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Dynamic Transformation Between a Skyrmion String and a Bimeron String in a Layered Frustrated System

Xichao Zhang,^{1,2,*} Jing Xia,^{1,2,*} Oleg A. Tretiakov,³ Hung T. Diep,⁴ Guoping Zhao,⁵
Jinbo Yang,⁶ Yan Zhou,^{2,†} Motohiko Ezawa,^{7,‡} and Xiaoxi Liu^{1,§}

¹*Department of Electrical and Computer Engineering,
Shinshu University, 4-17-1 Wakasato, Nagano 380-8553, Japan*

²*School of Science and Engineering, The Chinese University of Hong Kong, Shenzhen, Guangdong 518172, China*

³*School of Physics, The University of New South Wales, Sydney 2052, Australia*

⁴*Laboratoire de Physique Théorique et Modélisation, CY Cergy Paris Université, 95302 Cergy-Pontoise Cedex, France*

⁵*College of Physics and Electronic Engineering, Sichuan Normal University, Chengdu 610068, China*

⁶*State Key Laboratory for Mesoscopic Physics, School of Physics, Peking University, Beijing, 100871, China*

⁷*Department of Applied Physics, The University of Tokyo, 7-3-1 Hongo, Tokyo 113-8656, Japan*

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Frustrated topological spin textures have unique properties that may enable novel spintronic applications, such as the helicity-based information storage and computing. Here we report the statics and current-induced dynamics of two-dimensional (2D) pancake skyrmions in a stack of weakly coupled frustrated magnetic monolayers, which form a three-dimensional (3D) skyrmion string. The Bloch-type skyrmion string is energetically more stable than its Néel-type counterpart. It can be driven into translational motion by the dampinglike spin-orbit torque and shows the damping-dependent skyrmion Hall effect. Most notably, the skyrmion string can be transformed to a dynamically stable bimeron string by the dampinglike spin-orbit torque. The current-induced bimeron string rotates stably with respect to its center, which can spontaneously transform back to a skyrmion string when the current is switched off. Our results reveal unusual physical properties of 3D frustrated spin textures, and may open up new possibilities for spintronic applications based on skyrmion and bimeron strings.

Introduction. Topological spin textures are particlelike objects that can be used as robust information carriers for data processing [1–15]. Frustrated spin systems can host different species of topological spin textures [16–45], which show very different physical properties and behaviors compared to their common ferromagnetic (FM) counterparts. For example, skyrmions carrying different topological charges, either positive or negative, can be stabilized in a perpendicularly magnetized monolayer with exchange frustration [16–39, 41]. In contrast, skyrmions in common chiral magnets are stabilized by Dzyaloshinskii-Moriya (DM) exchange interactions [1–15, 46, 47], and skyrmions with large or negative topological charges are usually unstable in chiral magnets with symmetric DM interactions [48]. Other exemplary topological spin textures in frustrated spin systems include the so-called skyrmionium [41], bimeron [23, 36, 40, 49], and bimeronium [42], all of which are functional building blocks for spintronic applications [7, 8, 11–15, 50].

Recent studies on frustrated skyrmions have mainly focused on the static and dynamic properties of frustrated skyrmions in the two-dimensional (2D) space [16–43]. In particular, theoretical works have shown that the helicity dynamics of a 2D frustrated skyrmion is coupled to its center-of-mass dynamics [17, 18, 22, 24, 30, 33, 40]. This property is in stark contrast to that of 2D skyrmions stabilized in chiral magnets, where the helicity of a moving skyrmion is strictly locked by the DM exchange interaction [1–15]. This feature also implies that the 2D frustrated skyrmions have more degrees of freedom that, in principle, can be manipulated by external stimuli and used for building future spintronic devices [17, 22, 24, 33, 40–43]. For example, several studies

have suggested that the information can be encoded by the location of skyrmions with unity topological charges in chiral magnets [7, 8, 11–15]. In frustrated spin systems, the information can be carried by the topological charge of skyrmions or be encoded by the helicity of skyrmions [17, 22, 24, 33, 40–43].

However, the physical properties and potential applications of frustrated skyrmions in three-dimensional (3D) structures still remain elusive and thus represent an area of significant opportunity for research. As an analogy to the 3D vortex line forming by 2D pancake vortices [51, 52] in a stack of coupled superconducting layers [53, 54], a 3D frustrated skyrmion string can be constructed by a stack of pancake skyrmions in a frustrated multilayer [55, 56], where each frustrated pancake skyrmion is a 2D object. Such a 3D skyrmion string is an important component for future spintronic applications based on 3D nanostructures [55, 56] and layered systems [55, 57, 58]. In this Letter, we report the statics and dynamics of such a stack of frustrated pancake skyrmions, where the pancake skyrmions in two adjacent monolayer are coupled via a FM interlayer exchange coupling.

