

CHCRUS

This is the accepted manuscript made available via CHORUS. The article has been published as:

Relating spin-polarized STM imaging and inelastic neutron scattering in the van der Waals ferromagnet math xmlns="http://www.w3.org/1998/Math/MathML">mrow>ms ub>mi>Fe/mi>mn>3/mn>/msub>msub>mi>GeTe/mi>mn >2/mn>/msub>/mrow>/math>

Christopher Trainer, Olivia R. Armitage, Harry Lane, Luke C. Rhodes, Edmond Chan, Izidor Benedičič, J. A. Rodriguez-Rivera, O. Fabelo, Chris Stock, and Peter Wahl Phys. Rev. B **106**, L081405 — Published 15 August 2022 DOI: 10.1103/PhysRevB.106.L081405

Relating spin-polarized STM imaging and inelastic neutron scattering in the van-der-Waals ferromagnet Fe₃GeTe₂

Christopher Trainer,¹ Olivia R. Armitage,¹ Harry Lane,^{2,3,4} Luke C. Rhodes,¹ Edmond Chan,^{2,5}

Izidor Benedičič,¹ J. A. Rodriguez-Rivera,^{6,7} O. Fabelo,⁵ Chris Stock,² and Peter Wahl¹

¹SUPA, School of Physics and Astronomy, University of St Andrews, North Haugh, St Andrews, Fife, KY16 9SS, United Kingdom ²School of Physics and Astronomy, University of Edinburgh, Edinburgh EH9 3JZ, United Kingdom ³School of Chemistry and Centre for Science at Extreme Conditions, University of Edinburgh, Edinburgh EH9 3FJ, United Kingdom ⁴ISIS Pulsed Neutron and Muon Source, STFC Rutherford Appleton Laboratory, Harwell Campus, Didcot, Oxon, OX11 0QX, United Kingdom ⁵Institute Laue-Langevin, 6 rue Jules Horowitz, Boite Postale 156, 38042 Grenoble Cedex 9, France ⁶NIST Center for Neutron Research, National Institute of Standards and Technology, Gaithersburg, Maryland 20899, USA ⁷Department of Materials Science and Engineering, University of Maryland, College Park, Maryland 20742, USA (Dated: July 29, 2022)

Abstract

Van-der-Waals (vdW) ferromagnets have enabled the development of heterostructures assembled from exfoliated monolayers with spintronics functionalities, making it important to understand and ultimately tune their magnetic properties at the microscopic level. Information about the magnetic properties of these systems comes so far largely from macroscopic techniques, with little being known about the microscopic magnetic properties. Here, we combine spin-polarized scanning tunneling microscopy and quasi-particle interference imaging with neutron scattering to establish the magnetic and electronic properties of the metallic vdW ferromagnet Fe₃GeTe₂. By imaging domain walls at the atomic scale, we can relate the domain wall width to the exchange interaction and magnetic anisotropy extracted from the magnon dispersion as measured in inelastic neutron scattering, with excellent agreement between the two techniques. From comparison with Density Functional Theory calculations we can assign the quasi-particle interference to be dominated by spin-majority bands. We find a dimensional dichotomy of the bands at the Fermi energy: bands of minority character are predominantly two-dimensional in character, whereas the bands of majority character are three-dimensional. We expect that this will enable new design principles for spintronics devices.

I. INTRODUCTION

The discovery of ferromagnetic van-der-Waals (vdW) materials has enabled the possibility of manufacturing spintronics devices from vdW heterostructures [1]. Although, according to the Mermin-Wagner theorem, ferromagnetism should be unstable in two dimensions, recently a number of materials, including Fe₃GeTe₂, have been shown to exhibit ferromagnetism down to the monolayer limit [2-4]. The evolution of its magnetic order from 3D to 2D is an interesting open question [5]. The study of magnetic properties in 2D materials and at surfaces, however, is challenging. Conventional methods used to establish magnetic order parameters, such as neutron scattering, are not suitable for monolayer-thin samples and surfaces, at the same time, interesting new phenomena are expected in 2D magnetic systems[6]. In particular Fe₃GeTe₂ shows a surprising breadth of phenomena, including evidence for electronic correlation effects resulting in Kondo-lattice-like behaviour[7] and a magnetic ground state that sensitively depends on the exact stoichiometry and concentration of iron in the samples[8, 9]. Here, we use spin-polarised STM, quasiparticle interference imaging and neutron scattering to elucidate the interplay between the bulk and surface magnetic order and the low energy electronic structure of a quasi-2D ferromagnet. We identify two types of defects arising predominantly from Fe and Te vacancies, and show that quasiparticle scattering from these defects produces magnetic scattering dominated by the more two-dimensional electronic bands around the Fermi level. Imaging of a domain wall and comparison of its profile with the exchange coupling J and magnetic anisotropy K obtained from inelastic neutron scattering of bulk Fe₃GeTe₂ reveals good agreement, with evidence for a larger magnetic anisotropy and smaller exchange coupling in the surface layer.

