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### Superconductivity in Li-B-C system at 100 GPa

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#### 16 Abstract

Layer Li-B-C compounds have been shown to have feasible superconductivity. Using 17 the adaptive genetic algorithm, we predict the structures of the Li-B-C system at 100 18 19 GPa. We identify several low-enthalpy metallic phases with stoichiometries of LiB<sub>2</sub>C, LiB<sub>3</sub>C, Li<sub>2</sub>BC<sub>2</sub>, Li<sub>3</sub>B<sub>2</sub>C<sub>3</sub>, Li<sub>3</sub>BC, and Li<sub>5</sub>BC. Using a fast screening method of electron-20 phonon interaction, we find that LiB<sub>3</sub>C is a promising candidate for superconductivity. 21 22 The consecutive calculations using the full Brillouin zone confirm the existence of the strong electron-phonon coupling in this system. The anharmonic B-C phonon modes 23 near the zone center provide the major contribution to the electron-phonon coupling. 24 The electron-phonon coupling constant is 1.40, and the estimated critical temperature 25 is 22 K. Our study indicates superconductivity can also happen without a layered 26 structural motif in the Li-B-C system. It also demonstrates an effective strategy for 27 crystal structure prediction of superconducting materials. 28

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#### 1 **1. Introduction**

Exploring high-temperature superconductors is an important research goal in 2 physics, chemistry, and material science. Inspired by the discovery of a 3 superconducting transition around 40 K in the rather simple MgB<sub>2</sub> compound [1-3], 4 extensive research has been conducted on its related materials [4-9] (graphitelike 5 layered materials intercalated with alkali or alkali-earth) to obtain new possible 6 superconductors. Among them, graphitelike layered Li-B-C compounds have been the 7 subject of sustained interest, because these structures with light elements may have 8 strong covalent bonding and significant phonon frequencies, underling high- $T_c$ 9 (conventional) superconductivity [10, 11]. LiBC with P6<sub>3</sub>/mmc symmetry [12, 13] has 10 a similar crystal structure to MgB<sub>2</sub>. However, unlike MgB<sub>2</sub>, LiBC exhibits an insulating 11 nature [13]. According to Bardeen-Cooper-Schrieffer (BCS) theory [14], metallicity is 12 an important requirement for a conventional superconductor. Therefore, to achieve 13 superconductivity in LiBC, Rosner et al. suggested metalizing LiBC by introducing 14 vacancies at Li sites [15]. Based on the DFT calculations, they found that Li<sub>0.5</sub>BC 15 16 becomes superconducting at about 100 K. However, no experimental efforts have reported superconductivity of the Li-deficient LiBC compounds above 2 K [16-19]. 17 Further research shows that the absence of superconductivity of Li<sub>x</sub>BC can be attributed 18 to structural instability in the B-C layer at low Li deficiency, which leads to a dramatic 19 20 change in electronic structure [20]. Considering that hole doping by introducing Li 21 vacancies will cause structural instability in Li<sub>x</sub>BC, Gao *et al.* designed a freestanding LiB<sub>2</sub>C<sub>2</sub> trilayer [5]. Due to no vacancies involved in trilayer LiB<sub>2</sub>C<sub>2</sub>, the structural 22 distortion in the B-C layer may be prevented. And first-principles calculations predict 23 24 that this trilayer LiB<sub>2</sub>C<sub>2</sub> is a superconductor with  $T_c$  about 92 K. Furthermore, partially replacing carbons with borons in LiBC-type compounds was also proposed, such as 25 LiB<sub>1.1</sub>C<sub>0.9</sub> [21], Li<sub>3</sub>B<sub>4</sub>C<sub>2</sub> [22], Li<sub>2</sub>B<sub>3</sub>C [22] and Li<sub>4</sub>B<sub>5</sub>C<sub>3</sub> [7], which have all been 26 predicted to be superconductors. More recently, Quan et al. reported the 27 superconductivity in the honeycomb structure  $Li_{2x}BC_3$  at x = 0.5 by the theoretical 28 calculations [23]. The calculated superconducting critical temperature  $T_c$  is comparable 29

to that in MgB<sub>2</sub>. These results show that the design of stoichiometric constituents of
graphitelike layered Li-B-C compounds provides a feasible route to induce
superconductivity.