Model. To be specific, we consider a 3D skyrmion string forming by 11 aligned stacks of 2D pancake skyrmions in a frustrated spin system. Each 2D FM layer has 25×25 spins and is described by a J_1 - J_2 - J_3 classical Heisenberg model on a simple square lattice [18, 21, 24, 33, 39–41, 59], of which the Hamiltonian \mathcal{H}_n reads

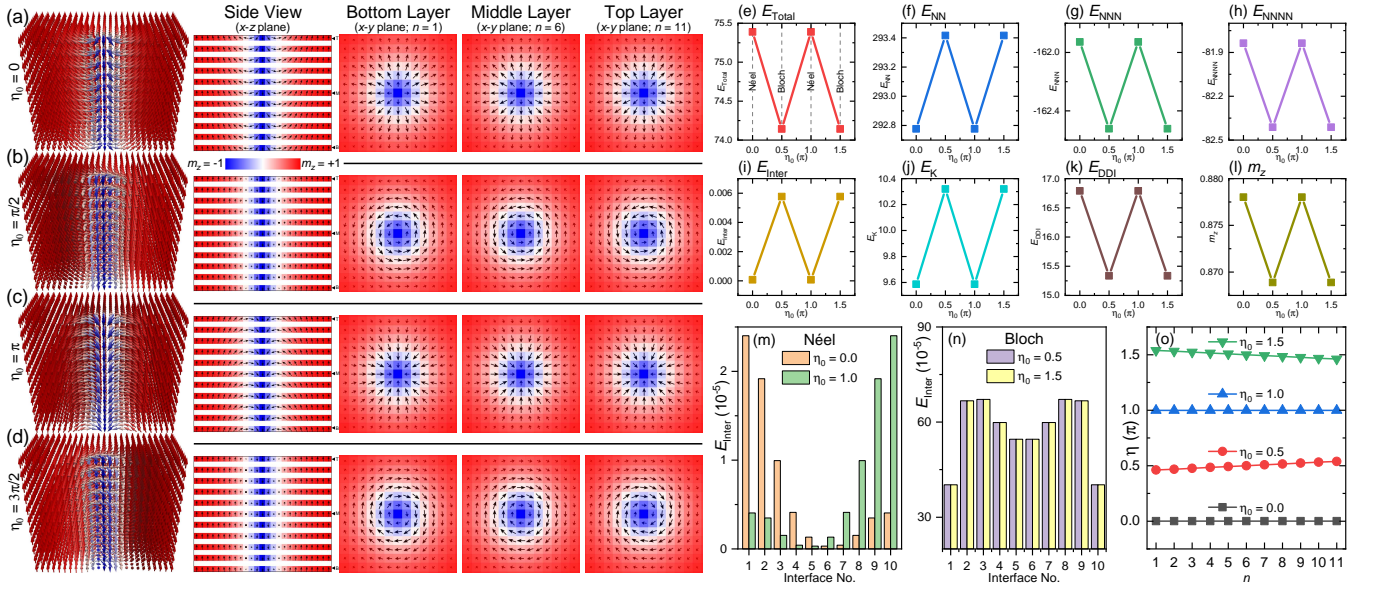


FIG. 1. 3D and 2D illustrations of static skyrmion strings that are relaxed with the initial helicity of (a) $\eta_0 = 0$, (b) $\eta_0 = \pi/2$, (c) $\eta_0 = \pi$, and (d) $\eta_0 = 3\pi/2$. The 3D and 2D side views show the vertical cross sections through the core of the skyrmion string. The 2D top views show the horizontal cross sections through the bottommost ($n = 1$), middle ($n = 6$), and topmost ($n = 11$) FM layers, and focus on the skyrmion core area. The arrow represents the spin direction. The color scale represents the out-of-plane spin component m_z , which has been used throughout the paper. (e) Total energy E_{Total} , (f) NN exchange energy E_{NN} , (g) NNN exchange energy E_{NNN} , (h) NNNN exchange energy E_{NNNN} , (i) total interlayer exchange energy E_{inter} , (j) PMA energy E_K , (k) DDI energy E_{DDI} , and (l) m_z as functions of η_0 are given. All energies are given in units of $J_1 = 1$. Interlayer exchange energies as functions of interface number are given for the skyrmion strings relaxed with (m) $\eta_0 = 0, 1$ and (n) $\eta_0 = \pi/2, 3\pi/3$. (o) Layer-dependent helicity η of the relaxed skyrmion strings.

$$\mathcal{H}_n = -J_1 \sum_{\langle i,j \rangle} \mathbf{m}_i^n \cdot \mathbf{m}_j^n - J_2 \sum_{\langle\langle i,j \rangle\rangle} \mathbf{m}_i^n \cdot \mathbf{m}_j^n - J_3 \sum_{\langle\langle\langle i,j \rangle\rangle\rangle} \mathbf{m}_i^n \cdot \mathbf{m}_j^n - K \sum_i (m_i^{n,z})^2 + H_{\text{DDI}}, \quad (1)$$

where n is the FM layer index ($n = 1, 2, \dots, 11$), \mathbf{m}_i^n represents the normalized spin at the site i of layer n , $|\mathbf{m}_i^n| = 1$. J_1 , J_2 , and J_3 denote the FM nearest-neighbor (NN), anti-ferromagnetic (AFM) next-NN (NNN), and AFM next-NNN (NNNN) intralayer exchange interaction constants, respectively. $\langle i, j \rangle$, $\langle\langle i, j \rangle\rangle$, and $\langle\langle\langle i, j \rangle\rangle\rangle$ run over all the NN, NNN, and NNNN sites in each FM layer, respectively. K is the perpendicular magnetic anisotropy (PMA) constant. H_{DDI} stands for the dipole-dipole interaction (DDI). In our model, two NN FM layers are separated by a nonmagnetic heavy-metal spacer layer, which is required for realizing the interlayer coupling and spin current [60]. We note that the spacers may consist of different heavy metals to ensure a net spin current. The Hamiltonian $\mathcal{H}_{\text{inter}}$ for the interlayer coupling reads

$$\mathcal{H}_{\text{inter}} = - \sum_{n=1}^{10} J_{\text{inter}} \sum_i \mathbf{m}_i^n \cdot \mathbf{m}_i^{n+1}. \quad (2)$$

