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Complex electronic structure evolution of NdSb across the magnetic transition

Anup Pradhan Sakhya,^{1,*} Baokai Wang,^{2,*} Firoza Kabir,^{1,*} Cheng-Yi Huang,² M. Mofazzel Hosen,¹ Bahadur Singh,³ Sabin Regmi,¹ Gyanendra Dhakal,¹ Klauss Dimitri,¹ Milo Sprague,¹ Robert Smith,¹ Eric D. Bauer,⁴ Filip Ronning,⁵ Arun Bansil,² and Madhab Neupane^{1,†}

¹Department of Physics, University of Central Florida, Orlando, Florida 32816, USA

²Department of Physics, Northeastern University, Boston, Massachusetts 02115, USA

³Department of Condensed Matter Physics and Materials Science,

Tata Institute of Fundamental Research, Mumbai 400005, India

⁴ MPA-Q, Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA

⁵Institute for Materials Science, Los Alamos National Laboratory, Los Alamos, New Mexico 87545, USA

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The rare-earth monopnictide (REM) family, which hosts magnetic ground states with extreme magnetoresistance, has established itself as a fruitful playground for the discovery of interesting topological phases. Here, by using high-resolution angle-resolved photoemission spectroscopy complemented by first-principles density-functional-theory based modeling, we examine the evolution of the electronic structure of the candidate REM Dirac semimetal NdSb across the magnetic transition. A complex angel-wing-like band structure near the zone center along with arc-like features at the zone center and the zone corner are observed. This dramatic reconstruction of the itinerant bands around the zone center is shown to be driven by the magnetic transition: Specifically, the Nd 5d electron band backfolds at the $\overline{\Gamma}$ point and hybridizes with the Sb 5p hole bands in the antiferromagnetic phase. Our study indicates that antiferromagnetism plays an intricate role in the electronic structure of the REM family.

PACS numbers:

1. INTRODUCTION

The rare-earth monopnictide (REM) materials family provides interesting possibilities for realizing exotic Dirac states and giant magnetoresistance (MR) [1–12]. Several members of this family, such as CeSb, LaBi, CeBi have been theoretically predicted and experimentally shown to host non-trivial topological electronic states [4–6, 8– 12. Other members, of this family, however, such as LaSb, YSb, LuBi, YBi, LaAs are topologically trivial [13–19]. Although, the heavier members of the REM family assume an antiferromagnetic (AFM) or ferromagnetic (FM) ground state, much of the existing work [4–7, 9– 13, 16, 17 has focused on non-magnetic phases with a few exceptions [19–27]. Magnetic phases of REMs present a rich environment for exploring magnetic interactions and Dirac physics [24, 25]. For example, the heavyfermion system CeSb exhibits an exotic magnetic phase diagram as a function of the magnetic field, known as a devil's staircase [20, 28, 29]. A challenge in heavy-fermion physics is to understand the relationship between magnetism and electronic structure associated with the interplay of conduction and f electrons. With such a versatile ground-state, the REM family is drawing increasing interest in the condensed matter community as a playground for exploring emergent phenomena.

NdSb has been suggested to host a Dirac-like dispersion at the corners of the Brillouin zone (BZ) in its paramagnetic (PM) phase. It undergoes an AFM transition at 15 K under zero magnetic field [7]. NdSb, thus, is an interesting platform for investigating effects of mag-

netism on the electronic structure and topology in the REM family. Neutron diffraction experiments on NdSb polycrystals in zero field at 2 K show commensurate AFM ordering with Nd magnetic moments directed along the ordering wavevector [30]. Resistivity measurements indicate that NdSb possesses extreme magnetoresistance of $\sim 10^4$ %. NdSb displays a complex H-T phase diagram at high fields, with multiple first-order transitions [31]. However, the electronic structure of NdSb in the low-temperature regime (below 15 K) has not been reported. The present study attempts to do so and helps understand the role of antiferromagnetism in the electronic structure of NdSb.

Here, we report the evolution of the complex electronic band structure of NdSb using high-resolution angle-resolved photoemission spectroscopy (ARPES) across the magnetic transition. Interestingly, an angel-wing-like feature appears at the zone center due to the backfolding of the Nd 5d electron pocket present at the \overline{X} point in going from the PM to the AFM phase, which leads to hybridization between the Nd 5d and Sb 5p bands. Our study reveals the presence of Dirac-like states in both the PM and the AFM phases at the center and corners of the BZ. We find that arc-like feature appears as the material undergoes PM to AFM phase transition.