So far, most attention has been focused on elucidating the nature of 4 superconductivity of Li-B-C compounds with a graphitelike layered structure. A natural 5 question remains whether there is any other Li-B-C structure that can lead to 6 superconductivity. To answer this question, a comprehensive investigation of the 7 crystal structures and superconductivity of the Li-B-C system should be carried out. 8 These studies can help establish correlations of structural stability and superconducting 9 properties with different structural motifs in the Li-B-C system, which, in turn, can be 10 used to guide other researchers to reveal more promising superconductors. On the other 11 12 hand, it has been shown that high pressure offers another effective strategy for identifying structural motifs for superconductivity [24-27]. Because high pressure 13 conditions can enhance the interatomic interaction, tune electronic properties, and 14 metalize materials. Furthermore, the application of pressure also can access unusual 15 16 chemistry and stable structures that cannot be realized under ambient conditions [28], which may raise the possibility of finding superconducting materials. Therefore, in this 17 paper, we investigate the structural and superconducting properties of the Li-B-C 18 system at 100 GPa with crystal structure predictions. We employ a recently developed 19 20 frozen-phonon method of electron-phonon coupling calculations [29] to fast screen possible Li-B-C superconductors. 21

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#### 23 **2.** Computational methods

The crystal structures of B-C, Li-C, and Li-B-C at 100 GPa were determined by using the adaptive genetic algorithm (AGA) method [30], which combines fast structure exploration by auxiliary classical potentials and accurate *ab initio* calculations adaptively and iteratively. In the GA-loop, the initial atomic position of the Li, B and C atoms were randomly generated without any assumption on the Bravais lattice type, symmetry, atom basis, or unit cell dimensions. The total structure pool in our GA search was set to 128. The structure search with auxiliary interatomic potentials was performed in 400 consecutive GA generations. Then, the 16 lowest-enthalpy structures at the end
of each GA search were selected for single-point DFT calculations according to the
AGA procedure [30], whose energies, force, and stress are used to adjust the
interatomic potential parameters for the next iteration of GA search. A total of 40
adaptive iterations were performed to obtain the final structures.

Here, the embedded-atom method (EAM) [31] was used as classical auxiliary
potential. In EAM, the total energy of an *N*-atom system was evaluated by

$$E_{total} = \frac{1}{2} \sum_{i,j(i\neq j)}^{N} \phi(r_{ij}) + \sum_{i} F_i(n_i), \qquad (1)$$

9 where  $\phi(r_{ij})$  denotes the pair repulsion between atoms *i* and *j* with a distance of 10  $r_{ij}$ ,  $F_i(n_i)$  is the embedded term with electron density term  $n_i = \sum_{j \neq i} \rho_j(r_{ij})$  at the 11 site occupied by atom *i*. The potential fitting is performed by the force-matching 12 method with a stochastic simulated annealing algorithm as implemented in the POTFIT 13 code [32, 33].

The first-principles calculations were performed by using the projector-augmented 14 15 wave (PAW) [34] representations with density functional theory as implemented in the Vienna ab initio simulation package (VASP) [35, 36]. The exchange and correlation 16 energy was treated within the spin-polarized generalized gradient approximation 17 (GGA) and parameterized by Perdew-Burke-Ernzerhof (PBE) formula [37]. Wave 18 functions were expanded in plane waves up to a kinetic energy cutoff of 520 eV. 19 Brillouin-zone integrations were approximated using special k-point sampling of the 20 Monkhorst-Pack scheme [38] with a k-point mesh resolution of  $2\pi \times 0.03 \text{\AA}^{-1}$ . Lattice 21 vectors and atomic coordinates were fully relaxed until the force on each atom was less 22 than  $0.01 \text{ eV} \cdot \text{Å}^{-1}$ . The fast screening of electron-phonon coupling (EPC) constant 23  $\lambda_{\Gamma}$  at the Brillouin zone center was carried out based on the frozen-phonon method 24 [29]. The zone-center phonon was computed by the PHONOPY software [39, 40], with 25 a finer k-point sampling grid of  $2\pi \times 0.02 \text{\AA}^{-1}$  spacing and a criterion of self-26 consistent calculation 10<sup>-8</sup> eV. 27

