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# A New Hexagonal Ternary Alloy Phase Stable in Fe-Si-H at 28.6–42.2 GPa and 3000 K

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Hydrogen (H) and silicon (Si) are considered as important light elements for the planetary cores. A large amount of H is able to alloy with pure Fe metal at high pressures. Si can also alloy well with Fe. However, it remains uncertain how much H can alloy with iron silicides and if it alloys how H can alter the crystal structures of Fe-Si alloys at high pressures-temperatures (P-T). We performed experiments on Fe-9Si and Fe-16Si alloys (9 and 16 wt% Si, respectively) in a H medium up to 42.2 GPa and 3000 K in diamond-anvil cells coupled with pulsed laser heating and gated synchrotron X-ray diffraction techniques. We found conversion of the Fe-Si alloys into Ferich (fcc and dhcp FeH<sub>x</sub>), Si-rich (B20 and B2 FeSi), and intermediate (Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub>) phases. The new Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> phase has a structure similar to the hexagonal Fe<sub>5</sub>Si<sub>3</sub> phase but with expanded volumes, and thus, possible H incorporation. Both the observed volume expansion and the H content estimated by density functional theory calculations support a significant amount of H with H/Fe  $\approx$  0.6 in the crystal structure. Because Fe<sub>5</sub>Si<sub>3</sub> is known to break down above  $\sim$ 1300 K at  $\sim$ 18 GPa, our results suggest that hydrogen stabilizes the hexagonal structure at high P-T. These results have implications for the crystallization of Fe-rich liquid at the solid-to-liquid boundary of planetary cores and possible existence of chemical heterogeneities in the solid cores.

## I. INTRODUCTION

Light siderophile (Fe-loving) elements partitioned into the core-forming iron metal liquid in the early stage of planets' history. They then play an important role in the subsequent dynamics and evolution of the cores [1, 2]. Hydrogen (H) is the most abundant element in the universe and is considered to be one of the possible light elements in Fe-rich planetary cores [3, 4]. Although it has been controversial [5–7], recent experimental and theoretical studies suggested that as much as 0.3–0.6 wt% H can be incorporated into Earth's core [8, 9]. Furthermore, because of the coexistence of abundant molten Fe and silicate melt during the formation of early planetary cores, a large amount of Si can alloy with Fe metal to form Fe-Si alloys under a reducing condition [10, 11]. For instance, some geochemical and geophysical constraints suggest that up to 12 wt% Si can exist in the Earth's core, which would make Si the most abundant light element there. Despite the significance of Fe–Si–H system for planetary cores, the effect of H on Fe–Si alloys under relevant pressure and temperature (*P-T*) conditions is still limited due to technical challenges involved in studying H in laser-heated diamond anvil cells (LHDACs).

The binary Fe–Si system has multiples of stable phases with different compositions at ambient conditions, such as the orthorhombic FeSi<sub>2</sub>, tetragonal Fe<sub>3</sub>Si<sub>7</sub>, hexagonal Fe<sub>5</sub>Si<sub>3</sub>, and cubic Fe<sub>2</sub>Si [12–14]. When H was involved, early studies show that the H content in hcp Fe<sub>0.88</sub>Si<sub>0.12</sub> (Fe-6.5Si) is 1.2–1.5 wt% by laser heating below 1000 K at 27 and 62 GPa [15], which is much smaller than that in pure Fe metal, up to 8 wt% H above 130 GPa [16–18]. However, the heating temperature is much lower than what expected for planetary cores. Furthermore, how the H incorporation in Fe-Si alloys would change the high *P-T* phase relations is still unclear.

In this study, we reacted Fe-Si alloys and H up to 42.2 GPa and 3000 K in LHDACs by using pulsed laser heating combined with gated synchrotron X-ray diffraction (XRD) techniques. Fe-9Si (Fe<sub>0.83</sub>Si<sub>0.17</sub>) and Fe-16Si (Fe<sub>0.72</sub>Si<sub>0.28</sub>) (9 wt% and 16 wt% Si, respectively) were studied separately. High-pressure XRD patterns and chemical analyses on the recovered heated spots show that both Fe-9Si and Fe-16Si convert into FeH<sub>x</sub> with  $x \approx 1$  (face-centered-cubic (fcc) and double hexagonal-close-packed (dhcp)), FeSi (B20 and B2), and a hexagonal-structured Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub>(x is close to 3). We conducted complementary density functional theory (DFT) calculations to estimate the amount of H from the experimentally measured unit-cell volume.

