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A-type antiferromagnetic order in semiconducting EuMg₂Sb₂ single crystals

Santanu Pakhira,¹ Farhan Islam,^{1,2} Evan O'Leary,^{1,2} M. A. Tanatar,^{1,2} Thomas Heitmann,³ Lin-Lin Wang,¹ R. Prozorov,^{1,2} Adam Kaminski,^{1,2} David Vaknin,^{1,2} and D. C. Johnston^{1,2}

¹Ames Laboratory, Iowa State University, Ames, Iowa 50011, USA
²Department of Physics and Astronomy, Iowa State University, Ames, Iowa 50011, USA
³The Missouri Research Reactor and Department of Physics and Astronomy,
University of Missouri, Columbia, Missouri 65211, USA
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Eu-based Zintl-phase materials EuA_2Pn_2 (A = Mg, In, Cd, Zn; Pn = Bi, Sb, As, P) have generated significant recent interest owing to the complex interplay of magnetism and band topology. Here, we investigated the crystallographic, magnetic, and electronic properties of the layered Zintlphase single crystals of EuMg₂Sb₂ with the trigonal CaAl₂Si₂ crystal structure (space group $P\overline{3}m1$). Electrical resistivity measurements complemented with angle-resolved photoemission spectroscopy (ARPES) studies and density functional theory (DFT) calculations find an activated behavior with intrinsic conductivity at high temperatures indicating a semiconducting electronic ground state with a narrow energy gap of 370 meV. Magnetic susceptibility and zero-field heat capacity measurements indicate that the compound undergoes antiferromagnetic (AFM) ordering at the Néel temperature $T_{\rm N} = 8.0(2)$ K. Zero-field neutron-diffraction measurements reveal that the AFM ordering is A-type where the Eu spins (Eu²⁺, S = 7/2) arranged in ab-plane layers are aligned ferromagnetically in the ab plane and the Eu spins in adjacent layers are aligned antiferromagnetically. Eu-moment reorientation within the ab planes in the trigonal AFM domains associated with a very weak inplane magnetic anisotropy is also evident below $T_{\rm N}$ at low fields < 0.05 T. Although isostructural semimetallic EuMg₂Bi₂ is reported to host Dirac surface states, the observation of narrow-gap semiconducting behavior in EuMg₂Sb₂ implies a strong role of spin-orbit coupling (SOC) in tuning the electronic states of these materials. Our DFT studies also suggest, besides the SOC, the more electronegative and smaller Sb than Bi shifts the low-lying conduction bands along the Γ -A direction to higher energy, resulting in an indirect bulk band gap between the Γ and M points for EuMg₂Sb₂.

I. INTRODUCTION

Tuning of electronic band structure through coupling between lattice, charge, and electronic degrees of freedom is key to recent discoveries in condensed-matter physics and material science. Materials with nontrivial band topology have been extensively studied owing to their possible applications in dissipationless electronic transport [1–4]. Many rare-earth-based magnetic materials also belong to this category and have been reported to host novel electronic states through a complex interplay of magnetism, spin-orbit coupling (SOC), and band topology [5–8]. For materials on the verge of timereversal-symmetry breaking associated with magnetism and the presence or absence of SOC, the electronic states of these materials can be tuned between metallic, insulating, semimetallic, narrow-gap and wide-gap semiconducting behavior.

In recent years, studies of Eu-based intermetallic compounds carried out in the search for novel electronic states have been reported [9–13]. EuMg₂Bi₂ is one such material which belongs to a class of rare-earth-based compounds that exhibit novel electronic states arising from a complex interplay of magnetism and electronband topology [14–16]. It has recently gained interest because it possesses Dirac points located at different energies with respect to the Fermi energy [14]. EuMg₂ Pn_2 (Pn = P, As, Sb, or Bi) crystallize in the trigonal CaAl₂Si₂ crystal structure with space group $P\overline{3}m1$, (No.

164) [17]. The Eu atoms form a triangular lattice in the ab plane and these planes are stacked along the c axis. The Mg and Pn atoms are arranged in two triangular layers between adjacent layers of Eu atoms. EuMg₂Bi₂ is a semimetal and exhibits A-type antiferromagnetic (AFM) order below the Néel temperature $T_{\rm N}=6.7~{\rm K}$ [15, 18]. In this case the Eu moments within an a plane are ferromagnetically aligned in the ab plane, where the moments in adjacent Eu planes along the c axis are aligned antiferromagnetically [18]. Moment reorientation within the ab plane associated with weak in-plane anisotropy was also observed at low fields below $T_{\rm N}$ [18]. Recently, it was shown that substituting Ca for Eu significantly affects the electronic states where a semimetal-to-semiconductor transition occurs [19]. This indicates that EuMg_2Pn_2 compounds offer a fertile ground to study the tunability of the electronic states in these materials.

EuMg₂Sb₂ is isostructural to EuMg₂Bi₂. Polycrystalline EuMg₂Sb₂ was reported to exhibit AFM ordering below $T_{\rm N}=8.2(3)$ K based on magnetic susceptibility χ measurements in the magnetic field H=0.002 T [20]. No information about single-crystal growth, the nature of the AFM ordering, it's field evolution, or its electronic properties is known so far to our knowledge. Since the SOC is considerably smaller in Sb compared to Bi, it is interesting to study the magnetic and electronic properties of EuMg₂Sb₂ in order to probe the role of SOC in these materials on the associated electronic and magnetic states.

Here, we report the growth of EuMg₂Sb₂ single crys-

tals and their crystallographic, electronic, and magnetic properties studied by means of room-temperature xray powder diffraction (XRD), temperature T-dependent electrical resistivity ρ , heat capacity C_p , $\chi(H,T)$ and magnetization M(H) isotherm measurements. We also report the results of angle-resolved photoemission spectroscopy (ARPES) and zero-field neutron-diffraction measurements. In contrast to the semimetallic behavior observed in isostructural EuMg₂Bi₂, EuMg₂Sb₂ is found to be a narrow-gap semiconductor, as revealed by our $\rho(T)$ and ARPES measurements. We suggest that the reduction in SOC by introducing Sb in place of Bi might be responsible for the change in the electronic band structure. Our $\chi(T)$ and $C_p(T)$ data reveal that EuMg₂Sb₂ undergoes a long-range AFM transition below $T_{\rm N}=8.0(2)$ K with the Eu²⁺ moments with spin S=7/2 aligned in the ab plane. The zero-field neutron measurements show the AFM ordering to be A-type below T_N . An additional cusp in the in-plane $\chi(T)$ of unknown origin is observed at $T \approx 3$ K for low applied magnetic fields. A reorientation of the in-plane orderedmoment alignment is observed in low ab-plane magnetic fields via M(H,T) measurements, indicating a very small in-plane anisotropy energy.

The experimental details are given in the following Sec. II. The results and discussion of the various measurements are presented in Sec. IV, and a summary is provided in Sec. V. The dependence of the Cartesian eigenvalues and eigenvectors of the magnetic-dipole-interaction tensor versus the c/a ratio from 0.5 to 3 in 0.1 increments for a stacked simple-hexagonal spin lattice with collinear A-type AFM order and with the moments aligned in the ab plane is given in both graphical and tabular forms in the Appendix.

II. EXPERIMENTAL DETAILS

EuMg₂Sb₂ single crystals were grown using the selfflux method with starting composition Eu:Mg:Sb = 1:4:16, where the self-flux therefore had composition Mg₂Sb₁₄. The elements were loaded in an alumina crucible with a quartz wool filter and sealed inside a silica tube under 1/4 atm high-purity argon. The assembly was then heated to 900 °C at a rate 50 °C/h followed by a dwell of 12 h at that temperature. It was then cooled to 750 °C at a rate of 3 °C/h. The crystals were obtained by removing the flux through centrifugation at that temperature. Structural characterization was performed by room-temperature powder x-ray diffraction (XRD) measurements on ground crystals using a Rigaku Geigerflex x-ray diffractometer with Cu- K_{α} radiation. Crystal-structure analysis was performed using Rietveld refinement with the FULLPROF software package [21]. The Laue image was obtained using PW1830 Philips X-ray generator equipped with tungsten anode at 30 kV/30 mA and Photonic Science fluorescent imaging detector. The sample homogeneity and chemical composition were confirmed using a JEOL scanning-electron microscope (SEM) equipped with an energy-dispersive x-ray spectroscopy (EDS) analyzer. The magnetic measurements were carried out in a Magnetic-Properties-Measurement System (MPMS) from Quantum Design, Inc., in the T range 1.8–300 K and with H up to 5.5 T (1 T \equiv 10⁴ Oe). A Physical Properties Measurement System (PPMS, Quantum Design, Inc.) was used to measure $C_{\rm p}(T)$ and $\rho(T)$ in the T range 1.8–300 K.