The full Brillouin-zone EPC calculation were performed with the Quantum ESPRESSO (QE) code [41, 42] based on density-functional perturbation theory 1 (DFPT) [43]. The ultra-soft pseudopotentials from the PSLibrary1.0.0 (high accuracy) 2 [44] for PBE functional were used, with  $2s^1$ ,  $2s^22p^1$ , and  $2s^22p^2$  as valence electrons of 3 Li, B, and C, respectively. The kinetic energy cutoffs were 75 Ry for wave functions 4 and 576 Ry for potentials. The charge densities were determined on a *k* mesh of 5  $24 \times 24 \times 24$ . The dynamical matrices were calculated on a *q* mesh of  $6 \times 6 \times 6$ . The 6 convergence threshold for self-consistency was  $1 \times 10^{-12}$  Ry.

7 The calculations of superconducting  $T_c$  are based on the Eliashberg spectral 8 equation  $\alpha^2 F(\omega)$  [45, 46] defined commonly now as

$$\alpha^{2}F(\omega) = \frac{1}{2\pi N(E_{f})} \sum_{qv} \frac{\gamma_{qv}}{\hbar \omega_{qv}} \delta(\omega - \omega_{q,v}), \qquad (2)$$

10 where  $N(E_f)$  is the density of states at the Fermi level,  $\omega_{qv}$  denotes the phonon 11 frequency of the mode v with wave vector  $\mathbf{q}$ .  $\gamma_{qv}$  is the phonon linewidth defined as

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$$\gamma_{qv} = \frac{2\pi\omega_{qv}}{\Omega_{BZ}} \sum_{ij} \int d^3k \left| g_{k,qv}^{ij} \right|^2 \delta(\epsilon_{q,i} - E_f) \delta(\epsilon_{k+q,j} - E_f), \qquad (3)$$

where  $\epsilon_{q,i}$  and  $\epsilon_{k+q,j}$  are eigenvalues of Kohn-Sham orbitals at given bands and vectors. **q** and **k** are wave vectors, and *i* and *j* denote indices of energy bands.  $g_{k,qv}^{ij}$  is the EPC matrix element, which describes the probability amplitude for the scattering of an electron with a transfer of crystal momentum **q**, determined by

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$$g_{k,qv}^{ij} = \left(\frac{\hbar}{2M\omega_{qv}}\right)^{1/2} \left\langle \Psi_{i,k} \left| \frac{dV_{SCF}}{d\hat{\mu}_{qv}} \cdot \hat{e}_{qv} \right| \Psi_{i,k+q} \right\rangle, \tag{4}$$

18 where M is the atomic mass,  $\hat{e}_{qv}$  is the phonon eigenvector.  $dV_{SCF}/d\hat{\mu}_{qv}$  measures 19 the change of self-consistent potential induced by atomic displacement.  $\Psi_{i,k}$  and 20  $\Psi_{i,k+q}$  are Kohn-Sham orbitals. The EPC constant  $\lambda$  can be determined through 21 summation over the first Brillouin zone or integration of the spectral function in 22 frequency space,

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$$\lambda = \sum_{qv} \lambda_{qv} = 2 \int \frac{\alpha^2 F(\omega)}{\omega} d\omega, \qquad (5)$$

24 where the EPC constant  $\lambda_{qv}$  for mode v at wave vector **q** using Eq. (5) can be written 25 as

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$$\lambda_{qv} = \frac{\gamma_{qv}}{\pi\hbar N(E_f)\omega_{qv}^2}.$$
(6)

The superconducting  $T_c$  is determined with the analytical McMillan equation modified by the Allen-Dynes formula [47, 48],

$$T_c = \frac{\omega_{log}}{1.2} \exp\left[\frac{-1.04(1+\lambda)}{\lambda(1-0.62\mu^*) - \mu^*}\right],$$
(7)