Both starting materials (Fe-9Si and Fe-16Si) were obtained as powders with average grain sizes of 3–5  $\mu$ m from GoodFellow Corporation. Electron probe micro analysis (EPMA) (JEOL JXA-8530F) was conducted on more than ten randomly selected points of each sample (Table S1) [19]. The results show that both alloys are chemically homogeneous with Si contents of 8.84±0.30 wt% (Fe-9Si) and 15.93±0.31 wt% (Fe-16Si). The Si content in Fe-9Si alloy is comparable to those reported in previous experiments within uncertainties: 8.62±0.03 wt% [20], 8.7±0.3 wt% [21], 8.75±0.40 wt% [22], and 8.87±0.54 wt% [23]. Both powders were pressed into 5–10  $\mu$ m thick foils and then separately loaded into DACs for high *P-T* experiments. The sample chambers were prepared by using symmetric DACs with culet sizes of 200  $\mu$ m. Re gaskets were pre-indented to 25–30 GPa for ~20  $\mu$ m thicknesses and 130- $\mu$ m holes were drilled in the pre-indented areas to serve as sample chambers. A layer of > 80-Å thick gold was coated on each side of prepared gaskets to prevent embrittlement by H at high *P-T*. To avoid contact between the loaded sample foils and diamond anvils, foils were propped on both sides by small pieces of the same starting materials. This configuration also provides better thermal insulation and laser coupling during heating. A piece of Au and ruby were placed close to the sample within the chamber to serve as pressure calibrants [24]. Pure H<sub>2</sub> gas was then loaded into DACs as a hydrogen source and pressure medium using a gas loading system at Arizona State University.

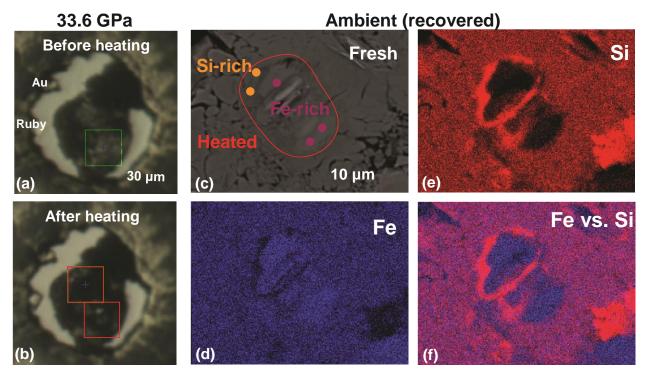


FIG. 1. Optical images of the sample chamber in a diamond anvil cell (a) before and (b) after heating at 33.6 GPa in a Fe-16Si run. The red rectangles in (b) show small transparent spots surrounded by dark areas after heating up to 3000 K, distinct from the flat and smooth surfaces of the fresh sample before heating (white rectangles). (c-f) Electron probe micro analysis on the recovered sample from a Fe-16Si run after high *P-T* reactions with H. (c) Electron back-scattered image of the recovered sample. A heated area is indicated by a red loop, showing a different texture from that of the unheated region. (d) and (e) Energy dispersive spectroscopy mapping of Fe and Si, respectively. (f) Chemical contrast between Fe and Si. The chemical mapping shows that the fresh Fe-16Si is chemically homogeneous, while the heated region has a Sirich rim with the Si-poor center. Quantitative chemical measurements were conducted on selected points using wavelength-dispersive spectroscopy and they are indicated by dots in (c) with results presented in Table S2 [19].

High P-T experiments were performed by employing pulsed laser heating together with synchrotron XRD at the 13-IDD beamline of the GeoSoilEnviroCARS (GSECARS) sector of the Advanced Photon Source (APS), Argonne National Laboratory (ANL). Two 1064-nm wavelength infrared laser beams at the beamline were focused on both sides of the sample with a flat-top spot size of around 15- $\mu$ m in diameter [25]. H can diffuse into diamonds and cause them to become brittle at high P-T. Therefore, laser heating was carried out in the pulsed mode at a repetition rate of 10 kHz. Because of the high diffusivity of H into metals,  $\sim 10^3 \, \mu$ m<sup>2</sup>/s even at low P-T [26], our experimental setup has shown to allow full reactions between the Fe-Si alloys ( $\sim 1 \, \mu$ m grain size at high pressure) and H [27]. The pulsed laser beams were co-axially aligned

with an incident monochromatic X-ray beam with a wavelength of 0.3344 Å and a spot size of 3  $\mu$ m × 4  $\mu$ m. The heating temperature was calculated by fitting the collected thermal radiation spectra from both sides of the sample to a Plank function based on a gray-body approximation [Fig. S1] [19].

In the Fe-9Si run, the sample in DAC was compressed to 28.6 GPa and pulsed heating was conducted up to 2610 K. XRD data were then collected during compression on both heated center and unheated region up to 42.2 GPa. Further heating experiments were performed on a new fresh Fe-9Si region to react with H at 42.2 GPa up to 2500 K. In the Fe-16Si run, we directly compressed the sample to 33.6 GPa and heated up to 3000 K [Fig. 1(a)-(b)]. During decompression, 2D XRD images were collected at the center of heated spots in both Fe-9Si and Fe-16Si runs. Diffraction images were collected using a Pilatus detector. PeakPo software was used for peak identifications [28]. Rietveld refinements were performed on XRD patterns to obtain the unit-cell parameters of synthesized phases using GSAS II [Figs 2–5] [29]. In this paper, we divided the unit-cell volume of each phase by the number of total Fe and Si atoms in a unit cell, which enables us to directly compare volumes of alloy phases with different compositions. Accordingly, the unit of volume is Å<sup>3</sup>/(# of Fe+Si Atoms). Electron probe micro analyses were conducted on the recovered samples at Eyring Materials Center of Arizona State University in order to determine the elemental distribution across the heated region [Fig. 1(c)-(f)] (Table S2) [19]. The JEOL JXA-8530F electron microprobe operated at an accelerating voltage of 15 eV and a beam current of 20 nA.