II. RESULTS

A. Sample characterization

Fe₃GeTe₂ has a layered crystal structure with weak interlayer interactions and becomes ferromagnetic below T = 230K[10]. The material typically comes with an off-stoichiometry, where the iron concentration deviates from three due to vacancies and interstitial iron. The magnetic properties vary with the excess iron concentration [8]. Previous STM and ARPES investigations have been interpreted as Kondo-lattice-like behaviour [7]. The material cleaves easily between the Fe_{3-y}GeTe₂ layers, exhibiting a Te-terminated surface. We have used single crystal neutron



FIG. 1: Sample characterisation. (a) Intensity of neutrons scattered at the atomic Bragg peak as a function of temperature. The signal will consist of the structural peak and the magnetic signal due to the ferromagnetic order. The red line represents a power law fit to the data giving a ferromagnetic transition temperature of 215K. (b) Magnetization M of the Fe₃GeTe₂ crystal used for the STM measurements. Zero field cooled (ZFC), field cooled (FC) and field warmed (FW) measurements are shown. The transition temperature T_c is found to be $T_c = 218$ K and is extracted by fitting a Curie Weiss law to the high temperature data. (c) A low temperature magnetization M vs. field H loop recorded in the ferromagnetic phase. Inset - close up of a 50mT window around zero field. (d) TEM image of the layered structure of Fe₃GeTe₂. Inset - side view of the crystal structure. (e) Schematic of the STM tunnel junction experimental set up. Inset the Fe₃GeTe₂ crystal structure. (f) A topographic STM image of the Fe₃GeTe₂ surface (V = 30mV, I = 1nA). Inset -Typical STS spectrum recorded on the surface of Fe₃GeTe₂ (I = 1nA, V = 100mV).

diffraction to determine the crystal structure and in particular the exact stoichiometry of our samples, revealing an iron deficiency y = 0.14 (see suppl. section S2).

Magnetic characterisation (Fig. 1(a, b)) reveals a behaviour in field-cooled measurements consistent between the neutron scattering intensity of the Bragg peak and magnetisation, as well as with previous reports [11]. We find the magnetic transition at about 220K and a suppression of magnetisation for zero-field cooled measurements starting below 100K, Fig. 1(b), indicating stabilization of a domain structure which results in zero net magnetisation. In measurements of the magnetization M as a function of field H, shown in Fig. 1(c), we find magnetic hysteresis, as expected for a ferromagnet.

Cross-sectional TEM images (Fig. 1(d)) show the stacking sequence as expected from the crystal structure and the high quality of the samples, confirming the AB layer stacking. This type of stacking results in a Rashba-like band crossing at the K point and leads to the formation of topological line nodes [12].

Fig. 1(e) shows the measurement set up for the STM measurement and expected surface termination. Topographic imaging of the Fe_3GeTe_2 surface (Fig. 1(f)) reveals a hexagonal lattice which can be attributed to the uppermost Te lattice. The surface further exhibits a pronounced electronic inhomogeneity, which likely originates from the off-stoichiometry of the sample due to the iron deficiency. STS spectra show a pronounced gap around the Fermi level (inset of Fig. 1(f)).

