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High Critical Field Superconductivity at Ambient Pressure in MoB₂ Stabilized in the P6/mmm Structure via Nb Substitution

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Recently it was discovered that, under elevated pressures, MoB₂ exhibits superconductivity at a critical temperature, T_c , as high as 32 K. The superconductivity appears to develop following a pressure-induced structural transition from the ambient pressure $R\bar{3}m$ structure to an MgB₂like P6/mmm structure. This suggests that remarkably high T_c values among diborides are not restricted to MgB₂ as previously appeared to be the case, and that similarly high T_c values may occur in other diborides if they can be coerced into the MgB₂ structure. In this work, we show that density-functional theory calculations indicate that phonon free energy stabilizes the P6/mmm structure over the R $\bar{3}m$ at high temperatures across the Nb_xMo_{1-x}B₂ series. X-ray diffraction confirms that the synthesized Nb-substituted MoB₂ adopts the MgB₂ crystal structure. High-field electrical resistivity measurements and specific heat measurements demonstrate that Nb_xMo_{1-x}B₂ exhibits superconductivity with T_c as high as 8 K and high critical fields approaching 6 T.

I. INTRODUCTION

The discovery of high-temperature superconductivity in the binary hydrides [1-3] reignited the dream of achieving room-temperature superconductivity through conventional electron-phonon coupling. Although these materials display T_c values of upwards of 100 K, very high pressures and complicated experimental setup are required to stabilize them. Recent efforts in lowering the pressure values have resulted in theoretical [4-6]and experimental [7] works where a third element stabilizes the clathrate-like cage of hydrogen atoms at much lower pressures. Another promising path for achieving high-temperature superconductivity is to search for superconducting materials containing light elements. The AlB₂-type diborides have been of particular interest since the discovery of (record-breaking at the time) ambient pressure conventional superconductivity $(T_c = 39 \text{ K})$ in MgB_2 [8].

Recently, Pei et al. [9] discovered high pressureinduced superconductivity in MoB₂ ($T_c = 32$ K above P = 60 GPa, where the structure changes from R3m to P6/mmm). The P6/mmm MoB₂ phase and the hydride superconductors, despite being different chemical systems share some similarities. Like the high-pressure superconducting hydrides[10, 11], P6/mmm MoB₂ does not occur on the ambient pressure DFT convex hull, and the perfect stoichiometric structure is dynamically unstable at low pressures. Our own similar work on WB₂ ($T_c = 17$ K above P = 50 GPa) [12], has focused our interest in finding such superconductivity stabilized at room pressure in the metal diborides. Since NbB₂ occurs with P6/mmm symmetry, prototype AlB₂ structure, space group 191 (in which MoB₂ under pressure exhibits superconductivity at 30 K), we investigated the phase stability of Nb_{1-x}Mo_xB₂ vs Mo concentration, by Density Functional Theory (DFT) calculations and experimentally, by arc-melting of the constituents and characterization measurements as discussed below.

An early experimental work by Kuz'ma [13], in which samples were formed at 1400 °C, found that $Nb_{1-x}Mo_xB_2$ remained in the P6/mmm, AlB₂ structure beginning at pure NbB₂ (x = 0) and up to x = 0.24. Kuz'ma went on to say that, based on their results, "continuous series of solid solutions may form between the isostructural compounds NbB_2 - $\mathrm{MoB}_2"$ at other temperatures. According to the Materials Platform for Data Science, the melting point of NbB_2 is just over 3000 °C. MoB_2 forms peritectally around 2350 °C [14]. As will be seen below in the Results section, arc-melting (an intrinsically high temperature process) of the constituents in $Nb_{1-x}Mo_xB_2$ indicates that these pseudobinary compounds remain in the P6/mmm structure upon cooling all the way from pure NbB_2 up to x=0.9. Thus, the Alflux grown MoB_2 of Pei et al., which formed in the R $\bar{3}m$ structure below 1500 °C and transforms to P6/mmm above 60 GPa, is readily stabilized at room pressure in the hexagonal P6/mmm AlB₂ structure with minor additions of Nb.