#### III. DENSITY FUNCTION THEORY CALCULATION

Complementary density functional theory (DFT) calculations were carried out to estimate the amount of H (x) in the synthesized Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> phase by comparing with our experimental observations. We employed the projector augmented-wave (PAW) method in combination with the Perdew-Burke-Ernzerhof (PBE) version of generalized gradient approximation (GGA) by using the GPAW package [30–32]. Previous studies on the unit-cell volumes of Fe-Si and Fe-H alloys using GGA have shown agreements with experiments (<1% difference) [33, 34]. In the crystal structure of Fe<sub>5</sub>Si<sub>3</sub>[35], H can occupy the interstitial sites, surrounded by 4Fe and 2Si at positions of (0.5, 0.5, 0.5), (0.5, 0, 0.5), and (0.5, 0, 0), to form Fe<sub>5</sub>Si<sub>3</sub>H<sub>3</sub>. Fe<sub>5</sub>Si<sub>3</sub>H<sub>3</sub> and Fe<sub>5</sub>Si<sub>3</sub> have 22 and 16 atoms per unit cell, respectively [Fig. 7(a)]. Electronic and structural convergence was carefully tested for each system. We eventually used a kinetic energy cutoff of 800 eV for Fe<sub>5</sub>Si<sub>3</sub> and 900 eV for Fe<sub>5</sub>Si<sub>3</sub>H<sub>3</sub> with  $\Gamma$ -centered k-point grids with a density of 3.5 Å<sup>-1</sup> or higher, which allows for calculations with a sufficient accuracy and efficiency in this study. We also attempted other possible H locations in Fe<sub>5</sub>Si<sub>3</sub>[19]. However, the sites discussed above yielded the best convergence.

In an Fe-Si alloy, magnetic ordering of Fe as well as H can affect its unit-cell volume. Accordingly, we considered both non-magnetic (NM) and ferromagnetic (FM) orderings for H-free and H-bearing phases in the calculation. Early Mössbauer and neutron-diffraction measurements have shown that Fe<sub>5</sub>Si<sub>3</sub> is ferromagnetic at 1 bar and has two crystallographically distinct Fe sites with spin directions parallel to the hexagonal c axis, where 4Fe(I) and 6Fe(II) have magnetic moments of  $1.05(15) \mu B$  and  $1.55(15) \mu B$ , respectively, at 100-290 K [36]. To understand the impact of magnetic ordering, we initiated the calculation on FM Fe<sub>5</sub>Si<sub>3</sub>H<sub>3</sub> using the same magnetic moments as FM Fe<sub>5</sub>Si<sub>3</sub>. At each selected volume for a given structure, the external and internal parameters were relaxed by calculating forces on atoms until the maximum total force on all individual atoms is less than  $0.005 \text{ eV/Å}^3$ , except for FM Fe<sub>5</sub>Si<sub>3</sub>H<sub>3</sub> at pressures above 25 GPa where the optimization became challenging. This calculation yields unit-cell parameters which were compared with experimentally observed values. We also conducted several tests on Fe<sub>5</sub>Si<sub>3</sub> at 0 GPa by using the DFT + U approach to account for potential electronic interactions in Supplementary Materials [19] (see also reference [37, 38] therein). We used different values of 1, 2, and 4 eV for the effective U parameter,  $U_{\text{eff}}$ . However, including U increases the discrepancy in magnetic moment between DFT and experimentally reported values [36]. Therefore, we did not consider the U term in our calculations. Our standard DFT calculations were conducted up to 40 GPa with a 10 GPa interval. A third order Birch-Murnaghan (BM) equation of state (EoS) was used to fit pressure-volume data from DFT calculations as well as experiments.

### IV. RESULTS AND DISCUSSION

At 1 bar, it has been debated if the stable crystal structure of Fe-9Si is body-centered cubic (bcc) [20, 21, 23] or D0<sub>3</sub> (BiF<sub>3</sub>-type) [22]. Studies suggested that with cold compression conversion of H-free Fe-9Si alloy to a hcp phase starts from  $\sim$ 16 GPa and completes at  $\sim$ 36 GPa [21, 39, 40]. Our XRD patterns show that the unheated Fe-9Si in a H environment completely converts to a hcp structure at 11.0 GPa without additional peaks belonging to bcc or D0<sub>3</sub> structures [Fig. 2(a)]. The unheated hcp Fe-9Si exhibits 3–5% greater unit-cell volumes than that of H-free Fe-9Si [Fig. 2(c)] (Table S3) [41], suggesting H has been incorporated to form hcp Fe<sub>0.83</sub>Si<sub>0.17</sub>H<sub>x</sub> by cold compression at 300 K.