To gain a better understanding of the inhomogeneity in our topographic images, we have simulated STM images for different types of defects. Fig. 2 shows DFT calculations and measured topographic images for the clean surface and two types of defects, an iron vacancy and a tellurium vacancy. Comparison of the DFT calculations with the STM image for the clean surface (Fig. 2(a)-(c)) suggests that the atomic corrugation in the STM images is due to the surface tellurium lattice. A vacancy of a tellurium atom (as indicated in Fig. 2(d)) results in a clear triangular-like defect (Fig. 2(e)) which can be easily identified in the topographic image (Fig. 2(f)). An Fe-vacancy, shown in Fig. 2(g), produces a more subtle depression of the local density of states, as shown in Fig. 2(h), which can nevertheless be easily identified in our STM topographies (Fig. 2(i)). This depression in the density of states is likely responsible for the inhomogeneity in topographic images as shown in Fig. 1(b), and has been shown to be responsible for the lowering in T_c as a function of Fe deficiency[8]. Interestingly, within our ferromagnetic DFT calculations for a monolayer of Fe_3GeTe_2 in a 3×3 supercell, we find that the total magnetic moment per Fe atom is reduced by the presence of a defect (2.004 $\mu_{\rm B}$ /Fe vs. 2.123 $\mu_{\rm B}$ /Fe without a defect, see the suppl. sect. S1). Previous studies by DFT have shown that the presence of defects can also have dramatic consequences for the magnetic interlayer coupling.[9]

B. Magnetic properties from STM and neutron scattering

We have studied the magnetism in Fe_3GeTe_2 using neutron scattering and spin-polarized STM to establish a better understanding of its magnetic properties, and the effect of the vacuum interface



FIG. 2: Identification of defects. (a) Top view of a 3×3 supercell of a monolayer of Fe₃GeTe₂. (b) Simulated STM topography of the supercell in (a). (c) STM topography of a region of the Fe₃GeTe₂ surface containing no defects. (d) Top view of supercell in (a) with a Te atom removed. (e) Simulated STM topography of the supercell in (d). (f) STM topography of the Fe₃GeTe₂ surface, showing a Te-site defect. (g) Same supercell as in (a), with an Fe atom removed, corresponding to y = 0.14 (i.e. Fe_{2.86}GeTe₂). (h) Simulated STM topography of the supercell in (g). (i) STM topography of the Fe₃GeTe₂ surface, showing an Fe-site defect. STM images (c), (f) and (i) taken with $V_s = 50$ mV, I = 50pA. Simulated images (b), (e) and (h) calculated for constant current and $V_s = 100$ mV.

which will become more important in the 2D limit.

Fig. 3(a) shows the inelastic neutron data obtained from a single crystal, with a clear magnon dispersion in a cut through the (0, 0, 2) peak starting from about 1meV. At long wavelengths, the magnetic excitations of an itinerant ferromagnet are well-described by a model of localized magnetic moments [13]. To describe the spin wave dispersion in Fe₃GeTe₂ at small q, we use an effective two-dimensional model of interacting Fe³⁺ ions on a honeycomb lattice with an easy-axis



FIG. 3: Magnon dispersion and magnetic imaging. (a) Inelastic neutron scattering measurement of the spin-wave dispersion of Fe₃GeTe₂ around $\mathbf{q} = (H, H, -2)$ for H = -0.2...0.2. The green line represents a parabolic fit to the data. The fit results in $J \approx 43(10)$ meV and $K \approx 0.6(1)$ meV (see main text for details). (b) A ferromagnetic domain wall imaged using spin polarized STM ($V_s = 100$ mV, $I_s = 125$ pA). The domain wall runs diagonally through the image. (c) The same area as in (b) imaged with a spin-polarized tip with the opposite spin polarization from that used in (b) ($V_s = 100$ mV, I = 125pA). (d) A line profile z(x) taken through the difference of images (b) and (c) perpendicular to the domain wall. The red line shows the expected profile from the neutron scattering measurement. (e) The height difference Δz recorded between oppositely polarized areas as a function of applied bias voltage. (f) dI/dV spectra (blue curve) recorded on either side of the domain wall shown in (b) and (c) ($V_s = 400$ mV, I = 250pA, $V_{\text{mod}} = 3$ mV). The spectroscopy setpoint was chosen at a bias voltage where the domain wall was not visible. The resulting spin polarization determined from the dI/dV spectra is also shown (red curve).

anisotropy,

$$\mathcal{H} = J \sum_{\mathbf{r}}^{j \in \{0,1,2\}} \mathbf{S}_A(\mathbf{r}) \cdot \mathbf{S}_B(\mathbf{r} + \mathbf{a}_j) + K[(\hat{S}_A^z(\mathbf{r}))^2 + (\hat{S}_B^z(\mathbf{r}))^2].$$
(1)