This work presents DFT calculations elucidating the effect of Nb addition and temperature on the stability of the P6/mmm MoB₂ phase. Coupled with these calculations, we present x-ray diffraction, resistivity, specific heat at low temperatures, and upper critical magnetic field, Hc2(0) for arc-melted samples of Nb_{1-x}Mo_xB₂, x= 0.25, 0.50, 0.75, and 0.9 – all of which show essentially

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II. METHODS

For performing the density functional theory calculations, we use VASP [16–19]. VASP calculations were performed using the projector augmented wave pseudopotentials [20] and Perdew-Burke-Ernzerhof (PBE) [21] generalized gradient approximation for the exchangecorrelation functional. A k-point density of 60 \AA^{-1} and plane wave cut-off of 520 eV was used in all the calculations. To estimate phonon entropy contributions to the free energy, we first calculate the phonon frequencies for a supercell containing 24 atoms in VASP using perturbation theory. Then the phonon density of states was obtained from the phonon frequencies by using the Gaussian smearing method, similar to the one adopted by Lim, et al. [22]. For smearing the electrons in the DFT calculations, we use the Methfessel-Paxton smearing with a σ of 0.1 eV for NbB₂, Nb_{0.75}Mo_{0.25}B₂, and $Nb_{0.5}Mo_{0.5}B_2 P6/mmm$ phases and for R3m MoB₂. For $P6/mmm Nb_{0.25}Mo_{0.75}B_2$, and MoB_2 phases we use the Fermi smearing with smearing values of 0.1, 0.25, and 0.5 eV, as discussed below.

For experimental measurements, $Nb_{1-x}Mo_xB_2$ (x = (0.25, 0.5, 0.75, 1) samples were formed via arc melting the constituent elements. A reasonable estimate for the temperature range for arc melting the constituent elements is between 2400° and 2700°. Resistivity measurements were done on a bulk sample with dimensions $\sim 4.2 \times 3.5 \times 0.4$ mm³ which was set up in Kelvin sensing configuration for 4-probe measurements. Quantum Design Physical Property Measurement System (PPMS) was used along with a Keithley 6221/2182A Delta Mode System for temperature control and voltage measurements. Current of 1 mA was used for all the measurements on this sample. The sample was idealized to be rectangular with uniform thickness for the measurements. Small-scale errors from these assumptions were not taken into consideration. Specific heat at low temperatures was measured using standard time constant methodology [23].

III. RESULTS AND DISCUSSION

A. DFT

In this section, we will discuss the DFT calculated stability of the P6/mmm phase in $Nb_{1-x}Mo_xB_2$ alloys at 0K and high temperatures. At 0K, it is determined by the compound convex hull construction. To estimate



FIG. 1. Calculated free energy of Nb_{1-x}Mo_xB₂ as a function of composition and temperature. The free energy was calculated with respect to 0K free energy of stable NbB₂ (P6/mmm) and MoB₂ (R $\bar{3}$ m) phases. The blue dots represent the P6/mmm phase and the red dots represent the R $\bar{3}$ m phase. Only vibrational entropy contribution to the free energy was considered. The black line is the convex hull line at various temperatures. Electron smearing of 0.5 eV was used for the phonon calculation of P6/mmm MoB₂ and Nb_{0.25}Mo_{0.75}B₂.

stability at high temperatures, we calculate the free energy of the compound and its competing phases, considering only the phonon contributions to entropy as a function of composition and temperature. We calculate the phonon dispersion curves for P6/mmm Nb_{1-x}Mo_xB₂ (x = 0.25, 0.5, 0.75, 1) and for R $\bar{3}$ m MoB₂ using the supercell method in VASP. Figure 1 shows the DFT calculated free energy of Nb_{1-x}Mo_xB₂ as a function of composition at three temperatures, T = 0 K, 1500 K and 2000 K. The figure also shows the structure of the supercells used in the DFT calculations. From this figure at 0 K, the P6/mmm Nb_{1-x}Mo_xB₂ is not stable (for x = 0.25, 0.5, 0.75, 1) with respect to decomposition to the stable end-point phases - NbB₂ (P6/mmm) and MoB₂ (R $\bar{3}$ m).