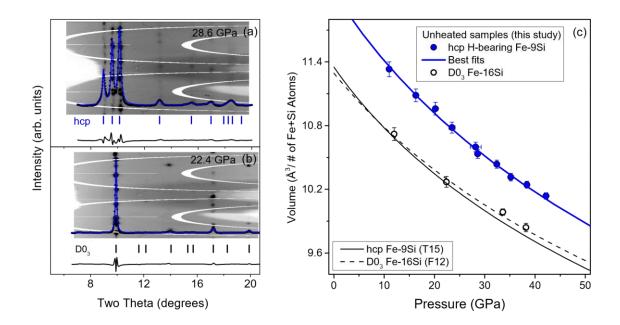


FIG. 2. X-ray diffraction results on cold-compressed, unheated Fe-Si alloys in a H medium at high pressure. (a) Cold-compressed hcp H-bearing Fe-9Si at 28.6 GPa. (b) Cold-compressed D0<sub>3</sub> Fe-16Si at 22.4 GPa. (c) Pressure-volume relationship of coldcompressed H-bearing Fe-9Si and Fe-16Si alloys. In (a) and (b), Rietveld refinements were performed to obtain the unit-cell parameters. The black circles are experimental data, the blue lines are the best fits, and the black lines are residuals. The blue and black ticks represent calculated peak positions of the hcp and D0<sub>3</sub> phases, respectively. Diffraction images are shown as backgrounds. The wavelength of incident X-ray is 0.3344 Å. In (c), the solid blue and open black circles are cold-compression data of hcp H-bearing Fe-9Si and D0<sub>3</sub> Fe-16Si, respectively. EoSs of H-free hcp Fe-9Si (T15) [41] and D0<sub>3</sub> Fe-16Si (F12) [42] were plotted as solid and dashed lines, respectively, for comparison. The solid blue line is the best 3rd order BM EoS fit for hcp H-bearing Fe-9Si (Table S4) [19]. We did not fit the *P-V* data of D0<sub>3</sub> Fe-16Si because of its agreement with EoS of H-free D0<sub>3</sub> Fe-16Si [42].

An empirical method [47] was used to estimate the hydrogen content (x) in metal alloys based on the volume expansion:  $x = (V_{\text{MHx}} - V_{\text{M}})/V_{\text{H}}$ , where  $V_{\text{H}}$ ,  $V_{\text{MHx}}$ , and  $V_{\text{M}}$  are the volume increase per H atom, the volume of metal hydride (MH $_x$ ) and the volume of H-free metal (M), respectively. We used an average value of ~2.5 Å $^3$ /(# of Metal Atoms) for  $V_{\text{H}}$  at ambient conditions from previous reports [47, 48]. The estimation yields  $x \approx 0.28$  in the hcp Fe<sub>0.83</sub>Si<sub>0.17</sub>H $_x$ , which is smaller than the H content (x = 0.50-0.64) reported for the hcp Fe<sub>0.88</sub>Si<sub>0.12</sub>H $_x$  alloys [15]. Note that for comparison, we corrected the x value in the hcp Fe<sub>0.88</sub>Si<sub>0.12</sub>H $_x$ , which was reported as 0.61–0.79 when using a  $V_{\text{H}}$  value of ~2.0 Å $^3$ /(# of Metal Atoms) [15]. In addition, Tagawa *et al.* [15] heated the sample to 1000 K, which may promote H solubility in the Fe<sub>0.88</sub>Si<sub>0.12</sub> alloy. Fitting the pressure-volume data of our hcp Fe<sub>0.83</sub>Si<sub>0.17</sub>H $_x$  at 300 K yields  $V_0 = 12.06$ (7) Å $^3$ /(# of Fe+Si Atoms),  $K_0 = 162$ (7) GPa, and  $K'_0 = 4.6$ (4) (Table S4) [19]. Compared with the H-free Fe-9Si (Table S4), the  $K_0$  of H-bearing Fe-9Si changes little but its and  $K'_0$  decreases by 10-16% even after considering the trade-off in EoS fittings.

Hydrogen-free Fe-16Si has a D0<sub>3</sub> structure up to 40 GPa at room temperature [42]. Our XRD patterns show that the unheated Fe-16Si in a H medium maintains a D0<sub>3</sub> structure at 12.0–38.2 GPa [Fig. 2(b)] and displays comparable volumes to H-free Fe-16Si [Fig. 2(c)] (Table S3) [42]. This indicates that little or no H enters into the structure of Fe-16Si without heating. Early studies show that pure metallic Fe can react with H to form dhcp FeH<sub>x</sub> above 3–4 GPa at room temperature [16, 17], while B20 and B2 FeSi do not exhibit such strong hydrogenation behavior with compression at 300 K [27]. Combining the cases of pure Fe metal [16], Fe-6.5Si [15], Fe-9Si, Fe-16Si, and FeSi alloys [27] collectively, we conclude that Si generally reduces the H solubility in Fe-Si alloys at high pressure and 300 K.