Hence, the total Hamiltonian of the system is written as $\mathcal{H} = \sum_{n=1}^{10} \mathcal{H}_n + \mathcal{H}_{\text{inter}}$. We assume that the adjacent FM layers are coupled through a weak FM interlayer coupling $J_{\text{inter}} = 0.01$

(in units of $J_1 = 1$). We also assume that the spin dynamics is induced by the dampinglike spin-orbit torque τ_d , which is described by the Landau-Lifshitz-Gilbert equation augmented with τ_d [61]

$$\frac{d\mathbf{m}}{dt} = -\gamma_0 \mathbf{m} \times \mathbf{h}_{\text{eff}} + \alpha \left(\mathbf{m} \times \frac{d\mathbf{m}}{dt} \right) + \tau_d, \quad (3)$$

where $\mathbf{h}_{\text{eff}} = -\frac{1}{\mu_0 M_S} \cdot \frac{\delta \mathcal{H}}{\delta \mathbf{m}}$ is the effective field, μ_0 is the vacuum permeability constant, M_S is the saturation magnetization, t is the time, α is the Gilbert damping parameter, and γ_0 is the absolute gyromagnetic ratio. $\tau_d = \frac{u}{b} (\mathbf{m} \times \mathbf{p} \times \mathbf{m})$ with $u = |(\gamma_0 \hbar / \mu_0 e)| \cdot (j \theta_{\text{SH}} / 2 M_S)$ being the spin torque coefficient. \hbar is the reduced Planck constant, e is the electron charge, b is the FM layer thickness, j is the current density, and θ_{SH} is the spin Hall angle. $\mathbf{p} = -\hat{y}$ denotes the spin polarization orientation.

The default parameters are [18, 24, 33, 40, 41]: $J_1 = 30$ meV, $J_2 = -0.8$ (in units of $J_1 = 1$), $J_3 = -0.6$ (in units of $J_1 = 1$), $K = 0.01$ (in units of $J_1/a^3 = 1$), $\alpha = 0.3$, $\gamma_0 = 2.211 \times 10^5$ m A $^{-1}$ s $^{-1}$, $\theta_{\text{SH}} = 0.2$, and $M_S = 580$ kA m $^{-1}$. The lattice constant is $a = 0.4$ nm. The mesh size is a^3 . We use the Object Oriented MicroMagnetic Framework (OOMMF) [61] upgraded with our extension modules to simulate the model. We have simulated the metastability diagram using the OOMMF minimizer, which shows that the frustrated skyrmion strings are a metastable state for a wide range of J_2 and J_3 (see Ref. 62). The minimum required value of J_3 for stabilizing a skyrmion string decreases with increasing J_2 .