Two types of samples were used in in-plane resistivity, $\rho(T)$, measurements. Samples #A and #B were asgrown single crystals with natural facets and with typical dimensions (2–3) ×1× (0.5–1) mm³. These samples were not in a shape of good rectangular bars, so there is big uncertainty in geometric factor determination. Samples #C and #D were mechanically polished into regular resistivity bars to enable quantitative resistivity determination. The longer side of the samples in all cases was along an arbitrary direction in the hexagonal crystal ab-plane. Contacts to the fresh surfaces of the crystals were made by attaching 50 μ m diameter silver wires with In solder and mechanically reinforcing contact with DuPont 4929N silver paint [22]. Contact resistance was typically in k Ω range.

ARPES data were collected using an ARPES spectrometer that consists of a Scienta R8000 electron analyzer and electron-cyclotron-resonance helium discharge lamp by Gamma Data with custom-designed focusing optics. We used 21.2 eV photon energy from the He-I line. The angular resolution was set at $\sim 0.1^{\circ}$ and 1° along and perpendicular to the direction of the analyzer slit, respectively, and the energy resolution was set at 10 meV. Samples were cleaved in-situ at a base pressure lower than 2×10^{-11} Torr and a temperature of 11 K. The samples were kept at the cleaving temperature during measurements.

Single-crystal neutron-diffraction experiments were performed in zero applied magnetic field using the TRIAX triple-axis spectrometer at the University of Missouri Research Reactor (MURR). An incident neutron beam with energy 14.7 meV was directed at the sample using a pyrolytic graphite (PG) monochromator. A PG analyzer was used to reduce the background. The neutron wavelength harmonics were removed from the beam using PG filters placed before the monochromator and in between the sample and analyzer. The beam divergence was limited using collimators before the monochromator; between the monochromator and sample; sample and analyzer; and between the analyzer and detector of 60' - 60' - 40' - 40', respectively. A 30 mg EuMg₂Sb₂ crystal was mounted on the cold tip of an Advanced Research Systems closed-cycle refrigerator with a nominal base temperature of 4 K (in this study 6.6 K was the lowest temperature achieved). The crystal was aligned in the (H0L) scattering plane. The lattice parameters at 6.6 K were determined to be a = 4.6531(5) A and c = 7.6668(5) A.

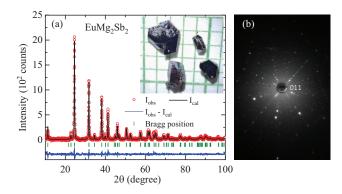


FIG. 1. (a) Room-temperature powder x-ray diffraction (XRD) pattern of crushed single crystals of ${\rm EuMg_2Sb_2}$ along with the Rietveld refinement. The open red circles are the experimental data points, the black solid line is the refined pattern, the difference between the experimental and refined diffraction patterns is shown by blue solid curve, and the allowed Bragg positions are marked by the green vertical bars. Inset: Image of as-grown crystals. (b) Laue image of a crystal along the [011] direction.

III. COMPUTATIONAL METHODS

The band structure of EuMg₂Sb₂ with spin-orbit coupling (SOC) in density-functional theory [23, 24] (DFT) has been calculated with the PBE [25] exchange-correlation functional, a plane-wave basis set and the projected-augmented-wave method [26] as implemented in VASP [27, 28]. To account for the half-filled strongly-localized Eu 4f orbitals, a Hubbard-like [29] $U=6.0~\rm eV$ is used. For A-type antiferromagnetism (AFMA), the hexagonal unit cell is doubled along the c axis with the moment in-plane pointing along the opposite a axis for neighboring cells. The DFT calculations use a Γ -centered Monkhorst-Pack [30] (11×11×3) k-point mesh with a Gaussian smearing of 0.05 eV. A kinetic-energy cutoff of 250 eV and experimental lattice parameters have been used with the atoms fixed in their bulk positions.

IV. RESULTS AND DISCUSSION

A. X-ray diffraction and crystal structure

The room-temperature powder x-ray diffraction (XRD) pattern of the crushed EuMg₂Sb₂ single crystals is shown in Fig. 1. All the peaks were indexed with the CaAl₂Si₂-type crystal structure with space group $P\overline{3}m1$. The refined lattice parameters are a=b=4.6861(3) Å and c=7.7231(5) Å, consistent with the previous results for polycrystalline material [20]. The composition obtained from the Rietveld refinement of the XRD data is EuMg_{1.99(2)}Sb_{2.02(3)}. The refined parameters are summarized in Table. I. The SEM-EDX measurements carried out at multiple points on the surfaces of the crystals further confirm the homogeneity and composition

TABLE I. Crystallographic and refinement parameters obtained from the structural analysis of room-temperature powder x-ray diffraction data for EuMg₂Sb₂.

Lattice parameters					
a(Å)		4.6861(3)			
c(Å)		7.7231(5)			
$V_{\rm cell}~({\rm \AA}^3)$		146.87(2)			
Refinement quality					
χ^2		1.61			
R_{Bragg} (%)		5.71			
R_f (%)		5.29			
Atomic coordinates					
Atom	Wyckoff Symbol	\boldsymbol{x}	y	z	
Eu	1a	0	0	0	
Mg	2d	1/3	2/3	0.6285(5)	
Bi	2d	1/3	2/3	0.2499(4)	

 $\mathrm{EuMg}_{1.96(4)}\mathrm{Sb}_{2.01(3)}$. Both compositions are thus consistent within the errors with the stoichiometric composition $\mathrm{EuMg}_2\mathrm{Sb}_2$.

B. Electrical resistivity

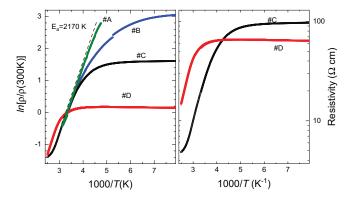


FIG. 2. Electrical resistivity of EuMg₂Sb₂ as determined from measurements on four crystals. Samples #A and #B were as grown with poorly- defined geometric factors. Samples #C and #D were dry polished into resistivity bars. The data are presented by Arrhenius plots using normalized resistivity $\ln[\rho(T)/\rho(300~{\rm K})]$ to remove the uncertainty in the geometric factor. All four samples show a similar intrinsic slope (activation energy) $E_{\rm a}/k_{\rm B}=2170~{\rm K}$ of the curves at high temperatures, where $k_{\rm B}$ is Boltzmann's constant. The resistivity value at low temperatures saturates for all samples at a sample-dependent value. This observation suggests extrinsic conductivity at low temperatures controlled by impurities and/or defects. The right panel shows the same data using actual resistivity values for samples #C and #D with controlled sample geometry.

Measurements of the temperature-dependent electrical resistivity ρ were performed on four different crystals. Samples #A and #B, were as grown, had natural facets and irregular shapes, giving only qualitative resistivitymagnitude measurements. Samples #C and #D were dry-polished into resistivity bars. The comparison between the two sets of samples was made using a normalized resistivity scale, $\rho(T)/\rho(300 \text{ K})$ to a notable extent diminishing uncertainty of the geometric factor determination. In Fig. 2 we plot the resistivity data using Arrhenius plots with an inverse temperature scale, 1000/T. It can be seen that the behavior of all samples at high temperatures is characterized by an activated-resistivity decrease on warming, with very close slopes of the curves in all four samples measured, $E_a = 2170$ K. This behavior is typical of a semiconductor. At low temperatures the resistivity of the samples becomes temperature independent, with a strong variation between different samples. This is characteristic of impurity/defect-controlled transport in a semiconductor. We note that the polished samples #C and #D show notably lower resistivities at low temperatures compared with the samples with as-grown surfaces. This observation suggests that strain and/or crack formation may increase the sample conductivity.

The right panel of Fig. 2 shows the temperature-dependent resistivity values for samples #C and #D. Compared with samples #A and #B, Sample #C has higher resistivity at low temperature and the transition to activated behavior at higher temperatures starts at a lower temperature, as expected in higher purity semiconductors. The $\rho(300~{\rm K})$ for sample #A was determined as 16 Ω -cm, and for sample #B as 1.5 Ω -cm.

As can be seen from the straight dashed line in the left panel of Fig. 2, the activation energy as determined from the slope of the Arrhenius plot is $E_{\rm a}/k_{\rm B}=2170~{\rm K}$ for all crystals, where $k_{\rm B}$ is Boltzmann's constant. For intrinsic conductivity this corresponds to an energy gap of $E_{\rm gap}/k_{\rm B}=2E_{\rm a}/k_{\rm B}=4340~{\rm K}$ or $E_{\rm gap}=0.3740~{\rm eV}$. For comparison, this value is about two times less that the indirect gap of silicon and is in the range observed for various narrow-gap semiconductors [31–34].