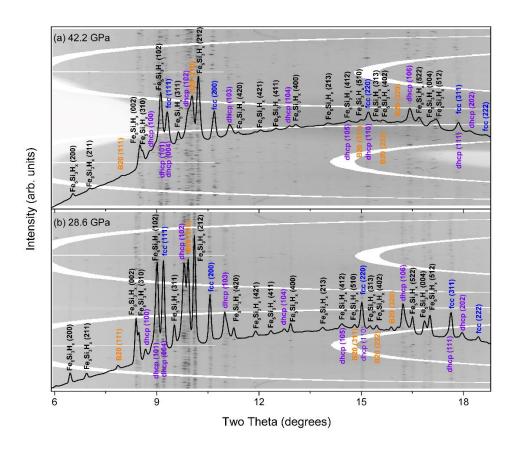


FIG. 3. X-ray diffraction patterns of the synthesized phases from high *P-T* reactions between Fe-9Si alloy and H. (a) 42.2 GPa and (b) 28.6 GPa. The diffraction peaks of Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> (black), fcc FeH<sub>x</sub> (blue), dhcp FeH<sub>x</sub> (purple), and B20 FeSi (orange) were labeled with their Miller indices. Although some of the diffraction peaks overlap due to the existence of multiple phases, more than 10 diagnostic peaks, that are distinct from any other phases, can be indexed with the hexagonal structure of Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub>. Diffraction images are plotted as backgrounds. The wavelength of incident X-ray is 0.3344 Å.

We separately laser heated Fe-9Si at 28.6–42.2 GPa and Fe-16Si at  $\sim$ 33.6 GPa in a H medium up to 2000–3000 K. Figures 3–5 and S2 show high-pressure XRD patterns of the reaction products measured after temperature quenched to 300 K during compression and/or decompression. Peak identification and indexing found that both reaction experiments on Fe-9Si and Fe-16Si yield almost identical phases, including B20 FeSi, fcc and dhcp FeH<sub>x</sub>, and a hexagonal-structured "Fe<sub>5</sub>Si<sub>3</sub>"-like phase (space group:  $P6_3/mcm$ ), except for the existence of an additional B2 FeSi in the Fe-16Si run. More than 10 diffraction peaks can be uniquely indexed to the "Fe<sub>5</sub>Si<sub>3</sub>"-like phase. In our diffraction patterns, the cubic B20 FeSi, B2 FeSi, and fcc FeH<sub>x</sub> phases each show more than 2 diagnostic peaks, and the dhcp FeH<sub>x</sub> phase has 4–5 diagnostic peaks. Rietveld refinements with small residual factor ( $R_{wp} < 2.4\%$ ) found that the "Fe<sub>5</sub>Si<sub>3</sub>"-like phase makes up approximately 10% of the synthesized products [Figs 3-5 and S2] (Table S5) [19]. Because of the higher molar mass of the "Fe<sub>5</sub>Si<sub>3</sub>"-like phase than other phases, it contributes significantly to the diffraction intensities in the measured XRD patterns [Fig. 5]. In addition, the smooth peak position shift trends with decompression as shown in Fig. S3 also support our peak assignments [19].

Comparison of the EoS data of the identified phases with previous experimental reports [Fig. 6] (Table S5) [19] suggests that: (1) The B2 phase has comparable high-pressure volumes to H-free B2 FeSi [39], while the B20 phase shows a slightly higher volume, < 1.5%, than H-free B20 FeSi [39]. This observation indicates limited H incorporation in the Si-rich FeSi alloy, which is consistent with recent reports on low H solubility in FeSi at high P-T [27]; (2) The unit-cell volumes of the fcc and dhcp phases agree well with those of fcc FeH $_x$  and dhcp FeH $_x$  with x = 1 [17, 43], respectively, indicating that these phases have H/Fe molar ratios close to 1; (3) The unit-cell volume of the hexagonal phase is 12–15% greater than that of H-free Fe<sub>5</sub>Si<sub>3</sub> ( $\Delta V \approx 1.57\pm0.09 \text{ Å}^3/(\text{# of Fe+Si Atoms}))$  [35, 45, 46]. Since H alloying in Fe metal can typically increase its unit-cell volume [16], we attribute the observed volume expansion to H incorporation into the structure of Fe<sub>5</sub>Si<sub>3</sub> to form Fe<sub>5</sub>Si<sub>3</sub>H $_x$ . The observed volume expansion could be used to estimate the H content in Fe<sub>5</sub>Si<sub>3</sub>H $_x$  by the empirical method [47]. However, validity of the empirical

method is not known for ternary hydrogen alloys (in our case Si-rich composition in particular) and the method is developed for binary hydrogen alloys (see later for our DFT approach).