II. EXPERIMENTAL AND COMPUTATIONAL DETAILS

Single crystals of NdSb were grown by the Sn flux technique as described elsewhere [32]. The synchrotron based ARPES experiments were performed at the ALS

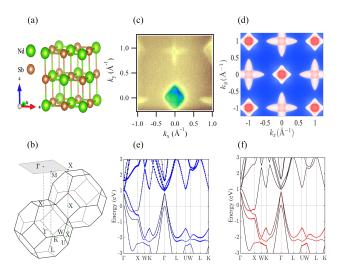


FIG. 1: Crystal and electronic structure of NdSb. (a) Rock-salt type crystal structure of NdSb. (b) Bulk and (001)-surface BZ. (c) Experimental Fermi surface in the PM phase taken at 20 K using a photon energy of 50 eV. (d) Theoretical Fermi surface (with SOC) in the PM phase. (e-f) Band structure (with SOC) along various high-symmetry lines.

beamlines 10.0.1.1 and 4.0.3 equipped with R4000 and R8000 hemispherical electron analyzer. The angular and energy resolution were set at better than 0.2° and 15 meV, respectively. High quality crystals were cut into small pieces and mounted on a copper post using a Torr seal. Ceramic posts were attached on top of the samples. After loading the sample into the main chamber, the chamber was cooled and pumped down for few hours. The crystals were cleaved at 20 K and the measurements were carried out over the temperature range of 7-30 K. The pressure in the UHV chamber was better than 1×10^{-10} torr. Electronic structure calculations were performed within the framework of the first-principles, density functional theory (DFT) using the projector augmented wave (PAW) method [33] as implemented in the VASP suite of codes [34, 35]. The exchange-correlation functional was treated using the SCAN meta-GGA [36] functional. An energy cutoff of 400 eV was used for the plane-wave basis set and a Γ -centered $11 \times 11 \times 11$ k-mesh was used for BZ integrations. The surface energy spectrum was obtained within the iterative Green function method using the WannierTools package [37–39]. For the antiferromagnetic (AFM) phase, an onsite Coulomb potential U = 14 eV was added to the f-orbital of Nd to move it away from the Fermi level. We constructed tight-binding models with atom-centered Wannier functions using the VASP2WANNIER90 interface both for the PM and the AFM phases [40].

III. RESULTS AND DISCUSSION

NdSb crystallizes in a rock-salt type crystal structure with space group Fm3m (Fig. 1(a)) with lattice constant, a = 6.319 Å [41]. The bulk BZ of NdSb and its projection on the (001) surface is shown in Fig. 1(b). Fig. 1(c) presents the Fermi surface (FS) map taken at 20 K, which shows the presence of spherical and diamondshaped pockets around the center $\overline{\Gamma}$ along with two concentric elliptical-electron-like pockets around the corner \overline{X} of the BZ consistent with the results of previous study [7]. The theoretical Fermi surface with SOC projected on the k_x - k_y plane, is shown in Fig. 1(d), and it is seen to be in excellent agreement with the corresponding experimental results of Fig. 1(c). This agreement implies significant k_z dispersion of the bulk bands. The associated broadening of the bulk features allows surface states to stand out more clearly in our spectra.

Band structure along the various k-directions with SOC is presented in Figs. 1(e-f), where the blue (red) circles represent contributions from Nd 5d (Sb 5p) orbitals. One can see that the two hole-pockets at the Γ point arise mainly from the Sb 5p orbitals, whereas the electron pocket at the X point involve a mixture of Nd 5d and Sb 5p orbitals. From the orbital character plots, we can see the presence of a band inversion between the Nd 5d and Sb 5p orbitals at the X point. The theoretical analysis of Wilson-loop spectra [42, 43] at $k_z = 0$ and $k_z = \pi$ are given in the SM, [44] and show a strong topological index $\mathbb{Z}_2 = 1$, suggesting that the material is topologically nontrivial.

Figs. 2(a) and 2(b) present the FS maps and the constant-energy-contours (CECs) in the PM (20 K) and AFM phases (7 K), respectively. A small circular pocket (arrow in Fig. 2(b), left panel), which is absent in the PM phase, appears at the center of the BZ in the AFM phase. This circular feature changes to an almost point like feature at around 60 meV below the Fermi level asserting the electron like nature of the band. At this binding energy, one can begin to resolve another larger circular pocket, which decreases in size on going further down to 120 meV, where the first circular pocket completely vanishes. Interestingly, at 300 meV below the Fermi level in the AFM phase, the circular pocket appears to be enlarged in size indicating the hole-like nature of the carriers at this binding energy. Moving further towards higher binding energies, the circular pocket enlarges, but the size of this hole pocket is smaller in the AFM phase compared to the PM phase, indicating that the hole band is pushed downwards in energy in the AFM phase.