C. Angle-resolved photoemission spectroscopy (ARPES)

The ARPES measurements also predict semiconducting behavior in $\operatorname{EuMg_2Sb_2}$. The map of ARPES intensity at the Fermi level is shown in Fig. 3(a). There is a round spot of intensity at Γ indicating proximity of the top of a hole band, but not crossing the Fermi energy, as that would result in a circle of intensity. There is also a weaker spot present near the zone boundary (point A) indicating proximity to a hole band there, as predicted by the DFT calculations. This is more evident in the constant-energy cut below the Fermi level shown in Fig. 3(b), where both spots are more intense. The band dispersion along the horizontal symmetry line is shown in Fig. 3(c). In this

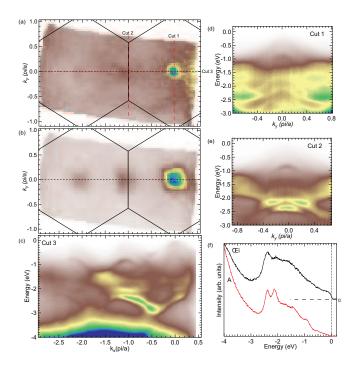


FIG. 3. Electronic structure of EuMg₂Sb₂ measured by ARPES. (a) ARPES intensity map at the Fermi level integrated within 5 meV. (b) Constant energy cut at 0.2 eV below Fermi level. (c) Band dispersion along the horizontal symmetry line (cut #1). (d,e) Band dispersion along cuts #2 and #3 [marked in panel (a)]. (f) Energy distribution curves (EDCs) at points Γ and A [marked in panel (a)].

plot both hole bands (one at Γ and the second at A) are clearly visible. They approach the Fermi level, but do not cross it. Both bands are very broad, with high intensity between parabolic arms, indicating their bulk origin. This is because often, the k_z selectivity can be quite poor for 3D bulk bands, which results in projection onto the (k_x, k_y) plane over a range of k_z momenta. The dispersions at Γ and A along cuts #2 and #3 are shown in Figs. 3(d, e), again confirming proximity of the tops of hole-like bands to the Fermi level. The EDC's at Γ and A are shown in Fig. 3(f). The band at Γ is closer to the Fermi level and its tail is being cut-off by the Fermi function, while the band at A is further from the Fermi level and its leading edge is better defined. Because ARPES cannot easily measure bands above the Fermi level, it is difficult to estimate the band gap, but we can put a lower limit of 0.8 eV for the band at A and 0.3 eV for the band at Γ .

D. Computational results

The DFT-calculated bulk band structure of EuMg₂Sb₂ in the ground state AFMA is plotted in Fig. 4. When compared to the isostructural EuMg₂Bi₂ {see Fig. 5(b) in Ref. [16]}, most of band dispersions at large energies are

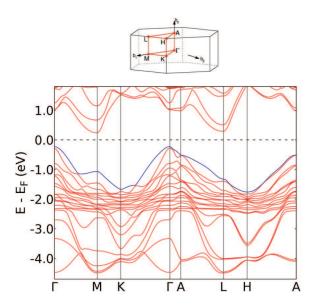


FIG. 4. Bulk band structure of AFMA EuMg₂Sb₂ calculated in PBE+U+SOC with U=6.0 eV. The magnetic moment is in-plane along the a axis. The highest-energy valence band is colored blue. The points in the Brillouin zone referenced in the band structure are shown above the main plot.

similar except for those near the $E_{\rm F}$. Very importantly, the low-lying conduction bands of EuMg₂Sb₂ along the Γ -A direction are flat and above $E_{\rm F}+1.0$ eV, while those of EuMg₂Bi₂ are highly dispersive with a band inversion near the Γ point. For this Zintl compound series as studied before [35], the low-lying conduction bands along the Γ -A direction are derived from the antibonding s orbitals (from Mg here), which are sensitive to the electronic negativity of the p orbitals they hybridize, the lattice constant and pressure, besides the strength of the SOC. For the more electronegative and lighter Sb compared with Bi, the hybridization with Mg 3s orbitals is more ionic and thus pushes these low-lying conduction bands along the Γ -A direction to higher energy, even higher than the conduction band near the M point. This results in an indirect bulk band gap between the Γ and M points for EuMg₂Sb₂. The calculated bulk gap of 0.46 eV is slightly larger than the measured 0.37 eV from transport. From the calculated band structure in Fig. 4, there are hole-like band dispersions around the Γ point both above $E_{\rm F}-1.0~{\rm eV}$ and below $E_{\rm F}-2.5~{\rm eV}$ with a very narrow range of dense bands in between, around $E_{\rm F}-2.0~{\rm eV}$ from the Eu 4f bands. These overall band dispersion features agree with the ARPES data in Fig. 3.

E. Zero-field neutron diffraction

Figure 5(a) shows neutron-diffraction scans along (00L) (in reciprocal-lattice units) at 6.6 and 10 K, where reflections at half-integer L values are apparent at T=6.6 K. For more clarity, Fig. 5(b) shows the dif-

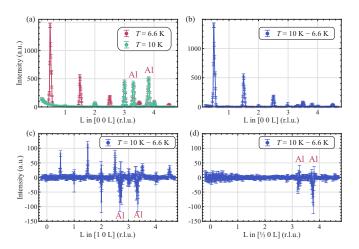


FIG. 5. (a) Neutron-diffraction pattern along (00L) of single-crystal EuMg₂Sb₂ at 6.6 and 10 K as indicated. The aluminum Bragg reflections marked on the figure originate from the sample holder. The magnetic Bragg reflections are obtained by subtracting the diffraction pattern at 10 K from that at 6 K for (b) (00L), (c) (10L), and (d) ($\frac{1}{3}$ 0L) scans. The difference patterns in (b–c) show clear magnetic peaks at half-integer L up to L=4.5, whereas no such peak is observed in (d) at half integer L, consistent with A-type AFM, i.e, the H=0 ground state is such that the intraplane moments are ferromagnetically aligned in the ab plane while the moments in adjacent Eu planes along the c axis are aligned antiferromagnetically.

ference between these two scans, where within experimental uncertainty, there is no evidence for other reflections associated with a modulated structure along the c axis. Similar differences [i.e., I(6.6 K) - I(10 K)] for a scan along (10L), shown in Fig. 5(c), also reveal new peaks at half-integer L values. Qualitatively, these newly-emerging Bragg reflections indicate a doubling of the unit cell along the c axis. We also note that the intensities of the new peaks become weaker at larger L values, roughly following the falloff expected from the magnetic form factor of Eu²⁺. These qualitative observations unequivocally establish that these reflections are associated with A-type AFM ordering with AFM propagation vector $\vec{\tau} = (0, 0, \frac{1}{2})$, consisting of layers of moments aligned ferromagnetically in the ab plane, with moments in adjacent planes along the c axis aligned antiferromagnetically. Figure 5(d) shows a (1/3,0,L) scan with no peaks at half-integer L, consistent with ferromagnetic (FM) inplane ordering. The $\chi(T)$ data discussed in the following section IVF also suggest that the ordered moments are aligned in the ab plane.

The proposed A-type AFM structure is shown in the right panel of Fig. 6, where adjacent NN FM layers along the c axis are rotated by 180° with respect to each other. The direction of the FM moment within an Eu layer cannot be determined from neutron diffraction alone. As noted for isostructural EuMg₂Bi₂ [18], the only possible directions are towards NN (a,a1) or next nearest neighbor (NNN) (b,b1) according to the Bilbao crystallographic

server [36]. Using published values for the structural parameters, we obtain good agreement with the intensities of the nuclear Bragg peaks, both above and below $T_{\rm N}$. Based on this, we are able to confirm the A-type magnetic structure and obtain an estimate for the Eu ordered magnetic moment $g\langle S\rangle$ $\mu_{\rm B}=4.0(5)$ $\mu_{\rm B}$ at T=6.6 K by calculating the magnetic and chemical structure factors, where S is the spin magnetic quantum number, g is the spectroscopic-splitting factor, and g is the Bohr magneton.

As noted, our refinement of the magnetic structure yields an average magnetic moment at $T=6.6~\mathrm{K}$ given by

$$\mu(6.6 \text{ K}) = \langle gS \rangle \,\mu_{\text{B}} = (4.0 \pm 0.5) \,\mu_{\text{B}}.$$
 (1)

This value is smaller than the zero-temperature ordered moment $\mu = gS\mu_{\rm B} = 7\,\mu_{\rm B}$ expected from the electronic configuration of Eu²⁺ [37] with angular-momentum quantum number L=0, spin quantum number S=7/2, and spectroscopic-splitting factor g=2 because μ is not yet saturated to its full value at T=0 K (see the left panel of Fig. 6).