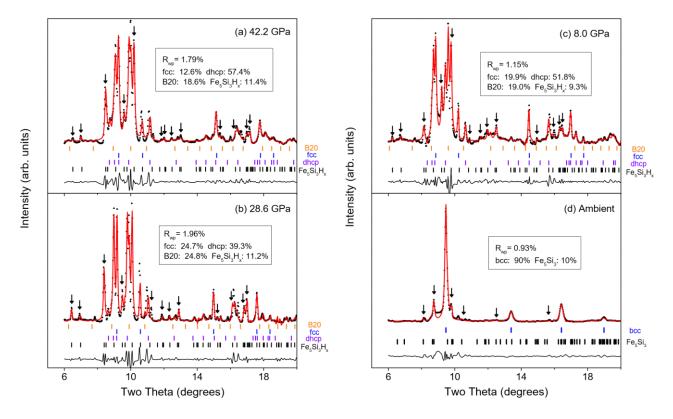


FIG. 4. Rietveld refinements on X-ray diffraction patterns of the synthesized products from Fe-9Si alloys and H. (a) 42.2 GPa. (b) 28.6 GPa. (b) 8.0 GPa. (d) After decompression to ambient conditions. The black circles are experimentally measured intensities, the red lines are the best fits, and the black lines are residuals. Peak positions of different phases are shown in the colored vertical ticks: B20 FeSi (orange), fcc FeH<sub>x</sub> (blue), dhcp FeH<sub>x</sub> (purple), and Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> (black). The diagnostic peaks that uniquely belong to Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> were labeled out with black arrows on top of them. Fit residue factor ( $R_{wp}$ ) and mole fractions of phases were provided in the legend. Upon decompression to ambient conditions, FeH<sub>x</sub> and Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> phases lose H and convert to bcc Fe and Fe<sub>5</sub>Si<sub>3</sub>, respectively. The wavelength of incident X-ray is 0.3344 Å.

Our experiments on Fe-Si alloys in a H medium were conducted at 28.6-42.2 GPa and the temperature was above 2000 K. McGuire *et al.* [45] show that H-free Fe<sub>5</sub>Si<sub>3</sub> is not stable at high temperature and will decompose into cubic FeSi and Fe<sub>3</sub>Si above 1300 K at 18 GPa, which is much lower than our experimental *P-T* conditions. This means that the incorporation of H could stabilize the hexagonal phase, and therefore Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub>. At pressures close to ambient conditions during decompression, dhcp and fcc FeH<sub>x</sub> phases recede and bcc Fe appears in the heated spot. This observation indicates that the FeH<sub>x</sub> phases lose H with decompression and convert to H-free bcc Fe, consistent with previous experimental observations [16]. The hexagonal phase (Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub>) maintains an expanded volume to ~1.1 GPa and then exhibits a volume shrink upon quenching to 1 bar. The volume at 1 bar is comparable to that of Fe<sub>5</sub>Si<sub>3</sub> [Fig. 6] [45], indicating H escaped during the decompression.

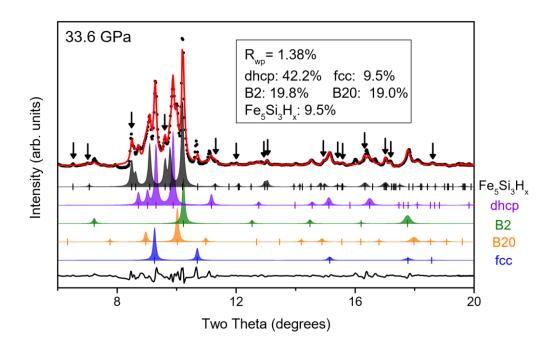


FIG. 5. Rietveld refinements on the XRD pattern of the synthesized products from Fe-16Si alloys and H at 33.6 GPa. The XRD pattern was collected after heating up to 3000 K. The black circles are measured intensities, the red lines are the best fits, and the black lines are fit residuals. Peak positions of B20 FeSi (orange), B2 FeSi (olive), fcc FeH<sub>x</sub> (blue), dhcp FeH<sub>x</sub> (purple), and Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> (black) were shown as colored ticks. The colored histograms of individual phases were calculated from the Rietveld refinements to show the contributions of different phases to the intensity of the measured pattern. The diagnostic peaks of Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> were indicated with black arrows. Residue factor ( $R_{wp}$ ) and mole fractions of the phases from the Rietveld refinements were provided in the legend. The wavelength of incident X-ray is 0.3344 Å.

The chemical mappings using EPMA show that the unheated region is chemically homogeneous with composition consistent with that of the starting material, while the heated spot has a Si-rich rim with a Si-poor center [Fig. 1(c)(f)]. Optical images of the heat regions show an apparent melting signature: removal of much material by the mobility of melt from the heated center toward lower-temperature surroundings [49]. Thus, we believe the liquidus phase exists at the margin, which crystallized first with higher melting temperatures, and the center region should be alloy phases converted from the melt during temperature quench. Quantitative wavelength-dispersive spectroscopy measurements on selected points of the recovered sample show that the Si-rich rim contains about 29 wt% Si, while the center area contains 5.9-7.5 wt% Si (Table S2) [19]. Considering the higher melting temperatures of Fe-Si alloys than that of FeH<sub>x</sub> [22, 50], the margin area may consist of FeSi (33.3 wt% Si) and Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> ( $\sim$ 23.1 wt% Si), and the center region most likely corresponds to the FeH<sub>x</sub> alloy observed in XRD. We note that, during decompression to ambient conditions, the sample chamber shrank due to the release of H pressure medium and the sample foil deformed, resulting in different sizes and shapes from that at high pressures [Fig. 1(c)-(f)]. Therefore, it is difficult to compare details of XRD and EPMA observations beyond first order distribution of the elements. It is also important to note that the excitation volume in EPMA experiments is larger than the alloy grains of the recovered sample foil, resulting in an averaging effect on measured compositions. On the other hand, XRD does not have the averaging effects and therefore can reveal more details. While transmission electron microscopy (TEM) could provide better resolution to detect single phases for laser-heated spots in DACs, sample recovery and preparation for TEM analysis were challenging because of the fragile nature of the sample laser heated in a soft H medium at high pressures.