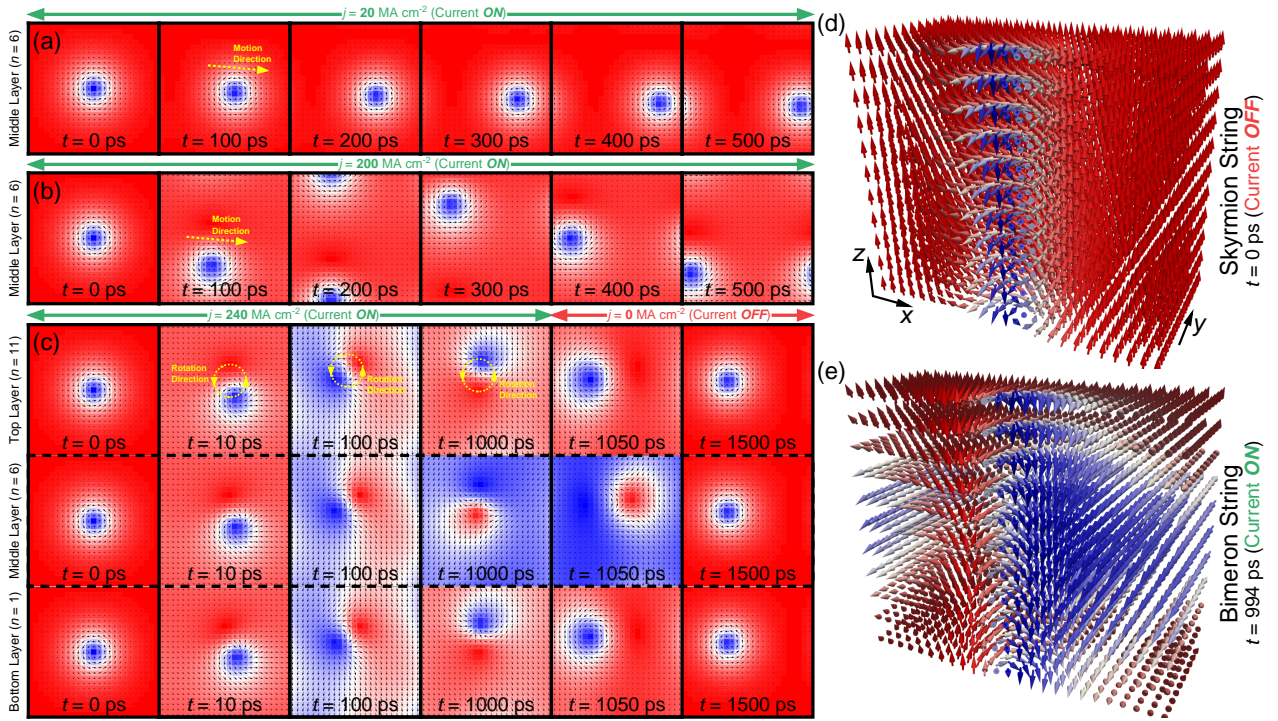


FIG. 2. Top views of a Bloch-type skyrmion string driven by (a) a small current $j = 20 \text{ MA cm}^{-2}$ and (b) a large current $j = 200 \text{ MA cm}^{-2}$. The spin configurations are similar in all FM layers, so only the spin configuration of the middle layer ($n = 6$) is given. (c) Top views of the current-controlled mutual transformation between a skyrmion string and a bimeron string. $j = 240 \text{ MA cm}^{-2}$ is applied for $t = 0 \sim 1000$ ps, followed by a 500-ps-long relaxation. The spin configurations of the bottommost ($n = 1$), middle ($n = 6$), and topmost ($n = 11$) layers are given. (d) 3D view of the core of the skyrmion string at $t = 0$ ps. (e) 3D view of the core of the bimeron string at $t = 994$ ps.

114 *Static structures.* We begin with simulating the static
 115 structure of a stack of coupled frustrated 2D pancake
 116 skyrmions in the absence of a driving current. The inter-
 117 layer coupling between adjacent pancake skyrmions leads
 118 to a 3D skyrmion string (Fig. 1). The static structure
 119 of each pancake skyrmion is described by the topological
 120 charge $Q = \frac{1}{4\pi} \int \mathbf{m}(\mathbf{r}) \cdot (\partial_x \mathbf{m}(\mathbf{r}) \times \partial_y \mathbf{m}(\mathbf{r})) d^2\mathbf{r}$. We
 121 parametrize each pancake skyrmion as $\mathbf{m}(\mathbf{r}) = \mathbf{m}(\theta, \phi) =$
 122 $(\sin \theta \cos \phi, \sin \theta \sin \phi, \cos \theta)$, where we define $\phi = Q_v \varphi + \eta$
 123 with φ being the azimuthal angle ($0 \leq \varphi < 2\pi$). Hence,
 124 $Q_v = \frac{1}{2\pi} \oint_C d\phi$ is the skyrmion vorticity and $\eta \in [0, 2\pi)$ is the
 125 skyrmion helicity defined mod 2π . We assume that $Q_v = +1$
 126 (i.e., $Q = -1$) and θ rotates by an angle of π for spins from
 127 the skyrmion center to the skyrmion edge [1, 4, 14, 15].

128 The relaxed skyrmion strings consisting of Néel-type ($\eta =$
 129 $0, \pi$) or Bloch-type ($\eta = \pm\pi/2$) pancake skyrmions are given
 130 in Fig. 1. Before the relaxation, a skyrmion with an initial
 131 helicity $\eta_0 = 0, \pi/2, \pi, 3\pi/2$ is placed at the center of
 132 each FM layer. η_0 is identical in all FM layers. Then, as
 133 shown in Figs. 1(a)-1(d), the Néel-type skyrmion strings with
 134 $\eta_0 = 0, \pi$ are relaxed to states with $\eta = \eta_0$ in each FM layer,
 135 while the Bloch-type skyrmion strings with $\eta_0 = \pi/2, 3\pi/2$
 136 are relaxed to states with slightly nonuniform $\eta \sim \eta_0$ in
 137 each FM layer [Fig. 1(o)]. The total energies of the relaxed
 138 Néel-type skyrmion strings are larger than that of the Bloch-
 139 type skyrmion strings [Fig. 1(e)], indicating the Néel-type

140 skyrmion strings are unstable states, largely due to the fact
 141 that the Bloch-type structures with $\eta = \pi/2, 3\pi/2$ are fa-
 142 vored by the DDI [Fig. 1(k)]. In general, the relaxed Bloch-
 143 type skyrmion strings have slightly smaller out-of-plane mag-
 144 netization [Fig. 1(l)], smaller NNN exchange [Fig. 1(g)],
 145 and NNNN exchange energies [Fig. 1(h)]. However, their
 146 NN exchange [Fig. 1(f)], interlayer exchange [Fig. 1(i)], and
 147 anisotropy energies [Fig. 1(j)] are slightly larger than that of
 148 relaxed Néel-type skyrmion strings.