Here, J is the nearest neighbour interaction, K the magnetic anisotropy, $\mathbf{S}_{A,B}$ is the spin operator acting on site A or B and the vectors $\mathbf{a}_0 = (0,0)$, $\mathbf{a}_1 = (0,1)$ and $\mathbf{a}_2 = (1,1)$ span between the unit cells containing nearest neighbor spins (in the $P6_3/mmc$ space group). We have neglected further nearest neighbors since their effect in the limit of small $|\mathbf{q}|$ is a simple renormalization of the spin-wave velocity and anisotropy gap. Out of plane couplings in materials where the interlayer coupling is due to van der Waals interactions are expected to be significantly weaker than the in-plane couplings J and are therefore neglected. The eigenvalues obtained from the model are $E_{\mathbf{q}}^{\pm} = v_S \pm |\gamma_{\mathbf{q}}|$, with $v_S = -(3JS + 2KS)$ and $\gamma_{\mathbf{q}} = JS \sum_j e^{i\mathbf{q}\cdot\mathbf{a}_j}$, where S is the spin [14, 15]. With a wavevector of $\mathbf{q} = (H, H)$, where H is here used to parametrize the reciprocal lattice vector, the dispersion is quadratic for small $H, E \approx v_S \pm 3JS \pm 4\pi^2 JSH^2$. We have fit Gaussian peaks to a series of constant energy cuts in the (H, H, -2) plane through the MACS data to obtain the magnon dispersion. The exchange coupling can be determined from the prefactor, $4\pi^2 JS$, of the quadratic term. Taking the reduced value of S = 0.8(1), the fit yields $J \approx 43(10)$ meV and $K \approx 0.6(1)$ meV. The magnetic anisotropy is non-negligible, consistent with previous reports [5, 16], though somewhat smaller than the one reported previously from neutron scattering, whereas the exchange coupling is larger [17]. The difference in these values suggests a strong influence of the iron deficiency on the magnetic excitations: while our crystal has y = 0.14, the one studied in Ref. 17 had y = 0.25, almost twice that of our sample.

We can compare these values with the magnetic properties of the surface layer. Using spinpolarized STM[18, 19] we were able to directly image ferromagnetic domain walls at the surface of Fe_3GeTe_2 (Fig. 3(a)). The tip cluster was found to have a sufficiently small moment so that the tip magnetisation can be switched by the magnetic interaction with the sample. Manipulating the tip magnetisation in this way allowed us to image the same area with an oppositely polarized tip without having to apply an external magnetic field which would at the same time move the domain wall and polarize the sample. Fig. 3(c) shows an image with the same tip after the tip magnetisation has flipped. By taking the difference of the images, we obtain an image of only the magnetic contrast (Fig. 3(d)). From a line profile normal to the domain wall (Fig. 3(d)), we can analyze its width by fitting $z(x) = a + b \tanh(\pi(x - x_0)/\delta)$ to the data [18, 20–23], assuming that the tip magnetization is parallel to the out-of-plane direction and reverses by 180° when changing its direction. We obtain a domain wall width of $\delta = 2.6 \pm 0.5$ nm. The domain wall width found here is smaller than that typically found in ferromagnetic films which are usually on the order of $10 \sim 100$ nm [22, 23]. We can compare the domain wall width δ with the expected width δ_n using the exchange interaction J and magnetic anisotropy K obtained from neutron scattering through $\delta_n = \pi \sqrt{\frac{A}{K}}$ [24], where A is the exchange stiffness of the spins of the system being considered which is related to the exchange interaction J. For a 2D hexagonal honeycomb lattice, this expression becomes $\delta_n = \pi d_{nn} \sqrt{\frac{3J}{4K}}$ [20, 21] (see suppl. sect. S5), where d_{nn} is the nearest neighbour

distance between Fe atoms. By taking the values of J and K determined from the magnon dispersion in Fig. 3(a), we find a domain wall width $\delta_n = 6.0 \pm 1.2$ nm which is somewhat larger than what is obtained from a fit to our spin-polarized STM measurement (see fig. 3(d)). We note, however, that visually, the domain wall profile suggested by neutron scattering appears very similar to the observed one. The smaller domain wall width which we observe at the surface suggests that the exchange coupling J is smaller in the surface layer compared to the bulk, and the magnetic anisotropy K larger.