In DFT calculations, electronic states near the Fermi energy are generally smeared out to help with the convergence of numerical integrals [24, 25]. The smearing of electronic states is especially used for metals where the occupation of electrons discontinuously changes from 1 to 0 at the Fermi energy at T=0K. For low values of electron smearing ($\sigma = 0.1$ eV) typically used in the DFT calculations, stoichiometric P6/mmm MoB₂ and Nb_{0.25}Mo_{0.75}B₂ exhibits dynamical instabilities, meaning the calculated phonon dispersion curves have imaginary phonons. On the other hand the calculated phonons



FIG. 2. (a) P6/mmm MoB₂ phonon dispersion curves and (b) Band structure diagram for varying electron smearing values. With increasing electron smearing the P6/mmm phase of MoB₂ becomes dynamically stable. Notice the downward shift of the Fermi level with increasing smearing.

for Nb_{0.75}Mo_{0.25}B₂ and Nb_{0.5}Mo_{0.5}B₂ are real and the structures are dynamically stable, indicating that the P6/mmm phases can be stabilized at high temperatures by entropy. Stable phonons for the P6/mmm MoB₂ and Nb_{0.25}Mo_{0.75}B₂ phases can be obtained by using high smearing values ($\sigma = 0.5$ eV, fermi smearing) for the electrons in the DFT calculations. A similar scheme with smearing value as high as ≈ 2.7 eV was used by Babu, and Guo [26] and Ivashchenko *et al.* [27] for stabilizing the phonons of the delta phase NbN.

Figure 2 shows the phonon dispersion curves and band structure for MoB₂ P6/mmm phase at various electron smearing values. The Fermi smearing method was used in the DFT calculations. Imaginary acoustic phonon frequencies are present at the 'M' and 'L' high symmetry points and also along 'L-M' path. From Fig. 2(a) the P6/mmm MoB₂ phase becomes dynamically stable at large electron smearing values, causing a downward shift of the Fermi energy. A similar downward shift of Fermi energy can also be expected in structures with Mo vacancies. We observe an analogous trend of stable phonons for high smearing values in Nb_{0.25}Mo_{0.75}B₂. For δ -NbN it has been argued that the large smearing values captures, to a first-order approximation, the effect of temperature and disorder due to the nitrogen vacancies present in the experimental delta phase NbN samples [26, 27].

Using the above-discussed smearing values for P6/mmm MoB₂ and Nb_{0.25}Mo_{0.75}B₂, we calculate the high-temperature free energy for P6/mmm Nb_{1-x}Mo_xB₂ alloys and R3m MoB₂. Fig. 1 also shows the estimated compound convex hull for 1500 and 2000 K. At higher temperatures, the doped P6/mmm Nb_{1-x}Mo_xB₂ (x=0.25,0.5) phases are on the convex hull. The distance from the convex hull for Nb_{0.25}Mo_{0.75}B₂ also decreases and is close to stability at high temperatures. We believe that our Nb_{0.25}Mo_{0.75}B₂ and MoB₂ arc-melted samples are dynamically stabilized by disorder. Thus, the P6/mmm Nb_{1-x}Mo_xB₂ is stabilized with respect to decomposition by the phonon entropy and can be obtained experimentally at high temperatures.