(8)

where  $\mu^*$  is the effective screened Coulomb repulsion constant whose values is generally between 0.1 and 0.15 [49, 50], and  $\omega_{log}$  is the logarithmic average frequency

 $\omega_{log} = \exp\left[\frac{2}{\lambda}\int\frac{d\omega}{\omega}\alpha^2 F(\omega)log\omega\right].$ 

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#### 3. Results and discussion

#### 8 3.1 AGA search of Li-B-C ternary phases at 100 GPa

9 Before we discuss ternary compounds in the Li-B-C system, the structural stability of elements and binary phases should be first clarified. At 100 GPa, calculations show 10 that the ground-state phases of elemental Li, B and C adopt the Pbca [51, 52], Cmca 11 ( $\alpha$ -Ga structure) [53] and  $Fd\bar{3}m$  (diamond) [54] symmetry, respectively. For the Li-B 12 binary phase, because previous crystal structure searches [55, 56] have already covered 13 the current study's pressure, we did not perform additional structure searches of Li-B 14 15 compounds. We re-calculated the enthalpies of these crystal structures. Our results show that five compounds with Li<sub>6</sub>B ( $R\overline{3}$ ), Li<sub>2</sub>B (*Cmcm*), Li<sub>3</sub>B<sub>2</sub>( $R\overline{3}m$ ), LiB ( $Fd\overline{3}m$ ) and 16 LiB<sub>4</sub> (I4/mmm) are stable at 100 GPa. For the B-C compounds, Jay et al investigated 17 from ambient pressure to 80 GPa [57]. We performed the AGA search at 100 GPa and 18 found no B-C binary compound was stable at 100 GPa, similar to Jay et al.'s high-19 pressure results [57]. For the Li-C system, our AGA searches indicate that  $Li_4C(P2_1/c)$ , 20  $Li_8C_3$  ( $R\bar{3}m$ ) and  $Li_2C_3$  (*Cmcm*) compounds are the ground-state phases at 100 GPa. 21 More details of AGA searches in B-C and Li-C systems can be found in Supplemental 22 23 Material [58]. The stable crystal structures of these elements and binary phases are 24 shown in Figure S3 of the Supplemental Material [58] and their structural parameters are listed in Supplementary Table S1 [58]. 25

In Figure 1, we present ternary compounds of Li-B-C at 100 GPa from the AGA searches. For simplicity, all chemical formulae are expressed as Li/B/C reduced ratios. For example, 111 represents the compound with LiBC. During the structural search, we select a range of different stoichiometries (i.e., 111, 112, 121, 211, 113, 122, 131, 212, 221, 311, 114, 123, 132, 141, 213, 231, 312, 321, 411, 115, 124, 133, 142, 151, 214,
223, 232, 241, 313, 322, 331, 412, 421, 511, 116, 125, 134, 143, 152, 161, 215, 233,
251, 314, 323, 332, 341, 413, 431, 512, 521 and 611) with 2 or 4 formula units to
perform the AGA search. The relative stability of these predicted Li-B-C compounds
was investigated under the corresponding pressure, depending on the calculated
formation enthalpies,

$$H_f = \frac{H(Li_x B_y C_z) - xH(Li) - yH(B) - zH(C)}{x + y + z}$$
(9)

8 where H (Li<sub>x</sub>B<sub>y</sub>C<sub>z</sub>) is the total enthalpy of the Li<sub>x</sub>B<sub>y</sub>C<sub>z</sub> compound. H (Li), H (B) and H9 (C) are the enthalpy of the ground state of Li, B and C at 100 GPa. Here,  $H_d$  is 10 introduced as the enthalpy above the convex hull to represent the relative stability on 11 the phase diagram. Ground-state phases have  $H_d = 0$ .



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Figure 1. The convex hull of the Li-B-C system at 100 GPa.