The left panel of Fig. 6 shows the integrated intensity of the $(0\ 0\ \frac{1}{2})$ magnetic peak as a function of temperature where we used a simple power-law function

$$I_{(0\,0\,0.5)}(T) = C|1 - T/T_{\rm N}|^{2\beta} \propto \mu^2$$
 (2)

to fit the data (solid blue line with sharp transition). The smooth line around $T_{\rm N}$ is obtained by the same power law but weighted by a Gaussian distribution of $T_{\rm N}$ (this form is sometimes used to account for crystal inhomogeneities) yielding $T_{\rm N}=(7.7\pm0.4)~{\rm K}$ and $\beta=0.36\pm0.05$. The $T_{\rm N}$ is consistent within the error bars with $T_{\rm N}=8.0(2)~{\rm K}$ measured by $\chi(T)$ and $8.0(1)~{\rm K}$ measured by $C_{\rm p}(T)$ below. The power-law parameter β used here is phenomenological in order to determine $T_{\rm N}$. Thus the value of β is not reliable as a critical exponent. Importantly, the data and phenomenological fit in the left panel of Fig. 6 show that the order parameter is still increasing strongly with decreasing T at $T=6.6~{\rm K}$ and is therefore not close at that T to its expected saturated value of $7~\mu_{\rm B}/{\rm Eu}$ at $T=0~{\rm K}$.

F. Magnetic susceptibility

1. High-temperature regime

The inverse magnetic susceptibility data obtained in an applied field H=0.1 T are plotted for $H\parallel ab$ in Fig. 7(a) and for $H\parallel c$ in Fig. 7(b). The data in the paramagnetic (PM) regime above 50 K for each field direction were fitted by the modified Curie-Weiss law

$$\chi_{\alpha}(T) = \chi_0 + \frac{C_{\alpha}}{T - \theta_{p\alpha}} \quad (\alpha = ab, c),$$
(3)

where χ_0 is an isotropic temperature-independent term, θ_p is the Weiss temperature, and C_{α} is the Curie constant

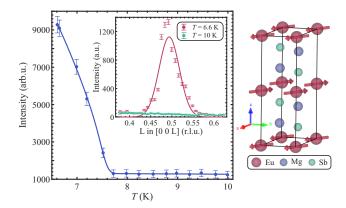


FIG. 6. Left panel: Integrated intensity as a function of temperature T of the $(0\ 0\ \frac{1}{2})$ magnetic Bragg reflection with the power-law fit (2) (solid blue line) yielding $T_{\rm N}=(7.7\pm0.4)~{\rm K}$ and $\beta=0.36\pm0.05$. The error of $T_{\rm N}$ includes an estimated systematic error. Right panel: Chemical and A-type AFM spin structure of EuMg₂Sb₂. Our neutron-diffraction data are insensitive to the direction of the FM moment in the ab plane although we show them to be pointing along the next-nearest-neighbor direction.

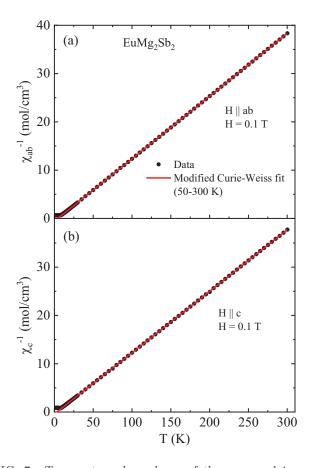


FIG. 7. Temperature dependence of the measured inverse magnetic susceptibilities (a) $\chi_{ab}^{-1}(T)$ and (b) $\chi_c^{-1}(T)$ (circles) along with the respective modified Curie-Weiss fits from 50 to 300 K (red straight lines).

TABLE II. Parameters obtained from fits of the data in Figs. 7(a) and 7(b) by Eqs. (3) and (4a). Listed are the T-independent contribution to the susceptibility χ_0 , Curie constant per mol C_α in $\alpha=ab,c$ directions, effective moment per Eu $\mu_{\rm eff}(\mu_{\rm B}/{\rm Eu})\approx \sqrt{8C}$ and Weiss temperature $\theta_{\rm p\alpha}$ obtained from the $\chi^{-1}(T)$ versus T data for H=0.1 T using Eq. (3). The negative signs of the χ_0 values indicate diamagnetic contributions, whereas the positive signs of the Weiss temperatures $\theta_{\rm p\alpha}$ indicate dominant ferromagnetic interactions.

Field	χ_0	C_{α}	$\mu_{\mathrm{eff}\alpha}$	$\theta_{\mathrm{p}lpha}$
direction	$\left(10^{-4} \frac{\text{cm}^3}{\text{mol}}\right)$	$\left(\frac{\text{cm}^3\text{K}}{\text{mol}}\right)$	$\left(\frac{\mu_{\mathrm{B}}}{\mathrm{mol}}\right)$	(K)
$H \parallel ab$	-2.2(2)	7.77(1)	7.88(1)	4.32(6)
$\mathbf{H} \parallel c$	-2.0(5)	7.92(2)	7.95(1)	3.2(1)

given by

$$C_{\alpha} = \frac{N_{\rm A} g_{\alpha}^2 S(S+1) \mu_{\rm B}^2}{3k_{\rm B}} = \frac{N_{\rm A} \mu_{\rm eff,\alpha}^2}{3k_{\rm B}},$$
 (4a)

where the effective magnetic moment is given by

$$\mu_{\text{eff},\alpha} = g_{\alpha} \sqrt{S(S+1)} \,\mu_{\text{B}},\tag{4b}$$

where N_A is Avogadro's number. The fits to the $h \parallel ab$ and $H \parallel c$ data by Eq. (3) are shown as red solid lines in Figs. 7(a) and 7(b), respectively, and the fitted parameters for each field direction are listed in Table II. The effective moment values obtained from C_{α} for both applied field directions are close to the value 7.94 μ_B /Eu expected from Eq. (4b) for Eu²⁺ spins with S = 7/2 and g = 2. The positive values of θ_{ab} and θ_c indicate dominant ferromagnetic (FM) interactions between the Eu spins, consistent with the A-type AFM structure obtained from the neutron-diffraction measurements where the in-plane ordered magnetic moments are ferromagnetically aligned and the nearest-neighbor moments along the c axis are antiferromagnetically aligned.

Now we make a rough estimate of the nearest-neighbor exchange interactions J_{ab} in the ab plane and along the c axis J_c , where a positive value is AFM and a negative value is FM. Further-neighbor interactions are neglected. According to molecular field theory (MFT) [38], for a lattice of spins that are identical and crystallographically equivalent, one has

$$\theta_{\rm p} = -\frac{S(S+1)}{3k_{\rm B}} \sum_{j} J_{ij},\tag{5a}$$

$$T_{\rm N} = -\frac{S(S+1)}{3k_{\rm B}} \sum_{j} J_{ij} \cos(\phi_{ji}),$$
 (5b)

where the sums are over all neighbors j of a central spin i, J_{ij} is the exchange interaction between spins i and j, and ϕ_{ji} is the angle between spins j and i in the magnetically-ordered state. Here we only consider the nearest-neighbor (NN) spins to a central spin i, of which

there are 6 NN spins in the ab plane with expected FM (negative) exchange interaction J_{ab} and two NN spins along the c axis with expected AFM (positive) exchange interactions. Then Eqs. (5) become

$$\theta_{\rm p} = -\frac{S(S+1)}{3k_{\rm B}}(6J_{ab} + 2J_c),$$
(6a)

$$T_{\rm N} = -\frac{S(S+1)}{3k_{\rm B}}(6J_{ab} - 2J_c).$$
 (6b)

Taking the average value $\theta_{\rm p,ave}=3.9~{\rm K}$ from Table II and $T_{\rm N}=8.0~{\rm K}$, Eqs. (6) yield FM $J_{ab}=-0.016~{\rm meV}$ and AFM $J_c=0.017~{\rm meV}$, with the expected FM and AFM signs of J_{ab} and J_c , respectively.

The relationship $\theta_{ab} > \theta_c$ in Table II and the preference for ordering of the Eu spins in the ab plane as opposed to along the c axis likely both arise at least in part from magnetic dipole interactions between the ordered Eu moment which strongly favor ab-plane moment alignment over c-axis alignment in the stacked triangular Eu lattice of EuMg₂Sb₂ shown in the right panel of Fig. 6 as follows.