B. X-ray diffraction

X-ray diffraction (XRD) results for arc-melted MoB₂ and Nb_{1-x}Mo_xB₂, x = 0.9, along with the calculated xray patterns for the low temperature structure R $\bar{3}$ m of MoB₂ and the high temperature P6/mmm structure for MoB₂, are shown in Fig. 3. Clearly, the arc-melted MoB₂ occurs in the R $\bar{3}$ m structure, while only 10% Nb stabilizes Nb_{0.1}Mo_{0.9}B₂ in the P6/mmm structure. Figure 4 shows data for Nb_{1-x}Mo_xB₂, x = 0.25, 0.50, and 0.75, and pure Nb, and calculated patterns for both MoB₂ and NbB₂ in the P6/mmm structure. The Nb_{1-x}Mo_xB₂ samples, x =0.25, 0.50, and 0.75, occur in the P6/mmm structure, with no evidence of second phase Nb.

The lattice parameters for all four Nb_{1-x}Mo_xB₂, x = 0.25, 0.50, 0.75, and 0.9 as well as for the calculated end compositions, NbB₂ and MoB₂, in the hexagonal P6/mmm structure (as well as measured parameters discussed below) are shown in Table I. As can be seen, the substitution of Mo by Nb does not lead to large lattice parameter changes.

C. Resistivity

The onset T_c in resistivity measurement for Nb_{0.25}Mo_{0.75}B₂ was found to be ~ 8 K in accordance with specific heat measurements. All the other samples (Nb_{1-x}Mo_xB₂, x = 0.25, 0.50, 0.75, and 0.9) show a onset T_c in resistivity measurement of less than 8 K. The residual resistivity ratios ($R(300 \text{ K})/R(T_{c+})$) for x = 0.25, 0.5, 0.75, and 0.9 are all between 1.08 and

Material	from ρ vs T (K)		ΔC	BBB	calculated Å		measured Å		H_{c2}	γ	DOS	β	Θ_D
	T_c^{onset}	$T_c^{\rm mid}$	$\overline{\gamma T_c}$	1.1111	a	c	a	c	(T)	$(\mathrm{mJ}/\mathrm{mol}\mathrm{K}^2)$		$\left(mJ/molK^{4} ight)$	(K)
MoB_2				2.74	3.028	3.3239					1.5213		
$\mathrm{Nb}_{0.1}\mathrm{Mo}_{0.9}\mathrm{B}_2$	7.82	6.91	0.32	1.11			3.0579	3.3533	$6.3{\pm}0.3$	3.31		0.0124	715
$Nb_{0.25}Mo_{0.75}B_2$	8.15	6.85	0.99	1.08	3.051	3.3323	3.0546	3.2637	$6.7 {\pm} 0.3$	3.80	1.36	0.0142	625
$\mathrm{Nb}_{0.5}\mathrm{Mo}_{0.5}\mathrm{B}_2$	6.51	5.25	0.44	1.15	3.0918	3.291	3.0812	3.2989	$5.1{\pm}0.3$	3.27	1.26	0.0128	693
$Nb_{0.75}Mo_{0.25}B_2$	6.98	5.88	0.27	1.31	3.100	3.3243	3.1053	3.3026	$2.2{\pm}0.3$	2.88	0.88	0.0105	845
NbB_2					3.1186	3.3385	3.1024[28]	3.3196[<mark>28</mark>]		1.99	1.06	0.0096	846

TABLE I. Parameters for Nb_{1-x}Mo_xB₂ P6/mmm phase, x = 0, 0.25, 0.50, 0.75, 0.9 and 1. DOS is states per eV per formula unit.



FIG. 3. X-ray patterns of arc-melted MoB₂ (upper trace, green) and arc-melted Nb_{0.1}Mo_{0.9}B₂ (third trace from the top, blue) compared to calculated patterns for R-3m structure MoB₂ (chartreuse, space group 166, second trace) and for P6/mmm structure MoB₂ (red, space group 191, bottom trace.) Although there are reflections in the measured patterns that do not agree with the calculated ones (e. g. there are extra lines at 30.0° and 45.4° 2θ in the arc-melted MoB₂ data which may be from a second phase of the P6/mmm structure), clearly the measured data support the conclusions that a.) arc-melted MoB₂ occurs primarily in the R-3m structure while 10% Nb doping (Nb_{0.1}Mo_{0.9}B₂) causes the arc-melted sample to occur essentially entirely in the P6/mmm structure.