The apparent height of the domain wall in the spin polarized STM images exhibits a strong dependence on the bias voltage. From images recorded at different bias voltages, we can determine how the spin polarization of the sample's electronic structure evolves with energy. For images recorded with a low bias voltage (< 50mV) the domain wall shows the largest contrast. As the bias voltage is increased the magnetic contrast decreases and disappears at 400mV before reversing at even higher bias values. For negative applied bias the magnetic contrast remains more or less constant. By recording STS spectra on either side of the domain wall (hence with different magnetization directions of the sample) with a set point condition where the domain wall is not visible it is possible to extract the spin polarization as a function of bias voltage. The spectra recorded on either side of the domain wall are shown in Fig. 3(f). The polarization can be extracted from the spectra using the relation $P = \frac{g_{\uparrow\uparrow}(V) - g_{\uparrow\downarrow}(V)}{g_{\uparrow\uparrow}(V) + g_{\uparrow\downarrow}(V)}$ [18, 19] (Fig. 3(f)). The spin polarization shows a sharp peak of up to 20% spin polarization just below the Fermi level at an energy of -43 ± 6 mV.

C. Quasi-particle interference

To characterize the interplay between magnetism and the electronic structure, we have used quasi-particle interference imaging. Fig. 4(a)-(c) show the Fourier transform of quasi-particle interference maps $\tilde{g}(\mathbf{q}, V)$ at three different bias voltages (0mV, -60mV and -300mV), with the calculated band structure in the first Brillouin zone for comparison, integrated over k_z . There are clear hexagonal features in the experimental data, marked with arrows, with equivalent scattering vectors shown in the calculated band structure. All of the vectors observed experimentally can be assigned to scattering processes between bands with majority spin character. These bands are also the ones which exhibit a more two-dimensional character, as represented by the opacity in the calculation. Despite being strongly two-dimensional, the minority band centred around the Γ point is not visible in any of our measurements. The DFT calculations show that the spin-minority



FIG. 4: Quasiparticle interference imaging. (a-c) Six-fold symmetrised FFT of the differential conductance $\tilde{g}(\mathbf{q}, V)$ and calculated constant energy contours, showing majority (red) and minority (blue) spin bands averaged over 16 k_z values from 0 to $2\pi/c$, at (a) 0mV, (b) -60mV and (c) -300mV. Corresponding scattering vectors are marked on the experimental data and band structure calculation. (d) $\tilde{g}(\mathbf{q}, V)$ as a function of bias V for \mathbf{q} along Γ -K and Γ -M taken from similar $\tilde{g}(\mathbf{q}, V)$ measurements to (a)-(c), averaged between $q_x/q_y = \pm 0.378$ nm⁻¹ for Γ -K/ Γ -M. Points fitted to the band dispersions along both directions are also plotted, with parabolic fits to the highest four energy points for each direction giving an average effective mass of $m^* = 5.3 \pm 0.8m_e$ (Γ -M: $4.5m_e$, Γ -K: $6.1m_e$). (e) Second derivative with respect to \mathbf{q} of the differential conductance map, $\frac{\partial^2 \tilde{g}(\mathbf{q}, V)}{\partial q^2}$, as a function of bias for \mathbf{q} along Γ -K and Γ -M. The $\tilde{g}(\mathbf{q}, V)$ data was smoothed along the \mathbf{q} -direction with a window of 5.060nm⁻¹ before calculating the second derivative. (f) DFT calculation of the band structure of Fe₃GeTe₂, showing majority (red) and minority (blue) spin bands averaged over 16 k_z values from 0 to $2\pi/c$.

bands have predominantly iron character with little weight on the outer-most Te atoms, whereas the majority bands have Te character, suggesting that we fail to detect the minority band due to matrix element effects.

A cut of the differential conductance along K- Γ -M in the 2D Brillouin zone is shown in Fig. 4(d) between -200 mV and +200 mV. From the QPI cuts we can extract the properties of the hole-like band that crosses the Fermi level. By fitting a parabolic dispersion, Fig. 4(d), and assuming that it is due to intra-band scattering we determine that it has an effective mass

 $m^* = 5.3 \pm 0.8 m_e$ and a Fermi wavevector $k_f = 4.1 \pm 0.3 \text{nm}^{-1}$ along $\Gamma - \text{K}$ (8.2nm⁻¹ in q-space) which is in approximate agreement with that of a hexagonal pocket centered around Γ seen in ARPES measurements [7, 12, 25]. From the fits we find a band maximum at $106 \pm 25 \text{mV}$ above the Fermi level. To highlight sharp features, the second derivative with respect to **q** of the smoothed dI/dV data is plotted in Fig. 4(e). In these, the hole band is more readily observed with a maximum at around 150mV at the Γ point. We assign this band to the two-dimensional band at the same energy in the calculated k_z -integrated band structure, Fig. 4(f).