In general, the eigenenergies $E_{i\alpha}$ of the magnetic dipole interaction tensor describing the interactions of magnetic dipole i with all other dipoles in an infinite crystal with a collinear magnetic structure is given by [39]

$$E_{i\alpha} = -\varepsilon \ \lambda_{\mathbf{k}\alpha},\tag{7a}$$

where

$$\varepsilon = \frac{\mu^2}{2a^3},\tag{7b}$$

 μ is the magnitude of the magnetic moment on each magnetic atom, a is the crystallographic lattice constant in the ab plane of the lattice of magnetic dipoles under consideration, and $\lambda_{\mathbf{k}\alpha}$ is the eigenvalue of the magnetic-dipole-interaction tensor for a particular magnetic propagation vector \mathbf{k} where α is the Cartesian principal-axis ordering direction of the collinear magnetic structure and hence the three principal axes are orthogonal to each other. In general, the value of $\lambda_{\mathbf{k}\alpha}$ depends on the c/a ratio of the particular magnetic structure under consideration except for cubic structures for which c=a.

As discussed in Sec. II, the trigonal structure of EuMg₂Sb₂ has lattice parameters $a=4.6531\,\text{Å}$ and $c=7.6668\,\text{Å}$ at T=6.6 K, yielding c/a=1.6477. Using the Eu moment $\mu=7\,\mu_{\rm B}$, Eq. (7b) gives

$$\varepsilon = 2.0916 \times 10^{-17} \text{ erg.}$$
 (8)

Following Ref. [39], for A-type ordering with AFM propagation vector $\mathbf{k} = (0,0,1/2)$ r.l.u. for the stacked triangular Eu spin lattice and after summing over a sphere of radius 200 a containing $N_{\rm max} = 2.35 \times 10^7$ spins, we find

$$\lambda_{(0,0,1/2)[1,0,0]} = 5.519$$
 (a axis ordering), (9a)

$$\lambda_{(0,0,1/2)[0,0,1]} = -11.038$$
 (c axis ordering). (9b)

These values are close to the values for a single FM triangular-lattice layer given by $\lambda_{[1,0,0],[0,1,0]} = 5.517088$

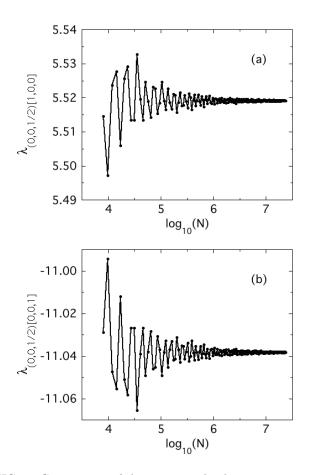


FIG. 8. Convergence of the magnetic dipole interaction tensor eigenvalues $\lambda_{k\alpha}$ for A-type AFM with A-type AFM propagation vector (0,0,1/2) r.l.u. and moment alignment along (a) the a axis and (b) the c axis.

and $\lambda_{[0,0,1]} = -11.034\,176$ [39], as expected from the dependence of these values on the c/a ratio as shown in the Appendix. The differences here are

$$\begin{split} \lambda_{(0,0,1/2)[100]} - \lambda_{(0,0,1/2)[001]} &= 16.557, \\ \lambda_{(0,0,1/2)[100]} - \lambda_{(0,0,1/2)[010]} &\approx -2.2 \times 10^{-12}. \ (10b) \end{split}$$

The respective convergences of $\lambda_{(0,0,1/2)[100]}$ and $\lambda_{(0,0,1/2)[001]}$ versus \log_{10} of the number of spins N in the sphere of calculation are shown in Figs. 8(a) and 8(b), respectively, where the accuracy of convergence of $\approx \pm 0.001$ for each λ for the above value of $N_{\rm max}$ are seen.

According to Eqs. (7a) and (10a), ab-plane ordering is favored over c-axis ordering at T = 0 K by an energy

$$\Delta E = 3.463 \times 10^{-16} \text{ erg} = 0.2162 \text{ meV}.$$
 (11)

This energy difference corresponds to a field difference $\Delta H = \Delta E/\mu = 5335$ Oe, where $\mu = 7\,\mu_{\rm B}/{\rm Eu}$. This value is similar to the difference in the critical fields at T=1.8 K in Fig. 11(a) below, where $H_c^{\rm c}$ ($H\parallel c$) = 3.4(1) T and $H_{\rm ab}^{\rm c}$ ($H\parallel ab$) = 2.6(1) T, yielding $H_c^{\rm c}-H_{ab}^{\rm c}=8$ kOe. This indicates that the

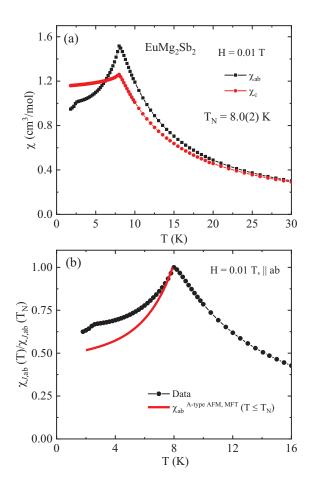


FIG. 9. (a) Magnetic susceptibility $\chi = M/H$ of EuMg₂Sb₂ as a function of T below 30 K for $H \parallel ab$ and $H \parallel c$ measured in H = 0.01 T. The $\chi_{ab}(T)$ and $\chi_c(T)$ are seen to be anisotropic for $T \lesssim 30$ K, which is greater than $T_{\rm N} = 8.0(2)$ K. (b) The ratio $\chi_{ab}(T)/\chi_{ab}(T_{\rm N})$ for H = 0.01 T (black symbols). The red solid line is the $\chi_{Jab}(T)/\chi_{Jab}(T_{\rm N})$ calculated for A-type AFM order for $T < T_{\rm N}$ according to MFT [38, 40].

magnetic-dipole interaction is an important source of magnetic anisotropy in $EuMg_2Sb_2$.

On the other hand, the magnetic-dipole anisotropy within the ab plane in Eq. (10b) is 13 orders of magnitude smaller than between the ab plane and the c axis in Eq. (10a), where according to Eqs. (7a) and (10b), ordering perpendicular to the a axis is slightly favored over ordering parallel to the a axis. It would be interesting to calculate the in-plane anisotropy using other methods.

2. Low-temperature regime

Figure 9(a) shows $\chi_{ab}(T)$ and $\chi_c(T)$ of EuMg₂Sb₂ measured in H=0.01 T for $T\leq 30$ K. Although χ is isotropic at T>30 K, anisotropy is seen below 30 K which increases with decreasing T. The compound exhibits a clear AFM transition on cooling below $T_{\rm N}=8.0(2)$ K, where sharp peaks are observed at

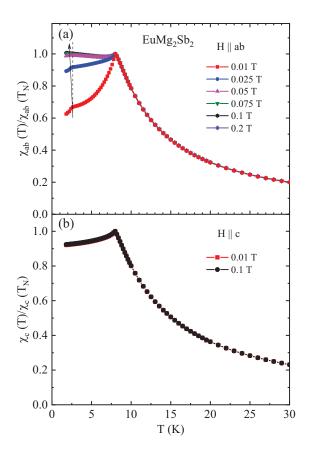


FIG. 10. Temperature dependence of χ_{ab} and χ_c of EuMg₂Sb₂ normalized to that at $T=T_{\rm N}$ for different applied magnetic fields in (a) and (b), respectively. In (a), increasing fields are indicated by an arrow. χ_{ab} for $T< T_{\rm N}$ is seen to strongly increase with increasing H before becoming independent of T and H for $H\gtrsim 0.075$ T, whereas χ_c is independent of H and H below H for fields of 0.01 and 0.1 T. The kink at H=10.01 T shifts to lower H=11 with increasing H=12. The dashed vertical line at constant H=13 included in (a) to more clearly show the small H=14 dependence of the transition at 3 K.

this temperature in both $\chi_{ab}(T)$ and $\chi_c(T)$. Below T_N , $\chi_{ab}(T)$ decreases with decreasing T, whereas $\chi_c(T)$ is almost independent of T indicating moment alignment in the ab plane, consistent with the A-type AFM structure obtained from the above neutron-diffraction measurements in which the moments are aligned ferromagnetically in the ab plane. A magnetic transition of unknown type also appears as a cusp at 3 K in the $\chi_ab(T)$ data, but there is no evidence of this transition in the $\chi_c(T)$ data. The entropy change associated with this phase transition is evidently quite small, because our $C_p(T)$ data in Sec. IV H below show no clear evidence for a phase transition at this temperature.