149 The interlayer coupling energy is found to have a layer de-
 150 pendence for both relaxed Néel-type and Bloch-type skyrmion
 151 strings. For the Néel-type skyrmion string with $\eta = 0$
 152 [Fig. 1(m)], the layer-dependent interlayer coupling energy
 153 reaches its maximum magnitude at the bottommost interface
 154 (i.e., the interface between $n = 1$ and $n = 2$). For the
 155 Néel-type skyrmion string with $\eta = \pi$, the layer-dependent
 156 interlayer coupling energy reaches its maximum magnitude at
 157 the topmost interface (i.e., the interface between $n = 10$
 158 and $n = 11$). In contrast, for the Bloch-type skyrmion strings
 159 with $\eta \sim \pi/2, 3\pi/2$, the layer-dependent interlayer coupling
 160 energy shows an identical M-profile dependence on the in-
 161 terfaces [Fig. 1(n)]. The interlayer coupling energy of the
 162 Bloch-type skyrmion string is larger than that of the Néel-
 163 type one, which is due to the slightly different in-plane spin
 164 configuration of each FM layer, as can be seen from the n -
 165 dependent η in Fig. 1(o). The n -dependent η in the relaxed

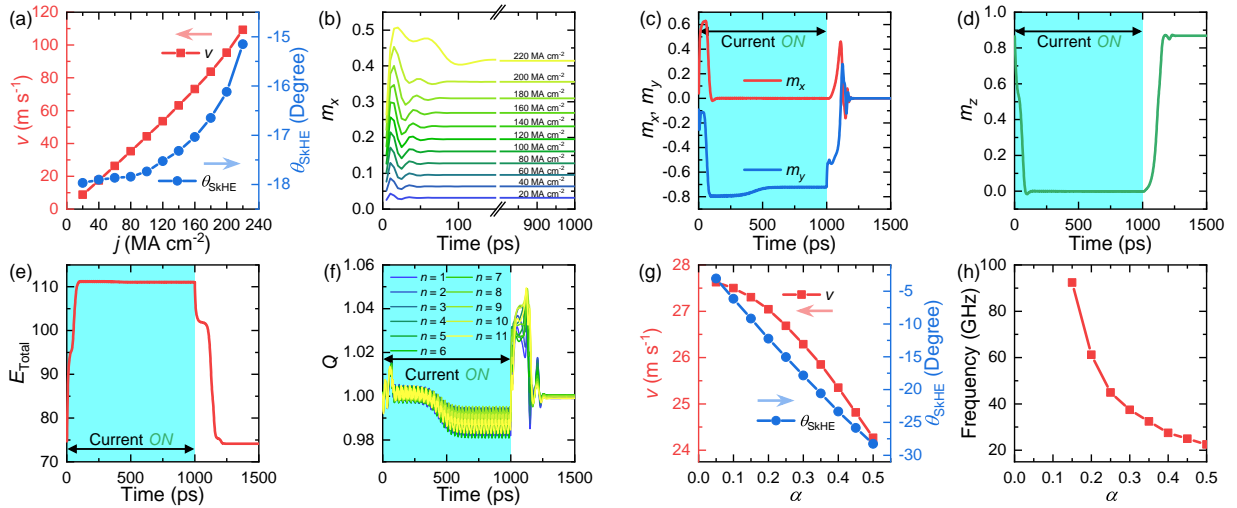


FIG. 3. (a) Velocity v and skyrmion Hall angle θ_{SkHE} as functions of j for a Bloch-type skyrmion string. (b) In-plane spin component m_x as a function of time at different j , corresponding to (a). (c) $m_{x,y}$, (d) m_z , (e) E_{Total} , and (f) n -dependent absolute topological charge $|Q|$ as functions of time for the current-controlled mutual transformation between a skyrmion string and a bimeron string, where $j = 240 \text{ MA cm}^{-2}$ is applied for $t = 0 \sim 1000 \text{ ps}$. (g) α -dependent v and θ_{SkHE} of a Bloch-type skyrmion string driven by $j = 60 \text{ MA cm}^{-2}$. (h) α -dependent rotation frequency of a bimeron string driven by $j = 240 \text{ MA cm}^{-2}$.

166 Bloch-type skyrmion string is caused by the DDI, which most
 167 commonly affects the in-plane spin configurations of the top-
 168 most ($n = 11$) and bottommost ($n = 1$) layers [Figs. 1(b)
 169 and 1(d)].

170 *Current-induced dynamics.* We further study the current-
 171 induced dynamics of a Bloch-type skyrmion string with $\eta \sim$
 172 $\pi/2$, which is initially relaxed at the sample center before the
 173 application of a driving current. The sample include 11 coupled
 174 FM layers with periodic boundary conditions in the x
 175 and y dimensions. We first apply a current with a current den-
 176 sity j ranging from 20 to 300 MA cm^{-2} to drive the pancake
 177 skyrmion in each FM layer. The effect of τ_d leads to the linear
 178 motion of the Bloch-type skyrmion string when $j = 20 \sim 220$
 179 MA cm^{-2} (see Video 1 in Ref. 62).