As shown in Figure 1, LiBC is the only ternary ground-state compound at 100 GPa. The crystal structure is the same as the experimental structure of LiBC (*P*6<sub>3</sub>/*mmc* symmetry) determined by Woerle *et al.* at ambient pressure [12]. This indicates that the

ambient-pressure LiBC phase is stable up to 100 GPa, which agrees with previous 1 studies [59]. Figure 2(a) shows the atomic structure of hexagonal LiBC at 100 GPa. 2 This structure is the same as the MgB<sub>2</sub> with alternating graphene-like B-C and Li layers. 3 The detailed structural parameters are listed in Supplementary Table S2 [58]. The 4 calculated phonon spectrum confirms that this phase is dynamically stable at 100 GPa 5 (Supplemental Material, Figure S4 (a) [58]). The electronic density of state (DOS) in 6 Figure S4 (b) of the Supplemental Material [58] shows that LiBC is an insulating phase 7 at 100 GPa. 8

9 Besides the ternary ground-state LiBC structure, we also identify a few lowenthalpy metastable structures with enthalpy very close to the convex hull ( $H_d < 100$ 10 meV/atom), namely LiB<sub>2</sub>C, LiB<sub>3</sub>C, Li<sub>2</sub>BC<sub>2</sub>, Li<sub>3</sub>B<sub>2</sub>C<sub>3</sub>, Li<sub>3</sub>BC and Li<sub>5</sub>BC. The H<sub>d</sub> are so 11 12 small that these compounds may be realized in experiments. We compute the Gibbs free energy of formation for one of the structures (LiB<sub>3</sub>C) to examine the effect of 13 temperature on structural stability with the quasiharmonic approximation. The results 14 suggest that the temperature may improve the stability of LiB<sub>3</sub>C (see Supplementary 15 16 Note 2 [58]). The crystal structures of these Li-B-C compounds are shown in Figure 2(b)-(g). The LiB<sub>2</sub>C in Figure 2(b) adopts the orthorhombic structure with Cmcm 17 symmetry. This structure is a 3D framework with PbO-type [60] layers of B<sub>2</sub> and C 18 chains, separated by Li atoms, which is similar to Cmcm CeNiSi<sub>2</sub>. The Cm LiB<sub>3</sub>C also 19 20 has a PbO-type layered motif of B<sub>3</sub>C, and Li atoms locate between two PbO-type layers as shown in Figure 2(c). This structure is similar to the BaFe<sub>2</sub>As<sub>2</sub> phase [61]. The 21 Li<sub>2</sub>BC<sub>2</sub> (*Pbam*) and Li<sub>3</sub>B<sub>2</sub>C<sub>3</sub> (*Pm*) in Figure 2(d)-(e) both have B-C layered structures 22 with five- and eight-membered rings and five-, six- and eight-membered rings, 23 24 respectively. The Cm Li<sub>3</sub>BC (Figure 2(f)) is found to form B-C nanoribbons structure, 25 while, for P-1 Li<sub>5</sub>BC (Figure 2(g)), B and C atoms connect to form chains. The structural parameters of these phases are listed in Supplementary Table S2 [58]. Figure 26 S5-S10 of the Supplemental Material [58] show the phonon dispersions, and DOS for 27 these metastable Li-B-C phases. The results show that, unlike the insulating LiBC, these 28 29 low-enthalpy Li-B-C compounds are metallic. Furthermore, phonon calculations confirm that these Li-B-C compounds are dynamic stability at 100 GPa. It should be 30

noted that the LiB<sub>3</sub>C structure has minor imaginary frequencies near the  $\Gamma$  point (Supplemental Material, Figure S6(a) [58]). However, it does not mean the dynamical instability of this material. Since the phonon calculations are based on the harmonic approximation, the presence of imaginary phonon frequencies may also be associated with a strongly anharmonic effect, which will be discussed later.



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Figure 2. Atomic structures of (a) P6<sub>3</sub>/mmc LiBC, (b) Cmcm LiB<sub>2</sub>C, (c) Cm LiB<sub>3</sub>C, (d)
Pbam Li<sub>2</sub>BC<sub>2</sub>, (e) Pm Li<sub>3</sub>B<sub>2</sub>C<sub>3</sub>, (f) Cm Li<sub>3</sub>BC, and (g) P-1 Li<sub>5</sub>BC at 100 GPa. The light
green rectangle denotes PbO-type motifs.