In order to explore effects of magnetism on band dispersions, temperature-dependent measurements along the $\overline{\Gamma}-\overline{X}$ high-symmetry direction were performed for both the PM and the AFM phase (Fig. 3). In the PM phase, there are two hole-like bands crossing the Fermi level along with a linear Dirac-like band at the $\overline{\Gamma}$ point marked α , see SM [44] for a clearer view. With the onset of antiferromagnetism, significant changes in the elec-

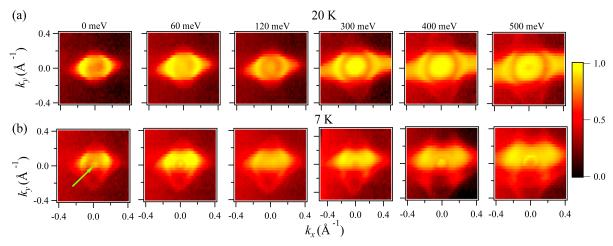


FIG. 2: Experimental Fermi surface and constant-energy-contours for (a) the paramagnetic phase (20 K) and (b) the antiferromagnetic phase (7 K). Green arrow points to the additional features that appear in the AFM phase. The measurements were performed using a photon energy of 57 eV.

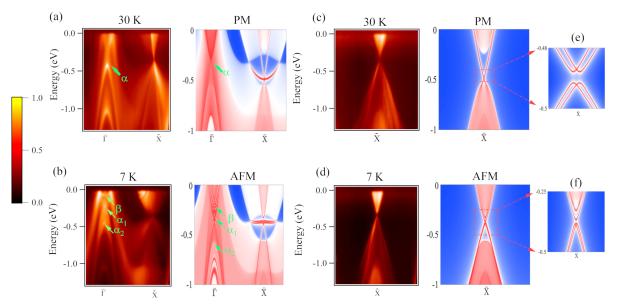


FIG. 3: Evolution of the electronic structure across the AFM transition. Experimental band dispersions along the $\overline{\Gamma}$ - \overline{X} direction using ARPES (left panel) and the DFT based (right panel) in (a) the PM and (b) the AFM phase. The green arrows identify the α , α_1 , α_2 and β bands. Experimental band dispersions along the \overline{M} - \overline{X} - \overline{M} direction (left) and the DFT-based results (right panel) in the (c) PM phase and (d) the AFM phase. The zoomed-in views of the rectangular regions in (c) and (d) are shown in (e) and (f), respectively. The measurements were performed using a photon energy of 50 eV.

tronic structure are observed as shown in Fig. 3(b). In the AFM phase, besides the α (relabeled as α_1), we also observed α_2 and β features. These two features appear inside the hybridization gap resulting from the mixing effect of the folded bands in the AFM phase. The band denoted as α_1 shows signature of a Dirac-like band in the AFM phase. The complex angel-wing-like structure β is robust against thermal recycling of the sample, indicating that it reflects effects of the magnetic transition, see SM [44] for details. The calculated band structures of the NdSb (001)-surface for the PM and AFM phases

are compared in Fig. 3 with the ARPES data where the bright-red bands are surface states. AFM calculations were performed by taking the ordering wavevector to lie along the c-axis. Comparison of theory and experiment shows that the observed Dirac-like α bands at the $\overline{\Gamma}$ point in the PM phase, α_1 in the AFM phase, and the Dirac-like bands at the \overline{X} point are all surface states [see SM for photon energy dependent measurements in the PM phase [44]. Our first-principles calculations reproduce the experimental ARPES data suggesting that the extra bands at the $\overline{\Gamma}$ point in the AFM phase arise from the

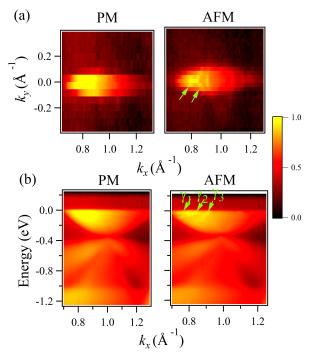


FIG. 4: Effect of the magnetic transition at the corner of the BZ. (a) Fermi surface plots around the zone corner in the PM phase (20 K) and the AFM phase (7 K). (b) Zoomed-in view of the temperature-dependent dispersion maps around the corner of the BZ in the PM and AFM phases. Dispersion maps were taken along the $\overline{\Gamma} - \overline{X} - \overline{\Gamma}$ direction. Green arrows point to additional bands in the AFM phase. The measurements were performed using a photon energy of 50 eV.