180 At a relatively smaller j , the skyrmion string moves stably
 181 and shows the skyrmion Hall effect [Fig. 2(a)], which is a nat-
 182 ural consequence of the skyrmion Hall effect of the pancake
 183 skyrmion in each FM layer. The variation of the skyrmion
 184 string in the z dimension is very small during its steady mo-
 185 tion, namely, there is almost no layer-dependent deformation
 186 in the skyrmion string. Hence, we calculate the skyrmion ve-
 187 locity and skyrmion Hall angle based on the skyrmion in the
 188 middle FM layer ($n = 6$). The skyrmion string velocity and
 189 its skyrmion Hall angle increase with j when $j = 20 \sim 220$
 190 MA cm^{-2} [Fig. 3(a)]. The change of the skyrmion Hall an-
 191 gle is due to the current-induced deformation of the skyrmion
 192 string, which can be seen from the selected top-view snap-
 193 shots at $j = 200 \text{ MA cm}^{-2}$ [Fig. 2(b)] and j -dependent m_x - t
 194 relation [Fig. 3(b)].

195 However, when $j \geq 240 \text{ MA cm}^{-2}$, the skyrmion string
 196 smoothly transforms to a bimeron string when the current is
 197 applied [Figs. 2(c)-2(e)]. The current-induced formation of
 198 the bimeron string is due to the fact that the effect of τ_d with

199 $\mathbf{p} = -\hat{y}$ tends to drag the spins in each FM layer from the $\pm z$
 200 direction to the in-plane $-y$ direction [Figs. 3(c) and 3(d)].
 201 Note that the bimeron in the in-plane magnetized system is a
 202 topological counterpart of the skyrmion in the perpendicularly
 203 magnetized system [40]. Once the bimeron string is formed
 204 under the driving current, it shows counter-clockwise rotation
 205 with a constant frequency determined by j (see Videos 2-4 in
 206 Ref. 62), which agrees well with the current-induced dynam-
 207 ics of the 2D frustrated bimeron [40]. The bimeron string is
 208 a dynamically stable only state, which shows certain layer-
 209 dependent deformation [Fig 2(e)]. The total energy increases
 210 to a stable value during the current application [Fig. 3(e)], in-
 211 dicating the bimeron string is an excited state maintained by
 212 τ_d . The numerically calculated topological charge of each FM
 213 layer only slightly varies during the transformation from the
 214 skyrmion string to the bimeron string [Fig. 3(f)], which im-
 215 plies that the transformation between a skyrmion string and a
 216 bimeron string is guaranteed by the topological conservation
 217 principle. Note that the topological charge has been calibrated
 218 by slightly shifting the curve vertically, which ensures an in-
 219 teger charge of relaxed state.

220 When the current is switched off at $t = 1000 \text{ ps}$, the
 221 bimeron string stops rotating and spontaneously transforms
 222 back to a Bloch-type skyrmion string [Fig. 2(c)]. During
 223 this process, the system evolves back to an energetically fa-
 224 vored perpendicularly magnetized configuration due to the ef-
 225 fect of PMA [Fig. 3(d) and 3(e)], and the topological charge
 226 shows more obvious damped oscillation [Fig. 3(f)]. Such a
 227 phenomenon suggests that the topological spin textures can
 228 be very robust solutions in a stack of coupled FM layers, ei-
 229 ther with perpendicularly magnetized or in-plane magnetized
 230 background.

231 In addition, we study the α -dependent linear motion of a

Bloch-type skyrmion string at a relatively smaller j as well as the α -dependent rotation of a bimeron string at a relatively larger j . The Bloch-type skyrmion string velocity and its corresponding skyrmion Hall angle decrease with increasing α [Fig. 3(g)]. The rotation frequency of the bimeron string is found to decrease with increasing α [Fig. 3(h)].

Conclusion. In conclusion, we have studied the static structures of Néel-type and Bloch-type skyrmion strings formed by 11 aligned stacks of 2D frustrated pancake skyrmions. The Bloch-type skyrmion strings with $\eta \sim \pi/2, 3\pi/2$ are metastable states, which shows slightly varied η in the z dimension. Their Néel-type counterparts with $\eta = 0, \pi$ are unstable states due to the effect of DDI. Both the Bloch-type and Néel-type skyrmion strings have layer-dependent interlayer exchange coupling energy. For the dynamics, the Bloch-type skyrmion string shows translational motion at a small current, and it is transformed to a rotating bimeron string at a large current. The bimeron string spontaneously transforms back to a skyrmion string when the current is switched off.

Our results reveal unusual static and dynamic properties of 3D topological spin textures in frustrated magnetic systems. The transformation between merons and skyrmions in a chiral magnet induced by the magnetic field has been realized in experiments [63]. Future experimental exploration on the current-induced mutual transformation between the skyrmion string and the bimeron string are important for the construction of an electrically controlled multistate information storage device [64] based on different 3D topological spin textures. Possible future directions that one can explore also include the effect of a tilting field [65] on the 3D skyrmion and bimeron strings, the system with a lattice of 3D skyrmion or bimeron strings, and the system with decoupled layers.

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* These authors contributed equally to this work.