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#### 12 **3.2 Fast screening of superconductivity of Li-B-C compounds**

Motivated by the metallic properties of these metastable Li-B-C compounds, we further investigated their superconductivity. To determine the phonon-mediated superconductivity, it is usually based on the calculations of electron-phonon coupling in the full Brillouin zone. However, these calculations are time-consuming, particularly

in complicated systems, which impedes the high-throughput superconducting material
 studies. Therefore we first employ a fast screening of these phases with the zone-center
 EPC strength λ<sub>Γ</sub> based on the frozen phonon method [29]. Here, the λ<sub>Γ</sub> can be defined
 by

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$$\lambda_{\Gamma\nu} = \frac{\tilde{\omega}_{\Gamma\nu}^2 - \omega_{\Gamma\nu}^2}{4\omega_{\Gamma\nu}^2},\tag{10}$$

6 where the  $\omega_{\Gamma\nu}$  and  $\tilde{\omega}_{\Gamma\nu}$  are screened and unscreened phonon frequencies of mode  $\nu$ 7 at zone-center, respectively. Using this method, we find only LiB<sub>3</sub>C has a high  $\sum_{\nu} \lambda_{\Gamma\nu}$ 8 (the summation of zone-center EPC of all modes) as shown in Figure 3(a). The high 9  $\sum_{\nu} \lambda_{\Gamma\nu}$  of LiB<sub>3</sub>C can be attributed to the large difference between screened and 10 unscreened phonon frequencies of mode 4 and mode 5 as shown in Figure 3(b).



Figure 3. (a) The enthalpy above the convex hull  $(H_d)$  versus EPC constant  $\sum_{\nu} \lambda_{\Gamma\nu}$  at the Brillouin zone center. (b) The screened and unscreened phonon frequency (top

15 panel) and zone-center EPC strength (bottom panel) in LiB<sub>3</sub>C phase at 100 GPa.

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To further quantify the electron-phonon interaction in LiB<sub>3</sub>C, we investigate its EPC with full Brillouin-zone calculations. Figure 4(a) shows the  $\gamma_{qv}$ -weighted phonon spectrum with DFPT calculations. Now one can see that phonon mode 4 and mode 5 have a large contribution to the phonon linewidth and correspondingly to the electron-

phonon interaction near the  $\Gamma$  point, which agrees well with the fast screening results. 1 These two modes mainly involve vibrations of boron and carbon atoms as shown in 2 3 Figure 4(b). Their vibrational configurations at the  $\Gamma$  point are shown in Figure 4(d) and Figure 4(e), respectively. Mode 4 corresponds to stretching vibrations of B2, B3, 4 and C atoms in the *a-b* plane. And for mode 5, B2-B3 atoms and B1-C atoms both show 5 symmetric stretching vibrations in the *a-b* plane. The calculated Eliashberg function 6  $\alpha^2 F(\omega)$  is shown in Figure 4(c). The integrated EPC parameter  $\lambda$  is 1.40. The  $\omega_{\log}$  can 7 be obtained from equation (8), which is 197.31 K. We predict  $T_c = 22$  K ( $\mu^* = 0.1$ ) for 8 9 the LiB<sub>3</sub>C. As a comparison, we also compute the full EPC for the LiB<sub>2</sub>C phase with *Cmcm* symmetry, which is not expected to show a strong EPC from zone-center EPC 10 calculations. We obtain  $\lambda = 0.37$  and  $T_c = 3 \text{ K} (\mu^* = 0.1)$  for LiB<sub>2</sub>C (see Figure S12 of 1112 the Supplemental Material [58]), indicating the accuracy of the zone-center EPC 13 screening method.