Using a spin-polarized tip allows to determine the spin character of the different bands. To this end, we have undertaken spin-polarized topographic imaging as a function of applied field. The relative orientation of the tip and sample magnetizations will switch at different fields (see Fig. 5(a-c)), enabling imaging of the quasi-particle scattering with parallel and anti-parallel alignment of their magnetizations. We observe a significant change in the topographic contrast when the tip and sample are not magnetized in the same direction anymore. Taking the difference of the Fourier transforms of topographies with parallel and antiparallel magnetization (Fig. 5(d)) reveals strong changes in the relative intensity of the scattering vectors. By comparing the Fourier transform with the quasi particle interference mapping at the Fermi level (Fig. 5(e)) we determine that the observed magnetic contrast is due to the spin-dependent imaging of Friedel oscillations between differently polarized bands at the Fermi level and thus reveals information about the spin polarization of the bands in the vicinity of the Fermi energy.

III. DISCUSSION

Our study of Fe₃GeTe₂ provides new insights from relating microscopic information obtained from low temperature scanning tunneling microscopy to bulk properties obtained from neutron scattering. We find that in the surface layer, the magnetic properties deviate slightly from those in the bulk, as might be expected from the 3D nature of some parts of the electronic structure. Comparison of the imaging of domain walls with the magnetic exchange interaction J and anisotropy K obtained from neutron scattering reveal a surprisingly good agreement. One would expect the ratio K/J to be slightly larger for the surface layer compared to the bulk due to a larger magnetic anisotropy and smaller exchange coupling: the smaller coordination number of atoms in the surface layer will lead to a decreased exchange energy J, while at the same time the lower symmetry is expected to result in a larger anisotropy K. It is well known from a number of systems that the



FIG. 5: Spin-polarized Quasi-particle interference. (a) SP-STM image $(30\text{mV}, 100\text{pA}, 41 \times 20\text{nm}^2)$ recorded with the tip polarized parallel to the sample by applying a 200mT field along the sample *c* axis. (b) Image of the same location with the same tip after the magnetization of the tip has been reversed relative to the sample by applying a 200mT field anti-parallel to the sample *c* axis. Slight differences in the topographic contrast can be observed. (c) The difference of (a) and (b). Sub-surface Fe clusters become apparent in the difference image. (d) The quasi-particle interference pattern recorded at the Fermi level (V = 0V). (e) Difference of the Fourier transform of topographies ($V_s = 30$ mV, $I_s = 100$ pA) recorded with opposite relative tip and sample spin orientations. Red vectors show up more intensely when the magnetization of tip and sample are parallel, and blue regions when they are antiparallel with respect to each other, showing the different spin-character of the bands.

magnetic anisotropy increases with reduced dimensionality [26]. The reduction in J in the surface layer is consistent with the lower Curie temperature $T_{\rm C}$ found in thin films and in the monolayer limit, where $T_{\rm C}$ is suppressed significantly [4, 5]. This system therefore confirms the previously observed trend that while the surface of a magnetic bulk material does not exhibit radically different magnetic properties, there are subtle differences [27].

From band structure calculations, we find that the Fermi surface is dominated by bands of spin

majority character with significant k_z -dispersion and quasi-2D bands of spin minority character. A comparison with quasi-particle interference imaging reveals dominant wave vectors which are broadly consistent with the band structure calculations. We use spin-polarized imaging to determine the spin-polarization of the bands near the Fermi energy, and find, consistent with the calculations, a hexagonal ring of scattering which we attribute to the bands with spin-majority character embedded in a rather broad distribution of electronic states with opposite spin character. While a more quantitative comparison, using e.g. a continuum calculation of the local density of states to model the quasi-particle interference[28], we expect that the large amount of scattering due to the iron deficiency and three-dimensionality of some of the bands will result in rather broad features[29, 30], as observed in the experiment - therefore not providing significant additional insight here.

IV. ACKNOWLEDGEMENTS

CT and PW acknowledge funding through EP/R031924/1 and EP/T031441/1, LCR through the Royal Commission for the Exhibition of 1851, IB through the International Max Planck Research School for Chemistry and Physics of Quantum Materials, and HL through the ISIS facility development studentship programme. Access to MACS was provided by the Center for High Resolution Neutron Scattering, a partnership between the National Institute of Standards and Technology and the National Science Foundation under Agreement No. DMR-1508249. Underpinning data will be made available at [31].