1.31, reflecting the scattering caused by alloying with Nb. Pure MoB_2 has RRR=2.74.

The T_c 's obtained for each Nb_xMo_{1-x}B₂ compound are around four times smaller than the 32 K observed in MoB₂ under high pressure (109.7 GPa) [9] and on par with $T_c \sim 9$ K in non-stoichiometric NbB₂ [28, 29]. Stoichiometric NbB₂, by recent accounts, is not a superconductor [28, 30, 31]. The finite T_c observed in the non-stoichiometric compounds containing either excess boron or niobium vacancies appears alongside a notable expansion of the *c*-axis lattice parameter. Shifts in the lattice parameter can indicate changes in the electronic structure, lattice vibrations, and electron-phonon coupling that ultimately affect superconductivity. Among these potential changes, increasing the electron-phonon



FIG. 4. Measured x-ray diffraction patterns for arc-melted Nb_{1-x}Mo_xB₂, x = 0.25, 0.50, and 0.75, and calculated patterns for both MoB₂ and NbB₂ in the P6/mmm structure, as well as for pure Nb. Again, all of the Nb_{1-x}Mo_xB₂ samples, x = 0.25, 0.50, and 0.75, occur in the P6/mmm structure, with no evidence of second phase Nb. Two second phase lines are, however, observed. In Nb_{0.25}Mo_{0.75}B₂ there is a second phase line at 23.9° 2 θ ; in Nb_{0.5}Mo_{0.5}B₂ there is a second phase line at 42.65° 2 θ . As shown, neither of these lines match the Nb x-ray pattern.

coupling to boron-p optical phonons offers a disproportionately large contribution to T_c in MoB₂ [32]. In Nb_xMo_{1-x}B₂, however, Nb primarily helps stabilize the P6/mmm structure at low pressures and does not recreate other conditions needed for an even higher T_c observed in MoB₂ under high pressure.

D. Specific Heat

The specific heat data of Nb_{1-x}Mo_xB₂, x = 0, 0.25, 0.50, 0.75, 0.9 are shown in Fig. 5. The derived values for $\gamma \ [= \lim_{T \to 0} C/T$, where $\gamma \propto N(0)$, the electronic density of states at the Fermi energy] and $\Delta C/(\gamma T_c)$ (a measure of the amount of bulk superconductivity, with $\Delta C/(\gamma T_c) = 1.43$ for BCS superconductivity or 1.64 for the unconventional, iron based superconductor[33] FeSe



FIG. 5. Specific heat data of $Nb_{1-x}Mo_xB_2$, x = 0, 0.25, 0.50, 0.75, 0.9.

 $T_c = 8.1 \,\mathrm{K}$ are listed in Table I. Based on the rough approximation that $\Delta C/(\gamma T_c) \approx 1.5$ for 100% bulk superconductivity, the specific heat data show that alloying MoB_2 with Nb and stabilizing the P6/mmm structure at ambient pressure creates between 20% to 70%bulk superconductivity in the pseudobinary alloys, with T_c 's between 6.5 and 8.15 K. Since R³m structure MoB₂ was found [9] to be superconducting above 60 GPa after transforming to P6/mmm, it seems likely that the small amounts of Nb in our sample simply act to stabilize the favorable structure for superconductivity. We note that these samples show no evidence of any second phase of Nb in the x-ray diffraction patterns (Figs. 3 and 4). Thus, these results indicate that Nb alloying into MoB₂ has succeeded in stabilizing superconductivity at ambient pressure in the same structure (P6/mmm) where Pei et al. found [9] superconductivity at high pressure, with the largest fraction of induced superconductivity occurring at only 25% Nb content. We suspect that the higher T_c value shown by our $Nb_{0.25}Mo_{0.75}B_2$ sample might be because of certain aspects of the ordering of the Nb and Mo atoms in the sample.