† zhouyan@cuhk.edu.cn

‡ ezawa@ap.t.u-tokyo.ac.jp

§ liu@cs.shinshu-u.ac.jp

- [1] U. K. Röbner, A. N. Bogdanov, and C. Pfleiderer, *Nature* **442**, 797 (2006).
- [2] S. Mühlbauer, B. Binz, F. Jonietz, C. Pfleiderer, A. Rosch, A. Neubauer, R. Georgii, and P. Böni, *Science* **323**, 915 (2009).
- [3] X. Z. Yu, Y. Onose, N. Kanazawa, J. H. Park, J. H. Han, Y. Matsui, N. Nagaosa, and Y. Tokura, *Nature* **465**, 901 (2010).
- [4] N. Nagaosa and Y. Tokura, *Nat. Nanotech.* **8**, 899 (2013).
- [5] M. Mochizuki and S. Seki, *J. Phys.: Condens. Matter* **27**, 503001 (2015).
- [6] R. Wiesendanger, *Nat. Rev. Mat.* **1**, 16044 (2016).
- [7] G. Finocchio, F. Büttner, R. Tomasello, M. Carpentieri, and M. Kläui, *J. Phys. D: Appl. Phys.* **49**, 423001 (2016).
- [8] W. Kang, Y. Huang, X. Zhang, Y. Zhou, and W. Zhao, *Proc. IEEE* **104**, 2040 (2016).
- [9] N. Kanazawa, S. Seki, and Y. Tokura, *Adv. Mater.* **29**, 1603227 (2017).
- [10] W. Jiang, G. Chen, K. Liu, J. Zang, S. G. Velthuis, and A. Hoffmann, *Phys. Rep.* **704**, 1 (2017).
- [11] A. Fert, N. Reyren, and V. Cros, *Nat. Rev. Mater.* **2**, 17031 (2017).
- [12] K. Everschor-Sitte, J. Masell, R. M. Reeve, and M. Kläui, *J. Appl. Phys.* **124**, 240901 (2018).
- [13] Y. Zhou, *Natl. Sci. Rev.* **6**, 210 (2019).
- [14] X. Zhang, Y. Zhou, K. M. Song, T.-E. Park, J. Xia, M. Ezawa, X. Liu, W. Zhao, G. Zhao, and S. Woo, *J. Phys. Condens. Matter* **32**, 143001 (2020).
- [15] B. Göbel, I. Mertig, and O. A. Tretiakov *Phys. Rep.* **895**, 1 (2021).
- [16] T. Okubo, S. Chung, and H. Kawamura, *Phys. Rev. Lett.* **108**, 017206 (2012).
- [17] A. O. Leonov and M. Mostovoy, *Nat. Commun.* **6**, 8275 (2015).
- [18] S.-Z. Lin and S. Hayami, *Phys. Rev. B* **93**, 064430 (2016).
- [19] S. Hayami, S.-Z. Lin, and C. D. Batista, *Phys. Rev. B* **93**, 184413 (2016).
- [20] L. Rózsa, A. Deák, E. Simon, R. Yanes, L. Udvardi, L. Szunyogh, and U. Nowak, *Phys. Rev. Lett.* **117**, 157205 (2016).
- [21] C. D. Batista, S.-Z. Lin, S. Hayami, and Y. Kamiya, *Rep. Prog. Phys.* **79**, 084504 (2016).
- [22] A. O. Leonov and M. Mostovoy, *Nat. Commun.* **8**, 14394 (2017).
- [23] Y. A. Kharkov, O. P. Sushkov, and M. Mostovoy, *Phys. Rev. Lett.* **119**, 207201 (2017).
- [24] X. Zhang, J. Xia, Y. Zhou, X. Liu, H. Zhang, and M. Ezawa, *Nat. Commun.* **8**, 1717 (2017).
- [25] H. Y. Yuan, O. Gomonay, and M. Kläui, *Phys. Rev. B* **96**, 134415 (2017).
- [26] Z. Hou, W. Ren, B. Ding, G. Xu, Y. Wang, B. Yang, Q. Zhang, Y. Zhang, E. Liu, F. Xu, W. Wang, G. Wu, X. Zhang, B. Shen, and Z. Zhang, *Adv. Mater.* **29**, 1701144 (2017).
- [27] Y. Hu, X. Chi, X. Li, Y. Liu, and A. Du, *Sci. Rep.* **7**, 16079 (2017).
- [28] S. von Malottki, B. Dupe, P. F. Bessarab, A. Delin, and S. Heinze, *Sci. Rep.* **7**, 12299 (2017).
- [29] J. J. Liang, J. H. Yu, J. Chen, M. H. Qin, M. Zeng, X. B. Lu, X. S. Gao, and J. Liu, *New J Phys.* **20**, 053037 (2018).
- [30] U. Ritzmann, S. von Malottki, J.-V. Kim, S. Heinze, J. Sinova, and B. Dupé, *Nat. Electron.* **1**, 451 (2018).