The $\chi_{ab}(T)$ normalized by the value of $\chi_{ab}(T_{\rm N})$ is shown in Fig. 9(b), together with expectation for A-type AFM order (red curve) to be discussed below. The magnetic-field dependence of $\chi(T)/\chi(T_{\rm N})$ below 30 K is shown in Figs. 10(a) and 10(b) for $H \parallel ab$ and $H \parallel c$, re-

spectively. Figure 10(a) shows that the transition seen in $\chi_{ab}(T)$ at T=3 K is suppressed by an in-plane magnetic field. Figure 10(a) also shows that $\chi_{ab}(T)$ for $T < T_{\rm N}$ is strongly enhanced even at low fields and becomes independent of T for $H \gtrsim 0.075$ T. We propose below that this behavior results from a field-induced magnetic-moment reorientation within the ab plane. In contrast, $\chi_c(T)$ does not change in H=0.1 T applied along the c axis compared to the behavior in H=0.01 T.

Our zero-field neutron-diffraction results indicate that the AFM structure from $T_{\rm N}$ to 6.6 K is A-type, where the magnetic moments are aligned ferromagnetically in the ab plane and the moments in adjacent Eu planes along the c axis are aligned antiferromagnetically. An A-type antiferromagnet with ab-plane moment alignment and turn angle $kd=180^{\circ}$ between adjacent layers is equivalent to a c-axis helix with a turn angle $kd \to 180^{\circ}$.

Here, we calculate $\chi_{ab}(T \leq T_{\rm N})$ for such an A-type AFM structure using MFT [38, 40]. To use this theory, the direction-averaged $\chi_{Jab}(T)$ for $T \geq T_{\rm N}$ is defined as

$$\chi_{Jab}(T) = \frac{2}{3}\chi_{ab}(T) + \frac{1}{3}\chi_c(T),$$
(12)

Then the $\chi_{ab}(T \leq T_{\rm N})$ data are shifted vertically to agree at $T_{\rm N}$ with $\chi_{Jab}(T_{\rm N})$. We designate the resulting data at $T \leq T_{\rm N}$ also as $\chi_{Jab}(T)$ and then form the ratio $\chi_{Jab}(T)/\chi_{Jab}(T_{\rm N})$ as plotted versus T in Fig. 9(b).

With the definition $f = \theta_{\rm p \, ave}/T_{\rm N} = 0.49$ from Table II, we have [38, 40]

$$\frac{\chi_{Jab}(T \le T_{\rm N})}{\chi_J(T_{\rm N})} = \frac{(1 + \tau^* + 2f + 4B^*)(1 - f)/2}{(\tau^* + B^*)(1 + B^*) - (f + B^*)^2},\tag{13a}$$

where

$$B^* = 2(1 - f)\cos(kd)\left[1 + \cos(kd)\right] - f,\tag{13b}$$

$$t = \frac{T}{T_{\rm N}}, \quad \tau^*(t) = \frac{(S+1)t}{3B_S'(y_0)}, \quad y_0 = \frac{3\bar{\mu}_0}{(S+1)t}, \quad (13c)$$

the ordered moment versus T in H=0 is denoted by μ_0 , the reduced ordered moment $\bar{\mu}_0 = \mu_0/\mu_{\rm sat}$ is determined by numerically solving the self-consistency equation

$$\bar{\mu}_0 = B_S(y_0),$$
 (13d)

 $B_S'(y_0) = [dB_S(y)/dy]|_{y=y_0}$, and the Brillouin function $B_S(y)$ is

$$B_S(y) = \frac{1}{2S} \left\{ (2S+1)\coth\left[(2S+1)\frac{y}{2} \right] - \coth\left(\frac{y}{2}\right) \right\}. \tag{13e}$$

At T = 0, one obtains [38, 40]

$$\frac{\chi_{Jab}(T=0)}{\chi_{Jab}(T_{\rm N})} = \frac{1}{2[1+2\cos(kd)+2\cos^2(kd)]}.$$
 (14)

Then taking the turn angle between moments in adjacent layers of Eu spins as $kd \rightarrow 180^{\circ}$ for the

A-type AFM structure in EuMg₂Sb₂ discussed above with the moments aligned in the ab plane gives $\chi_{Jab}(T=0)/\chi_{Jab}(T_{\rm N}) \rightarrow 1/2$, as typically observed.

The $\chi_{Jab}(T)/\chi_{Jab}(T_{\rm N})$ calculated for EuMg₂Sb₂ is shown as the red curve in Fig. 9(b). However, as seen from the figure, the experimental data appreciably differ from the predicted behavior for A-type antiferromagnetism, evidently due to presence of the additional transition at T=3 K and the associated influence on $\chi_{ab}(T)$ at $T< T_{\rm N}$. We could not probe the magnetic structure below 3 K using neutron diffraction because the cryostat used has a low-T limit of 6.6 K. Future neutron-diffraction experiments at lower temperatures would be of great interest.

G. Isothermal magnetization versus field

1. Overview

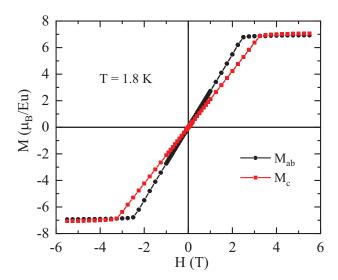


FIG. 11. Magnetic hysteresis curves measured at T=1.8 K for $H \parallel ab \ (M_{ab})$ and $H \parallel c \ (M_c)$.

In order to provide further insight into the field-induced evolution of the magnetic properties, isothermal magnetization versus field M(H) measurements were carried out on EuMg₂Sb₂ crystals. Figure 11 shows M(H) hysteresis curves for $-5.5~\mathrm{T} \leq H \leq 5.5~\mathrm{T}$ measured at $T=1.8~\mathrm{K}$ for both $H\parallel ab~(M_{ab})$ and $H\parallel c~(M_c)$. Over this field range, both M_{ab} and M_c appear to increase linearly with increasing field and saturate above the critical fields $H^c_{ab}=2.6(1)~\mathrm{T}$ and $H^c_c=3.4(1)~\mathrm{T}$. The saturation moment $\mu_{\mathrm{sat}}=7.0(5)~\mu_{\mathrm{B}}/\mathrm{Eu}$ at $T=1.8~\mathrm{K}$ is observed for both field directions, which agree within the errors with the theoretical value $\mu=gS\mu_{\mathrm{B}}=7~\mu_{\mathrm{B}}/\mathrm{Eu}$ expected for Eu²⁺ with $g=2~\mathrm{and}~S=7/2$.

Figure 12 shows the temperature evolution of the M(H) isotherms from 1.8 to 100 K. The data at 5 K show a decrease in the critical fields to $H_{ab}^{\rm c}=2.0$ T and

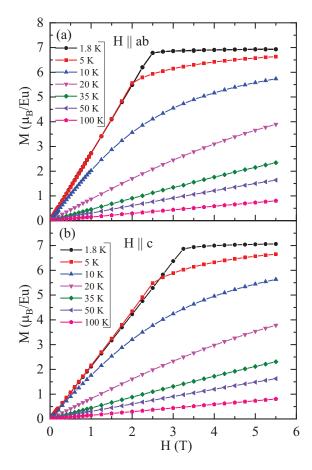


FIG. 12. Field dependence of magnetic isotherms measured at different temperatures when the applied field is (a) in the ab plane and (b) along the c axis.

 $H_c^c = 2.5$ T. The data at higher temperatures are in the paramagnetic regime where the M(H) data become linear.

2. Magnetic moment reorientation in small ab-plane magnetic fields at low temperatures

The derivative dM/dH versus H at T=1.8 K is plotted versus H in Fig. 13(a) for both $H \parallel ab$ and $H \parallel c$. The data show that $M_{ab}(H)$ is nonlinear in the low-field region $H \lesssim 0.1$ T, whereas $M_c(H)$ is linear. The temperature dependence of the nonlinear $M_{ab}(H)$ behavior is shown in Fig. 13(b) and the corresponding field derivatives in Fig. 13(c). It is evident that the nonlinearity in $M_{ab}(H)$ persists up to $T_N=8$ K with a maximum slope at $H\sim 0.025$ T for T=1.8 K, where a peak in dM_{ab}/dH is observed. The peak shifts to lower fields with increasing T. This behavior is similar to our earlier observations for two other trigonal Eu-based compounds EuMg₂Bi₂ and EuSn₂As₂ [15, 41], where we argued that the nonlinearity results from magnetic-field-induced ordered-moment reorientation in the three trigonal AFM domains associated with a very weak in-plane

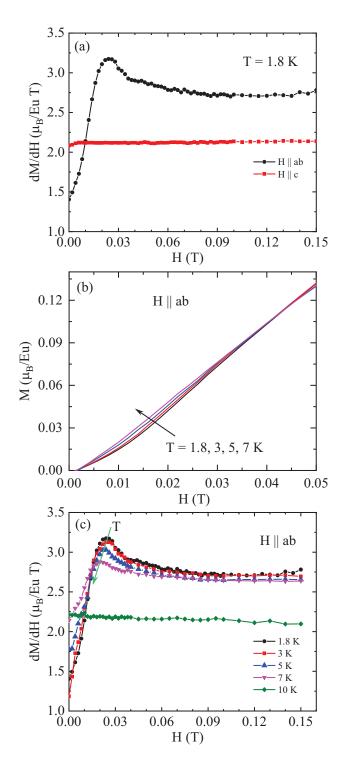


FIG. 13. (a) Low-field dM/dH vs. H from Fig. 11. The data for $H \parallel ab$ exhibit a distinct nonlinearity. (b) Temperature dependence of $M_{ab}(H)$ emphasizing the low-field region; the corresponding dM/dH versus H is presented in (c).

magnetic anisotropy. This scenario is plausible here as well. The antiparallel AFM spins in each of the three domains present at zero-field rotate to become perpendicular to \mathbf{H} at $H \sim 0.06$ T, apart from a small canting

towards **H** to produce the observed magnetization.