The chemical homogeneity of our samples can be inferred from the width of high angle XRD lines (Fig. 4) and from the width of the specific heat anomaly at the the transition (Fig. 5). The width of the specific heat anomaly, ΔC , clearly indicates a distribution of concentration for all our samples. The highest T_c alloy, Nb_{0.25}Mo_{0.75}B₂, perhaps demonstrates a lower level of homogeneity as indicated by the wide high-angle XRD lines (at $\approx 108^{\circ}$, full width half maximum $\approx 1^{\circ}$) and specific heat anomaly, as compared to the homogeneity of Nb_{0.5}Mo_{0.5}B₂, and Nb_{0.75}Mo_{0.25}B₂.



FIG. 6. Resistivity dependence of Nb_{0.25}Mo_{0.75}B₂ (a) on temperature for different magnetic fields, and (b) on magnetic field at constant temperature of 2K. T_c is found to be 8.03 K. (c) Upper critical field values for H_{c2}(0) for Nb_{0.25}Mo_{0.75}B₂ extracted from (a) and (b). The solid line shows the fitting to Ginzburg-Landau formula given by: $H_{c2} = H_{c2}(0)[(1 - t^2)/(1 + t^2)]$, where t is the temperature normalized by the zero-field transition temperature [9]. This fitting gives $H_{c2}(0)$ of 6.71 T.

E. Upper Critical Field

Figure 6(a) shows the suppression of transition temperature with applied field in $Nb_{0.25}Mo_{0.75}B_2$. Resistivity dependence of $Nb_{0.25}Mo_{0.75}B_2$ on magnetic field at 2 K is shown in Fig. 6(b). In Fig. 6(c), the experimental data are fit to the empirical formula given by $H_{c2} = H_{c2}(0)[(1-t^2)/(1+t^2)]$, where, $t = T/T_c$ [9]. Using this fit, the upper critical field at T = 0, $H_{c2}(0)$, is found to be 6.71 T. This unusually large critical field of $Nb_{0.25}Mo_{0.75}B_2$ is interesting. There are other conventional superconductors with a relatively large upper critical field to Tc ratio. For example NbC has a $H_{c2} \approx 2 \text{ T}[34]$ $(T_c = 11.5 \text{ K})$ and NbTi has a $H_{c2} \approx 15 \text{ T}[35] (T_c = 9 \text{ K})$. Pei et al., in their measurements of pure MoB_2 , transformed by high pressure to form in the P6/mmm structure with a Tc of about 32 K, found $H_{c2}(0)$ of only 9.4 T whereas the $32 \text{ K} T_c$ is a factor of four higher than that in $Nb_{0.25}Mo_{0.75}B_2$. Our work [12] on WB_2 under high pressure which, due to defects, has a similar structure to the P6/mmm, showed $H_{c2}(0) = 2.4$ T and $T_c = 17$ K, again arguing for $Nb_{0.25}Mo_{0.75}B_2$ - due to its unusually high $H_{c2}(0)$.

IV. CONCLUSIONS

In summary, we were able to successfully stabilize the high pressure P6/mmm phase of MoB_2 at ambient pressure by doping with Nb. The Nb-stabilized MoB_2 P6/mmm samples are superconducting with the highest T_c of 8 K for Nb_{0.25}Mo_{0.75}B₂. Density functional theories confirm that the favorable P6/mmm structure, also believed responsible for 18K superconductivity in WB₂[12], is likely to be stabilized entropically at ambient pressure. The doping of other borides by Nb may therefore also help to stabilize the P6/mmm and lead to higher transition temperatures

We note in closing that the relatively high $H_{c2}(0) \simeq 6.7T$ of Nb_{0.25}Mo_{0.75}B₂ (Nb has a similar T_c with an H_{c2} of only 4.4T) makes it a suitable candidate for coating the inside of Nb superconducting radio-frequency particle accelerators. This high H_{c2} coating could help further improve cavity performance.

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