- [31] T. Kurumaji, T. Nakajima, M. Hirschberger, A. Kikkawa, Y. Yamasaki, H. Sagayama, H. Nakao, Y. Taguchi, T.-h. Arima, and Y. Tokura, *Science* **365**, 914 (2019).
- [32] L. Desplat, J. V. Kim, and R. L. Stamps, *Phys. Rev. B* **99**, 174409 (2019).
- [33] J. Xia, X. Zhang, M. Ezawa, Z. Hou, W. Wang, X. Liu, and Y. Zhou, *Phys. Rev. Applied* **11**, 044046 (2019).
- [34] R. Zarzuela, H. Ochoa, and Y. Tserkovnyak, *Phys. Rev. B* **100**, 054426 (2019).
- [35] V. Lohani, C. Hickey, J. Masell, and A. Rosch, *Phys. Rev. X* **9**, 041063 (2019).
- [36] B. Göbel, A. Mook, J. Henk, I. Mertig, and O. A. Tretiakov, *Phys. Rev. B* **99**, 060407(R) (2019).
- [37] I. F. Sharafullin, M. Kh. Kharrasov, and H. T. Diep, *Phys. Rev. B* **99**, 214420 (2019).
- [38] I. F. Sharafullin and H. T. Diep, *Symmetry* **12**, 26 (2020).
- [39] H. T. Diep, *Entropy* **21**, 175 (2019).
- [40] X. Zhang, J. Xia, L. Shen, M. Ezawa, O. A. Tretiakov, G. Zhao, X. Liu, and Y. Zhou, *Phys. Rev. B* **101**, 144435 (2020).
- [41] J. Xia, X. Zhang, M. Ezawa, O. A. Tretiakov, Z. Hou, W. Wang, G. Zhao, X. Liu, H. T. Diep, and Y. Zhou, *Appl. Phys. Lett.* **117**, 012403 (2020).
- [42] X. Zhang, J. Xia, M. Ezawa, O. A. Tretiakov, H. T. Diep, G. Zhao, X. Liu, and Y. Zhou, *Appl. Phys. Lett.* **118**, 052411 (2021).
- [43] C. Psaroudaki and C. Panagopoulos, *Phys. Rev. Lett.* **127**, 067201 (2021).
- [44] R. Zarzuela, D. Hill, J. Sinova, and Y. Tserkovnyak, *Phys. Rev. B* **103**, 174424 (2021).
- [45] R. Zarzuela and J. Sinova, *arXiv:2107.13330* (2021).
- [46] W. Jiang, X. Zhang, G. Yu, W. Zhang, X. Wang, M. Benjamin Jungfleisch, J. E. Pearson, X. Cheng, O. Heinonen, K. L. Wang, Y. Zhou, A. Hoffmann, and S. G. E. Velthuis, *Nat. Phys.* **13**, 162 (2017).
- [47] K. Litzius, I. Lemesch, B. Kruger, P. Bassirian, L. Caretta, K. Richter, F. Buttner, K. Sato, O. A. Tretiakov, J. Forster, R. M. Reeve, M. Weigand, I. Bykova, H. Stoll, G. Schutz, G. S. D. Beach, and M. Klau, *Nat. Phys.* **13**, 170 (2017).
- [48] X. Zhang, Y. Zhou, and M. Ezawa, *Phys. Rev. B* **93**, 024415 (2016).
- [49] R. Zarzuela, V. K. Bharadwaj, K.-W. Kim, J. Sinova, and K. Everschor-Sitte, *Phys. Rev. B* **101**, 054405 (2020).
- [50] K. Everschor-Sitte, M. Sitte, T. Valet, A. Abanov, and J. Sinova, *New J. Phys.* **19**, 092001 (2017).
- [51] J. R. Clem, *Phys. Rev. B* **43**, 7837 (1991).
- [52] J. R. Clem, *J. Supercond. Nov. Magn.* **17**, 613 (2004).
- [53] C. J. Olson, C. Reichhardt, and V. M. Vinokur, *Phys. Rev. B* **64**, 140502(R) (2001).
- [54] Z.-L. Liu, P. Kang, Y. Zhu, L. Liu, and H. Guo, *APL Mater.* **8**, 061104 (2020).
- [55] C. Reichhardt, C. J. O. Reichhardt, and M. V. Milosevic, *arXiv:2102.10464*.
- [56] S.-Z. Lin and C. D. Batista, *Phys. Rev. Lett.* **120**, 077202 (2018).
- [57] C. Reichhardt and C. J. O. Reichhardt, *Phys. Rev. B* **84**, 174208 (2011).
- [58] J. Xia, X. Zhang, K. Mak, M. Ezawa, O. A. Tretiakov, Y. Zhou, G. Zhao, and X. Liu, *Phys. Rev. B* **103**, 174408 (2021).
- [59] E. E. Kaul, H. Rosner, N. Shannon, R. V. Shpanchenko, and C. Geibel, *J. Magn. Magn. Mater.* **272-276**, 922 (2004).
- [60] J. Sinova, S. O. Valenzuela, J. Wunderlich, C. H. Back, and T. Jungwirth, *Rev. Mod. Phys.* **87**, 1213 (2015).
- [61] M. J. Donahue and D. G. Porter, "OOMMF User's Guide, Version 1.0", Interagency Report NO. NISTIR 6376 (National Institute of Standards and Technology, Gaithersburg, MD, 1999) [<http://math.nist.gov/oommf/>].
- [62] See Supplemental Material at [URL] for more information regarding the parameter dependency diagrams and supplementary videos showing the current-induced dynamics.
- [63] X. Z. Yu, W. Koshibae, Y. Tokunaga, K. Shibata, Y. Taguchi, N. Nagaosa, and Y. Tokura, *Nature* **564**, 95 (2018).
- [64] Y. Wang, L. Wang, J. Xia, Z. Lai, G. Tian, X. Zhang, Z. Hou, X. Gao, W. Mi, C. Feng, M. Zeng, G. Zhou, G. Yu, G. Wu, Y. Zhou, W. Wang, X. Zhang, and J. Liu, *Nat. Commun.* **11**, 3577 (2020).
- [65] S.-Z. Lin and A. Saxena, *Phys. Rev. B* **92**, 180401(R) (2015).