The empirical method [47] to estimate the H content in metals was developed for the close-packed alloys. However, the crystal structure of Fe<sub>5</sub>Si<sub>3</sub> is quite different from close-packed structures and therefore the question arises whether the method can be applied to Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub>. To further gain insights on the amount of H in the hexagonal phase, we conducted DFT calculations (see section III for detailed DFT calculations setup on FM and NM structure models of Fe<sub>5</sub>Si<sub>3</sub>H<sub>3</sub> and Fe<sub>5</sub>Si<sub>3</sub>). Results on FM and NM Fe<sub>5</sub>Si<sub>3</sub> and FM and NM Fe<sub>5</sub>Si<sub>3</sub>H<sub>3</sub> were compared with our experimental data on Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> as well as H-free Fe<sub>5</sub>Si<sub>3</sub> [35, 45, 46].

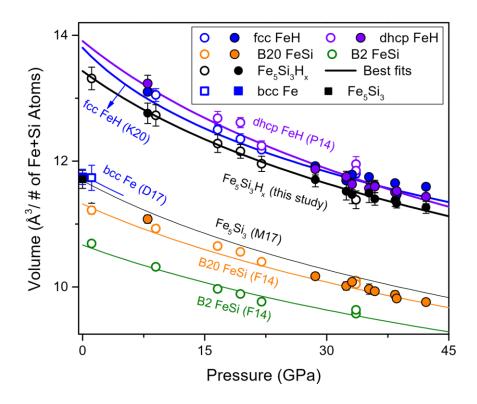


FIG. 6. Pressure-volume relationship of phases synthesized from Fe-Si alloys and H reactions. The measurements were conducted on the reaction products at 300 K during compression and/or decompression. The solid and open symbols are from the runs of Fe-9Si and Fe-16Si, respectively: B2 FeSi (olive circles), B20 FeSi (orange circles), fcc FeH<sub>x</sub> (blue circles), dhcp FeH<sub>x</sub> (purple circles), and Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> (black circles). The solid black line is the best 3rd order BM EoS fit to the Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> data together from two different runs. Previous experimental reports on B2 FeSi (F14) [39], B20 FeSi (F14) [39], fcc FeH (K20) [43] and dhcp FeH (P14) [17], were plotted as solid lines with corresponding colors for comparison. FeH<sub>x</sub> and Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> phases lose H and convert to bcc Fe (blue squares) and Fe<sub>5</sub>Si<sub>3</sub> (black squares), respectively, upon recovery to 1 bar. Previous results on bcc Fe (D17) [44] and Fe<sub>5</sub>Si<sub>3</sub> (M17) [45] were plotted as blue and black thin lines, respectively. We note that existing EoS data for H-free Fe<sub>5</sub>Si<sub>3</sub> [35, 45, 46] are consistent with each other and here we show data points from McGuire *et al.* [45].

Our calculated volumes of FM Fe<sub>5</sub>Si<sub>3</sub> agree well with previous experimental reports on H-free Fe<sub>5</sub>Si<sub>3</sub> within uncertainty (< 0.8% difference) at 0–40 GPa [Fig. 7(b)] [45, 46]. DFT calculations on NM Fe<sub>5</sub>Si<sub>3</sub> predict about 1.8–5.1% smaller volumes than the experimental data of H-free Fe<sub>5</sub>Si<sub>3</sub> [45, 46]. Earlier Mössbauer study showed a FM ordering for H-free Fe<sub>5</sub>Si<sub>3</sub> at 1 bar [36]. Our results also anticipate that Fe<sub>5</sub>Si<sub>3</sub> is more likely to be FM at 0–40 GPa. Our measured volumes of the hexagonal Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> show a good agreement (< 1.5% difference) with those of both NM and FM Fe<sub>5</sub>Si<sub>3</sub>H<sub>3</sub> from DFT calculations, considering the experimental uncertainties [Fig. 7(b)]. Fitting the experimental pressure-volume data of Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> to 3rd order BM EoS yields  $V_0 = 13.43(9)$  Å<sup>3</sup>/(# of Fe+Si Atoms),  $K_0 = 147(12)$  GPa, and  $K'_0 = 5.1(6)$ . In comparison, we obtained  $K_0 = 155.6$  GPa and  $K'_0 = 4.1$  ( $V_0 = 13.5$  Å<sup>3</sup>/(# of Fe+Si Atoms), fixed) for FM Fe<sub>5</sub>Si<sub>3</sub>H<sub>3</sub>, and  $K_0 = 169.1$  GPa and  $K'_0 = 4.5$  ( $V_0 = 13.1$  Å<sup>3</sup>/(# of Fe+Si Atoms), fixed) for NM Fe<sub>5</sub>Si<sub>3</sub>H<sub>3</sub>, respectively (Table S4) [19]. Taking into account the trade-off in BM EoS fittings and experimental uncertainties, the  $K_0$  of synthesized Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> is comparable with both FM and NM phases, while its  $K'_0$  is higher. Compared to H-free Fe<sub>5</sub>Si<sub>3</sub> (Table S4) [35, 45, 46], the  $V_0$  of our experimental Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> is about 14.7% higher, while its  $K_0$  decreases and  $K'_0$  increases, indicating a strong H incorporation effect on the EoS parameters of Fe-Si alloys. We should note that the DFT was conducted for static lattice conditions, while experimental measurements were performed at 300 K.