zone-folding effect [Detailed band structure with orbital characters given in SM [44], shows that the angel-wing-like structure arises mainly due to the Nd 5d states]. The Dirac-like bands, arrows in Fig. 3(b) have contributions from both the Nd 5d and the Sb 5p orbitals, suggesting that the Nd 5d electron-like pocket at \overline{X} backfolds at $\overline{\Gamma}$ in the AFM phase. We have unfolded the band structure in the AFM phase and compared it with PM bands and find both band structures to display band inversion at X point of the BZ. No other band inversion was found in the AFM phase, so that the AFM phase is also topologically nontrivial, see SM [44].

From our slab calculations, right panels of Figs. 3(a) and (3b), we can see the presence of two surface states at \overline{X} (red-colored bands) within the inverted band gap. The two surface states are tied to the two distinct X points in the bulk BZ when they are projected to the \overline{X} point on the surface BZ. Following Ref [6], a mirror Chern number of, C+ = +1 may be inferred for NdSb since the two surface states at \overline{X} are gapped through hybridization. The presence of one odd surface state at $\overline{\Gamma}$ and two surface states at \overline{X} , which is demonstrated in Fig. 3 (a) and 3(b), strongly supports the nontrivial band topology induced by the observed parity inversion. The Dirac-like state at \overline{X} can be seen more clearly when the measurements are

carried out along the $\overline{M} - \overline{X} - \overline{M}$ direction as shown in Fig. 3(c,d), in good agreement with a previous report [7]. Our DFT results, shown in the right panel of Fig. 3 (c,d), reproduce our ARPES results. Interestingly, our calculations find a small band gap at \overline{X} , see zoomed-in view in Fig. 3(e,f). However, the corresponding measured gap at \overline{X} is larger in both the magnetic and the paramagnetic phases. The Fermi level is also slightly shifted in the experiments compared to the DFT calculations. This discrepancy between the experimental and theory likely reflects inadequacy of the DFT generally in handling low carrier density systems [45–47]. For gaining more clarity into the effects of the magnetic transition at the corner of the BZ, a zoomed-in view of the Fermi surface at \overline{X} is shown in Fig. 4(a) for the PM and AFM phases, where additional features in the AFM Fermi surface (arrows in Fig. 4(a)) can be seen clearly. An electron-like pocket and a linear Dirac-like state is observed at \overline{X} in the PM as well as the AFM case, several extra features can be seen near the Fermi level γ_1 , γ_2 and γ_3 , which is absent in the PM phase. These features are reproducible with temperature recycling and exist only in the AFM phase (see SM [44]) for details, but are not produced in our DFT calculations. Further modeling with better treatment of electron correlation effects is needed to get a handle on this discrepancy between theory and experiment at the \overline{X} point. Recently, strikingly similar arc like features have been reported for NdBi, NdSb and CeBi using high-resolution ARPES measurements in the AFM phase [48, 49]. Wang et al. [50] were able to reproduce the Fermi arcs in the AFM phase of NdBi using DFT calculations. They discovered that AFM multi-q structures with two (2q) and three (3q) wave vectors gives rise to unconventional surface state pairs on (001) surface of NdBi that is in good agreement with the ARPES data.

IV. CONCLUSIONS

In summary, we have carried out an ARPES study along with parallel first-principles modeling of the electronic and magnetic structures of the rare-earth monopnictide NdSb in the PM and AFM phases. A significant reconstruction of the electronic states is found to take place with the onset of antiferromagnetic transition. A complex angel-wing-like band structure near the zone center and arc-like features at the zone center and the zone corner are observed. The theoretical analysis of Wilson-loop spectra shows a strong topological index $Z_2 = 1$, suggesting that the material is topologically nontrivial. We demonstrate the presence of a linear, Dirac-like band at $\overline{\Gamma}$ and two Dirac-like bands at the X point in the BZ in both the PM and the AFM phase, indicating the non-trivial topology of the material. Our study, thus, highlights the interplay between magnetism and topology in the rareearth monopnictides.

Note added: During the reviewing process of our paper, we became aware of a strikingly similar study showing

the presence of Fermi arcs in NdBi, NdSb and CeBi in the antiferromagnetic phase [48, 49].

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- * These authors contributed equally in this work.

 † corresponding author: Madhab.Neupane@ucf.edu
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