H. Heat capacity

The temperature dependence of the zero-field heat capacity $C_{\rm p}$ of EuMg₂Sb₂ is shown in Fig. 14(a). A sharp λ -type peak is observed at $T_{\rm N}=8.0(1)$ K. The $C_{\rm p}$ value of EuMg₂Sb₂ at T=300 K is ≈ 117.5 J/mol K, which is smaller than the expected classical Dulong-Petit high-T limit 3nR=124.71 J/mol K for the compound shown as the horizontal dashed line in Fig. 14(a), where n=5 is the number of atoms per formula unit and R is the molar gas constant.

We first fitted the $C_{\rm p}(T)$ data for T=50–300 K by the Debye model according to the general expression

$$C_{\rm p}(T) = \gamma T + n \ C_{\rm V \, Debye}(T), \tag{15}$$

$$C_{\rm V}(T) = 9R \left(\frac{T}{\Theta_{\rm D}}\right)^3 \int_0^{\Theta_{\rm D}/T} \frac{x^4 e^x}{(e^x - 1)^2} dx,$$

where γ is the Sommerfeld electronic specific heat coefficient and $\Theta_{\rm D}$ is the Debye temperature. The lower limit of 50 K for the fit was chosen to avoid any contribution from short-range magnetic ordering of the Eu spins above $T_{\rm N}$. We used $\gamma=0$ since EuMg₂Sb₂ is a semiconductor. The fitted Debye temperature is $\Theta_{\rm D}=270(3)$ K. As shown in Fig. 14(b), the $C_{\rm p}(T)$ is not fitted well using the Debye model. The failure of the Debye model to fit the lattice heat capacity suggests the presence of one or more optic-phonon modes that would give Einstein contributions to the lattice heat capacity.

We therefore next fitted the $C_{\rm p}(T)$ data from 50 to 300 K with a combination of the Debye model and an Einstein contribution associated with a single optic-phonon mode according to

$$C_{\rm p}(T) = (1 - \alpha)C_{\rm V \, Debye}(T) + \alpha C_{\rm V \, Einstein}(T),$$
 (16a)

where

$$C_{\text{V Einstein}}(T) = 3R \left(\frac{\Theta_{\text{E}}}{T}\right)^2 \frac{e^{\Theta_{\text{E}}/T}}{(e^{\Theta_{\text{E}}/T} - 1)^2},$$
 (16b)

 $\Theta_{\rm E}$ is the Einstein temperature, and the parameter α determines the relative contributions of the Debye and Einstein components to the lattice heat capacity. The fitted parameters were $\Theta_{\rm D}=415(12)~{\rm K},\,\Theta_{\rm E}=111(3)~{\rm K},$ and $\alpha=0.48(2)$. We found that although the fit in the low-T region improved significantly, there is still a significant discrepancy between the theory and experimental data for $T\geq150~{\rm K}$ as shown in Fig. 14(b).

We next considered a model containing a combination of the Debye model and two Einstein modes using the relation

$$C_{\rm p}(T) = (1 - \alpha_1 - \alpha_2) C_{\rm V \, Debye}(\Theta_{\rm D}, T) + (17)$$

$$\alpha_1 C_{\rm V \, Einstein}(\Theta_{\rm E_1}, T) + \alpha_2 C_{\rm V \, Einstein}(\Theta_{\rm E_2}, T).$$

The parameters obtained from a fit of the $C_{\rm p}(T)$ data from 50 to 300 K are $\Theta_{\rm D}=309(18)$ K, $\Theta_{\rm E_1}=94(5)$ K

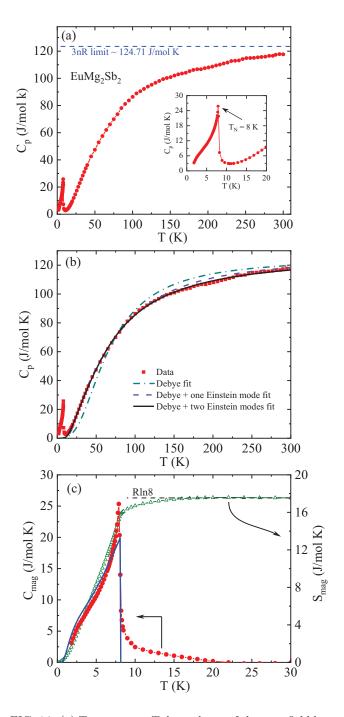


FIG. 14. (a) Temperature T dependence of the zero-field heat capacity $C_{\rm p}$ of an EuMg₂Sb₂ single crystal. The horizontal blue dashed line is the high-T Dulong-Petit limit. Inset: Expanded plot showing the λ -type peak at $T_{\rm N}=8.0(1)$ K. (b) $C_{\rm p}(T)$ fitted above T=50 K by the Debye model with $\gamma=0$ [blue dash-dotted line, Eq. (15)] and with one [dashed purple line, Eqs. (16a)] or two [solid black line, Eq. (17)] Einstein contributions. (c) Magnetic contribution $C_{\rm mag}(T)$ to $C_{\rm p}(T)$ (filled red circles, left ordinate) obtained by subtracting the fitted $C_{\rm p}(T)$ [Eq. (17)] from the experimental data. Also shown are the MFT prediction for $C_{\rm mag}(T)$ [Eq. (18), solid blue line] and the magnetic entropy $S_{\rm mag}(T)$ calculated from $C_{\rm mag}(T)$ using Eq. (19) (green diamonds, right ordinate).

with $\alpha_1 = 0.30(4)$, and $\Theta_{E_2} = 749(80)$ K with $\alpha_2 = 0.08(2)$. As seen in Fig. 14(b) (black curve), this is clearly the best fit to the data over the temperature range 50–300 K.

The magnetic contribution to the heat capacity $C_{\rm mag}(T)$ was obtained by subtracting the lattice contribution based on the model in Eq. (17) from the measured $C_{\rm p}(T)$ data over the temperature range 1.8 to 30 K. The result is shown in Fig. 14(c). According to MFT [38], $C_{\rm mag}(T)$ is given by

$$C_{\text{mag}}(t) = R \frac{3S\overline{\mu}_0^2(t)}{(S+1)t[\frac{(S+1)t}{3B_S'(t)} - 1]},$$
(18)

where the symbols are defined in Eqs. (13). The solid blue curve in Fig. 14(c) depicts $C_{\rm mag}(T)$ calculated using Eq. (18) with $T_{\rm N}=8$ K and S=7/2, where the agreement between theory and experiment is seen to be quite good, although the λ shape of the measured heat capacity and the short-range ordering that is clearly observed in the data above $T_{\rm N}$ are, of course, not reproduced by MFT.

The magnetic entropy $S_{\text{mag}}(T)$ was calculated according to

$$S_{\text{mag}}(T) = \int_0^T \frac{C_{\text{mag}}(T)}{T} dT. \tag{19}$$

The temperature dependence of $S_{\rm mag}$ is shown in Fig. 14(c) (green triangles, right ordinate). $S_{\rm mag}(T)$ reaches the expected high-T limit $S_{\rm mag}=R \ln(2S+1)=17.29$ J/mol K for S=7/2 at $T\gtrsim 20$ K rather than at $T_{\rm N}$. The short-range magnetic ordering above $T_{\rm N}$ noted above is responsible for this difference, as reported previously for the similar Eu-based compounds EuMg₂Bi₂, EuSn₂As₂, EuCo₂P₂, and EuCo₂- $_{\rm V}$ As₂ [15, 41–43].