Vibrational pattern for Mode 5 at  $\Gamma$  point

Figure 4. (a) Phonon spectrum of LiB<sub>3</sub>C. Red solid circles represent the phonon
 linewidth (γ<sub>qv</sub>) with a radius proportional to the strength. (b) projected phonon DOS.
 (c) Eliashberg spectral function α<sup>2</sup>F(ω) with integrated EPC parameter λ(ω). The
 vibrational patterns for (d) mode 4 and (e) mode 5 at the Γ point.

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#### 6 **3.3 Anharmonic effect of LiB<sub>3</sub>C**

As mentioned above, there are small imaginary phonon frequencies contributed in 7 LiB<sub>3</sub>C shown in Figure 4(a) and Figure S6(a) of the Supplemental Material [58]. 8 9 Specifically, we find the frequency of mode 4 shows a strong dependence on the magnitude of displacement in the frozen phonon calculations. To further investigate 10 11 this behavior, we calculated the energy changes as all atoms displaced along the eigenmodes of mode 4 at the  $\Gamma$  point in Figure 5. The displacement for atom *i* is  $D_i =$ 12  $u \frac{v_i}{\sqrt{m_i}}$ , where u is the displacement amplitude,  $v_i$  is the eigenvector,  $m_i$  is the atomic 13 mass. To compare, we also plot mode 8, which is a harmonic mode mainly contributed 14 15 by the Li vibration. Compared to the harmonic mode, the potential well of mode 4 is very flat at small displacement and increases rapidly at large displacement. It can only 16 be fit to  $E(u) = A_2 u^2 + A_4 u^4$  with a vanishing  $A_2$  and a large  $A_4$  as shown in Figure 17 5(a). This indicates that mode 4 has unusually large anharmonicity and the conventional 18 19 harmonic phonon calculations are in a nonpertubative regime. Therefore, the current harmonic energy, 1.10 THz or 4.56 meV, should be much lower than the actual energy. 20 The correct treatment of anharmonic effects on superconductivity can be complicated. 21 22 But such large anharmonicity has been seen previously and its influence on EPC and  $T_c$  has also been discussed in the literature [62, 63]. The EPC constant  $\lambda$  can be expected 23 24 in general to be somewhat smaller. However, the influence of this change on  $T_c$  is not unique due to the significant increase of  $\omega_{log}$  when the anharmonicity is included. Due 25 to such cancellation effects, different formulas can produce the increase or decrease of 26  $T_c$ , however overall this effect seems to be small [62]. The phonon dispersions of LiB<sub>3</sub>C 27 are also computed at 0 GPa and 50 GPa (see Figure S13 in the Supplemental Material 28

1 [58]). No negative frequency is found, suggesting that LiB<sub>3</sub>C is dynamically stable at

#### 2 low pressures.



Figure 5. Frozen-phonon calculation of the total energy change as a function of atomic
displacement for two zone-center modes. (a) The anharmonic mode 4 and (b) harmonic
mode 8. The red curve shows the fitting.

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#### 8 4. Conclusions

In summary, we use the AGA method to study the Li-B-C system at 100 GPa. We 9 identify several low-enthalpy metallic phases with stoichiometries of LiB<sub>2</sub>C, LiB<sub>3</sub>C, 10 Li<sub>2</sub>BC<sub>2</sub>, Li<sub>3</sub>B<sub>2</sub>C<sub>3</sub>, Li<sub>3</sub>BC, and Li<sub>5</sub>BC. By a fast evaluation of zone-center electron-11 12 phonon interactions in these metallic Li-B-C structures, we identify that LiB<sub>3</sub>C can be a promising candidate for superconductivity. The calculations of EPC in the full 13 Brillouin and analysis with Eliashberg function  $\alpha^2 F(\omega)$  verify the superconductivity of 14 LiB<sub>3</sub>C with EPC constant  $\lambda = 1.40$  and  $T_c = 22$  K. The electron-phonon interactions are 15 mainly contributed by low-frequency anharmonic phonon modes involving vibrations 16 of boron and carbon atoms. Our results indicate rich structural motifs in the Li-B-C 17 system at high pressure, and the superconductivity in this system can happen in the 18

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- 15

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