on the same nanocluster. Therefore, we ascribe the varying Q_0 to the variations of local work functions.

IV. SUMMARY

In conclusion, Coulomb blockade and staircases have been clearly identified on the clean surface of the superconducting PSNO thin films after Ar^+ ion sputtering and annealing treatments. The remarkable Coulomb staircases are investigated as a function of the nanocluster sizes, tip-sample distances and residual charges, which corroborate a SET process described by the DBTJ model. More importantly, the crossover from Coulomb blockade to Coulomb staircases has been well evidenced. Our results reveal the significant Coulomb blockade effects that should be carefully considered to explain the tunneling spectra of nano-clustered surface in infinite-layer nickelates.

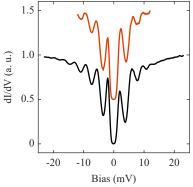


FIG. 5. Two dI/dV spectra measured on the same nanocluster with different energy ranges. The spectra are vertically shifted for clarity. The setpoints of the lower spectrum are V = 23 mV, I = 8.0 nA and those of the upper spectrum are V = 12 mV, I = 3.0 nA.

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Appendix: Spectra at different energy scales

The oscillatory peaks from Coulomb staircases are obvious only when the effective resistances R_1 and R_2 satisfies an appropriate relationship, which makes us measure the dI/dV spectra at different setpoint conditions. However, it should be emphasized that the period E_c does not change at a wide range of setpoints as long as the DBTJ forms [Figs. 4(a, d)]. To further validate this point, we show two dI/dV spectra at different energy scales in Fig. 5, where the spectrum at larger energy encompasses the oscillatory patterns of the one at smaller energy.

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