The DFT calculations predict that FM Fe<sub>5</sub>Si<sub>3</sub>H<sub>3</sub> has 2.1–3.1% higher volumes than the NM case at 0–40 GPa. The volume expansion caused by magnetic ordering is much smaller than that by H incorporation, suggesting that our observed volume expansion in Fe<sub>5</sub>Si<sub>3</sub> should mainly result from the H solubility. Although we do not have direct experimental chemical or neutron diffraction measurements on the H content in the synthesized phase in this study, to first order, the great agreement on the volumes between DFT and experimental data supports the synthesis of the new ternary alloy Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub>. More detailed information on other properties of FM and NM Fe<sub>5</sub>Si<sub>3</sub>H<sub>3</sub> is provided in Supplementary Materials drawn from our DFT calculations [19] (see also references [51, 52] therein). While we believe that the level of agreement is adequate to explain the experimental observed volume expansion, future detailed DFT investigation is still required to decipher the structure, composition, and magnetic ordering of the new Fe<sub>5</sub>Si<sub>3</sub>H<sub>x</sub> ternary phase.

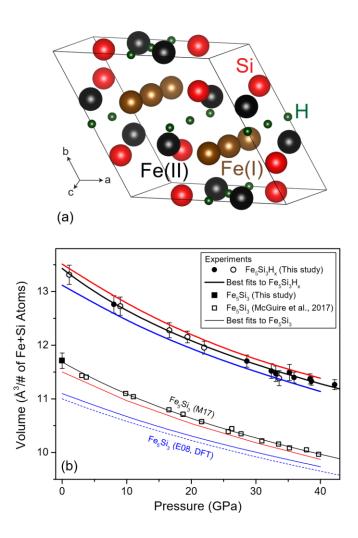


FIG. 7. Density functional theory calculations on  $Fe_5Si_3H_3$  and  $Fe_5Si_3$  at high pressure. (a) A crystal structure model of  $Fe_5Si_3H_3$  (Z=22) at 0 GPa from the DFT calculations. The crystal structure of  $Fe_5Si_3H_3$  is modified from that of  $Fe_5Si_3$  [35] by placing H atoms at (0.5, 0.5), (0.5, 0, 0.5), and (0.5, 0, 0). (b) Pressure-volume relationship. Thick and thin lines are for  $Fe_5Si_3H_3$  and  $Fe_5Si_3$ , respectively, and red and blue colors are used for ferromagnetic and nonmagnetic calculations, respectively. Solid and open circles are our experimental data points of the synthesized  $Fe_5Si_3H_x$  from the runs of  $Fe_9Si$  and  $Fe_16Si$ , respectively. The solid black squares are from the recovered sample at ambient conditions. Open black squares are for H-free  $Fe_5Si_3$  from McGuire *et al.* [45]. Thick and thin black lines are the best 3rd order BM EoS fit to  $Fe_5Si_3H_x$  in this study and  $Fe_5Si_3$  by McGuire *et al.* [45], respectively. The dashed blue line is from an earlier DFT calculation on H-free  $Fe_5Si_3$  [46] for comparison.

#### V. CONCLUSIONS

We found the appearance of a hexagonal-structured Fe-Si-H ternary phase,  $Fe_5Si_3H_x$ , at high pressures after heating up to 3000 K, which was observed for the first time to our knowledge. Comparison between the observed volume expansion and DFT calculations suggests the H/Fe ratio is about 0.6 in this phase. This is in contrast with Si-rich B20 and B2 FeSi alloys with little H solubility [27]. It is important to note that  $Fe_5Si_3$  is not stable above 1300 K at 18 GPa [45] and therefore H plays an important role for the high P-T stability.

Our high-pressure experiments also showed that Fe-9Si and Fe-16Si break down in a H medium upon laser heating up to 3000 K at 28.6–42.2 GPa. The reaction produces Fe-rich (dhcp and fcc FeH<sub>x</sub>), Si-rich (B20 and B2 FeSi) and a Fe-Si-H ternary phase. In our experiments, the sample was heated above the melting temperatures of Fe–Si–H. The texture and chemical measurements show that Si-rich alloys are likely formed as solidus phases and H-rich alloys are from the quenched melt. Such an observation can have important implications for the crystallization at the solid-liquid boundary of planetary cores, such as the Earth's inner and outer core boundary. In the Earth's inner core, significant heterogeneities have been documented in seismic studies [53],

which could be a record of time-dependent crystallization pattern at the solid-to-liquid core boundary. The role of light elements on the crystallization process of Fe-rich metal is important to understand the compositional effect on dynamo generation [54]. Although our study did not reach the pressure of Earth's core, the experimental conditions here are relevant to the cores of Mars or Mars-sized exoplanets [55]. Recently InSight mission revealed that the Martian core is much larger than previously believed, and thus, should have a low density and large concentrations of light elements [56]. Furthermore, geodetic measurements have shown that the significant part of the Martian core is in a liquid state [57]. Therefore, the phase relations found in this study will be important for understanding the metallic cores of such smaller planets and their magnetic history.

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