V. SUMMARY

We have grown high-quality single crystals of the layered compound $\operatorname{EuMg_2Sb_2}$ and have studied its crystal-lographic, magnetic, electronic-transport, and thermal properties. The compound crystallizes in the trigonal $\operatorname{CaAl_2Si_2}$ -type crystal structure where the Eu atoms form a simple-triangular lattice in the ab plane that is stacked along the c axis.

The temperature dependence of zero-field electrical resistivity $\rho(T)$ indicates that EuMg₂Sb₂ is a narrow-gap semiconductor with an intrinsic energy gap $E_g=0.37~{\rm eV}$. This semiconducting state is also evident from the ARPES measurements. Although the similar isostructural compound EuMg₂Bi₂ was recently reported to have a semimetallic electronic ground state, the formation of a narrow-gap semiconducting state in EuMg₂Sb₂, where Sb has a smaller spin-orbit coupling (SOC) compared to Bi, suggests an important role of SOC coupling in tuning the electronic states of these Zintl-phase compounds.

Our DFT calculations further reveal that besides the SOC, hybridization of s-p orbitals also play a crucial role in tuning the electronic states. In these Zintl compounds the low-lying conduction bands along the Γ -A direction originate from the anti-bonding of s orbitals from Mg and are quite sensitive to the electronic negativity of the hybridized p orbitals. In this case, the hybridization with Mg 3s orbitals is more ionic for EuMg₂Sb₂ compared to EuMg₂Bi₂ as Sb is more electronegative and lighter than Bi, and pushes the low-lying conduction bands along the Γ -A direction to higher energy resulting in an indirect bulk band gap between the Γ and M points in the Brillouin zone for EuMg₂Sb₂.

The magnetic susceptibility $\chi(T)$ reveals a paramagnetic to AFM transition below the Néel temperature $T_{\rm N}=8.0(2)$ K. An additional sharp cusp is observed in the in-plane susceptibility $\chi_{ab}(T)$ at T=3.0 K which shifts to lower temperature with increasing H, whereas no such feature is observed in the $\chi_c(T)$ data. In addition, no anomaly in the heat capacity is observed at this temperature. The nature of this 3 K transition remains to be identified.

Our zero-field neutron-diffraction measurements in the temperature range 6–10 K showed that the AFM structure below $T_{\rm N}$ is A-type. In this magnetic structure, the Eu²⁺ spins 7/2 within an ab plane are aligned ferromagnetically within the plane with the Eu spins in adjacent Eu planes along the c axis aligned antiferromagnetically.

The magnetization in fields both in the ab plane and along the c axis saturates to a value of $7.0(5)\mu_{\rm B}/{\rm Eu}$ at T=1.8 K, consistent with expectation for S=7/2 with g=2, above the critical fields $H_{ab}^{\rm c}=2.6(1)$ T and $H_c^{\rm c}=3.4(1)$ T at T=1.8 K.

A sharp λ -type peak is observed at T_N in the zero-field heat capacity $C_p(T)$ data, consistent with the expected second-order nature of the long-range AFM transition. The release of the full magnetic entropy at a temperature of 30 K that is higher than T_N signifies the presence of significant short-range magnetic correlations above T_N .

Magnetic field-dependent $\chi(T)$ and isothermal magnetization M(H) data suggest that the A-type AFM ground state consists of threefold trigonal AFM domains, each containing antiferromagnetically-aligned magnetic moments in zero field, but where the moments reorient under the influence of a weak external ab-plane magnetic field to become nearly perpendicular to H for $H \sim 0.06$ T, apart from the weak canting of the moments towards the field which gives rise to the observed magnetization. Such a weak field-induced spin reorientation indicates the presence of a very weak in-plane anisotropy. The in-plane anisotropy arising from the magnetic-dipole interaction is indeed found to be extremely small. On the other hand, the magnetic dipole interaction is found to be responsible for much of the difference between the critical magnetic fields measured in the ab plane and along the c axis.

Appendix: Dependence of the Magnetic-Dipole Eigenvalues on the c/a Ratio of the Stacked-Triangular Lattice with A-type Antiferromagnetic Order

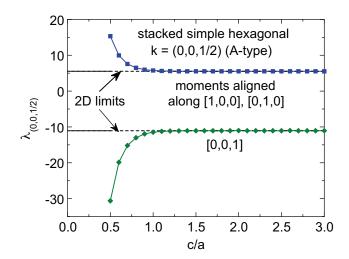


FIG. 15. Magnetic dipole eigenvalues $\lambda(0,0,1/2)$ versus the crystallographic c/a ratio for a stacked triangular lattice with A-type AFM ordering [k=(0,0,1/2) r.l.u.] and magnetic-moment orientations parallel to the hexagonal [0,0,1], [1,0,0], or [0,1,0] directions.

Figure 15 shows the dependence of the magnetic dipole eigenvalues $\lambda(0,0,1/2)$ for A-type AFM ordering with wavevector k = (0, 0, 1/2) reciprocal-lattice units on a a stacked triangular lattice as a function of the c/a ratio of the crystallographic lattice from 0.5 to 3 in increments of 0.1 for all spins in a radius of 50 times the hexagonal lattice constant a. The number of spins included varied from 1.2×10^6 for c/a = 0.5 to 2.0×10^5 for c/a = 3. As noted in the text, $\lambda(0, 0, 1/2)[0, 0, 1]$ and $\lambda(0,0,1/2)[1,0,0]/[0,1,0]$ rapidly approach the respective 2D limits of a single triangular spin layer with increasing c/a. Thus for the experimental c/a ratio of 1.6477 for EuMg₂Sb₂ at 6.6 K, the eigenvalues are close to the 2D limits of $\lambda(0,0,1/2)$ for the magnetic moments aligned along [1,0,0]/[0,1,0] and [0,0,1] given by 5.517088 and -11.034176, respectively, as seen in Fig. 15 and also noted in the main text.

Experimentally, in the AFM state the moments in ${\rm EuMg_2Sb_2}$ are aligned in the ab plane as discussed in the main text. This is consistent with Fig. 15 and Eqs. (7) which show that ab-plane moment alignment has a much lower energy than c-axis alignment. We note that due to an oversight, the calculations in Fig. 15 were not carried out in Ref. [39], which otherwise was quite comprehensive.

The values plotted in Fig. 15 are listed in Table III, which can be interpolated if desired. The accuracy of the eigenvalues is estimated to be ± 0.01 .

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TABLE III. Stacked Simple Hexagonal Spin Lattices with A-type AFM order with $\mathbf{k}=(0,0,1/2)$. Eigenvalues $\lambda_{\mathbf{k}\alpha}$ and eigenvectors $\hat{\mu}=[\mu_x,\mu_y,\mu_z]$ in Cartesian coordinates of the magnetic dipole interaction tensor $\widehat{\mathbf{G}}_i(\mathbf{k})$ in Eq. (16c) for various values of the magnetic wavevector \mathbf{k} in reciprocal lattice units (r.l.u.) for simple tetragonal spin lattices with **collinear** magnetic moment alignments. The most positive $\lambda_{\mathbf{k}\alpha}$ value(s) corresponds to the lowest energy value according to Eq. (16d). The Cartesian x,y and z axes are along the a,b and c axes of the tetragonal lattices, respectively. The accuracy of the values is estimated to be $\lesssim \pm 0.001$. Also shown are the differences between the eigenvalues for different ordering axes for a given \mathbf{k} , which determine the anisotropy energies via Eq. (16d).

	10 0	1 ()	
c/a		$\lambda_{(0,0,1/2)\alpha}$	
	$\alpha = [100], [010]$	[001]	[100] - [001]
0.5	15.301	-30.603	45.904
0.6	9.9432	-19.886	29.830
0.7	7.5810	-15.162	22.743
0.8	6.4963	-12.993	19.489
0.9	5.9848	-11.970	17.954
1.0	5.7431	-11.486	17.229
1.1	5.6246	-11.249	16.874
1.2	5.5707	-11.141	16.712
1.3	5.5417	-11.083	16.625
1.4	5.5304	-11.061	16.591
1.5	5.5219	-11.044	16.566
1.6	5.5193	-11.039	16.558
a 1.7	5.5181	-11.036	16.554
1.8	5.5191	-11.038	16.557
1.9	5.5184	-11.037	16.555
2.0	5.5143	-11.029	16.543
2.1	5.5185	-11.037	16.556
2.2	5.5154	-11.031	16.546
2.3	5.5183	-11.037	16.555
2.4	5.5151	-11.030	16.545
2.5	5.5207	-11.041	16.562
2.6	5.5147	-11.029	16.544
2.7	5.5172	-11.034	16.551
2.8	5.5204	-11.041	16.561
2.9	5.5152	-11.030	16.546
3.0	5.5155	-11.031	16.546

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