- [2] C. Gong, L. Li, Z. Li, H. Ji, A. Stern, Y. Xia, T. Cao, W. Bao, C. Wang, Y. Wang, et al., Nature 546, 265 (2017), ISSN 1476-4687, URL https://doi.org/10.1038/nature22060.
- [3] B. Huang, G. Clark, E. Navarro-Moratalla, D. R. Klein, R. Cheng, K. L. Seyler, D. Zhong,
 E. Schmidgall, M. A. McGuire, D. H. Cobden, et al., Nature 546, 270 (2017), ISSN 1476-4687,
 URL https://doi.org/10.1038/nature22391.
- [4] Z. Fei, B. Huang, P. Malinowski, W. Wang, T. Song, J. Sanchez, W. Yao, D. Xiao, X. Zhu, A. F. May, et al., Nat. Mater. 17, 778 (2018), URL https://doi.org/10.1038/s41563-018-0149-7.

^[1] J. He, S. Li, A. Bandyopadhyay, and T. Frauenheim, ACS NANO LETTERS 21, 3237 (2021), URL https://doi.org/10.1021/acs.nanolett.1c00520.

- [5] Y. Deng, Y. Yu, Y. Song, J. Zhang, N. Z. Wang, Z. Sun, Y. Yi, Y. Z. Wu, S. Wu, J. Zhu, et al., Nature 563, 94 (2018), ISSN 1476-4687, URL https://doi.org/10.1038/ s41586-018-0626-9.
- [6] M. Costa, N. M. R. Peres, J. Fernández-Rossier, and A. T. Costa, Phys. Rev. B 102, 014450 (2020), ISSN 2469-9950, 2469-9969, URL https://link.aps.org/doi/10.1103/PhysRevB. 102.014450.
- Y. Zhang, H. Lu, X. Zhu, S. Tan, W. Feng, Q. Liu, W. Zhang, Q. Chen, Y. Liu, X. Luo, et al., Sci. Adv.
 4, eaao6791 (2018), ISSN 2375-2548, URL http://advances.sciencemag.org/lookup/ doi/10.1126/sciadv.aao6791.
- [8] A. F. May, S. Calder, C. Cantoni, H. Cao, and M. A. McGuire, Phys. Rev. B 93, 014411 (2016), ISSN 2469-9950, 2469-9969, URL https://link.aps.org/doi/10.1103/PhysRevB. 93.014411.
- [9] X. Kong, G. D. Nguyen, J. Lee, C. Lee, S. Calder, A. F. May, Z. Gai, A.-P. Li, L. Liang, and T. Berlijn, Phys. Rev. Materials 4, 094403 (2020), URL https://link.aps.org/doi/10. 1103/PhysRevMaterials.4.094403.
- [10] H.-J. Deiseroth, K. Aleksandrov, C. Reiner, L. Kienle, and R. K. Kremer, European Journal of Inorganic Chemistry 2006 (2006), ISSN 1099-0682, URL https://onlinelibrary.wiley. com/doi/abs/10.1002/ejic.200501020.
- [11] C.-K. Tian, C. Wang, W. Ji, J.-C. Wang, T.-L. Xia, L. Wang, J.-J. Liu, H.-X. Zhang, and P. Cheng, Phys. Rev. B 99, 184428 (2019), URL https://link.aps.org/doi/10.1103/PhysRevB. 99.184428.
- [12] K. Kim, J. Seo, E. Lee, K.-T. Ko, B. S. Kim, B. G. Jang, J. M. Ok, J. Lee, Y. J. Jo, W. Kang, et al., Nature Materials 17, 794 (2018), ISSN 1476-4660, URL https://doi.org/10.1038/ s41563-018-0132-3.
- [13] S. W. Lovesey, <u>Theory of neutron scattering from condensed matter</u> (Clarendon Press, United Kingdom, 1984), ISBN 0-19-852017-4.
- [14] S. A. Owerre, Journal of Physics: Condensed Matter 28, 386001 (2016), ISSN 0953-8984, 1361-648X.
- [15] S. S. Pershoguba, S. Banerjee, J. C. Lashley, J. Park, H. Ågren, G. Aeppli, and A. V. Balatsky, Phys. Rev. X 8, 011010 (2018), URL https://link.aps.org/doi/10.1103/PhysRevX. 8.011010.

- [16] C. Tan, J. Lee, S.-G. Jung, T. Park, S. Albarakati, J. Partridge, M. R. Field, D. G. McCulloch, L. Wang, and C. Lee, Nature Communications 9, 1554 (2018), ISSN 2041-1723, URL https://doi.org/ 10.1038/s41467-018-04018-w.
- [17] S. Calder, A. I. Kolesnikov, and A. F. May, Phys. Rev. B 99, 094423 (2019), URL https://link. aps.org/doi/10.1103/PhysRevB.99.094423.
- [18] R. Wiesendanger, Rev. Mod. Phys. 81, 1495 (2009), URL https://link.aps.org/doi/10. 1103/RevModPhys.81.1495.
- [19] M. Bode, Reports on Progress in Physics 66, 523 (2003), URL https://doi.org/10.1088/ 0034-4885/66/4/203.
- [20] R. Moreno, R. F. L. Evans, S. Khmelevskyi, M. C. Muñoz, R. W. Chantrell, and O. Chubykalo-Fesenko, Phys. Rev. B 94, 104433 (2016), URL https://link.aps.org/doi/10.1103/ PhysRevB.94.104433.
- [21] A. Aharoni, <u>Introduction to the Theory of Ferromagnetism</u>, International Series of Monographs on Physics (Clarendon Press, 2000), ISBN 9780198508090, URL https://books.google.co. uk/books?id=Ru-z9b3WcfMC.
- [22] L. Berbil-Bautista, S. Krause, M. Bode, and R. Wiesendanger, Phys. Rev. B 76, 064411 (2007), URL https://link.aps.org/doi/10.1103/PhysRevB.76.064411.
- [23] R. Ravlić, M. Bode, A. Kubetzka, and R. Wiesendanger, Phys. Rev. B 67, 174411 (2003), URL https://link.aps.org/doi/10.1103/PhysRevB.67.174411.
- [24] S. Blundell, <u>Magnetism in condensed matter</u> (Oxford ; New York : Oxford University Press, 2001., 2001), includes bibliographical references and index., URL https://search.library.wisc. edu/catalog/999921680802121.
- [25] X. Xu, Y. W. Li, S. R. Duan, S. L. Zhang, Y. J. Chen, L. Kang, A. J. Liang, C. Chen, W. Xia, Y. Xu, et al., Phys. Rev. B 101, 201104 (2020), URL https://link.aps.org/doi/10.1103/ PhysRevB.101.201104.
- [26] P. Gambardella, Science 300, 1130 (2003), ISSN 00368075, 10959203, URL https://www. sciencemag.org/lookup/doi/10.1126/science.1082857.
- [27] C. Trainer, M. Songvilay, N. Qureshi, A. Stunault, C. M. Yim, E. E. Rodriguez, C. Heil, V. Tsurkan,
 M. A. Green, A. Loidl, et al., Phys. Rev. B 103, 024406 (2021), ISSN 2469-9950, 2469-9969, URL
 https://link.aps.org/doi/10.1103/PhysRevB.103.024406.
- [28] A. Kreisel, C. A. Marques, L. C. Rhodes, X. Kong, T. Berlijn, R. Fittipaldi, V. Granata, A. Vecchione,

P. Wahl, and P. J. Hirschfeld, npj Quantum Mater. 6, 100 (2021), ISSN 2397-4648, URL https: //www.nature.com/articles/s41535-021-00401-x.

- [29] L. C. Rhodes, M. D. Watson, T. K. Kim, and M. Eschrig, Phys. Rev. Lett. 123, 216404 (2019), ISSN 0031-9007, 1079-7114, URL https://link.aps.org/doi/10.1103/PhysRevLett. 123.216404.
- [30] C. A. Marques, M. S. Bahramy, C. Trainer, I. Marković, M. D. Watson, F. Mazzola, A. Rajan, T. D. Raub, P. D. C. King, and P. Wahl, Nat Commun 12, 6739 (2021), ISSN 2041-1723, URL https: //www.nature.com/articles/s41467-021-27082-1.
- [31] C. Trainer, O. Armitage, H. Lane, L. Rhodes, E. Chan, I. Benedičič, J. Rodriguez-Rivera, O. Fabelo, C. Stock, and P. Wahl (2022), Underpinning data for 'Relating spin-polarized STM imaging and inelastic neutron scattering in the van-der-Waals ferromagnet Fe₃GeTe₂', URL https: //dx.doi.org/<tobeinsertedonacceptance>.